Search for $B \to K^* \nu \bar{\nu}$ decays


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We present a search for the decays $B \to K^* \phi$ using $454 \times 10^6$ $B \bar{B}$ pairs collected at the $\Upsilon(4S)$ resonance with the BABAR detector at the SLAC PEP-II $B$-Factory. We first select an event sample where one $B$ is reconstructed in a semileptonic or hadronic mode with one charmed meson. The remaining particles in the event are then examined to search for a $B \to K^* \phi$ decay. The charged $K^*$ is reconstructed as $K^{*+} \to K_S^0 \pi^+$ or $K^{*+} \to K^+ \pi^0$; the neutral $K^*$ is identified in $K^{*0} \to K^+ \pi^-$ mode. We establish upper limits at 90% confidence level of $\mathcal{B}(B^+ \to K^{*+} \phi) < 8 \times 10^{-5}$, $\mathcal{B}(B^0 \to K^{*0} \phi) < 12 \times 10^{-5}$, and $\mathcal{B}(B^0 \to K^{*0} \phi) < 8 \times 10^{-5}$.
In the Standard Model (SM) the $b \to s \nu \tau$ process occurs via one-loop box or electroweak penguin diagrams, as shown in Fig. 1, and it is therefore expected to be highly suppressed. Due to the absence of photon penguin contributions and long distance effects, the corresponding rate is predicted in the SM with smaller theoretical uncertainties than $b \to s \ell^+ \ell^-$. In particular, the SM branching fraction for $B \to K^* \nu \tau$ is expected to be $(1.3^{+0.4}_{-0.3}) \times 10^{-5}$ [1]. However, this could be enhanced in many new physics (NP) scenarios, where several mechanisms contribute to the rate. In Ref. [1] nonstandard $Z^0$ coupling contributions are computed, giving an enhancement of up to a factor 10. Moreover, new sources of missing energy, such as light dark matter candidates [2] or unparticles [3, 4], could contribute to the rate and produce a final state with a $K^*$ [6] plus missing energy. The kinematics of the decay is described in terms of $s_{\nu\nu} = m^2_{\nu\nu}/m^2_B$, where $m_{\nu\nu}$ is the invariant mass of the neutrino pair and $m_B$ is the $B$ meson mass. NP effects can strongly affect the shape of the $s_{\nu\nu}$ distribution [1, 4], and this is taken into account in the present work to obtain a model independent limit.

A previous search by the Belle Collaboration [5] sets upper limits of $B(B^+ \to K^{*+} \nu \tau) < 1.4 \times 10^{-4}$ and $B(B^0 \to K^{*0} \nu \tau) < 3.4 \times 10^{-4}$ at 90% confidence level [6]. In this paper we present the first BABAR search for both neutral and charged $B \to K^* \nu \tau$ decays. The analysis is based on the data collected with the BABAR detector [7] at the PEP-II storage ring. The sample corresponds to an integrated luminosity of 413 fb$^{-1}$ at the $\Upsilon(4S)$ resonance, consisting of about 454 $10^6 B \bar{B}$ pairs. An additional sample of 41 fb$^{-1}$ was collected at a center of mass energy 40 MeV below the $\Upsilon(4S)$ resonance in order to study continuum events: $e^+ e^- \to q\bar{q} \ (q = u, d, s, c)$ and $e^+ e^- \to \tau^+ \tau^-$. Charged-track reconstruction is provided by a silicon vertex detector and a drift chamber operating in a 1.5 $T$ magnetic field. Particle identification is based on the energy loss in the tracking system and the Cherenkov angle in an internally reflecting ring-imaging Cherenkov detector. Photon detection is provided by a CsI(Tl) electromagnetic calorimeter (EMC). Finally, muons are identified by the instrumental magnetic-flux return.

Pairs of photons with invariant mass between 115 and 150 MeV/c$^2$ are considered as $\pi^0$ candidates. The $K^0_s$ candidates are reconstructed from pairs of oppositely charged pions.

A GEANT4-based [8] Monte Carlo (MC) simulation is used to model the detector response and test the analysis technique. Approximately $13 \times 10^6$ events are simulated where one $B$ meson decays to a signal candidate mode and the other $B$ decay is unconstrained (signal MC sample), and the kinematics of the signal decay is described by a pure phase space model. Simulated generic $B \bar{B}$ and continuum samples are used to investigate the background contamination and perform systematic studies.

