

Influence of liquid structure on diffusive isotope separation in molten silicates and aqueous solutions

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Abstract

Molecular diffusion in natural volcanic liquids discriminates between isotopes of major ions (e.g., Fe, Mg, Ca, and Li). Although isotope separation by diffusion is expected on theoretical grounds, the dependence on mass is highly variable for different elements and in different media. Silicate liquid diffusion experiments using simple liquid compositions were carried out to further probe the compositional dependence of diffusive isotopic discrimination and its relationship to liquid structure. Two diffusion couples consisting of the mineral constituents anorthite ($\text{CaAl}_2\text{Si}_2\text{O}_8$; denoted AN), albite ($\text{NaAlSi}_3\text{O}_8$; denoted AB), and diopside ($\text{CaMgSi}_2\text{O}_6$; denoted DI) were held at 1450°C for 2 h and then quenched to ambient pressure and temperature. Major-element as well as Ca and Mg isotope profiles were measured on the recovered quenched glasses. In both experiments, Ca diffuses rapidly with respect to Si. In the AB–AN experiment, $D_{\text{Ca}}/D_{\text{Si}} \sim 20$ and the efficiency of isotope separation for Ca is much greater than in natural liquid experiments where $D_{\text{Ca}}/D_{\text{Si}} \sim 1$. In the AB–DI experiment, $D_{\text{Ca}}/D_{\text{Si}} \sim 6$ and the efficiency of isotope separation is between that of the natural liquid experiments and the AB–AN experiment. In the AB–DI experiment, $D_{\text{Mg}}/D_{\text{Si}} \sim 1$ and the efficiency of isotope separation for Mg is smaller than it is for Ca yet similar to that observed for Mg in natural liquids.

The results from the experiments reported here, in combination with results from natural volcanic liquids, show clearly that the efficiency of diffusive separation of Ca isotopes is systematically related to the solvent-normalized diffusivity—the ratio of the diffusivity of the cation (D_{Ca}) to the diffusivity of silicon (D_{Si}). The results on Ca isotopes are consistent with available data on Fe, Li, and Mg isotopes in silicate liquids, when considered in terms of the parameter $D_{\text{cation}}/D_{\text{Si}}$. Cations diffusing in aqueous solutions display a similar relationship between isotopic separation efficiency and $D_{\text{cation}}/D_{\text{H}_2\text{O}}$, although the efficiencies are smaller than in silicate liquids. Our empirical relationship provides a tool for predicting the magnitude of diffusive isotopic effects in many geologic environments and a basis for a more comprehensive theory of isotope separation in liquid solutions. We present a conceptual model for the relationship between diffusivity and liquid structure that is consistent with available data.

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1. INTRODUCTION

Natural variations in the isotopic composition of some 50 chemical elements are used in geochemistry for studying transport processes, estimating temperature, and even for classifying planets and meteorites (Johnson et al., 2004). Within the past decade there has been growing interest in

measuring isotopic variations in a wider variety of elements, and improved techniques make it possible to measure very small effects (Eiler and Shauble, 2004; Ono et al., 2006; Eiler, 2007). Interpreting the small isotopic variations has required a closer look at how transport processes affect isotopic distributions (Eiler and Shauble, 2004). It is now recognized that the mass dependence of isotopic transport coefficients can be variable both in absolute value and in functional form for different elements and molecules (Weingartner et al., 1989; Young et al., 2002).

For many years the thinking among geochemists on isotope fractionation (or separation) by diffusion has been guided by application of the laws of kinetic theory – where in diffusion is the result of purely translational motion and elastic collisions of geometrically simple molecules. Even in some dilute gas systems, however, there are deviations from the expected behavior (e.g., Merlivat, 1978; Barkan and Luz, 2007; Luz et al., 2009). The picture becomes significantly more complicated in liquids because chemical bonding, and the shape and rotation of molecules, influence transport. There are models that adequately describe diffusive isotope separation in some simple liquids, but for more complex liquid solutions such as silicate melts, where the compositions of the diffusing species are ambiguous and dynamic, there is no general theory (see Appendix A.1). In a previous study (Watkins et al., 2009) involving natural magmatic liquids, we observed isotopic fractionations that suggested a composition-dependence to the diffusive isotope separation for calcium. In those experiments the compositional dependence was equivocal because of other possible contributing effects and the fact that natural silicate melt compositions are complicated.

In this diffusion study we use silicate liquids of simple composition to further probe the compositional dependence

of diffusive isotopic discrimination and its relationship to liquid structure. All of the starting materials are combinations of the three mineral constituents anorthite ($\text{CaAl}_2\text{Si}_2\text{O}_8$; denoted AN), albite ($\text{NaAlSi}_3\text{O}_8$; denoted AB), and diopside ($\text{CaMgSi}_2\text{O}_6$; denoted DI), so that the resulting silicate liquids are considerably less complicated than natural basalt and rhyolite. Two diffusion couples were constructed: one consisting of AB and AN (1% AN versus 15% AN), and the other consisting of AB and DI (1% DI versus 15% DI). The ends of the diffusion couple with a greater proportions of AN (or DI) have much higher Ca concentration than the AB-rich ends, and hence Ca diffuses down a substantial concentration gradient during the experiments. Albite was chosen as the main component of the liquids because of its relatively low melting temperature (1203 °C at 8 kbar; Birch and LeComte, 1960), permitting us to use temperature and pressure conditions similar to those used in previous experiments on natural magmatic compositions (Richter et al., 2003, 2008, 2009; Watkins et al., 2009). The variation in SiO_2 concentration among the synthetic starting compositions is also relatively small (Figs. 1 and 2). As diffusion coefficients for most elements in silicate liquids vary with the concentration of SiO_2 , this characteristic simplifies analysis as we can assume that the diffusion coefficients are uniform across the couple, and that they do not change over the course of the experiment.

