Measurement of Resonance Parameters of Orbitally Excited Narrow $B^0$ Mesons

We report a measurement of resonance parameters of the orbitally excited ($L = 1$) narrow $B^0$ mesons in decays to $B^{(*)}+\pi^-$ using 1.7 fb$^{-1}$ of data collected by the CDF II detector at the Fermilab Tevatron. The mass and width of the $B^0_{s1}^{(0)}$ state are measured to be $m(B^0_{s1}^{(0)}) = 5740.2^{+1.7}_{-1.8}(\text{stat.})^{+0.9}_{-0.8}(\text{syst.})$ MeV/c$^2$ and $\Gamma(B^0_{s1}^{(0)}) = 22.7^{+3.2}_{-3.0}(\text{stat.})^{+3.2}_{-3.2}(\text{syst.})$ MeV/c$^2$. The mass difference between the $B^0_s$ and $B_{s1}^{(0)}$ states is measured to be $14.9^{+2.2}_{-2.1}(\text{stat.})^{+1.4}_{-1.4}(\text{syst.})$ MeV/c$^2$, resulting in a $B^0_s$ mass of $5725.3^{+1.6}_{-1.5}(\text{stat.})^{+1.4}_{-1.5}(\text{syst.})$ MeV/c$^2$. This is currently the most precise measurement of the masses of these states and the first measurement of the $B^0_{s1}^{(0)}$ width.

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Mesons consisting of a light and a heavy quark are an interesting laboratory for the study of quantum chromodynamics, the theory of strong interactions. The role of the heavy-light quark mesons is similar to that played by the hydrogen atom in understanding quantum electrodynamics. The bound states of a \( b \) quark with either a light up or down quark are referred to as \( B \) mesons. The states with zero internal orbital angular momentum \((L = 0)\) and spin parity \( J^P = 0^- \) (\( B \)) and \( 1^- \) (\( B^* \)) are well established [1], but the spectroscopy of the orbitally excited states has not been well studied. For \( L = 1 \), the total angular momentum of the light quark is \( j = \frac{1}{2} \) or \( j = \frac{3}{2} \). With the addition of spin of the heavy quark, two doublets of states are expected: states with \( j = \frac{1}{2} \), named \( B_0^0 \) \((J = 0)\) and \( B_1^0 \) \((J = 1)\), and states with \( j = \frac{3}{2} \), named \( B_1^1 \) \((J = 1)\) and \( B_2^1 \) \((J = 2)\). These four states are collectively referred to as \( B^* \).

Heavy quark effective theory [2] predicts that the mass splitting within each doublet of a heavy-light quark meson is inversely proportional to the heavy quark mass \([2-8]\). The \( j = \frac{1}{2} \) states are expected to decay to \( B^1 \pi \) via an S-wave transition and to exhibit resonance widths in the range \( 100 - 200 \text{ MeV}/c^2 \) [9]. The \( j = \frac{3}{2} \) states are expected to decay to \( B^{*1} \pi \) via a D-wave transition and to have widths of \( 10 - 20 \text{ MeV}/c^2 \) [7, 8]. This Letter focuses on the \( B_1 \) and \( B_2^0 \) observed in \( B \pi \) final states. The decay \( B_1 \to \pi^+ \pi^- \) is forbidden by conservation of angular momentum and parity, while both \( B_2^* \to \pi \pi \) and \( B_2^* \to \pi \pi \) decays are allowed. Decays to a \( B^* \) are followed by \( B^* \to \gamma \), where the photon is not reconstructed in CDF due to its low energy. Because of the missing photon, the measured \( B \pi \) mass in \( B_1 \to B \pi \to B \pi \pi \gamma \) and \( B_2^* \to B \pi \to B \pi \gamma \) events is lower than the \( B^* \) mass by \( 45.78 \pm 0.35 \text{ MeV}/c^2 \) [1], resulting in an expected signal structure of three narrow \( B \pi \) peaks for the \( B_1 \) and \( B_2^0 \).

Previous measurements of properties of the \( j = \frac{3}{2} \) \( B_1^0 \) and \( B_2^0 \) mesons using inclusive or partially reconstructed decays did not separate the narrow states [10, 11] or were limited by low sample statistics [12]. Recently the D0 Collaboration resolved the \( B_1^0 \) and \( B_2^0 \) masses [13]. The superb mass resolution of the CDF II detector allows better precision and enables us to measure the \( B_2^0 \) width. Here, we present measurements of the masses of the \( B_1^0 \) and \( B_2^0 \) states and the width of the \( B_2^0 \) state. We reconstruct \( B^{*0} \) in \( B^+ \pi^- \) and \( B^+ \pi^- \) decays, where the \( B^+ \) candidates decay into \( J/\psi K^+ \), \( D^0 \pi^+ \), and \( D^0 \pi^+ \pi^- \) final states with \( J/\psi \to \mu^+ \mu^- \) and \( D^0 \to K^+ \pi^- \). Throughout this paper, any reference to a specific charge state implies the charge conjugate state as well.