Due to the presence of two undetected neutrinos in the final state, the $B \to K^* \nu \tau$ decays cannot be fully reconstructed. Hence, one of the two $B$ mesons produced in the $\Upsilon(4S)$ decay (the tagging $B$) is reconstructed in a semileptonic ($B_d$) or a hadronic ($B_{\text{had}}$) mode containing a charmed meson. Then a $K^*$ and missing energy are searched for in the rest of the event (ROE), defined as the set of tracks and EMC clusters not associated with the tagging $B$. The two tagging strategies provide non overlapping samples and the corresponding results can be combined as independent measurements. Selection criteria are applied to suppress the background contamination and an extended maximum likelihood fit is performed to extract the signal yields ($N_s$), which are finally used to determine the decay branching fractions ($B$). In general, these can be written as:

$$B = \frac{N_s}{\varepsilon \cdot N_{BB}}, \quad (1)$$

where $\varepsilon$ is the total signal efficiency measured with the signal MC sample and $N_{BB}$ the number of produced $B \bar{B}$ pairs. In the semileptonic (SL) tagged analysis we
adopt Eq. (1) and use control samples to correct for small data/MC disagreements in the efficiency. In the hadronic (HAD) analysis, in order to avoid large systematic uncertainties associated with the MC estimate of the reconstruction efficiency for the $B_{\text{had}}$, we normalize the branching fraction with respect to the number of data events with a correctly reconstructed $B_{\text{had}} (N_{B_{\text{had}}})$:

$$B = \frac{N_s}{\varepsilon_{B_{\text{sig}}} \cdot \varepsilon_{B_{\text{had}}}} \cdot \frac{\varepsilon_{B_{\text{had}}}}{\varepsilon_{B_{\text{had}}} \cdot \varepsilon_{B_{\text{had}}}} \cdot \frac{\varepsilon_{B_{\text{had}}}}{\varepsilon_{B_{\text{had}}}} \cdot \frac{\varepsilon_{B_{\text{had}}}}{\varepsilon_{B_{\text{had}}}} \cdot \frac{\varepsilon_{B_{\text{had}}}}{\varepsilon_{B_{\text{had}}}}$$

(2)

where $\varepsilon_{B_{\text{sig}}}$ is the efficiency related to the signal side reconstruction and selection, while $\varepsilon_{B_{\text{had}}}$ and $\varepsilon_{B_{\text{had}}}$ are the $B_{\text{had}}$ reconstruction efficiencies in events with generic $B \bar{B}$ decays and events containing the signal process, respectively; to account for differences among them, observed in the MC samples, their ratio $\varepsilon_{B_{\text{had}}} / \varepsilon_{B_{\text{had}}}$ is used in Eq. 2 as a correction factor.

The event selection starts from the reconstruction of the tagging $B$. In the SL analysis, we search for a $B \rightarrow D^{(*)} l \nu$ decay. Neutral $D$ mesons are reconstructed in the $K^{-}\pi^{+}\pi^{0}$, $K^{-}\pi^{+}\pi^{+}\pi^{-}$ and $K^{0}_{s}\pi^{+}\pi^{-}$ modes. Charged $D$ mesons are reconstructed in the $K^{-}\pi^{+}\pi^{0}$ and $K^{0}_{s}\pi^{+}\pi^{-}$ final states. The $D^{0}$ candidates are reconstructed in the $D^{*0} \rightarrow D^{0}\gamma$ channel and the $D^{*+}$ candidates in the $D^{*+} \rightarrow D^{0}\pi^{+}$ or $D^{*+} \rightarrow D^{+}\pi^{0}$ channels. Finally, a lepton (electron or muon) candidate is associated to the $D$ meson and a kinematical fit is performed to find the $B_{\text{sl}}$ decay vertex. Preliminary selection requirements are applied on the $D$ mass (within 0.07 GeV/$c^2$ of the nominal mass in the $K^{-}\pi^{+}\pi^{0}$ mode, within 0.04 GeV/$c^2$ elsewhere) and the momentum of the lepton in the center of mass (CM) frame ($|p_{B,\text{sl}}| > 0.8$ GeV/$c$). We also require the CM angle between the $B_{\text{sl}}$ and the $D^{(*)} l$ pair to satisfy $-5.0 < \cos\theta_{B,\text{sl}} < 1.5$, where $\cos\theta_{B,\text{sl}}$ can be calculated from the $D^{(*)} l$ four-momentum assuming that only one massless particle is missing:

$$\cos\theta_{B,\text{sl}} = \frac{2 E_{B,\text{sl}} E_{l,\text{sl}} - m_{B,\text{sl}}^2 - m_{l,\text{sl}}^2}{2 |p_{B,\text{sl}}| |p_{l,\text{sl}}|}$$