2. EXPERIMENTAL METHODS

2.1. Starting materials

Synthetic mineral compositions were made by weighing out dehydrated, reagent-grade oxides and carbonates and mixing them together in ethanol as a slurry in an

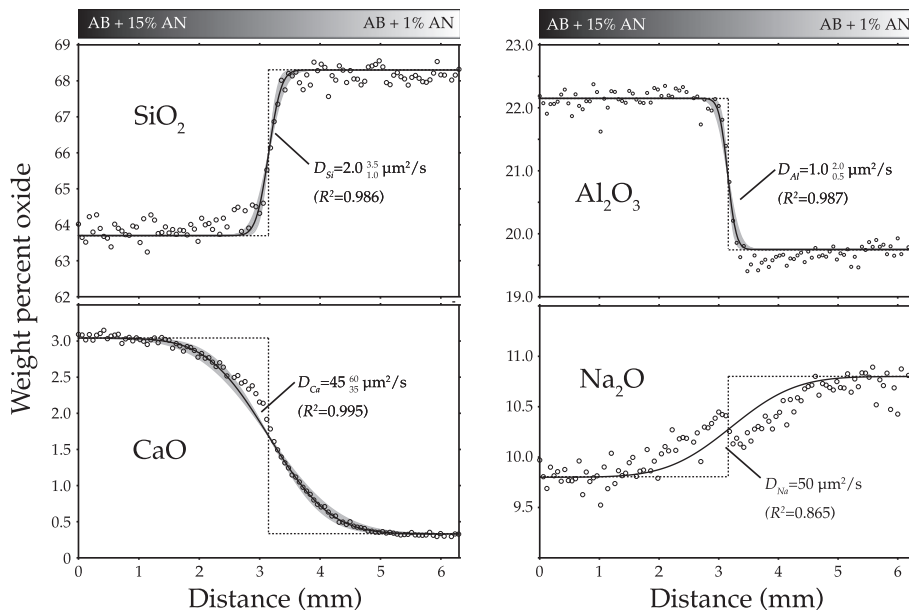


Fig. 1. Chemical concentration profiles of major cations from diffusion experiments involving simplified molten silicate composition (AB–AN) as measured by electron microprobe. Dashed lines represent the starting concentrations and initial condition for the diffusion model. Solid lines are best-fit model profiles with associated diffusivities (D_i). The diffusivity D_i of each of the major cations is roughly constant across the diffusion couple, as evidenced by the observed symmetry in each of the profiles about the initial interface between starting liquids. An estimate of the uncertainty in D_i is obtained from the range of model profiles spanned by the shaded area.

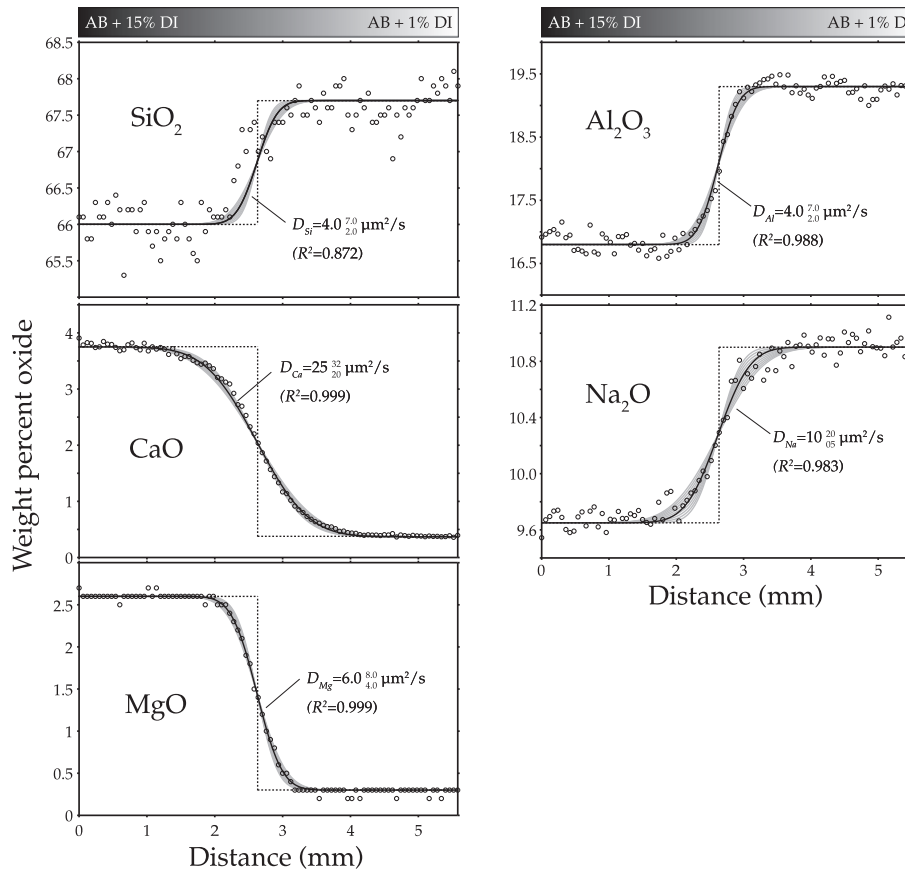


Fig. 2. Chemical concentration profiles of major cations from diffusion experiments involving simplified molten silicate composition (AB–DI) as measured by electron microprobe. Dashed lines represent the starting concentrations and initial condition for the diffusion model. Solid lines are best-fit model profiles with associated diffusivities (D_i). The diffusivity D_i of each of the major cations is roughly constant across the diffusion couple, as evidenced by the observed symmetry in each of the profiles about the initial interface between starting liquids. An estimate of the uncertainty in D_i is obtained from the range of model profiles spanned by the shaded area.

automated mortar and pestle. The mixture was placed in a Pt crucible and fused at 1550 °C under atmospheric conditions in a Deltech furnace. After about 1 h, the melt was quenched to glass and the entire procedure repeated to ensure homogenization of the final mixture. The measured bulk composition of each powder differs slightly from the target stoichiometric AB–AN or AB–DI mixture (Table 1), which may be due to variable Na loss during the fusing step.