We use a data sample of events produced in \( pp \) collisions at \( \sqrt{s} = 1.96 \text{ TeV} \) recorded by the CDF II detector at the Tevatron, corresponding to an integrated luminosity of \( 1.7 \text{ fb}^{-1} \). The components and performance parameters of CDF II [14] most relevant for this analysis are the tracking, the muon detectors, and the trigger on displaced vertices. The tracking system lies in a uniform axial magnetic field of \( 1.4 \text{ T} \). The inner tracking volume is instrumented with a layer of single-sided silicon microstrip detectors mounted directly on the beam pipe at a radius of \( 1.5 \text{ cm} \), and 7 layers of double-sided silicon that extend out to a radius of \( 28 \text{ cm} \) [15]. This system provides excellent resolution of the impact parameter, \( d_0 \), defined as the distance of closest approach of the track to the interaction point in the transverse plane. The outer tracking volume contains an open-cell drift chamber (COT) up to a radius of \( 137 \text{ cm} \) [16]. Muons are detected in planes of drift tubes and scintillators [17] located outside the hadronic and electromagnetic calorimeters. The muon detectors used in this study cover the pseudorapidity range \( \eta \leq 1.0 \), where \( \eta = -\ln \tan(\theta/2) \) and \( \theta \) is the polar angle measured from the proton beam.

A three-level trigger system selects events in real time. A dimuon trigger [14] requires two tracks of opposite charge that match track segments in the muon chambers and have a combined dimuon mass consistent with the \( J/\psi \) mass. An extremely fast tracker at level 1 (XFT) [18] groups COT hits into tracks in the transverse plane. A silicon vertex trigger at level 2 (SVT) [19] adds silicon hits to tracks found by the XFT, thus providing better-defined tracks and allowing candidate selection based on the impact parameter. A displaced vertex trigger [20] requires two tracks each with a scalar transverse momentum, \( p_T \), greater than \( 2 \text{ GeV}/c \) and with \( 0.12 < d_0 < 1 \text{ mm} \). Additionally, the intersection point of the track pair must be transversely displaced from the \( pp \) interaction point by at least \( 0.2 \text{ mm} \), and the pair must have a scalar sum \( p_T (1) + p_T (2) > (5.5 \text{ GeV}/c) \).

Decays \( B^+ \to J/\psi K^+ \) are reconstructed from the dimuon trigger data while decays \( B^+ \to D^0 \pi^+ (\pi^- \pi^-) \) are reconstructed from the displaced vertex trigger data. In each decay, the tracks are constrained in a three-dimensional kinematic fit to the appropriate \( B^+ \) vertex topology with the \( J/\psi \) and \( D^0 \) masses constrained to the world average values [1]. Each track compatible with originating from the same interaction point as the \( B^+ \) and not used to reconstruct the \( B^+ \) is considered as a pion candidate, and its 4-momentum is combined with that of the \( B^+ \) candidate to form a \( B^{*0} \) candidate. We search for narrow resonances in the mass difference distribu-
bution of \( Q = m(B^+\pi^+) - m(B^+) - m_\pi \), where \( m(B^+\pi^+) \) and \( m(B^+) \) are the reconstructed invariant masses of the \( B^+\pi^- \) pair and the \( B^+ \) candidate, and \( m_\pi \) is the pion mass.

The \( B^+ \) candidates are selected using independent artificial neural networks for each of the three \( B^+ \) decay modes. The neural networks are based on the NEUROBAYES package [21]. For the decays \( B^+ \to J/\psi K^+ \) and \( B^+ \to D^0\pi^+ \), we use the training and selection methods developed in Ref. [22]. For the decay \( B^+ \to \bar{D}^0\pi^+\pi^+\pi^- \) we closely follow the construction of the neural networks for the other two decays. To train this last neural network we use data from the region \( 5325 < m(B^+) < 5395 \) MeV/c\(^2\) as the background sample and simulated \( B^+ \) events as the signal sample [23]. The most discriminating inputs to the neural networks are \( p_T(B^+) \), \( d_0(B^+) \), \( d_0 \) of the kaon or pion with respect to the \( B^+ \) decay vertex, and the projected distance of the \( B^+ \) decay vertex from the primary vertex along the \( B^+ \) transverse momentum. We select approximately 51 500 \( B \) events in the \( J/\psi K^+ \) decay channel, 40 100 in the \( \bar{D}^0\pi^+ \) channel, and 11 000 in the \( \bar{D}^0\pi^+\pi^+\pi^- \) channel.