(3)

In Eq. 3, $m_{B}$ is the nominal $B$ mass, $E_{B,\text{sl}}$, $E_{l,\text{sl}}$, and $|p_{B,\text{sl}}|$, $|p_{l,\text{sl}}|$ are the expected $B$ energy and momentum, fixed by the energies of the beams and evaluated in the CM frame, and $|p_{B,\text{sl}}|$ is the $D^{(*)} l$ pair momentum in the CM frame. Values of $\cos\theta_{B,\text{sl}}$ out of the physical range $[-1,1]$ are due to resolution effects and missing particles in the $B_{\text{sl}}$ reconstruction. The distributions of the $D$ mass and the lepton momentum in the CM frame, after the reconstruction of the signal $B$, are shown in Fig. 2. The plots are made after the signal reconstruction since in case of multiple $B_{\text{sl}}$ candidates, the selection of the best one depends on the signal side reconstruction too, as will be discussed later; events where in the signal side a $K^{*-} \rightarrow K^{+}\pi^{0}$ channel is reconstructed are shown. If one $B \rightarrow D^{(*)} l \nu$ candidate can be reconstructed in the ROE with the same procedure adopted for the tag side, the event is selected as a control sample of double-tagged events for systematic studies.

In the HAD analysis, we reconstruct $B_{\text{had}}$ decays of the type $B \rightarrow D Y$, where $D$ refers to a charm meson, and $Y$ represents a collection of hadrons with a total charge of $\pm 1$, composed of $n_{1}\pi^{\pm} + n_{2}K^{\pm} + n_{3}K_{s} + n_{4}\pi^{0}$, where $n_{1} + n_{2} \leq 5$, $n_{3} \leq 2$, and $n_{4} \leq 2$. Using $D^{0}(D^{+})$ and $D^{0}(D^{+})$ as seeds for $B^{-}(\bar{B}^{0})$ decays, we reconstruct about 1000 different decay chains. Charmed mesons are reconstructed in the same final states used in the SL analysis, along with the additional channels $D^{+} \rightarrow K^{+}\pi^{+}\pi^{-}\pi^{0}$, $K^{0}_{s}\pi^{+}\pi^{-}\pi^{0}$, $K^{0}_{s}\pi^{+}\pi^{-}$ and $D^{0} \rightarrow D^{0}\pi^{0}$. $B_{\text{had}}$ candidates are selected by the two kinematical variables:

$$m_{ES} = \sqrt{E_{\text{beam}}^{2} - |p_{B,\text{sl}}|^{2}}$$

$$\Delta E = E_{B} - E_{\text{beam}}$$

(4)

where $E_{\text{beam}}$ is the beam energy and $E_{B}$ and $|p_{B}|$ are the energy and the momentum of the $B_{\text{had}}$ in the CM frame. For correctly tagged $B$ candidates, the $m_{ES}$ distribution peaks at the nominal $B$ mass value and $\Delta E$ at zero. Hence, a selection is applied by requiring $-0.09 < \Delta E < 0.05$ GeV and $5.270 < m_{ES} < 5.288$ GeV/$c^2$. The number of correctly reconstructed $B_{\text{had}}$ events, to be used in Eq. 2, is extracted from the $m_{ES}$ distribution of on-peak data. Background events are classified in four categories: combinatorial $B^{0}\bar{B}^{0}$, combinatorial $B^{+}B^{-}$, $e^{+}e^{-} \rightarrow \mu^{+}\mu^{-}$ and $e^{+}e^{-} \rightarrow q\bar{q}$ ($q = u, d, s$). Other sources of background are found to be negligible. For each category, we extract the $m_{ES}$ shape from MC simulations. The normalizations of the continuum contributions are taken from off-resonance data, scaled by the luminosity. The normalization of the $B\bar{B}$ contribution is extracted from a $\chi^{2}$ fit in the $5.22 < m_{ES} < 5.26$ GeV/$c^2$ region. The number of misreconstructed $B_{\text{had}}$ in the signal region is extrapolated from the fit and subtracted from the data yield. In Fig. 3 the $m_{ES}$ distributions for charged and neutral $B_{\text{had}}$ are shown: the
on-peak data are superimposed to the estimated background contribution. After background subtraction, including correction factors and systematic uncertainties that will be discussed later, we determine $N_{\text{had}} = (7.175 \pm 0.008 \text{(stat)} \pm 0.222 \text{(syst)}) \times 10^5$ for neutral $B_{\text{had}}$ and $N_{\text{had}} = (10.128 \pm 0.010 \text{(stat)} \pm 0.344 \text{(syst)}) \times 10^5$ for the charged $B_{\text{had}}$.