2.2. Piston cylinder experiments

In each diffusion couple experiment, the two powders of different composition were juxtaposed by pressing one atop the other in a graphite capsule. The capsule was placed in a standard 3/4-in. piston cylinder assembly and cold-pressurized to 8 kbar. The sample was brought to 1450 °C at a ramp rate of 150 °C/min. Pressure and temperature were monitored and controlled to within 0.1 kbar and 3 °C of those conditions. By trial and error we found that 2 h was about the right duration for maximizing the length scales of diffusion while maintaining approximately a fixed concentration at both ends of the capsule.

2.3. Electron microprobe analysis

Post-run diffusion couples were sectioned down their vertical axis and axis-parallel major-element profiles were measured with a Cameca SX-51 electron microprobe at UC-Berkeley. We used a 15 nA beam current rastered at 12,000× magnification ($\sim 12 \times 9 \mu\text{m}$ beam dimensions) with an accelerating voltage of 15 kV. Na was measured first at each spot to avoid effects of Na migration.

2.4. Ca and Mg isotope analysis

For isotope analysis, diffusion couples were sectioned into thin ($\sim 465 \mu\text{m}$) wafers using a Bico diamond wafer saw with blade thickness of $\sim 165 \mu\text{m}$. Each wafer was dissolved in a mixture of hydrofluoric and perchloric acids before Ca and Mg were isolated by cation exchange chromatography. The Mg portion of this step is modified from Wombacher et al. (2009) by scaling for use with Bio-Rad polypropylene columns (#731-1550EDU). Ca isotope ratio measurements were carried out by thermal ionization mass spectrometry (TIMS) at UC-Berkeley on a Thermo-Finnigan Triton TI with nine moveable Faraday

collectors. For considerations regarding beam intensities and corrections for machine mass discrimination, the reader is referred to DePaolo (2004) and Watkins (2010). The Ca isotope composition is expressed as (DePaolo, 2004)

$$\delta^{(44/40)}\text{Ca} = 1000 \times \left[\frac{(^{44}\text{Ca}/^{40}\text{Ca})_{\text{sample}}}{0.0212076} - 1 \right],$$

and all Ca isotope data are reported in Table 2.

Mg isotope measurements were carried out at Lawrence Berkeley National Lab on a Micromass Isoprobe multi-collector inductively coupled plasma mass spectrometer (MC-ICP-MS) using a sample-standard bracketing technique (Galy et al., 2003). Sample concentrations between 500 and 1000 ppb Mg in dilute HNO₃ (matched to bracketing standard concentrations) were introduced through a CETAC Aridus desolvating nebulizer using only Ar gas to avoid CN-interference. The Isoprobe uses a gas collision cell to normalize ion beam kinetic energy and remove isobaric interferences. Based on experiments, gas bleed rates into the cell were found to be optimal at 8.0 mL/min for He and 0.8 mL/min for H. Cone extraction potential was set at 190 V, and the remaining tuning parameters were optimized daily for maximum signal intensity. Total beam varied from 6 to 9 V. The Mg isotope composition is expressed as:

$$\delta^{(26/24)}\text{Mg} = 1000 \times \left[\frac{(^{26}\text{Mg}/^{24}\text{Mg})_{\text{sample}}}{(^{26}\text{Mg}/^{24}\text{Mg})_{\text{DSM3}}} - 1 \right].$$

All Mg isotope measurements are normalized to the DSM3 standard (Young and Galy, 2004) and are reported in Table 2.

Each reported data point consists of the average of 2–7 replicate measurements (except ABDI4-7); each replicate consists of a single 60 s on-peak background measurement and a block of 20 10 s static measurements, bracketed by similar measurements of the DSM3 mono-elemental standard. The system was washed for 5–10 min with successive dilute HNO₃ solutions between measurement cycles. Replicates of the Cambridge1 mono-elemental standard ($n = 9$) yield $\delta^{(26/24)}\text{Mg} = -2.73 \pm 0.35$, within uncertainty of the established value of -2.58 ± 0.14 (Galy et al., 2003).

3. RESULTS

3.1. Major element diffusion profiles

Figs. 1 and 2 show the major-element diffusion profiles corresponding to the AB–AN and AB–DI experiments,

Table 1

Targeted versus measured bulk compositions of starting materials used in diffusion couple experiments. The difference between the target and measured compositions is not significant for the purpose of this study.

		CaO	MgO	SiO ₂	Al ₂ O ₃	Na ₂ O	Total
85AB + 15AN	Calculated	3.02	0.00	64.91	22.02	10.05	100.00
	Measured	3.04	–	63.70	22.15	9.80	98.69
99AB + 01AN	Calculated	0.20	0.00	68.48	19.61	11.70	100.00
	Measured	0.33	–	68.30	19.75	10.80	99.18
85AB + 15DI	Calculated	3.88	2.79	66.75	16.53	10.05	100.00
	Measured	3.75	2.60	66.00	16.80	9.65	98.80
99AB + 01DI	Calculated	0.26	0.19	68.61	19.25	11.70	100.00
	Measured	0.37	0.30	67.70	19.30	10.90	98.57

respectively. In both experiments, Ca and Na are observed to diffuse more rapidly than the network-forming cations Si and Al. This difference is different from what is observed in natural silicate liquids under similar experimental conditions, where the length scales of Ca, Na, and Si diffusion are nearly identical (Richter et al., 2003, 2008, 2009; Watkins et al., 2009). In the AB–DI experiment, Mg diffuses more slowly than Ca and Na, its behavior resembling that of the network-forming cations. The slow diffusion of Mg relative to Ca has also been observed for tracer diffusion in liquids of nearly pure albite composition over the temperature range 645–1025 °C (Rosalieb and Jambon, 2002).

