Evidence for coupling between collective state and phonons in
two-dimensional charge-density-wave systems

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Abstract

We report on a Raman scattering investigation of the charge-density-wave (CDW), quasi two-dimensional rare-earth tri-tellurides \( R\text{Te}_3 \) (\( R = \text{La, Ce, Pr, Nd, Sm, Gd and Dy} \)) at ambient pressure, and of \( \text{LaTe}_3 \) and \( \text{CeTe}_3 \) under externally applied pressure. The observed phonon peaks can be ascribed to the Raman active modes for both the undistorted as well as the distorted lattice in the CDW state by means of a first principles calculation. The latter also predicts the Kohn anomaly in the phonon dispersion, driving the CDW transition. The integrated intensity of the two most prominent modes scales as a characteristic power of the CDW-gap amplitude upon compressing the lattice, which provides clear evidence for the tight coupling between the CDW condensate and the vibrational modes.

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The electron-phonon coupling is of fundamental relevance for the development of several types of charge ordering in solids, of which the charge-density-wave (CDW) state, first predicted by Peierls [1], is an interesting realization. Peierls argued that one-dimensional (1D) metals are intrinsically unstable, and that a new broken-symmetry ground state results from the selfconsistent rearrangement of the electronic charge density in response to the (static) modulation of the ionic positions [1, 2]. The new lattice periodicity leads moreover to the opening of a gap at the Fermi level. The consequences of this intimate connection between electronic properties and lattice dynamics have been intensively investigated in a number of prototype quasi-1D materials [3].

CDW’s have been observed in transition metal di- and trichalcogenides [4, 5], in the ladder compounds Sr$_{14-x}$Ca$_x$Cu$_{24}$O$_{41}$ [6] and in some copper oxide high temperature superconductors [7] (where they are known as “stripes”) as well, suggesting that similar effects are to be expected also in layered quasi-2D systems. A recent theoretical study [8] confirms that this is indeed the case, and that two orthogonal CDW’s may even combine to generate a checkerboard-like charge pattern. However, high temperature superconductors are bad candidates for a systematic study of the interplay between electronic and phononic degrees of freedom in quasi-2D materials, given the strongly correlated nature of the electrons in these systems. One class of quasi-2D compounds well suited to address this issue are the rare-earth (R) tri-tellurides [9, 10, 11]. They host a CDW state already at 300 K and their structure consists of alternating double Te (ac) planes (where the CDW resides) sandwiched between RTe layer blocks and stacked along the long b axis in the weakly orthorhombic (pseudo-tetragonal) cell. In our first optical investigations, we have established the excitation across the CDW-gap and discovered that this gap is progressively reduced upon compressing the lattice either with chemical substitution (i.e., by changing R) or with externally applied pressure [12, 13].

The formation of the CDW condensate in RTe$_3$ only partially gaps the Fermi surface [14] and therefore these materials remain metallic even well below the critical temperature $T_{CDW}$ at which the CDW appears [11]. This prevents the investigation of the phonon modes and more generally of the impact of the lattice dynamics on the CDW state [2] in an infrared absorption experiment, as the corresponding signals are overwhelmed by the metallic
contribution. We therefore address the issue of the coupling between vibrational modes and CDW condensate in these prototype 2D systems from the perspective of the Raman scattering response. Our data, combined with the measured CDW-gap, and supported by first principles calculations, allow us to identify the expected Raman active modes and to determine their evolution under pressure [15]. We provide clear cut evidence for a tight coupling between CDW condensate and vibrational modes as well as robust predictions for the incipient Kohn anomaly, i.e. the “freezing in” of a lattice distortion associated with the formation of the CDW phase [1, 2, 3].

