Measurement of the t-channel single top quark production cross section

The D0 collaboration reports direct evidence for electroweak production of single top quarks through the $t$-channel exchange of a virtual $W$ boson. This is the first analysis to isolate an individual single top quark production channel. We select events containing an isolated electron or muon, missing transverse energy, and two, three or four jets from 2.3 fb$^{-1}$ of $p\bar{p}$ collisions at the Fermilab Tevatron Collider. One or two of the jets are identified as containing a $b$ hadron. We combine three multivariate techniques optimized for the $t$-channel process to measure the $t$- and $s$-channel cross sections simultaneously. We measure cross sections of $3.14^{+0.94}_{-0.80}$ pb for the $t$-channel and $1.05 \pm 0.81$ pb for the $s$-channel. The measured $t$-channel result is found to have a significance of 4.8 standard deviations and is consistent with the standard model prediction.

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The D0 and CDF collaborations at the Fermilab Tevatron $p\bar{p}$ Collider have recently observed electroweak production of single top quarks [1, 2], measuring the total single top quark production cross section as well as the Cabibbo-Kobayashi-Maskawa (CKM) matrix element [3] $|V_{tb}|$ directly. In the standard model (SM), the two main production modes at the Tevatron resulting in a single top (or antitop) quark final state are the $t$-channel exchange of a $W$ boson shown in Fig. 1a and the $s$-channel production via the decay of a virtual $W$ boson. The two observation analyses measured only the combined single top quark cross section, assuming
the SM ratio of the two production modes. This ratio is modified in several new physics scenarios, for example in models with additional quark generations, new heavy bosons [4], flavor-changing neutral currents [5], or anomalous top quark couplings [6–8]. In this Letter we remove this assumption and use the t-channel characteristics to measure the t-channel and s-channel cross sections simultaneously, thus providing a t-channel measurement independent of the s-channel cross section model. The main characteristic of the t-channel which separates it both from the s-channel and the backgrounds is the pseudorapidity distribution of the light quark jet, shown in Fig. 1b. The predicted cross section for t-channel (s-channel) production is 2.34 ± 0.13 pb (1.12 ± 0.04 pb) for a top quark mass $m_t = 170$ GeV [9].

![Feynman diagram for t-channel single top quark production and decay](attachment:image.png)

**FIG. 1:** Representative Feynman diagram for t-channel single top quark production and decay (a) and parton-level pseudorapidity distribution of the final state objects in top production (excluding antitop), requiring each object to have transverse momentum $p_T > 15$ GeV (b).

This analysis extends the D0 single top evidence [10, 11] and observation analyses [1], utilizing the same dataset, event selection, and signal/background modeling as the observation analysis, but training multivariate filters specifically to extract t-channel single top quark events. We use 2.3 fb$^{-1}$ of data collected by the D0 experiment [12] at the Fermilab Tevatron $p\bar{p}$ Collider between 2002 and 2007 (Run II). The measurement selects final states containing one high transverse momentum ($p_T$) isolated lepton (electron or muon), large missing transverse energy ($E_T$), a b quark jet from the decay of the top quark ($t \rightarrow Wb$), a light quark jet produced in association with the top quark, and a spectator b quark jet from gluon splitting in the initial state. We allow for one of these jets not to be identified as well as for the presence of an additional jet from gluon radiation. The backgrounds are $W$ bosons produced in association with jets, $t\bar{t}$ pairs, and multijet production, where a jet is misreconstructed as an electron or a heavy-flavor quark decays to a muon that satisfies isolation criteria. $Z$+jets and diboson processes form minor additional background components. We treat s-channel single top quark production as a background during the multivariate training but measure its cross section simultaneously with the t-channel measurement as explained below.

We look for t-channel and s-channel single top quark production in events with two to four jets with $p_T > 15$ GeV and pseudorapidity $|\eta| < 3.4$, with the leading jet additionally satisfying $p_T > 25$ GeV. We require $20 < E_T < 200$ GeV for events with two jets and $25 < E_T < 200$ GeV for events with three or four jets. Events must contain only one isolated electron with $p_T > 15$ GeV and $|\eta| < 1.1$ ($p_T > 20$ GeV for three- or four-jet events), or one isolated muon with $p_T > 15$ GeV and $|\eta| < 2.0$. The background from jets misidentified as leptons is kept to approximately 5% by requiring the total transverse energy of all final state objects $H_T(\ell, E_T, \text{jets})$ to be greater than 110 to 160 GeV, depending on the analysis channel, and by demanding that the $E_T$ is not along the direction of the lepton or the leading jet in the transverse plane. To enhance the signal fraction, one or two of the jets are required to originate from $b$ hadrons, as implemented through a neural network (NN) b-jet tagging algorithm [13]. We divide the dataset into 24 independent analysis channels (separated by data taking period, lepton type, $b$-tag and jet multiplicity) and combine the results to maximize the signal sensitivity. Details on the selection criteria and background modeling are given in Ref. [11].