![FIG. 3: The $m_{\text{ES}}$ distributions for charged a) and neutral b) $B_{\text{had}}$. The points represent the on-peak data and the hatched area shows the estimated background contribution.](image)

For each reconstructed tagging $B$, we search for a $K^*$ candidate in the ROE. A neutral $K^*$ can be reconstructed in the $K^+ \pi^-$ mode, while a charged $K^*$ can be reconstructed in the $K^0_s \pi^+$ and $K^+ \pi^0$ channels. The number of tracks in the ROE is required to match exactly the number of expected tracks for the selected mode. The signal $B$ must have opposite flavor (inferred from the $K^*$ flavor) with respect to the tagging $B$.

If more than one $B_{\text{sl}}(B_{\text{had}}) - B_{\text{sig}}$ pair has been reconstructed, only one of them is selected. In the SL analysis, we adopt a Bayesian approach to define the probability that both signal and tag side have been correctly reconstructed, given a set $x$ of observed quantities:

$$P(TT|x) = \frac{P(x|TT)P(TT)}{\sum_i P(x|i)P(i)} , \quad i = TT, TF, FT, FF$$

where $TT$ ($FF$) indicates that both sides are correctly (wrongly) reconstructed and $TF$ ($FT$) that only the tag (signal) side is correctly reconstructed. The candidate with the highest $P(TT|x)$ is retained. The set $x$ is composed of the $x^2$ probabilities of the $B_{\text{sl}}$ and the $K^*$ vertex fit. The corresponding likelihoods and prior probabilities are modeled from MC simulations with truth information to identify the correctly reconstructed candidates. In the HAD analysis, if more than one $B_{\text{had}}$ is reconstructed, the best one is selected according to the smallest $\Delta E$; if there are multiple $K^*$ candidates associated to the best $B_{\text{had}}$, the one with a reconstructed mass closest to the world average value [9] is chosen.

Background contamination is reduced by applying a further selection on the $B\bar{B}$ candidates. Event shape variables, namely $\cos \theta_{B,T}$ (the angle between the tag side reconstructed momentum and the thrust axis [10] of the ROE) and $R_2$ (the ratio of the second and zeroth Fox-Wolfram moments [11]), are used to reject the continuum background. The $K^*$ mass ($m_{K^*}$) and, for the $K^0_s \pi^+$ mode, the $K^0_s$ mass ($m_{K^0_s}$) allow rejection of combinatorial $K^*$ candidates. We define the missing 4-momentum due to unreconstructed neutrinos as the difference between the $Y(4S)$ 4-momentum and the reconstructed tagging $B$ and $K^*$ 4-momenta. It is exploited in the selection through the combination $E_{\text{miss}}^* + |p_{\text{miss}}^*|$ (the sum of the missing energy and the missing momentum evaluated in the CM frame) and the angle $\cos \theta_{\text{miss}}^*$ (the azimuthal angle of the missing momentum in the CM frame). The extra neutral energy $E_{\text{extra}}$, defined as the sum of the energies of the EMC neutral clusters not used

<table>
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<tr>
<th>Variable</th>
<th>Mode</th>
<th>Range</th>
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<tr>
<td>$m_{D^*}^{PDG}$</td>
<td>$D^+$ modes</td>
<td>[-2.00,1.00]</td>
</tr>
<tr>
<td>$m_{D^*}^{PDG}$</td>
<td>$D^-$ modes</td>
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</tr>
<tr>
<td>$m_{D^*}^{PDG}$</td>
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<tr>
<td>$\Delta m$</td>
<td>$B^+ \rightarrow D^0(K^- \pi^+ \rho^0)^{\pm \mp} \nu$</td>
<td>[-0.035,0.035]</td>
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<td>$\Delta m$</td>
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<tr>
<td>$\Delta m$</td>
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<tr>
<td>$\Delta m$</td>
<td>$D^0 \rightarrow D\nu$</td>
<td>[0.14,0.15]</td>
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</table>

TABLE I: Discriminating variables used in SL and HAD analyses and specific selection requirements. Values given in the squared brackets represent the lower and upper selection criteria imposed on the respective quantity.