Our Raman scattering experiments were performed on the rare-earth series $R$Te$_3$ ($R$=La, Ce, Pr, Nd, Sm, Gd and Dy, with $T_{CDW} > 300$ K [11]) at ambient pressure as well as on LaTe$_3$ and CeTe$_3$ under externally applied pressure. The single crystalline samples of $R$Te$_3$ were grown by slow cooling of a binary melt [10]. Raman spectra were collected on cleaved [010] surfaces with a commercial micro-Raman spectrometer equipped with a He-Ne laser (632.8 nm wavelength, 16 mW power), a 20× microscope objective (10 μm$^2$ laser spot), a notch filter to reject the elastic contribution, a 1800 lines/mm grating, and a cooled charge-coupled-device detector. Additionally we have performed polarization-dependent Raman experiments on LaTe$_3$ at ambient pressure by varying the angle between the incident light polarization and the crystal axes by means of a λ/2 polarization rotator and selecting the scattered polarization parallel to the incident one. High pressures were generated by means of a Betsa membrane diamond-anvil-cell (DAC) equipped with high-quality type IIA diamonds (800 μm culet diameter) and a stainless steel gasket (300 μm hole diameter and 50 μm thickness). A small ($\approx 100 \times 100$ μm$^2$) sample piece was placed inside the DAC together with the pressure transmitting medium (a 4:1 methanol-ethanol mixture [16]) and a small ruby chip for pressure measurement [17].

Figure II(a) summarizes the Raman scattering spectra, collected for the whole $R$Te$_3$ series (i.e., chemical pressure). Four distinct modes at 72, 88, 98 and 109 cm$^{-1}$ and a weak bump at 136 cm$^{-1}$ (labeled P1-P5, respectively) can be identified in the La compound. The P1 mode slightly softens from La to Nd and slowly moves outside the measurable spectral range at ambient pressure (i.e., in SmTe$_3$ only its high frequency tail is still observable). The remaining modes weakly disperse and progressively disappear when going from the La
FIG. 1: (color online) Raman scattering spectra at 300 K for the $RTe_3$ series at ambient pressure (a), and for $LaTe_3$ (b) and $CeTe_3$ (c) for increasing (continuous lines) and decreasing (dashed lines) pressure. All spectra have been shifted for clarity.

to the Dy compound along the rare-earth series.

Panels (b) and (c) in Fig. 1 display the Raman scattering spectra of $LaTe_3$ and $CeTe_3$, under increasing and decreasing externally applied pressure. The spectral range covered within the DAC is limited at low frequencies at about 75 cm$^{-1}$, so that the lowest zero-pressure mode P1 cannot be clearly detected in the applied pressure experiment. As in the chemical pressure case, all other modes slightly disperse and disappear upon applying pressure. This qualitative equivalence between chemical and applied pressure is also supported by the fact that the peaks in $LaTe_3$ disappear at a slightly higher pressure than in $CeTe_3$. The pressure dependence is fully reversible since upon decreasing pressure the modes reappear again.

The space-group of the undistorted structure is $Cmcm$ ($D_{2h}^{17}$) for all rare earth tritellurides. From the occupied atomic positions [18] and the factor-group analysis we determine the symmetry and multiplicity of the Raman-active phonons [19], namely: $4A_{1g} + 4B_{1g} + 4B_{3g}$. The corresponding Raman tensors imply that for our experimental configuration, in which both incident and scattered light are polarized parallel to the $ac$ crystal plane, only the $A_{1g}$ symmetry phonons can be observed.

The vibrational modes at the $\Gamma$ point of the Brillouin zone for the undistorted structure at ambient pressure have been obtained from first principles, using the Dmol$^3$ code developed by one of us [20]. First, the positions of the 8 atoms in the primitive unit cell were optimized
FIG. 2: (color online) (a) Raman-active phonon frequencies of $R$Te$_3$, obtained experimentally (solid symbols) and calculated for the undistorted structure (open symbols). The calculated extra peaks arising in the distorted structure (see text) are also shown with star symbols for LaTe$_3$. The lattice constant values are from Ref. 22. (b) Atomic displacements for the Raman active $A_{1g}$ vibrational modes in LaTe$_3$. The figure shows the $ab$ plane, whereas large (small) spheres represent atoms having a positive (negative) $c$ coordinate. The dotted lines represent the Te planes. The primitive unit-cell and crystal axes are also shown. Arrows-lengths are proportional to the calculated displacements.

at the experimental lattice constants $a$ and $b$, obtained by averaging the values listed in the tables of Ref. 22. A frozen-phonon calculation then yielded the 24 sought-after frequencies. Only 4 of these correspond to the expected Raman active modes with $A_{1g}$ symmetry.