3.2. Ca and Mg isotope profiles

Fig. 3 shows the Ca and Mg isotopic composition along the diffusion profiles. As the isotopic composition is initially uniform across the two diffusion couples ($\delta^{44}\text{Ca} = -0.3\text{‰}$ and $\delta^{26}\text{Mg} = -1.2\text{‰}$), the observed isotopic variability develops as a result of diffusion during the experiment. In the AB–AN experiment (Fig. 3a), the variation in $\delta^{44}\text{Ca}$ of $\sim 10\text{‰}$ is the largest fractionation of Ca isotopes so far observed in such chemical diffusion experiments. In this experiment, the isotopic composition at the boundaries changed slightly from the initial condition, indicating that diffusive effects have reached both ends of the capsule. In the AB–DI experiment (Fig. 3b), the range in $\delta^{44}\text{Ca}$ is $\sim 6\text{‰}$, comparable to the maximum range previously observed in natural compositions, and the isotopic composition at both ends of the capsule is unchanged from the initial condition. In the same experiment, the range in $\delta^{26}\text{Mg}$ is only $\sim 1.3\text{‰}$ and the length scale of Mg isotope variability from the initial state is comparable to that for Ca isotopes. In both experiments, the overall shape of the profiles match those expected for the simplest model of chemical diffusion in which Ca and Mg diffuse in response to their own concentration gradients.

4. ANALYSIS

The essential and unexpected result of the experiments described above is that the Ca isotopic separation due to diffusion in chemically simple diffusion couples is both larger than observed in natural volcanic liquids (e.g., Richter et al., 2003; Watkins et al., 2009) and variable. It was originally postulated by Richter et al. (2003) based on the data available, that the Ca isotopic selectivity due to diffusion in

Table 2

Ca and Mg isotope compositions measured on post-run diffusion couples. The isotopic compositions represent an average for each wafer; therefore the distance values are shifted slightly from the center of each wafer to account for the gradient in concentration across each wafer.

Sample (wafer no.)	Distance (mm)	$\delta^{44}\text{Ca}^a$ (‰)	No. of analyses
<i>Albite–anorthite experiment</i>			
ABAN2-1	6.019	-0.98	3
ABAN2-2	5.337	-3.19	2
ABAN2-3	4.724	-7.49	3
ABAN2-4	4.054	-7.86	2
ABAN2-5	3.431	-2.03	3
ABAN2-6	2.812	0.95	3
ABAN2-7	2.215	1.21	2
ABAN2-8	1.558	0.50	2
ABAN2-9	0.960	0.03	2
ABAN2-10	0.300	0.07	2

Sample (wafer no.)	Distance (mm)	$\delta^{44}\text{Ca}^a$ (‰)	No. of analyses	$\delta^{26}\text{Mg}$ (2 σ) (‰)	No. of analyses
<i>Albite–diopside experiment</i>					
ABDI4-1	5.279	-0.42	2	-1.40 (29)	3
ABDI4-2	4.678	-1.43	3	-1.04 (34)	3
ABDI4-3	4.008	-4.82	2	-1.51 (47)	7
ABDI4-4	3.394	-4.86	2	-2.51 (16)	2
ABDI4-5	2.726	-0.57	3	-1.45 (17)	3
ABDI4-6	2.148	0.68	2	-1.10 (47)	2
ABDI4-7	1.557	0.31	2	-1.15 (-)	1
ABDI4-8	0.900	-0.27	2	-1.12 (87)	3
ABDI4-9	0.300	-0.33	2	-1.23 (42)	3

^a Uncertainties in $\delta^{44}\text{Ca}$ are within $\pm 0.15\text{‰}$.

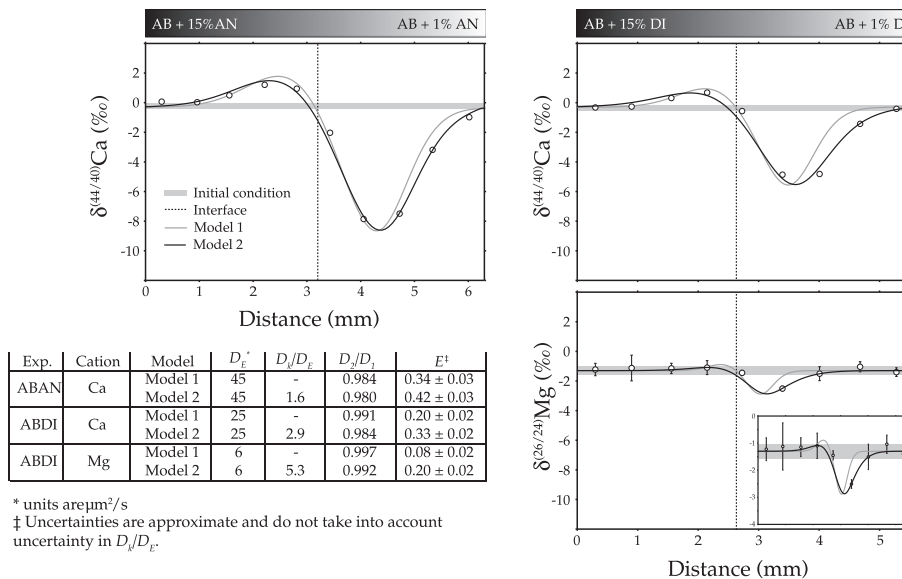


Fig. 3. Ca and Mg isotope profiles from the AB–AN and AB–DI diffusion experiments depicted in Figs. 1 and 2, showing isotopic separation by diffusion. The initial isotopic ratio was constant across the experimental charge and is denoted by the gray horizontal bar. Solid lines are model isotope profiles (see text) used to quantify the efficiency of isotope separation E , which is equal to $2\ln(D_2/D_1)/\ln(m_1/m_2)$, where m is the solute element’s atomic mass and subscripts denote different isotopes.

