Optical properties of ZnO/ZnS and ZnO/ZnTe heterostructures for photovoltaic applications

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Although ZnO and ZnS are abundant, stable, environmentally benign, their band gap energies (3.44 eV, 3.72 eV) are too large for optimal photovoltaic efficiency. By using band-corrected pseudopotential density-functional theory calculations, we study how the band gap, optical absorption, and carrier localization can be controlled by forming quantum-well like and nanowire-based heterostructures of ZnO/ZnS and ZnO/ZnTe. In the case of ZnO/ZnS core/shell nanowires, which can be synthesized using existing methods, we obtain a band gap of 2.07 eV, which corresponds to a Shockley-Quiesser efficiency limit of 23%. Based on these nanowire results, we propose that ZnO/ZnS core/shell nanowires can be used as photovoltaic devices with organic polymer semiconductors as p-channel contacts.

I. INTRODUCTION

The growing awareness of the consequences of greenhouse gas emissions associated with energy production has increased efforts to reduce the cost of solar energy conversion. Economical production of silicon-based photovoltaics are limited by the high cost and energy input required to create the highly purified silicon (comprising 40-50% of the cost of a finished photovoltaic module). Alternative approaches, such as thin-film devices, rely on toxic and somewhat less abundant CdTe and CdSe, and organic photovoltaics suffer from low efficiency and short-operating lifetimes (due to oxidative damage to the polymers), respectively.¹ Given this motivation, oxide-based semiconductor materials are attractive due to their abundance, chemical stability, and lack of toxicity—e.g., ZnO is widely used as a paint pigment and as a sunscreen. Besides merely using the bulk, one may also consider whether quantum-size effects may be useful, especially since there is a great deal of expertise in synthesizing ZnO nanowires both by
vacuum\textsuperscript{2,3} and solution-based\textsuperscript{4–6} methods. In addition, more complicated structures such as nanobelts\textsuperscript{7,8}, nanohelices\textsuperscript{9}, and others\textsuperscript{10–12} have been synthesized. Unfortunately, the ZnO band gap (3.4 eV) is too large for use in efficient photovoltaic devices.\textsuperscript{13} Nonetheless, this has not prevented numerous attempts to construct photovoltaics from this material, with schemes such as n-ZnO/p-CdTe thin film heterojunctions,\textsuperscript{14,15} ZnO/CdSe composites,\textsuperscript{16} n-ZnO/p-Cu\textsubscript{2}O heterojunctions,\textsuperscript{17,18} n-ZnO/p-Si heterostructures,\textsuperscript{19,20} ZnO-nanocrystal/organic-polymer hybrid photovoltaics,\textsuperscript{21–28} and ZnO-nanocolumns as electrodes for dye-sensitized photoelectrochemical cells.\textsuperscript{29}

One idea to reduce the band gap of ZnO is to stack it with another environmentally benign and abundant material, such as ZnS. Due to the staggered type-II band alignment, the band gap of the composite structure could be much smaller than either of the individual materials. The oscillator strength for such a transition would be small for two semi-bulk slabs, but in nanometer-scaled structures the spatial proximity of the band-edge wavefunctions to the interface would lead to an increase in the oscillator strength. Thus, it is critically important to know how small a band gap can be in these structures and how large the absorption can be near the band gap. We were encouraged by the variety of efficient experimental methods for the partial conversion of ZnO nanowires into ZnO/ZnS core/shell nanowires.\textsuperscript{30–36}

In this letter, we apply theoretical calculations to determine the optical properties of ZnO/ZnS and ZnO/ZnTe structures, and thus study whether these materials may be practical for photovoltaic devices. Since density functional theory (DFT) calculations perform poorly on the value of the band-gap, we utilize a band-corrected pseudopotential scheme which adds a small empirical correction to the \textit{ab initio} pseudopotential to reproduce the experimental bulk band-gaps. We then apply this approach to the study of two prototype systems: planar superlattices (shown in Figure 2a) and core/shell quantum wires (shown in Figure 4a), considering ZnO/ZnS and ZnO/ZnTe structures. Finally, we discuss the implications of these results for the creation of photovoltaic devices.