TABLE II: Further selection requirements applied to the $B_{\text{sl}}$ candidate ($m_{D^*}^{PDG}$ is the nominal $D$ mass [9]).
FIG. 4: Fit results for the extra EMC energy $E_{\text{extra}}$ a) - c) for the SL analysis and the neural network output $NN_{\text{out}}$ d) - f) for the HAD analysis. From left to right, $K^{*+} \rightarrow K^+\pi^0$, $K^{*+} \rightarrow K^0_\pi^+$ and $K^{*0} \rightarrow K^+\pi^-$. Data are shown as points, and the fit result is shown with a solid line. The dotted and dashed lines show the estimated signal and background contributions respectively.

to reconstruct either the tag or the signal $B$, is exploited, considering that signal events have no additional neutral particles produced in association with the $K^*$. The requirements applied on the selection variables described above are listed in Tab. I.

In the SL analysis, the selection is optimized in the MC samples by maximizing the Punzi figure of merit [12], given by $\varepsilon/(n_s/2 + \sqrt{N_b})$, where $\varepsilon$ is the total signal efficiency, $N_b$ is the number of expected background data events and $n_s = 1.285$ corresponds to a one-side 90% confidence level. We also refine the $B_{sl}$ selection with respect to the one applied before the choice of the best candidate, and the corresponding requirements are summarized in Tab. II, where, $\Delta m$ is the difference between the $D$ and $D^*$ masses, expected to be 142.17 ± 0.07 [9]. The total signal efficiency, evaluated with MC simulations, is given in Tab. III. The variable $E_{\text{extra}}$ is not used in the selection optimization, and its distribution is used in an extended maximum likelihood fit in order to extract the signal yield. Due to the lower bound on the energy of detected photons (50 MeV), the distribution of $E_{\text{extra}}$ is not continuous, so we define the likelihood in the following form:

$$
\mathcal{L}(N_s, N_b) = \frac{e^{-[(1-f_s)N_s + (1-f_b)N_b]}}{N_1!} \times \prod_{i=1}^{N_1} [P_{\text{sig}}(E_{\text{extra},i}|p_{\text{sig}})(1-f_s)N_s + P_{\text{bkg}}(E_{\text{extra},i}|p_{\text{bkg}})(1-f_b)N_b] \\
\times \frac{(f_sN_s + f_bN_b)^{N_0}e^{-(f_sN_s + f_bN_b)}}{N_0!}, \tag{6}
$$

where $N_s$ and $N_b$ are the expectation values for the numbers of signal and background events; $f_s$ and $f_b$
Table III: Expected signal and background yields ($N_s$ and $N_b$ respectively) from MC studies (assuming the SM $B$ for the signal) and results of the data fit, along with signal efficiencies, corrected for systematic effects. Expected signal yields are evaluated according to the SM expected $B$. The first error on the fitted signal yield and on $N_{B\text{had}}$ is statistical, the second is systematic. The corresponding upper limits are also quoted.

<table>
<thead>
<tr>
<th>$K^+$ mode</th>
<th>$K^+\pi^0$</th>
<th>$K^0\pi^+$</th>
<th>$K^+\pi^-$</th>
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<tr>
<td><strong>SL ANALYSIS</strong></td>
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<tr>
<td>Expected Yields</td>
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<tr>
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<td>4.07</td>
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<td>468</td>
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<td>$E_{\text{extra}}$ Fit Results</td>
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<tr>
<td>$N_s$</td>
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<td>$3 \pm 17 \pm 15$</td>
<td>$35 \pm 13 \pm 9$</td>
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<tr>
<td>Expected Yields</td>
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<tr>
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<td>$3 \pm 7 \pm 4$</td>
<td>$-10 \pm 9 \pm 6$</td>
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<tr>
<td>$N_b$</td>
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<td>$\varepsilon_{\text{sig}} \times 10^{-2}$</td>
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<td>5.2</td>
<td>16.6</td>
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<tr>
<td>$N_{B\text{had}} \times 10^5$</td>
<td>$10.128 \pm 0.010 \pm 0.344$</td>
<td>$7.175 \pm 0.008 \pm 0.222$</td>
<td></td>
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<tr>
<td><strong>UL (90% CL)</strong></td>
<td>$9 \times 10^{-9}$</td>
<td>$18 \times 10^{-9}$</td>
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</table>