silicate liquids might be roughly constant; that is, independent of liquid composition. Watkins et al. (2009) provided evidence that the isotopic selectivity might be more pronounced in high silica liquids, but the complexity of the experimental results did not allow for more definitive con-

clusions. The present results, however, show unequivocally that Ca isotope fractionation during diffusion can be highly variable. In the following section we analyze this variability and show that the efficiency of isotope separation appears to be correlated with both the magnitude of the diffusivity,

and more precisely, the ratio of the Ca diffusivity to that of Si. The systematic relationships we have discovered allow us to move closer to a general model of isotopic fractionation during diffusion in silicate liquids, and also shed light on the bonding of cations within these liquids and the structure of the liquids themselves.

4.1. Model for the elemental diffusion profiles

In non-equilibrium thermodynamics, fluxes are directly proportional to forces. For chemical fluxes, the forces are gradients in chemical potential, but since chemical potentials are difficult to measure, gradients in concentration are generally used as an approximation. In the most general model of chemical diffusion, the flux of component i may be driven by a concentration gradient in any of the other components j :

$$J_i = - \sum_{j=1}^{n-1} D_{ij} \nabla C_j, \quad (1)$$

where the D_{ij} 's are terms in the multicomponent diffusivity matrix and C_j is the concentration of component j . Eq. (1) does not specifically account for the fact that chemical elements have isotopes, but it has been demonstrated by experiment that isotopic species diffuse at different rates depending on mass. To model these effects, it has been customary to treat each isotope as an independent chemical species, diffusing in response to its own concentration gradient. This ignores the role of isotopic exchange, or self diffusion, superimposed on chemical diffusion. It is therefore preferable to write the diffusive flux of isotope k of element i as (Liang, 1994; Richter et al., 1999; Liang, 2010):

$$J_i^k = -D_i^k \nabla C_i^k - \sum_{j=1}^{n-1} f_i^k (D_{ij}^k - \delta_{ij} D_i^k) \nabla C_j, \quad (2)$$

where D_i^k is the self diffusion coefficient; C_i^k is the concentration of isotope k ; f_i^k is the mole fraction of isotope k in element i , and $\delta_{ij} = 1$ if $i = j$ and $\delta_{ij} = 0$ if $i \neq j$. When the elements of the diffusivity matrix are unknown, as is the case in our systems, Eq. (2) can be cast in terms of the effective binary diffusion coefficient (EBDC) (Liang, 2010):

$$J_i^k = -D_i^E \nabla C_i^k - f_i^k (D_i^E - D_i^k) \nabla C_i, \quad (3)$$

where D_i^E is the EBDC. The EBD model obscures aspects of diffusion that may be of interest, and is only applicable when the chemical diffusion profile is monotonic. In our previous experiments on natural volcanic liquids (Watkins et al., 2009) we observed that isotopic discrimination for Ca isotopes during diffusion depends on the magnitude and direction of the Al concentration gradient relative to those of the Ca concentration gradient. To model these effects we used a multi-component diffusivity matrix that explicitly accounts for Ca–Al coupling. In this study, however, the mass dependence on the off-diagonal terms cannot be resolved because the Al, Si, and Na gradients are relatively small (see Appendix A.2). The advantage of the EBD model is that only one parameter (D_i^E) is required to obtain a chemical diffusion profile and nearly all diffusivi-

ties in minerals and melts are obtained using this approach (Zhang, 2010).

To simplify the notation we remove the subscripts i except where necessary in later sections to distinguish between EBDCs of different elements. Substituting $C_k = f_k C$ and applying mass conservation leads to the following one-dimensional diffusion equation (assuming the D 's are constant):

$$\frac{\partial C_k}{\partial t} = D_E f_k \nabla^2 C + (D_E + D_k) \nabla C \nabla f_k + D_k C \nabla^2 f_k. \quad (4)$$

In this formulation, there are actually two potentials driving the net flux of an isotope: ∇C represents a driving force for chemical homogenization and ∇f_k represents a driving force for isotopic homogenization. Eq. (4) holds for two end-member scenarios. When there is only one isotope ($f_k = 1$) we recover the effective binary diffusion equation:

$$\frac{\partial C}{\partial t} = D_E \nabla^2 C. \quad (5)$$

When the elemental composition is uniform ($C = \text{constant}$) but there are gradients in isotopic ratios, we recover the self diffusion equation:

$$\frac{\partial f_k}{\partial t} = D_k \nabla^2 f_k, \quad (6)$$

which describes diffusion of an isotope ratio.

Numerical solutions to the one-dimensional form of Eq. (4) were calculated using an explicit finite difference scheme in MATLAB. For our experiments the appropriate boundary conditions are zero flux ($\partial C_k / \partial x = 0$) at either end of the capsule. The code was validated against the analytical solution to Eq. (5) with zero-flux boundary conditions given by Trial and Spera (1994).