**II. METHODS**

Unless otherwise noted, all electronic structure calculations were performed using plane-wave norm-conserving pseudopotential DFT with the PETot code.\textsuperscript{37} In all of the results described here, the Zn 3\textit{d} electrons are included in the valence, and a 75 Ryd kinetic energy cutoff is used for the plane-wave basis. We first obtain the atomic norm-conserving local pseudopotential \(V_{\text{loc}}(\vec{r})\) and \((s, p, d\text{-dependent})\) nonlocal pseudopotential \(V_{\text{nonloc}}(\vec{r})\) from self-consistent local-density-approximation (LDA) calculations of atoms. However, as a result of the well-known deficiency of LDA, the resulting bulk calculations yield erroneous band gaps of 1.025, 1.981, and 1.163 eV for ZnO, ZnS, and
ZnTe, respectively, which are much smaller than the experimental values of 3.44, 3.8, and 2.391 eV.\textsuperscript{38}

To correct the band gap error, we modify the nonlocal part of the atomic pseudopotentials for the Zn, O, S, and Te atoms by adding extra potentials $\beta \sin(r\pi/r_c)/r$ (zero outside $r_c$, where $r_c$ is the cutoff radius used for the pseudopotential) to each of the $s$, $p$, $d$ nonlocal parts, where $\beta$ are empirical parameters fitted to reproduce the experimental bulk band gaps and other high-symmetry $k$-point band energies,\textsuperscript{38–41} as shown in Supplementary Table IS; we also fix the energy of the valence band maximum (VBM) to its original LDA result to avoid altering the valence band alignment. This “band-corrected pseudopotential” approach has been used previously for the treatment of nanocrystals\textsuperscript{42} and isovalent impurities\textsuperscript{43}. To minimize concerns about transferability, we fitted separate ZnO/ZnS and ZnO/ZnTe sets of parameters $\beta$, shown in Supplementary Tables IIS and IIIS, respectively. In the case of ZnTe we have also included the spin-orbit coupling using the relativistic Te pseudopotential yielding the experimental valence band splitting of 0.91 eV.\textsuperscript{38} Following this procedure, we obtain band gaps of 3.334/3.716 for the ZnO/ZnS fitting, and 3.361/2.337 for the ZnO/ZnTe fitting, with good ($\sim$ 0.1 eV) agreement with the experimental results.

To summarize, in the electronic structure calculations described below, we first perform a self-consistent calculation using the original \textit{ab initio} pseudopotentials to yield the local potential, then (non-self-consistently) calculate the corrected eigenenergies with this local potential plus the band-corrected nonlocal pseudopotentials. The wavefunctions and eigenenergies obtained from this step are used for the subsequent absorption spectrum calculations and wavefunction plots. The imaginary part of the dielectric function, which is proportional to the optical absorption spectrum by a volume factor, is calculated as a function of the photon frequency, $\omega$, as\textsuperscript{44}

$$
\epsilon_i(\omega) = \sum_{k, c, v} |\langle \phi_c(k) | \hat{p} | \phi_v(k) \rangle|^2 \delta(E_c(k) - E_v(k) - \hbar\omega),
$$

where $e$, $m$, and $V$ are the electron charge, electron mass, and volume of the system, the summations over $k$, $c$, and $v$ run over the k-points, conduction-bands, and valence bands, respectively, for the eigenstates $\phi_c(k)$ and eigenenergies $E_c(k)$, respectively, and the $\hat{p}$ is the momentum operator. The spectra results shown in Figure 2 and Figure 4 include a gaussian broadening term of 20 meV.
FIG. 1: Calculated VBM and CBM alignments for (a) ZnO/ZnS and (b) ZnO/ZnTe. The solid lines show the strained band alignments for the heterostructures similar to Figure 2a, and the dashed lines show the calculated natural band alignments. The blue arrows indicate the effective band gap due to the transition from the VBM of ZnS (ZnTe) to the CBM of ZnO.

III. RESULTS

A. Bulk heterostructures

In this section, we examine the cases of planar heterostructure superlattices, shown schematically in Figure 2a. To obtain the geometry we constructed a model consisting of the interfaces between zincblende ZnO and ZnS (ZnTe) slabs in the (001) direction each consisting of 7 monolayers (Figure 2a). There is significant lattice mismatch, since the corresponding bulk zincblende lattice constants for ZnO, ZnS, and ZnTe are 4.6 Å, 5.42 Å, and 6.1 Å, respectively.

To find the optimal geometry within such planar zinc-blende structure, the supercell was optimized with respect to three independent lattice parameters: $a$, $c_1$, $c_2$, where $c_1$ and $c_2$ are the z-direction lattice constants in the ZnO and ZnS(ZnTe) slabs in the supercell, respectively, and $a$ is the lattice constant along the x- and y-directions. This relaxation was performed by ultrasoft-pseudopotential projector augmented wave (PAW) generalized gradient approximation (GGA) DFT calculations, using the commercial VASP program. From this geometry, the optical properties were calculated using the norm-conserving pseudopotential/band-correction approach discussed in Section II, using 200 irreducible $k$-points to sample the Brillouin zone.

