Minijet deformation and charge-independent two-particle correlations on momentum subspace \((\eta, \phi)\) in Au-Au collisions at \(\sqrt{s_{NN}} = 130\) GeV

We present first measurements of charge-independent correlations on momentum-space difference variables $\eta_1 - \eta_2$ (pseudorapidity) and $\phi_1 - \phi_2$ (azimuth) for charged primary hadrons with transverse momentum within $0.15 \leq p_t \leq 2$ GeV/c and $|\eta| \leq 1.3$ from Au-Au collisions at $\sqrt{s_{NN}} = 130$ GeV. We observe strong charge-independent correlations associated with minijets and elliptic flow. The width of the minijet peak on $\eta_1 - \eta_2$ increases by a factor 2.3 from peripheral to central collisions, suggesting strong coupling of partons to a longitudinally-expanding colored medium. New methods of jet analysis introduced here reveal nonperturbative medium effects in heavy ion collisions.

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Correlations and fluctuations access properties of the colored medium produced in ultrarelativistic heavy ion collisions.
collisions at RHIC \cite{1,2,3}. In-medium modification of string fragmentation and hard parton scattering in heavy ion collisions should affect large-momentum-scale correlations ($|\phi_1 - \phi_2| \sim \pi/2$, $|\eta_1 - \eta_2| \sim 1$). Charge-independent correlations are produced by initial-state multiple scattering (Cronin effect \cite{4}, minijet production \cite{3}) and in-medium dissipation \cite{4}. Previous studies of parton-medium interactions included angular correlations of high-$p_t$ particles (e.g., leading-particle $p_t > 4$ GeV/c) in which the away-side jet structure was strongly reduced in central Au-Au collisions \cite{6}. Theoretical descriptions of parton energy loss and medium-modified fragmentation include, respectively, pQCD-based jet-quenching models \cite{5,8} and parton recombination models \cite{9}.

In this Letter we report the first measurements in heavy ion collisions of charge-independent joint autocorrelations \cite{10} on difference variables $\phi_\Delta \equiv \phi_1 - \phi_2$ (azimuth) and $\eta_\Delta \equiv \eta_1 - \eta_2$ (pseudorapidity) for charged particles with $0.15 \leq p_t \leq 2$ GeV/c. The observed correlation structure is dominated by minijets and elliptic flow. These low-$p_t$ measurements of jet correlations suggest that in central collisions strong coupling of partons to a longitudinally-expanding medium \cite{11} produces dramatic changes in the angular distributions of parton fragments not anticipated by theoretical models \cite{5,8,12}.

This analysis is based on $\sqrt{s_{NN}} = 130$ GeV Au-Au collisions observed with the STAR detector at the Relativistic Heavy Ion Collider (RHIC).

The charge-independent (CI - all charged particles) autocorrelations obtained in this study access the complete structure of two-particle density $\rho(\vec{p}_1, \vec{p}_2)$ projected onto momentum-space variables $(\eta_1, \eta_2, \phi_1, \phi_2)$. Differential analysis is achieved by comparing distributions of particle pairs taken from single events (sibling pairs) with particles paired from different but similar events (mixed pairs). The corresponding correlation function and ratio distribution are defined by

$$C(\vec{p}_1, \vec{p}_2) = \rho_{mix}(\vec{p}_1, \vec{p}_2) [r(\vec{p}_1, \vec{p}_2) - 1],$$

$$r(\vec{p}_1, \vec{p}_2) = \rho_{sib}(\vec{p}_1, \vec{p}_2)/\rho_{mix}(\vec{p}_1, \vec{p}_2).$$

Pair densities $\rho(\vec{p}_1, \vec{p}_2)$ are projected onto variable pairs $(\eta_1, \eta_2)$, $(\phi_1, \phi_2)$ and $(\eta_\Delta, \phi_\Delta)$ as histograms $n_{ij} \simeq \epsilon_x \epsilon_y \rho(x_i, y_j)$, where $\epsilon_x, \epsilon_y$ are bin widths on $x, y \in \{\eta, \phi, \eta_\Delta, \phi_\Delta\}$. Sibling- and mixed-pair histograms are separately normalized to the total number of detected pairs in each event class: $n_{ij} = n_{ij}/\sum_{ij} n_{ij}$. Normalized ratios $\tilde{n}_{ij} = n_{ij,sib}/n_{ij,mix}$ are the basis for this analysis.