4.2. Comparison between model and measured elemental profiles

Model versus measured diffusion profiles for Ca, Mg, Na, Al and Si and the associated EBDCs for both diffusion couples are shown in Figs. 1 and 2. Note that the elemental profiles for Ca and Mg are insensitive to the self diffusivities because $\nabla C \gg \nabla f_k$. The contrast between Ca and Si diffusivity is largest in the AB–AN experiment where the diffusivity of Ca is greater than that of Si by a factor of 22.5 ($D_{Ca} = 45 \mu\text{m}^2/\text{s}$ and $D_{Si} = 2.0 \mu\text{m}^2/\text{s}$). In the AB–DI experiment, where there is greater abundance of network-modifying cations (Mg + Ca), the diffusivity of Ca is reduced ($D_{Ca} = 25 \mu\text{m}^2/\text{s}$) and the diffusivity of Si is increased ($D_{Si} = 4.0 \mu\text{m}^2/\text{s}$) such that D_{Ca}/D_{Si} is about 6. This latter value is still large in comparison to D_{Ca}/D_{Si} in natural silicate liquids, which is close to unity. In the same experiment, the diffusivity of Mg is less than that of Ca yet similar to that of Si.

4.3. Model for the isotope ratio profiles

The Ca and Mg isotope ratio profiles require that the diffusion coefficients for the isotopes of Ca and Mg vary with mass. Assuming the ratio of isotopic diffusion coeffi-

icients is constant, a single parameter E describes the efficiency of isotope separation (after Schoen, 1958):

$$E = 2 \frac{\ln(D_2/D_1)}{\ln(m_1/m_2)}, \quad (7)$$

where m_k is the mass of isotope k and the D 's are isotope-specific EBDCs. There is a mass dependence on D_k (Richter et al., 1999) but it cannot be resolved using the setup of the AB-AN and AB-DI experiments wherein $\nabla C \gg \nabla f_k$. The parameter E is related to the analogous parameter β used by Richter et al. (2003), by the simple relationship $E = 2\beta$. The magnitude of E is affected by the number and masses of other atoms whose motions are correlated with the motion of the atom of interest. Larger values of E correspond to greater mass discrimination between isotopes and imply that the diffusing atom is decoupled from the motion of other atoms (Rothman and Peterson, 1965). The value of E approaches unity for diffusion in gases but is generally much smaller in liquids and solids. Values for D_2/D_1 (i.e., $D^{44}\text{Ca}/D^{40}\text{Ca}$) can be obtained from the model fit to the isotopic profiles and E derived from Eq. (7) and the isotopic masses of Ca.

4.4. Comparison between model and measured isotope profiles

Two sets of model profiles are compared to the measured isotope profiles in Fig. 3. The gray curves show the result when isotopic exchange superimposed on chemical diffusion is ignored; they represent the analytical solution to Eq. (5) (Trial and Spera, 1994) and involve the minimum number of free parameters required to generate a model isotope profile (D_E and E). In all three plots, the gray curves are in relatively good agreement with the Ca and Mg isotopic data. In detail, however, there is misfit in the low-(Ca, Mg) side of the couple; the low- δ trough does not extend far enough into the low-concentration liquid.

The black curves show that a nearly perfect fit can be achieved once self diffusion is taken into account. The isotopic effects extend further into the low-concentration liquid because isotopic exchange affects δ -values without contributing to the net elemental flux. The quality of the fits indicate that D_k is greater than D_E by a factor of about 2 for Ca and about 5 for Mg in albitic liquid at 1450 °C, which is consistent with the observation that isotope ratios tend to re-equilibrate faster than elemental concentrations by diffusion in molten silicates (Baker, 1989; Leshner, 1990, 1994; Van der Laan et al., 1994; Liang, 2010). It is important to emphasize that consideration of isotopic exchange superimposed on chemical diffusion increases the derived values of E , and that the correction to E tends to increase with increasing D_k/D_E .

There is also significance in the nearly exact fit of the $\delta^{(44/40)}\text{Ca}$ data on the high-Ca side of both experiments, because in most of the experiments conducted using natural basalt-rhyolite diffusion couples, linear variations in $\delta^{(44/40)}\text{Ca}$ have been observed in the high-Ca end that could not be accounted for with a simplified chemical diffusion model (Richter et al., 2003). Such variations have been attributed to undesired temperature gradients in the experimental capsules because temperature gradients can pro-

duce a similar isotopic signature (Richter et al., 2008). However, our failure to observe linear variations in $\delta^{(44/40)}\text{Ca}$ in the AB-AN and AB-DI experiments, and in an isochemical experiment under the same conditions (Watkins et al., 2009), suggests that these unexpected isotopic effects in the natural systems have other causes. We postulate that non-ideal mixing may generate the unexpected isotopic gradients, reflecting a complex relationship between diffusive flux and concentration gradients near the interface of the diffusion couple. It may be noteworthy that mixing in the system albite-anorthite and albite-diopside is nearly athermal in the area of composition space spanned by our experiments (Navrotsky et al., 1989).

5. DISCUSSION

5.1. Isotope separation by diffusion in silicate melts

Our results demonstrate, in contrast to previous proposals (Richter et al., 2003; Watson and Müller, 2009) that diffusive isotopic separation for Ca is sensitive to even slight changes in liquid composition. The compositions of the diffusion couples are similar in terms of SiO_2 content, and yet E for Ca varies from 0.33 in the AB-DI experiment to 0.42 in the AB-AN experiment. Both values are significantly greater than that found in natural silicate liquid experiments ($E = 0.07\text{--}0.15$), and show that there is no single value of E that can describe the diffusive fractionation behavior of Ca isotopes in silicate liquids. E_{Ca} does, however, appear to be strongly correlated with the ratio $D_{\text{Ca}}/D_{\text{Si}}$ (Fig. 4), which represents the ratio of the diffusivity of a “solute” component relative to that of the “solvent” component, in this case represented by Si. Among the silicate melt compositions for which diffusive fractionation of calcium has been measured, $D_{\text{Ca}}/D_{\text{Si}}$ varies by a factor of ~ 200 and E varies systematically between 0.07 and 0.42. The variation in D_i/D_{Si} is even larger, ~ 1000 , if experimental data for Ca, Mg, Fe and Li are considered, and the strong correlation between E_i and D_i/D_{Si} , suggests that D_i/D_{Si} is an excellent predictor of the magnitude of the isotope effect in silicate liquids.