We first examine the bulk band alignments of ZnO/ZnS and ZnO/ZnTe. Our calculated results are shown in Figure 1. The valence band alignments were determined from the difference of the VBM energies of the bulk materials (calculated by self-consistent LDA with the ab initio pseudopotentials), then adjusted by the offset of the electrostatic potential in the strained superlattice. The natural valence band alignments (defined as the band alignment when the two materials are both at their natural lattice constants without strain) were then deduced by subtracting both the uniaxial and hydrostatic strain effects using the recent absolute valence band deformation potentials of Li et al.\textsuperscript{46,47}
The conduction bands were then determined by adding the gaps calculated with the band-corrected pseudopotentials for strained and unstrained bulk materials. In the present calculations, the effect of the crystal-field splitting (due to uniaxial strain) is much larger than the absolute deformation potential term (due to hydrostatic strain), which explains why even though the volume changes have opposite signs for the ZnO and ZnS(ZnTe) regions, the strained VBM energies are both higher than the natural band energies for both materials. Our calculated natural valence band alignments are in good agreement with recent theoretical results by Moon et al., while it is in disagreement with the earlier band alignment results of Ref. 49 for the reasons discussed in Ref. 46. Note that our subsequent calculations are performed directly, and do not suffer from any of the assumptions of the nature of the absolute deformation potentials. For ZnO/ZnS (Figure 1a) we observe a staggered Type-II band alignment for both the strained and natural cases. The strain has a large effect, shifting the band gaps from the unstrained bulk values (dashed lines) of 3.334/3.716 eV for ZnO/ZnS to the strained bulk values (solid lines) of 2.614/3.494 eV. Similarly, due to the even larger lattice mismatch between the ZnO/ZnTe interface (Figure 1b), the band gaps are shifted from 3.361/2.337 eV for unstrained ZnO/ZnTe (dashed lines) to 2.615/1.364 eV for the strained bulk materials (solid lines). The strain also reduces the energy of the transition between the top of the bulk ZnS (or ZnTe) valence band to the bottom of the bulk ZnO conduction band (without the quantum confinement effects discussed below), from 2.39 eV to 1.82 eV in ZnO/ZnS and from 1.01 eV to 0.42 eV in ZnO/ZnTe. Thus, the strain can also be used to reduce the total system band gap. Depending on the geometry of the nanostructure, the strain effect can be varied, providing a degree of freedom for band gap engineering.

To study the effects of nanometer scale confinement in superlattices, we examined first the ZnO/ZnS heterostructure, shown in Figure 2a and Figure 2b, using the band-corrected pseudopotential approach described in Section II. The first absorption peak occurs at 2.316 eV (indicated by the red arrow in Figure 2b). This corresponds to the direct transition between the valence band maximum (VBM) and conduction band minimum (CBM) in the interface area, as can be seen clearly in the VBM and CBM wavefunctions plotted in Figure 3a,b. The band edge states are predominantly localized either in one material or the other, but that the interface atoms have significant overlap of the VBM and CBM. We find that the oscillator strength of lowest energy transition is 3% of the magnitude of the VBM-to-CBM transition in bulk ZnO. The imaginary part of the dielectric constant at the VBM-to-CBM edge is 0.017, which is quite small. While from the band alignment of Figure 1a, it might be expected that the absorption onset should occur at 1.8 eV, in this structure, the quantum confinement effects lead to an increase in the band gaps in the superlattice. This illustrates a trade-off when making these types of nanometer-scale structures: namely,
FIG. 2: (a) Relaxed geometry for the ZnO/ZnS bulk heterostructure superlattice interface, demonstrating the type of geometry discussed in Section III A. Below are the calculated optical-absorption for the (b) ZnO/ZnS and (c) ZnO/ZnTe bulk-heterostructures. The red arrows indicate the values of the lowest observed peaks, and the vertical red (ZnO) and blue (ZnS or ZnTe) dashed lines correspond to the bulk band gaps. The sharp peak features result from the finite (200) number of $k$-points used in the calculation.

decreasing the layer thickness improves the oscillator strength for transitions between the two materials by bringing the spatially-localized band-edge wavefunctions closer to each other, but at the same time, quantum confinement effects increase the band gap which is quite the opposite of our goal.