The frequencies of the calculated $A_{1g}$ modes at $\Gamma$ for the $R$Te$_3$ series are summarized in Fig. 2a along with the experimental values, while Fig. 2b pictures the $A_{1g}$ lattice displacements of the undistorted structure, which, as predicted from the factor-group analysis, are along the $b$ axis. The agreement with the experimental findings is satisfactory. There is an obvious assignment of the calculated modes, for instance at 67, 87 and 141 cm$^{-1}$ for LaTe$_3$, with the corresponding features in the measured spectra (P1, P2, and P5). The calculated mode at about 106 cm$^{-1}$ lies between the experimentally observed modes P3 and P4 for LaTe$_3$. This situation persists throughout the whole rare earth series (Fig. 2b). Our
polarization dependent measurements on LaTe$_3$ (Fig. 3a) yield an angle-dependent intensity with a period of 90° for the P4 mode and 180° for the adjacent peaks P2 and P3 [23]. Since a 180° period is expected for the $A_{1g}$ symmetry, the P4 mode cannot be assigned within the undistorted structure.

In order to improve the mode assignment and to clarify the origin of the P4 peak, we have, in a first step, computed the phonon dispersion in LaTe$_3$ along the $\Gamma - Z$ direction of the Brillouin zone, using a supercell consisting of a 16-fold repetition along the $c$-axis of the primitive unit cell. This yields phonon frequencies at wave vectors $(0, 0, q_z)$, where $q_z = \frac{n}{16}c^*$, with $c^* = \frac{2\pi}{c}$, and $n$ between 0 and 8. A symmetry constrained spline interpolation between these results is shown in Fig. 3b (similar results have been obtained along the $a$ axis). The dashed branches highlight the phonon dispersion for the modes with $A_{1g}$ symmetry at $\Gamma$. The calculated phonon spectrum also shows a distinct Kohn anomaly at $q_z$ slightly below 0.3$c^*$ (thick lines), i.e. in the region expected from the electron diffraction results [9] and the angle-resolved photoemission spectroscopy data on CeTe$_3$ [14]. In a second step, we have generated a commensurate approximant to the distorted structure in the presence of the incommensurate CDW by repeating the calculation for a 14-fold repetition of the primitive unit cell along the $c$-axis (in which case a true instability occurs at $q_z = \frac{2}{7}c^*$,

FIG. 3: (color online) (a) Raman spectra of LaTe$_3$ as a function of the polarization angle of the incident light. (b) Calculated phonon dispersion along the $c$ axis. (c) Enlargement of the P2 peak in CeTe$_3$ detailing its double-feature nature.
FIG. 4: (color online) Comparison between the amplitude of the CDW-gap (open circles) [12, 13] and the integrated intensities \( I \) of the P2 (full triangles) and P4 (full squares) peaks, raised to 1/4 and 1/2, respectively (see text) as a function of the lattice constant for the \( \text{RTe}_3 \) series (a) and for \( \text{CeTe}_3 \) under pressure (b). The pressure dependence of the lattice constant in \( \text{CeTe}_3 \) was achieved following the procedure of Ref. 13. All quantities are normalized to their starting values.

i.e. the frequency of the soft phonon becomes imaginary), then moving the atoms along the eigenvectors of the soft phonon, and reequilibrating their positions in the corresponding \((1 \times 1 \times 7)\) supercell [24]. As a consequence of the lower symmetry, vibrational modes with \( A_1 \) and \( B_1 \) symmetry become Raman-active [25]. Although there are 56 \( A_1 \) symmetry modes, their frequencies accumulate around those of the \( A_{1g} \) modes of the undistorted structure, suggesting that the distortion does not particularly affect the \( \Gamma \)-point vibrational energies. This is consistent with the fact that the phonon branches having \( A_{1g} \) symmetry at \( \Gamma \) are weakly dispersing (Fig. 3b). The main effect of the distortion is the appearance of 28 \( B_1 \) modes, which accumulate around 84 and 116 cm\(^{-1}\). The latter frequency compares very nicely with the frequency of the P4 peaks in our experiment. The second \( B_1 \) mode at about 84 cm\(^{-1}\) falls in the range of the P2 peak. A closer look at the experimental data (Fig. 3c for \( \text{CeTe}_3 \)) indeed suggests that the P2 peak may be a double feature.