The observed range in D_i/D_{Si} and its explanation have been described previously (Dingwell, 1990) and it has been shown that D_i/D_{Si} generally increases with increasing liquid viscosity η (cf. Dingwell, 2006). The reason that D_i/D_{Si} is lower in the AB-DI system than in the AB-AN system can be attributed to the sensitivity of η to changes in bulk composition. Generally, the addition of network modifying cations such as Ca and Mg lowers viscosity by forming non-bridging oxygen bonds that reduce the average interconnectivity of Si-O structures (e.g., Zhang et al., 2009). The average viscosity calculated from the model of Hui and Zhang (2007) is lower in the AB-DI system ($\eta_{\text{avg}} \approx 800$ Pa s) than in the AB-AN system ($\eta_{\text{avg}} \approx 6300$ Pa s) due to the former having a greater abundance of network-modifying cations ($\text{CaO} + \text{MgO} \approx 3.3$ wt% versus $\text{CaO} \approx 1.5$ wt%, respectively). The observation that $D_{\text{Ca}}/D_{\text{Si}}$ is greater in the AB-AN system is therefore consistent with previously observed trends, and we can now see that the isotope effects follow logically, at least at a qualitative level.

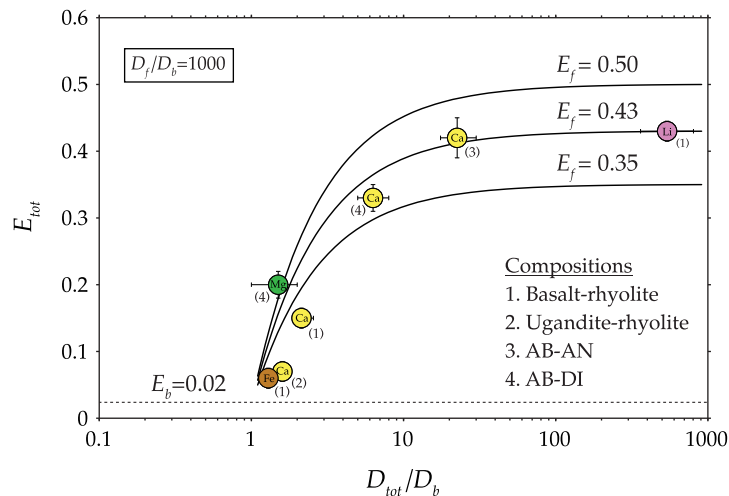


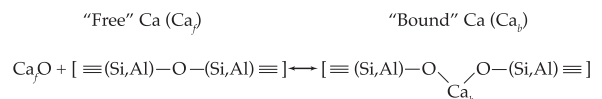
Fig. 4. The observed relationship between the efficiency of isotope separation E_{tot} (or E_i) and the mobility of the diffusing solute element (D_{tot} or D_i) relative to the mobility of the silicate liquid matrix (D_b or D_{Si}). The error bars shown are estimates and have slightly different meanings for different sets of data. In the natural silicate liquid experiments (compositions 1 and 2), the diffusion couples used spanned a large range of liquid compositions, including a large range of SiO_2 concentration. Because the diffusivities are a function of SiO_2 , the D_i/D_{Si} values shown are referenced to a particular value of 66 wt% SiO_2 ; and the error bars include how D_i/D_{Si} varies over the range from 61 to 71 wt% SiO_2 . For the AB-AN and AB-DI compositions (3 and 4), the SiO_2 content has minimal variability and is close to 66 wt% SiO_2 . However, for these compositions, the x -error bars do not include the relatively large uncertainties in D_{Si} . The model curves show the expected relationship between the efficiency of isotope separation and the normalized diffusivity for different values of E_f (see Eqs. (11) and (12)). The model views the cation as being partitioned between two species – one that is strongly bound and one that is weakly bound to the liquid matrix – such that the diffusivity is the sum of two mechanisms of transport: (1) site-hopping among and (2) translating or rotating with larger aluminosilicate matrix units. The net diffusivity (D_{tot}) and net efficiency of isotope separation (E_{tot}) depends on how the cation is partitioned between species. The curves shown are for a single value of $D_f/D_b = 1000$. The lower bound of $E_b = 0.02$ is comparable to the value of $E < 0.05$ inferred for Ge (used as an analog for Si) in GeO_2 (Richter et al., 1999).

The relationship between E_i and D_i/D_{Si} can be understood in terms of the strength of solute-solvent interactions. In the situation where the diffusivity of an element (like Li in natural liquids, or Ca in the AB-AN experiment) is much greater than the diffusivity of Si, it is likely that the element is not strongly bound to the aluminosilicate matrix, and hence is diffusing mostly as an isolated atom through a quasi-stationary aluminosilicate framework. This condition results in the large mass discrimination between isotopes of Li in natural silicate liquids and Ca in albitic liquids. For elements like Ca, Mg, and Fe in basaltic liquids, where the diffusivities are approximately the same as that of Si, these elements must be more strongly bound to the aluminosilicate matrix and hence are diffusing effectively as part of more massive multi-atom complexes that include Si.