Next we consider a similar type of planar heterostructure comprised of ZnO/ZnTe. In Figure 2c, see the first peak at 1.168 eV, similar to the bulk Si band gap. As in the previous ZnO/ZnS case, the band-edge wavefunctions for this ZnO/ZnTe heterostructure are localized in the two different materials, as shown in Figure 3c,d, and this lowest transition has an oscillator strength which is 4% of the direct VBM-to-CBM transition in bulk ZnO. The imaginary part of the dielectric constant at 1.2 eV is 0.11, much greater than silicon at this wavelength. The increase in the dielectric constant, as compared to the ZnO/ZnS structure discussed above, results from a combination of the higher
(a) ZnO/ZnS VBM
(b) ZnO/ZnS CBM
(c) ZnO/ZnTe VBM
(d) ZnO/ZnTe CBM

FIG. 3: Band edge wavefunction plots for the bulk heterostructures, with positive and negative signs indicated by green and red, respectively. (a) Valence band maximum (VBM), and (b) conduction band minimum (CBM) for ZnO/ZnS heterostructure. (c) VBM, and (d) CBM for ZnO/ZnTe heterostructure. The ZnO/ZnTe plots, which were calculated including spin-orbit coupling, only show the real part of the spin-up component; the spin-down component is qualitatively similar.

oscillator strength and the lower energy in the denominator term of Eq.(1). As in the case of the ZnO/ZnS case, quantum confinement has significantly increased the band gap as compared to the strained band alignment in Figure 1b.

B. Heterostructured quantum wires

For the superlattice heterostructures discussed above, there is a trade off between the oscillator strength and quantum confinement effects for solar cell applications, especially for ZnO/ZnS. In addition, the large elastic strain might render synthesis of the large area superlattice heterostructures difficult. Thus, it is worthwhile to explore other geometries where the strain profiles are different. We focus here on ZnO/ZnS, due to its benign environmental properties, and the need to further reduce the band gap identified in the above discussion. Here we examine ZnO/ZnS core/shell quantum wire, shown schematically in Figure 4a. This structure consists of an interior core of ZnO with radius 11.7 Å (about 4 monolayers), surrounded by a shell of 4 monolayers of ZnS, for a total radius of 23.4 Å. This relatively small nanowire is considered to obtain appreciable oscillator strength. Similar ZnO/ZnS core/shell nanowires have been synthesized experimentally although with much larger diameter.\textsuperscript{2,4,30–36} We note that our structure is much larger than the very narrow ZnO nanowires which recent DFT calculations have shown to undergo structural
FIG. 4: (a) Relaxed geometry for the ZnO/ZnS core/shell nanowire discussed in Section III B. (b) Calculated optical-absorption using the band-corrected pseudopotentials. The vertical red (ZnO) and blue (ZnS) dashed lines correspond to the bulk band gaps, and the vertical orange line corresponds to the band gap of the planar ZnO/ZnS heterostructure of Figure 2b, discussed in Section III A.

transformations to graphitic structures,\textsuperscript{50} so we use the wurtzite structure. Structural relaxation were performed using the generalized valence force field (G-VFF) model.\textsuperscript{51} The parameterizations developed to reproduce the experimentally observed elastic constants (from Ref. 38) are shown in Supplementary Table IVS. In the case of ZnO, we used the relationship of Martin\textsuperscript{52} to transform the experimental wurtzite elastic constants into the equivalent (hypothetical) zinc-blende form used to fit the G-VFF parameters. For the optical calculations 25 irreducible $k$-points are used to sample the periodicity along the wire axis.

Although the first pronounced peak in Figure 4 occurs at 2.070 eV, this is due to transitions from the two valence band states below the VBM (shown in Figure 5a,b) to the CBM (Figure 5d); the transition between the VBM (Figure 5c) and CBM at 1.935 eV is zero due to symmetry. This is due to an inplane anti-inversion symmetry of the VBM envelope function, as shown in Figure 5c, resulting in an envelope-function induced dark exciton. For solar cell applications, this dark exciton can suppress electron-hole recombination, thus enhancing the carrier collection efficiency.
FIG. 5: Band edge wavefunctions of the ZnO/ZnS core/shell nanowire calculated in Section III B, with positive and negative signs indicated by green and red, respectively. (a) VBM-2; (b) VBM-1; (c) VBM; (d) CBM. The peak at 2.07 eV in Figure 4 arise from the transition between (a)→(d) and (b)→(d); (c)→(d) has a very small oscillator strength.