Data for this analysis were obtained with the STAR detector \cite{13} using a 0.25 T uniform magnetic field parallel to the beam axis. Event triggering and charged-particle measurements with the time projection chamber (TPC) are described in \cite{13}. Track definitions, tracking efficiencies, quality cuts and primary-particle definition are described in \cite{14,15}. Tracks were accepted in $|\eta| \leq 1.3$, $0.15 \leq p_t \leq 2$ GeV/c and full azimuth. Particle identification was not implemented. Corrections were made to $\tilde{r}$ for two-track inefficiencies due to track merging and splitting \cite{16}. Small-scale momentum correlations (SSC) due to HBT and Coulomb effects \cite{17} were suppressed by eliminating track pairs with $|\eta_\Delta| < 0.3$, $|\phi_\Delta| < \pi/6$, $|p_{t1} - p_{t2}| < 0.15$ GeV/c, if $p_t < 0.8$ GeV/c for either particle. Ratios were formed from subsets of events with similar centrality (multiplicity differs by $\leq 50$) and primary-vertex location (within 7.5 cm along beam axis) and combined as weighted averages within each centrality class. Four centrality classes (labeled (a) - (d) from central to peripheral) were defined \cite{13} by cuts on track multiplicity $N$ within the acceptance, relative to endpoint $N_0$ \cite{19}.

If correlation structure is invariant on sum variables $\eta_1 + \eta_2$ and $\phi_1 + \phi_2$, as in these heavy ion collisions \cite{20}, distributions $\tilde{r}$ can be projected along those sum variables to form 1D autocorrelations on corresponding difference variables without information loss. 2D joint autocorrelations on difference variables $(\eta_\Delta, \phi_\Delta)$ then compactly represent all correlations on momentum subspace $(\eta_1, \eta_2, \phi_1, \phi_2)$ using only two variables. Plotted in Fig. \ref{fig} are perspective views of CI joint autocorrelations $\bar{N}(\tilde{r} - 1)$ on $(\eta_\Delta, \phi_\Delta)$ for central (a) to peripheral (d) collisions.

FIG. 1: Perspective views of two-particle CI joint autocorrelations $\bar{N}(\tilde{r} - 1)$ on $(\eta_\Delta, \phi_\Delta)$ for central (a) to peripheral (d) collisions.
We expect back-to-back ($\phi_\Delta \sim \pi$) azimuth correlations from momentum conservation in hard parton scattering. However, at low $p_t$ the away-side di-jet structure is broad, and indistinguishable from the dipole $\cos(\phi_\Delta)$ component describing momentum conservation in the bulk system. We subtract dipole and quadrupole $\cos(2\phi_\Delta)$ components from distributions in Fig. 1 to obtain Fig. 2 by minimizing their residuals on the away side ($|\phi_\Delta| > \pi/2$) and for $|\eta_\Delta| \sim 2$. The same-side 2D peaks in this figure are the main subject of this analysis. We observe that the away-side hemicylinder in Fig. 2 is featureless, even for the most peripheral collisions. If Lund-model strings [21] remained dynamically relevant we would expect in this $p_t$ interval significant correlation structure on the away side of Fig. 2, a prominent gaussian on $\eta_\Delta$ due to local charge conservation as observed in p-p collisions [22,23]. Lack of such structure suggests that longitudinal strings are not significant, even for the most peripheral collisions in this study (Fig. 2d).

The same-side peak isolated by the multipole subtraction varies strongly with centrality, transitioning from nearly symmetric on ($\eta_\Delta, \phi_\Delta$) for peripheral collisions to dramatically broadened along $\eta_\Delta$ for the more central collisions. The small excess in (0,0) bins is due to conversion-electron pairs. SSC pair cuts reduce the bins nearest (0,0) by 10\% or less. 1D projections and model fits on difference variables $\phi_\Delta$ and $\eta_\Delta$ are shown in Fig. 4. Solid dot (open triangle) data symbols correspond to $\eta_\Delta$ ($\phi_\Delta$) projections.

Statistical errors for joint autocorrelations approximately double as $|\eta_\Delta|$ increases from 0 to 2 because of limited $\eta$ acceptance, but are uniform on $\phi_\Delta$ because $\phi$ is periodic. Statistical errors for $\hat{r}$ at $|\eta_\Delta| = 0$ vary from 0.0001 for central collisions to 0.001 for peripheral collisions. Statistical errors for $\hat{N}(\hat{r} - 1)$ ($\sim 0.1$) are nearly independent of centrality. Systematic errors were estimated as in [14]. Contamination from photon conversions to $e^\pm$ pairs is significant only within the bin defined by $|\eta_\Delta| < 0.1$, $|\phi_\Delta| < 0.1$ which was excluded from model fits. The dominant source of systematic error is non-primary background [15], whose correlation with primary particles is unknown and is estimated by assuming correlations vary from zero to the measured correlation amplitude for primary particles [14]. Total systematic errors for data presented in Fig. 1 are $\pm 7\%$ of signal, but increase to $\pm 8\%$ for $|\eta_\Delta| < 0.5$ and to $\pm 11\%$ for $|\phi_\Delta| < 0.05$. Correlations from resonance ($p^0, \omega$) decays were 3\% of peaks in Fig. 2 in $|\eta_\Delta| < 0.5$, $|\phi_\Delta| < 2$.