To select \( B^{*+0} \) mesons, three additional neural networks are trained on a combination of a simulated signal sample and real data for a background sample. The data for the background sample are taken from the entire \( Q \) range of 0 to 1000 MeV/c\(^2\), which includes only a small contribution from the signal in the data. To avoid biasing the network training, the simulated events are generated with the same \( Q \) distribution as the data. The \( B^{*+0} \) neural networks use the same inputs as the \( B^+ \) neural networks, together with the kinematic and particle identification quantities for the pion from the \( B^{*+0} \) decay. The most important discriminants are the \( p_T \) and \( d_0 \) of the pion from the \( B^{*+0} \) decay vertex and the output of the \( B^+ \) neural network.

For each \( B^+ \) decay channel, we require fewer than six \( B^{*+0} \) candidates in an event in order to enhance the signal-to-background ratio. The observed \( B^{*+0} \) signals are consistent for all three \( B^+ \) decay channels. Therefore we combine the \( B^{*+0} \) events for all decay channels and use this combined \( Q \) distribution to measure the \( B^{*+0} \) properties. We count the number of Monte Carlo signal events, \( N_{MC} \), and the number of signal and background events in the data, \( N_{data} \), in the \( Q \) signal region of 200 to 400 MeV/c\(^2\) for a given cut on each of the three network outputs. We then optimize the \( B^{*+0} \) selection for each \( B^+ \) decay channel to maximize the combined significance, \( N_{MC}/\sqrt{N_{data}} \). The resulting combined \( Q \) distribution is shown in Figure 1.

The \( B^{*+0} \) signal structure is interpreted as resulting from the three signal processes \( B^{0}_s \to B^{*+}\pi^- \), \( B^{0}_s \to B^{*+}\pi^+ \), and \( B^{*0}_s \to B^{*+}\pi^- \), with \( B^{*+} \to B^+\gamma \). The \( Q \) distribution for each signal process is modeled by a non-relativistic fixed-width Breit-Wigner function convoluted with the detector resolution model. The resolution on \( Q \) is determined from simulation and modeled as a sum of two Gaussian distributions, a dominant narrow core and a broad tail with \( Q \)-dependent standard deviations of about 2 MeV/c\(^2\) and 4 MeV/c\(^2\), respectively. The fraction of events in the broad tail is fixed to be 0.2.

We perform an unbinned maximum-likelihood fit to the combined \( Q \) distribution, from which we extract the \( Q \) value of the \( B^{*0}_s \to B^{*+}\pi^- \) decay, the mass difference between the \( B^{*+}_s \) and \( B^{0}_s \) states, the width of the \( B^{*0}_s \), and the number of events in each signal process. The following parameters in the fit are constrained to their values from either previous measurements or theoretical predictions: the energy of the \( B^{*+} \) decay photon, \( E(\gamma) = 45.78 \pm 0.35 \) MeV/c\(^2\) [1]; the ratio of the \( B^{*+}_s \) and \( B^{0}_s \) widths, \( \Gamma(B^{*+}_s)/\Gamma(B^{0}_s) = 0.9 \pm 0.2 \) [7]; and the ratio of the \( B^{*0}_s \) branching fractions, \( B_{BR}(B^{*0}_s \to B^{*+}\pi^-)/B_{BR}(B^{*0}_s \to B^{*+}\pi^+) = 1.1 \pm 0.3 \) [11], consistent with the value measured in Ref. [13].

The background is modeled by a sum of two components, each being the product of a power law and an exponential function. We also expect reflections from \( B^{*+}_s \to B^+K^- \) decays when the kaon is mistakenly assigned the pion mass. The shape of the reflection in the \( Q \) distribution is determined in simulations of \( B^{*+}_s \) states [22] and fixed in the fit. The normalization of the \( B^{*+}_s \) is obtained by correcting the observed yield from Ref. [22] by a ratio of efficiencies to reconstruct a \( B^{*+}_s \) decay as a \( B^{*+0} \) and \( B^{*0}_s \). In the \( B^{*+0} \) data sample we expect \( 24 \pm 12 B^{*+0}_{s1} \) events and \( 62 \pm 31 B^{*+0}_{s2} \) events. These
normalizations enter the fit as Gaussian constraints.

Sources of systematic uncertainty on the mass difference and width measurements include mass scale, mass-dependent signal efficiency, fit model bias, assumptions entered as Gaussian constraints in the fit, choice of background and resolution models, and location and amount of \( B^{*0} \) broad states. The systematic uncertainties are summarized in Table I.