The main result of our experimental investigation is the observation of a systematic decrease of the integrated intensity \( I \) of the most prominent peaks P2 and P4 in the Raman spectra of Fig. 1 with pressure [26], which bears a striking similarity with the behaviour of
the amplitude of the CDW-gap $\Delta$ (i.e., the order parameter) upon compressing the lattice, as obtained from the optical conductivity [12, 13]. One could first argue that these modes disappear because of an enhancement of their width and a concomitant decrease of their apparent amplitude due to the increase in free carrier concentration upon compressing the lattice [12]. The modes’ width remains, however, almost constant so that this possibility is rather unlikely. Our optical data [12] also allow us to exclude the possibility that the phonon modes disappear due to an increase of the absorption coefficient at the laser frequency with decreasing lattice constant. Figure 4 shows that the intensities of the P2 and P4 peaks scale with $\Delta^4$ and $\Delta^2$, respectively [27], suggestive of a coupling between the lattice vibrational modes and the CDW condensate. This is not at all surprising for the P4 mode, as our calculations predict this peak only in the distorted structure. For the P2 peak we should consider its two components, namely the $A_{1g}$ mode in the undistorted structure and the $B_1$ mode in the distorted one (Fig. 3c). For the latter the intensity is obviously correlated with the CDW, whereas for the former at 87 cm$^{-1}$ the correlation can be explained by looking at the corresponding atomic displacements (Fig. 2b), which strongly distort the Te-planes and therefore should couple to the CDW [28]. Furthermore, the specific behaviour ($I \sim \Delta^q$, $q=2$ or $4$) is consistent with theoretical predictions for the intensity in the distorted phase of originally silent modes, obtained from a group theoretical analysis in the framework of Landau’s theory of second order phase transitions [29].

In summary, we have been able to draw a consistent picture of the Raman response of the CDW rare-earth tri-tellurides, by combining experimental observations and numerical simulations. In particular, we have provided clear evidence for the tight coupling between the CDW-gap and the lattice degrees of freedom and have made a robust prediction for the Kohn anomaly inducing the CDW phase transition. Therefore, the easily tunable $R$Te$_3$ series provides a rather unique playground for a systematic study of the mechanism leading to the formation of the CDW state.

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[15] As the temperature dependence of the CDW-gap is not known in RTe3, we choose pressure (both chemical and applied) as tunable variable.
[20] The calculations were done with hardness-conserving semilocal pseudopotentials for all states below the 4d shell for Te and the 5s shell for the rare-earth atoms [B. Delley, Phys. Rev. B 66 155125 (2002)], and used the DNP basis set [B. Delley, J. Chem. Phys. 92 508 (1990); J. Chem. Phys. 113, 7756 (2000)]. The k-space integrations have been performed with an
unshifted $6 \times 2 \times 6$ ($2 \times 2 \times 6$) mesh, which amounts to 40 (16) symmetry unique k-points in the calculations for the primitive (super-) cell. A thermal broadening of 1 mHartree has been used. The total energy has been modified with the entropy term proposed by M. Weinert and J.W. Davenport [Phys. Rev. B 45, 13709 (1992)] to make the energy functional variational.

[21] An orthorhombic pseudotetragonal ($a = c$) structure was considered, as the small deviations between $a$ and $c$ were found to be insignificant in an earlier high precision calculation of the Fermi surface [J. Laverock et al., Phys. Rev. B 71, 085114 (2005)].


[23] We also collected data (not shown here) with the scattered light polarization orthogonal to the incident one and obtained results fully consistent with those of the parallel polarization (Fig. 3a).


[25] The unit cell in the distorted structure is not centrosymmetric anymore, so that the $A_{1g}$ symmetry turns into $A_1$. The period of the angle-dependent intensity is $180^\circ$ ($90^\circ$) for the $A_1$ ($B_1$) symmetry.

[26] The sudden disappearance of the modes in the Raman spectra of Gd and Dy tri-tellurides (Fig. 1a) could also originate from the fact that the data were collected at 300 K, i.e. just slightly below their own $T_{CDW}$ [11].

[27] The behaviour of the weak P3 and P5 peaks is less well defined, while the intensity of the P1 peak, which is only partially seen in the chemical-pressure series, does not seem to change much.