Joint autocorrelations in Fig. 4 (but without factor $\hat{N}$) were fitted with a model function consisting of dipole and quadrupole terms on $\phi_\Delta$, a 1D gaussian on $\eta_\Delta$ only and a 2D same-side gaussian on ($\eta_\Delta, \phi_\Delta$), plus constant offset

$$F = A_{\phi_\Delta} \cos(\phi_\Delta) + A_{2\phi_\Delta} \cos(2\phi_\Delta) + A_0 e^{-\left(\frac{\eta_\Delta}{\sigma_{\eta_\Delta}}\right)^2} + A_1 e^{-\left(\frac{\phi_\Delta}{\sigma_{\phi_\Delta}}\right)^2 + \left(\frac{\eta_\Delta}{\sigma_{\eta_\Delta}}\right)^2} + A_2.$$ 

Best-fit parameters for the model fits shown in Fig. 4 are listed in Table I including efficiency-correction factor $S$ [25]. Those fit parameters confirm that with increasing centrality 2D peak structures exhibit 1) strong and non-monotonic amplitude variation, 2) strong $\eta_\Delta$ width increase and 3) significant $\phi_\Delta$ width reduction.
TABLE I: Parameters and fitting errors (only) for model fits [Eq. 2] to joint autocorrelation data in Fig. 4 for centrality bins (a) - (d) (central - peripheral). Total systematic error for efficiency-corrected amplitudes is 11% [23].

<table>
<thead>
<tr>
<th>centrality</th>
<th>(d)</th>
<th>(c)</th>
<th>(b)</th>
<th>(a)</th>
<th>error* (%)</th>
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<tr>
<td>( S )</td>
<td>1.19</td>
<td>1.22</td>
<td>1.25</td>
<td>1.27</td>
<td>8 (syst)</td>
</tr>
<tr>
<td>( \bar{N} )</td>
<td>115.5</td>
<td>424.9</td>
<td>790.2</td>
<td>983.0</td>
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</tr>
<tr>
<td>( S \bar{N}A_1 )</td>
<td>1.93</td>
<td>3.23</td>
<td>3.72</td>
<td>3.10</td>
<td>5-2</td>
</tr>
<tr>
<td>( \sigma_\phi^a )</td>
<td>0.61</td>
<td>0.55</td>
<td>0.54</td>
<td>0.53</td>
<td>4-2</td>
</tr>
<tr>
<td>( \sigma_\eta^a )</td>
<td>0.58</td>
<td>1.05</td>
<td>1.34</td>
<td>1.36</td>
<td>5-2</td>
</tr>
<tr>
<td>( S \bar{N}A_0 )</td>
<td>0.60</td>
<td>0.32</td>
<td>—</td>
<td>—</td>
<td>0.16-0.1b</td>
</tr>
<tr>
<td>( \sigma_0 )</td>
<td>1.11</td>
<td>0.24</td>
<td>—</td>
<td>—</td>
<td>28-22</td>
</tr>
<tr>
<td>( S \bar{N}A_2 )</td>
<td>-0.67</td>
<td>-0.55</td>
<td>-0.67</td>
<td>-0.58</td>
<td>0</td>
</tr>
<tr>
<td>( S \bar{N}A_\phi^{a} )</td>
<td>-0.31</td>
<td>-0.76</td>
<td>-0.97</td>
<td>-0.74</td>
<td>22-5</td>
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<tr>
<td>( S \bar{N}A_\phi^a )</td>
<td>1.05</td>
<td>2.72</td>
<td>1.30</td>
<td>0.32</td>
<td>2-17</td>
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<tr>
<td>( \chi^2/\text{DoF} )</td>
<td>419</td>
<td>419</td>
<td>416</td>
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</table>

*Range of fitting errors in percent from peripheral to central.