To determine the mass scale uncertainty, we reconstruct \( \psi(2S) \to J/\psi \pi^+\pi^- \) with \( J/\psi \to \mu^+\mu^- \), which has a similar \( Q \) value as the \( B^{*0} \) decays. We compare the measured \( Q \) to the world average [1] and take the difference as the mass scale uncertainty. To evaluate the effect of signal efficiency with changing \( Q \), we generate a large number of samples of the same size as the data, called pseudoexperiments, with the \( Q \)-dependent efficiency obtained from simulation. We then apply the default fit to the pseudoexperiments.

Tests of the fit model on pseudoexperiments show a small fit bias on the \( B^{*0} \) signal parameters, which is included as a systematic uncertainty. Signal parameters entered as Gaussian constraints in the fit contribute to the fit uncertainty. To determine their systematic contribution, we refit the data with these constrained parameters fixed. This fit returns the statistical fit uncertainties, which are subtracted in quadrature from the total fit uncertainties to obtain the systematic contribution.

To estimate the uncertainties due to the choice of background and resolution models, we generate pseudoexperiments with varied background parameterizations or worse mass resolution. The background is also well-modeled by the sum of a broad Breit-Wigner function with the product of a power law and an exponential function. From comparisons of the detector resolution in data and Monte Carlo for the \( \psi(2S) \) sample, we expect the Monte Carlo to underestimate the resolution by no more than 20%. These pseudoexperiments are fit with the default fit and the generating model. The distribution of the differences between these fit results is modeled by a Gaussian, whose mean is assigned as the systematic uncertainty.

Possible effects of \( B_0^0 \) and \( B_1^0 \) decays on our background model are studied by adding two Breit-Wigner functions of identical width varied over the range 100–200 MeV/\( c^2 \). The \( Q \) values of the states are independently varied in the range 240 to 360 MeV/\( c^2 \), the region around the narrow \( B^{*0} \) peaks. We refit the data for various masses and widths of the broad states, with the normalizations of the broad Breit-Wigner functions as additional free parameters in the fit model. We then take the largest variation in the narrow \( B^{*0} \) parameters from any configuration of broad states as the systematic uncertainty due to the \( B^{*0} \) broad states.

The result of the likelihood fit to the data is shown in Figure 1, and we measure the following:

\[
m(B_2^{*0}) - m(B^+) - m_\pi = 321.5^{+1.7}_{-1.8} \text{(stat.)}^{+0.9}_{-0.7} \text{(syst.)} \text{ MeV}/c^2;
\]

\[
\Gamma(B_2^{*0}) = 22.7^{+3.8}_{-3.2} \text{(stat.)}^{+3.2}_{-1.0} \text{(syst.) MeV}/c^2.
\]

The signal is consistent with theoretical predictions [5, 6], and Gaussian-constrained parameters remain close to their input values, the largest departure being 0.4 standard deviations. The numbers of events are \( N(B_1^0) = 503^{+75}_{-68} \), \( N(B_2^{*0} \to B^+\pi^-) = 385^{+48}_{-45} \), and \( N(B_2^{*0} \to B^{*0}\pi^-) = 351^{+48}_{-35} \) where uncertainties are statistical only. Using the mass of the \( B^+ \) [1] and the correlations between the fit parameters, the masses of the \( B_1^0 \) and \( B_2^{*0} \) are \( m(B_1^0) = 5740.2^{+1.2}_{-1.8} \text{(stat.)}^{+0.9}_{-0.7} \text{(syst.)} \text{ MeV}/c^2 \) and \( m(B_2^{*0}) = 5725.3^{+1.6}_{-2.2} \text{(stat.)}^{+1.4}_{-1.5} \text{(syst.) MeV}/c^2 \). With the current statistics the data are also consistent with containing only the \( B_1^0 \) and \( B_2^{*0} \to B^+\pi^- \) peaks.

In summary, using the three fully reconstructed decays \( B^+ \to J/\psi K^+, \ B^+ \to D^0\pi^+, \ \text{and} \ B^+ \to D^0\pi^+\pi^- \), we observe two narrow \( B^{*0} \) states in the decays \( B_1^0 \to B^{*0}\pi^- \) and \( B_2^{*0} \to B^{(*)+}\pi^- \). This is the most precise measurement of the narrow \( B^{*0} \) masses to date. We have also measured the \( B_2^{*0} \) width for the first time. There is some discrepancy between these measurements and those reported by the D0 collaboration [13], the largest being close to a 3 \( \sigma \) difference in the mass splitting of the two \( B^{*0} \) states.

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[23] We use several single $b$ hadron simulations, all using the $B$ hadron $p_T$ and $y$ distributions obtained from $B$ decays in CDF Run II data. The $b$ hadron decays are generated with the EvtGen package, D. J. Lange, Nucl. Instrum. Methods A 462, 152 (2001). Monte Carlo samples that also contain the hadronization backgrounds were generated by the PYTHIA program, T. Sjöstrand et al., Comput. Phys. Commun. 135, 238 (2001).