are the fractions of signal and background events with $E_{\text{extra}} = 0$, and are fixed from the results obtained in the MC samples; $N_0$ and $N_1$ are the numbers of observed events with $E_{\text{extra}} = 0$ and $E_{\text{extra}} > 50$ MeV respectively; and $P_{\text{sig}}$ and $P_{\text{bkg}}$ are the probability distribution functions (PDF) for signal and background, depending on a set of parameters $p_{\text{sig}}$ and $p_{\text{bkg}}$ respectively. MC studies show that the background distribution is well described by a first-order polynomial PDF, while the signal shape can be parameterized with an exponential function and, in the charged modes, with an additional Landau contribution that accounts for photons from a tag side $D^*$ not associated to the $B_{\text{had}}$ during the reconstruction. The parameters of the PDFs are evaluated in the MC samples and fixed when fitting the real data. The fit strategy is validated by means of simulation studies which do not show any significant bias on the signal yields. The fits to the $E_{\text{extra}}$ distributions in the data sample are shown in Fig. 4 and the fitted yields are quoted in Tab. III along with the total efficiencies $\varepsilon$.

In the HAD analysis, we apply a loose selection (Tab. I), then all discriminating variables are used as inputs for a Neural Network (NN), whose output variable $NN_{\text{out}}$ is fitted in the region $NN_{\text{out}} > 0.6$, where the events from the signal MC sample are mostly concentrated. The upper bound of the fit region is different among the three $K^*$ modes, reflecting the shape of $NN_{\text{out}}$ in the signal MC sample. Three different NN are trained, one for each $K^*$ decay mode. The signal output is described with an exponential function for the $K^{*0} \rightarrow K^+\pi^-$ mode and a Crystal Ball PDF [13] for the charged $K^*$ channels. The background is parameterized by

$$f(x) \propto \frac{x + k_1}{1 + e^{k_2 x}}. \quad (7)$$

Also in this case, in the fit to real data the signal and background PDF parameters are fixed to the values extracted from the MC simulations. Simulated experiments are used to validate the fit strategy. The fits to the $NN_{\text{out}}$ distributions in the data sample are shown in Fig. 4, the fitted yields and the $B_{\text{sig}}$ efficiencies $\varepsilon_{B_{\text{sig}}}$ are quoted in Tab. III.

The branching fraction measurement is affected by systematic uncertainties related to the signal efficiency estimate, the $B$ normalization and the signal yield extraction from the fit.

The signal efficiency has an uncertainty due to the limited MC statistics. Control samples are used to estimate and correct for data/MC disagreement in the charged particle tracking, neutral particle reconstruction and particle identification. Uncertainties associated with the event selection criteria are computed depending on the specific selection strategy. Data/MC comparisons and expected detector resolutions provide an estimate of possible discrepancies in the distribution of the selection variables. For the SL analysis these values are used to vary the selection requirements and evaluate the impact on the efficiency; for the HAD analysis they are used to randomly smear the distributions of the NN inputs and
evaluate the impact on the efficiency after the NN cut. The uncertainty due to the residual model dependence of our measurement is estimated as follows. We apply a weight to each MC event, based on the generated value of $s_{ud}$, in such a way that the weighted distribution matches the expected distribution in the SM or some specific NP model. Then the efficiency is evaluated taking into account the weights and is compared to the nominal efficiency (obtained from the unweighted MC events, generated with a pure phase space model). For the SL analysis two further uncertainties are associated with the best candidate selection and the $B_s$ selection efficiency. The former is evaluated by modifying the input likelihoods of Eq. (5) according to data/MC comparisons. Concerning the $B_s$ selection efficiency, we apply a correction given by the square root of the data/MC ratio of the number of double-tagged events. Alternative approaches are used to compute the same correction factor and the largest discrepancy with respect to the nominal approach is taken as a systematic uncertainty.