We generate t-channel and s-channel single top events with the SingleTop Monte Carlo (MC) generator [14]. The kinematics of the generated events closely match those predicted by next-to-leading-order (NLO) calculations [15, 16]. The Alpgen leading-order MC event generator [17], interfaced to Pythia [18], is used to model $t\bar{t}$, $W$+jets, and $Z$+jets background events. We use the CTEQ6L1 parton distribution functions [19] and set the top quark mass to 170 GeV. We use GEANT [20] to simulate the response of the D0 detector to the MC events. The $t\bar{t}$ background is normalized to the predicted cross section [21]. The $Z$+jets contributions are normalized to NLO cross sections [22]. The $W$+jets background normalization as well as its jet flavor composition are obtained from data samples. We model the background from multijet production where a jet is misidentified as an isolated electron or muon using events from data containing lepton candidates which pass all of the lepton identification requirements except one, but otherwise resemble the signal events. We use Pythia to model diboson production.

We select 4519 lepton+jets events with at least one $b$-tagged jet, which are expected to contain $130 \pm 17$ t-channel (93 ± 14 s-channel) single top events with an acceptance of $(2.5 \pm 0.3)\% ((3.7 \pm 0.5)\%)$. The expected sample composition is shown in Table I. Systematic uncertainties in the signal and background models are described in detail in Ref. [11]. The main uncertainties are due to the jet energy scale (JES) corrections and the tag-rate functions (TRF), with smaller contributions from MC statistics, correction for jet-flavor composition in $W$+jets events, and from the $W$+jets, multijets, and $tt$ normalizations. The total uncertainty on the background is (8–16)% depending
on the analysis channel. Uncertainties on JES, TRFs and the modeling of $W+\text{jets}$ kinematics affect not only the normalization but also the shape of the discriminant distributions.

We apply three independent multivariate analysis techniques to separate the small $t$-channel single top signal from the large backgrounds, based on boosted decision trees (BDT) [23–25], Bayesian neural networks (BNN) [26, 27], and the matrix element (ME) method [28, 29]. These techniques and their application are described in detail in Ref. [11]. For this analysis we use the same set of variables as in the observation Letter [1]. However, only $t$-channel single top events are considered signal during the optimization, whereas $s$-channel single top events are included in the background, normalized to the SM expectation. Fig. 2 shows comparisons between the $t$-channel signal, the background model, and data for the three individual discriminants.

The three multivariate techniques use the same data sample but are not completely correlated. Their combination leads to increased sensitivity and a more precise measurement of the cross section. We achieve this by training a combination BNN which uses the three individual discriminant outputs as inputs. Fig. 3 shows the combination discriminant output for data superimposed on the background and signal models.

We verify the accurate modeling of the data in background-dominated control regions for the two main background categories. Fig. 4a shows the $t$-channel discriminant in a $W+\text{jets}$ dominated sample of 2-jet, 1-tag events with $H_T < 175$ GeV. Fig. 4b shows the $t$-channel discriminant in a $t\bar{t}$ dominated sample of 4-jet, 1-tag or 2-tag events with $H_T > 300$ GeV. These studies confirm that backgrounds are well-modeled across the full range of the discriminant output.

We use a Bayesian statistical analysis [30] to measure the production cross sections. In a first step we compute the two-dimensional posterior probability density as a function of both $t$-channel and $s$-channel single top quark cross sections. The combination discriminants for $t$-channel and $s$-channel single top, remaining background, and data are used to build a binned likelihood as a product over all analysis channels and bins. We assume

TABLE I: Number of expected and observed events in 2.3 $fb^{-1}$ for $e$ and $\mu$, and one and two $b$-tagged analysis channels combined, with uncertainties including both statistical and systematic components. The $t$-channel and $s$-channel contributions are normalized to their SM expectation.