The absorption peak at 2.070 eV is a 0.3 eV improvement upon the ZnO/ZnS heterostructure case studied in Section III A, and the imaginary dielectric constant at this peak is 0.06, which is also larger than that of the first peak in the ZnO/ZnS superlattice (Figure 2b). Thus, the ZnO/ZnS core/shell nanowire improves upon both the bandgap and oscillator strength of its superlattice counterpart. However, the core/shell nanowire does have reduced absorption at higher photon energies when compared to the planar ZnO/ZnS heterostructure (Figure 2b), although this is not too grave of a problem for solar cell applications, since it is still larger than the lower energy absorption. The valence band-edge wavefunctions responsible for the first absorption peak (Figure 5a-b) are predominantly localized in the exterior ZnS layer and the CBM (Figure 5d) predominantly localized in the the interior ZnO core, much like the behavior for the planar heterostructure in Figure 3a,b. From our analysis in the previous section on the competition between strain and quantum confinement effects, we can make a few general remarks on the properties of larger structures. First, strain is a useful property to take advantage of as it is observed to reduce the band gap for these materials, and these types of nanostructures can accommodate strains which may not be possible in planar heterostructures. Second, as the size of the system is increased, quantum confinement effects would be reduced, which leads to a smaller band gap, although at the penalty of a smaller oscillator strength. To estimate how large an oscillator strength is sufficient for
FIG. 6: Absorption length calculations, as a function of light energy. The blue and green lines indicate the values calculated for the ZnO/ZnS and ZnO/ZnTe planar heterostructures discussed in Section III A; the red line indicates the value calculated for the ZnO/ZnS core/shell nanowire discussed in Section III B. The dotted black line shows the experimental data for bulk Si at 300K.\textsuperscript{53–55}

Photovoltaic applications, one can compare the absorption coefficient near the band edge to that of bulk Si at room temperature.\textsuperscript{53} The bulk Si near edge absorption comes from the phonon-assisted transition, which is much smaller than the band edge absorption of 0.06 calculated for the ZnO/ZnS nanowire. To emphasize this point, in Figure 6 we show the calculated absorption length (in microns) for the planar and nanowire nanostructures studied in the present paper, as compared to the experimental data for bulk silicon at 300K.\textsuperscript{53–55} We find that all of the nanostructures studied in this work have an absorption length on the order of microns, comparable to that of bulk silicon. Thus an equivalent overall volume of the packed nanowires will be sufficient to absorb incident light as well as Si devices.

Photovoltaic device operation involves three processes: light absorption, carrier separation, and carrier collection. Concerning light absorption, as shown in Figure 6, a similar film thickness is required as in bulk Si solar cells. This can be achieved by growing long ZnO nanowires\textsuperscript{2,4,6} and packing many nanowires together on a surface. Concerning carrier separation, the natural separation of the electron and hole into the ZnO and ZnS regions reduces the barrier to exciton dissociation and carrier separation under the electric field of the electrodes. Finally, concerning carrier collection in the contacts, we can take advantage of the localization of the VBM in the exterior ZnS layer (as shown in Figure 5a) for these core/shell wires. One can imagine constructing a device in which the ZnO makes a direct connection to one contact (e.g., a conductive glass substrate\textsuperscript{58}), and the hole, after separating into the ZnS region is extracted from the nanowire into a surrounding p-channel organic semiconductor, e.g. poly(3-hexylthiophene)
(P3HT), which are typically more conductive and air stable than typical $n$-channel polymers.$^{59}$

IV. CONCLUSIONS

The calculations presented in this work demonstrate that the formation of ZnO/ZnS and ZnO/ZnTe nanoheterostructures can substantially reduce the optical band-gap, while simultaneously maintaining required optical absorption. Using the Shockley-Quiesser$^{13}$ model as guidance for the theoretical limit of ideal solar cell efficiency, we obtain efficiency limits of 19% and 30% for planar ZnO/ZnS and ZnO/ZnTe quantum-well heterostructures and 23% for ZnO/ZnS core/shell quantum wires. In all cases, this shows a dramatic improvement over bulk ZnO, which has a theoretical efficiency limit of only 7%. We also find dark exciton formation in the ZnO/ZnS nanowire which could improve the carrier collection in solar cells by reducing the exciton recombination rate. In conclusion, the current results demonstrate the feasibility of the scheme proposed in Section III B, and it is our hope that this will stimulated more detailed experimental investigation. Many other features of the ZnO/ZnS system can be explored in the future to further reduce the band gap and increase the oscillator strength, including piezoelectric effects, alloying, and interfacial roughening.

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Supporting Information Available: Tables listing the band-structure fitting points, band-correction potential terms, and the bulk elastic constants. This material is available free of charge via the Internet at http://pubs.acs.org

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