The error on the number of produced $B\overline{B}$ events is estimated as described in Ref [14]. The systematic error for $N_{B_{\text{had}}}$, used in the HAD analysis, is computed by varying the MC $B\overline{B}$ component both in shape and normalization. The ratio $\varepsilon_{B_{\text{had}}}^{K^+\pi^-}/\varepsilon_{B_{\text{had}}}^{D^+\pi^-}$ is used to correct the tag yield and to assign further systematic uncertainties. Since the tagging efficiency depends on the global event multiplicity, this ratio is expected to be different from 1 and to depend on the signal side decay and the $B_{\text{had}}$ charge. From MC simulations it is found to be $1.008 \pm 0.007$ for the charged tag and $1.176 \pm 0.013$ for the neutral one.

The systematic uncertainties associated with the signal yield are due to the statistical errors on the PDF parameters (fixed from the MC sample) and potential data/MC disagreement for the shapes. We vary the parameters according to their statistical error and correlations.

### Table IV: Summary of systematic uncertainties on the signal efficiency, signal yield, and normalization.

<table>
<thead>
<tr>
<th>$K^*$ mode</th>
<th>$K^+\pi^0$</th>
<th>$K^0_S\pi^+$</th>
<th>$K^+\pi^-$</th>
<th>$K^+\pi^0$</th>
<th>$K^0_S\pi^+$</th>
<th>$K^+\pi^-$</th>
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<tbody>
<tr>
<td>SL ANALYSIS</td>
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<td></td>
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<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>MC statistics</td>
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<td>1.7</td>
<td>1.3</td>
<td>2.9</td>
<td>3.1</td>
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<td>–</td>
<td>–</td>
<td>–</td>
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<tr>
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The cross-feed between the different channels is found to be negligible in the MC events, but is included in the calculation for completeness. We extract the combined upper limits:

\[
\begin{align*}
B(B^+ \to K^{**}\bar{\nu}\bar{\tau}) &< 8 \times 10^{-5} \\
B(B^0 \to K^{*0}\nu\bar{\tau}) &< 12 \times 10^{-5} \\
B(B \to K^{*}\nu\bar{\tau}) &< 8 \times 10^{-5}.
\end{align*}
\]

(9)

In summary, we search for \(B \to K^*\nu\bar{\tau}\) decays in a data sample corresponding to 413 fb\(^{-1}\), collected by the BaBar experiment at the \(\Upsilon(4S)\) resonance. We do not observe a significant signal in any of the modes studied and set upper limits on the decays \(B^0 \to K^{*0}\nu\bar{\tau}\) and \(B^+ \to K^{**}\nu\bar{\tau}\), and the combined channel \(B \to K^*\nu\bar{\tau}\). Since no constraints were applied to the kinematics of the final state \(K^*\) meson, or the undetected \(\nu\bar{\tau}\) system, these results can be interpreted in the context of new physics models where invisible particles, other than neutrinos, are responsible for the missing energy [2–4]. In this way, the results presented here are model independent. These results represent the most stringent upper limits reported to date and they are still consistent with the SM expectation [1].

We are grateful for the extraordinary contributions of our PEP-II colleagues in achieving the excellent luminosity and machine conditions that have made this work possible. The success of this project also relies critically on the expertise and dedication of the computing organizations that support BaBar. The collaborating institutions wish to thank SLAC for its support and the kind hospitality extended to them. This work is supported by the US Department of Energy and National Science Foundation, the Natural Sciences and Engineering Research Council (Canada), the Commissariat à l’Energie Atomique and Institut National de Physique Nucléaire et de Physique des Particules (France), the Bundesministerium für Bildung und Forschung and Deutsche Forschungsgemeinschaft (Germany), the Istituto Nazionale di Fisica Nucleare (Italy), the Foundation for Fundamental Research on Matter (The Netherlands), the Research Council of Norway, the Ministry of Education and Science of the Russian Federation, Ministerio de Educación y Ciencia (Spain), and the Science and Technology Facilities Council (United Kingdom). Individuals have received support from the Marie-Curie IEF program (European Union) and the A. P. Sloan Foundation.

[6] Charge conjugation is implied throughout this document, unless explicitly stated, and \(K^+\) refers to \(K^*(892)\).