Same-side peak amplitudes and widths from model fits are plotted vs centrality measure \( \nu \) in Fig. 4 with values obtained from p-p collisions. Same-side autocorrelations in Fig. 2 differ strongly from those for p-p collisions, where a nearly-symmetric 2D gaussian peak dominates same-side structure with similar widths on \( \eta_\Delta \) and \( \phi_\Delta \) (\( \sim 0.5 \) and 0.7 respectively) [23]. Same-side correlations for peripheral Au-Au collisions (Fig. 2d) are similar to the p-p result. In central Au-Au collisions the two widths of the gaussian peak differ by a factor 2.6. Per-particle amplitude \( S \bar{N}A_1 \) for the same-side peak increases nearly linearly with path-length as expected for independent binary collisions. However, peak volume \( \equiv S \bar{N}A_1 \sigma_\eta \sigma_\phi \) (\( \propto \) minijet fragment number) has a more complex variation, strongly departing from linear \( \nu \) scaling (dotted line) above \( \nu = 2.5 \) (left-panel dashed curve is derived from curves for amplitude and peak widths). The volume excess beyond the linear extrapolation may indicate onset of a strongly dissipative medium in which more fragments with less \( p_t \) result from each scattered parton. It is notable that the amplitude does not deviate from a linear trend, except for the most central point.

Symmetric same-side angular correlations in p-p collisions, and the peripheral Au-Au result in this study, represent expected in \( \text{vacuum} \) jet fragmentation. We speculate that the mechanism modifying the same-side peak in central Au-Au collisions is strong coupling of \( \text{minimum-bias} \) semi-hard partons (no high-\( p_t \) trigger is imposed) to a longitudinally-expanding colored medium developed in the more central Au-Au collisions. Hadron fragments sample the local velocity structure of the pre-hadronic parton-medium coupled system. Growth of the colored medium with collision centrality is then indicated by increased width on \( \eta_\Delta \) of the same-side correlation peak.

Hijing [2] same-side angular correlations increase in width by 10% on both \( \eta_\Delta \) and \( \phi_\Delta \) with jet quenching imposed, seriously underpredicting the large width increase on \( \eta_\Delta \) and contradicting the width decrease on \( \phi_\Delta \) observed in data. The pQCD jet-quenching mechanism in Hijing does not produce an asymmetry on \( (\eta_\Delta, \phi_\Delta) \), given the symmetry about the jet thrust axis of its perturbative bremsstrahlung quenching model. Prominent low-\( p_t \) string-fragment correlations on \( \eta_\Delta \) appear in all Hijing centralities. RQMD [12] CI correlations are essentially featureless except for flow-related correlations on \( \phi_\Delta \).

In conclusion, we have for the first time measured charge-independent joint autocorrelations on difference variables \( \phi_\Delta \) and \( \eta_\Delta \) for Au+Au collisions at \( \sqrt{s_{NN}} = 130 \) GeV. Low-\( p_t \) string-fragment correlations prominent in p-p collisions are not observed for any centrality; longitudinal string degrees of freedom are strongly suppressed even for the most peripheral Au-Au collisions in this study. However, other large-amplitude correlation structures are observed. In addition to azimuth structures associated with elliptic flow and transverse momentum conservation we observe a near-side peak structure varying from a symmetric shape on \( (\eta_\Delta, \phi_\Delta) \) in peripheral collisions to a highly elongated shape on \( \eta_\Delta \) in central collisions. That deformation trend, observed in this first jet analysis with low-\( p_t \) hadrons, can be interpreted as a transition from in \( \text{vacuum} \) jet fragmentation in p-p and peripheral Au-Au collisions to coupling of minimum-bias partons to a longitudinally-expanding colored medium in the more central collisions as part of a dissipation process. The concept of parton energy loss in heavy ion collisions is thereby extended to strongly non-perturbative aspects.

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[9] An autocorrelation is a projection by averaging of a distribution on \((x_1, x_2)\) onto difference variable \(x_1 - x_2\).
[15] Track cuts required minimum track separations 5, 12 and 20 cm at radii 50, 127 and 200 cm from the TPC axis.

Crossing pairs with separations less than 10 cm (z) and 30 cm (azimuth) at mid-radius were also excluded.

[18] Centrality classes d) - a) for 300k events were defined by \(N/N_0\) cuts at > 0.03, 0.21, 0.56 and > 0.79.
[19] \(N_0\), the half-max point at the end of the minimum-bias distribution plotted as \(d\sigma/dN_{ch}^{1/4}\), is an estimator on multiplicity \(N\) for the maximum number of participant nucleons; \(N/N_0 \simeq N_{part}/N_{part,max}\) within 4%.
[25] Extrapolation factors \(S\) for \(N(\hat{r} - 1)\) correct for contamination and inefficiency \(10\). Systematic error in \(S\) was estimated to be \(\pm 8\%\). Total systematic error for extrapolated quantities in Table I was 11%.
[26] Quantity \(\nu \equiv (N_{part}/2)^{1/3} \simeq 5.5(N/N_0)^{1/3}\) for Au \(N_{part}\) is participant number) estimates mean participant path length in number of encountered nucleons.