<table>
<thead>
<tr>
<th>Source</th>
<th>2 jets</th>
<th>3 jets</th>
<th>4 jets</th>
</tr>
</thead>
<tbody>
<tr>
<td>$t$-channel</td>
<td>77 ± 10</td>
<td>39 ± 6</td>
<td>14 ± 3</td>
</tr>
<tr>
<td>$s$-channel</td>
<td>62 ± 9</td>
<td>24 ± 4</td>
<td>7 ± 2</td>
</tr>
<tr>
<td>$W+\text{jets}$</td>
<td>1829 ± 161</td>
<td>637 ± 61</td>
<td>180 ± 18</td>
</tr>
<tr>
<td>$Z+\text{jets}$</td>
<td>229 ± 38</td>
<td>85 ± 17</td>
<td>26 ± 7</td>
</tr>
<tr>
<td>$t\bar{t} \to \ell\ell, \ell+\text{jets}$</td>
<td>222 ± 35</td>
<td>436 ± 66</td>
<td>484 ± 71</td>
</tr>
<tr>
<td>Multijets</td>
<td>196 ± 50</td>
<td>73 ± 17</td>
<td>30 ± 6</td>
</tr>
<tr>
<td>Total prediction</td>
<td>2615 ± 192</td>
<td>1294 ± 107</td>
<td>742 ± 80</td>
</tr>
<tr>
<td>Data</td>
<td>2579</td>
<td>1216</td>
<td>724</td>
</tr>
</tbody>
</table>
a Poisson distribution for the observed counts, and flat prior probabilities for positive values of the t-channel and s-channel signal cross sections. Systematic uncertainties are described by Gaussian priors, and their correlations amongst all bins in all channels are preserved. The posterior probability density is shown in Fig. 5. Also shown are the SM expectation as well as several representative new physics models to illustrate the sensitivity of this analysis: flavor-changing neutral currents with a $Z$ boson coupling to the top and up quark with a strength of 4% of the SM coupling [4], a 4-quark-generations scenario with CKM matrix element $|V_{ts}| = 0.2$ [31], a top-flavor model with new heavy bosons at a scale $m_x = 1$ TeV [4], and a top-color model with a $t\bar{b}$ bound state (Top Pion) with a mass of $m_{\pi} = 250$ GeV [4].

![FIG. 5: Posterior probability density for t-channel and s-channel single top quark production in contours of equal probability density. Also shown are the measured cross section, SM expectation, and several representative new physics scenarios [4, 31].](image)

In a second step we obtain the t-channel posterior probability density from the two-dimensional posterior in Fig. 5 by integrating over the s-channel axis, thus not making any assumptions about the value of the s-channel cross section. We have analyzed ensembles of pseudo-datasets generated at several different t-channel and s-channel cross sections to verify the linearity of the measured t-channel cross section and its independence of the input s-channel cross section. From the t-channel posterior we extract the cross section and uncertainty for t-channel single top quark production as $3.14^{+0.94}_{-0.80}$ pb. We similarly extract the s-channel cross section as $1.05 \pm 0.81$ pb by integrating over the t-channel axis.

We compute the significance of the t-channel cross section measurement using pseudo-datasets generated from the background model (including SM s-channel single top) and taking all systematic uncertainties into account in a log-likelihood-ratio approach [2, 32]. For each pseudo-dataset we calculate the ratio of the probabilities for two hypotheses: that the pseudo-dataset is described by the background model only (including SM s-channel), and that it is described by SM t-channel single top plus backgrounds. We measure the p-value by counting the fraction of background-only pseudo-datasets with a ratio that is more signal-like than the one observed in data. The observed p-value is $8.0 \times 10^{-7}$, corresponding to a Gaussian significance of 4.8$\sigma$, and the expected p-value is $9.7 \times 10^{-5}$, corresponding to a Gaussian significance of 3.7$\sigma$.

![FIG. 6: (a) reconstructed top quark mass (b), light quark jet pseudorapidity multiplied by lepton charge (c), and t-channel top quark spin correlation (d, see text) for events with a ranked combination output > 0.91. The t-channel and s-channel contributions have been normalized to their measured cross sections.](image)

We have checked the consistency of the observed signal with SM t-channel events in several kinematic distributions. Fig. 6 shows comparisons between the observed data, the background model, and the t-channel signal for four different kinematic distributions for events with a ranked discriminant output > 0.91. Shown are four important kinematic variables for t-channel single top quark production: $H_T$; the reconstructed top quark mass; the lepton charge multiplied by the pseudorapidity of the leading non-b-tagged jet (cf. Fig. 1b); and the t-channel spin correlation in the optimal basis [33, 34], i.e. the cosine of the angle between the light quark jet and the lepton, both in the reconstructed top quark rest frame. While the background shapes resemble the signal in the high ranked discriminant output region, the presence of the t-channel signal is nevertheless clearly evident in each distribution.

In summary, we have presented the first direct evidence of the t-channel mode of single top quark production using 2.3 fb$^{-1}$ of data at the DØ experiment. We measure a t-channel cross section of $3.14^{+0.94}_{-0.80}$ pb and a s-channel...
cross section of $1.05 \pm 0.81$ pb. The measured cross sections are consistent with the SM expected values. The observed $t$-channel signal corresponds to an excess over the predicted background with a significance of $4.8 \sigma$.

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