5.2. Model for diffusive isotope effects in silicate liquids

The goal in this section is to describe an idealized quantitative model that can account for the relationship between E_i and D_i/D_{Si} in silicate liquids. The main idea behind our approach is that the chemical diffusivity and its mass dependence represent the sum of two (or possibly more) distinct mechanisms of transport (Bryce et al., 1999): site-hopping among, and translating or rotating with, larger aluminosilicate structures in the melt. To represent these two diffusion mechanisms, we depict an element such as Ca as being partitioned between two distinct chemical species – one that is relatively mobile (Ca_f) and one in which Ca is no more mo-

bile than the matrix itself (Ca_b). Hereafter we refer to these two species using the subscripts f for “free” and b for “bound”, respectively.



This model views the silicate liquid as if it were a liquid ion exchange resin having a large molecular weight. Ca is partitioned between the “free” form and the “bound” form, and it is assumed that the rate of exchange between free and bound phases is infinitely fast (i.e., local equilibrium applies). The diffusivity of Ca will be determined by the partition coefficient ($K = \text{Ca}_b/\text{Ca}_f$). If the isotopic dependence of diffusivity is different for the free and bound species, then there will be a correlation between E_{Ca} and D_{Ca} , or between E_{Ca} and D_{Ca}/D_{matrix} .

To derive the relationship that follows from this model, we begin with the total flux of the element, which is the sum of the flux of each of the species:

$$J_{tot} = J_f + J_b. \quad (8)$$

Using Fick’s First Law, this can be expressed for one-dimensional diffusion as

$$D_{tot} \frac{\partial C_{tot}}{\partial x} = D_f \frac{\partial C_f}{\partial x} + D_b \frac{\partial C_b}{\partial x}, \quad (9)$$

where C_{tot} is the total concentration, C_f is the concentration of species f and C_b is the concentration of species b . Substituting $C_b = KC_f$ and $C_{tot} = (1+K)C_f$ into Eq. (9) leads to an expression for the net diffusivity (assuming K is constant):

$$D_{tot} = \frac{D_f + KD_b}{1 + K}, \quad (10)$$

The equation for the normalized diffusivity is

$$\frac{D_{tot}}{D_b} = \frac{D_f + KD_b}{D_b(1 + K)}. \quad (11)$$

Finally, the ratio of the diffusivities of two isotopes i and j is

$$\frac{D_{tot,i}}{D_{tot,j}} = \frac{D_{f,i} + K_i D_{b,i}}{D_{f,j} + K_j D_{b,j}} \cdot \frac{1 + K_j}{1 + K_i}. \quad (12)$$

Fig. 4 shows the expected relationship between E from Eq. (12) and the normalized diffusivity from Eq. (11). There are three input parameters: (1) D_f/D_b , (2) E_f for D_f and (3) E_b for D_b , each of which is fixed and then K is varied to generate the model curve. For this initial evaluation of the model, we assume there is no isotopic partitioning between species ($K_i = K_j$). The intriguing result is that this simplified picture of chemical diffusion leads to a relationship between D_{tot}/D_b and E_{tot} that is similar to what is observed in the data; for $1 < D_{tot}/D_b < 10$, E_{tot} varies significantly, and for $D_{tot}/D_b > 10$, E_{tot} is relatively constant. The curve depends somewhat on the input parameters, which may be different for each isotope system as well as each bulk composition. An important question is whether E_f and E_b (which represent the upper and lower limits to E_{tot} in this model) can be assumed to be equivalent for different elements and compositions. If so, and assuming the ratio D_f/D_b were known for a given cation and composition, then the observed relationship between the normalized diffusivity and efficiency of isotope separation across different systems could be interpreted in terms of the relative abundance K of the “free” versus “bound” species. There is some information on D_f/D_b , but only for CO_2 and only in a limited number of com-

positions (Nowak et al., 2004). Assuming $D_f/D_b = 1000$ and $E_f = 0.43$ for Ca in albitic liquid, a value of $E_{tot} = 0.36$ would indicate that $K \approx 27$ for the Ca-bearing species. It is unclear, however, whether this model represents an adequate description of the diffusion process and the observed relationship between D_{tot}/D_b and E_{tot} . It may be the case that a more complicated model is warranted or that other parameters may be important. For example, the timescale of exchange between species may not be sufficiently short to warrant the local equilibrium approximation, and if the kinetics of exchange are important, the rate of exchange for the lighter isotope may be faster than that for the heavier isotope.

5.3. Comparison to aqueous solutions

The relationship between diffusivity and the efficiency of isotope separation by diffusion may be applicable to other non-molecular liquids. Fig. 5 combines results from silicate liquid experiments with results from experiments on cation diffusion in aqueous solutions. To generalize the terminology we plot E_{solute} versus the ratio $D_{solute}/D_{solvent}$ where the solvent is H_2O in the aqueous solution case and the aluminosilicate matrix in the silicate liquid case. For $D_{solvent}$ we use the self-diffusion coefficient of H_2O (Bourg and Sposito, 2007) and the measured diffusion coefficient of Si. For the aqueous solutions, $D_{\text{H}_2\text{O}}$ is constant for a given temperature, so the data indicate that there is a correlation between E and diffusivity of the solute. For the silicate liquids, D_{Si} is variable so there is not a one-to-one correspondence between D_{solute} and $D_{solute}/D_{solvent}$. A summary of the data used in the compilation of Fig. 5 is provided in Table 3.

In the case of ions in aqueous solution, recent studies offer a molecular scale explanation of the pattern shown in Fig. 5. The efficiency of isotope separation for a cation (and its diffusivity) correlates with the residence time of water molecules in its first solvation shell as determined from molecular dynamics simulations (Bourg and Sposito, 2007, 2008; Bourg et al., 2010). If the water molecules are

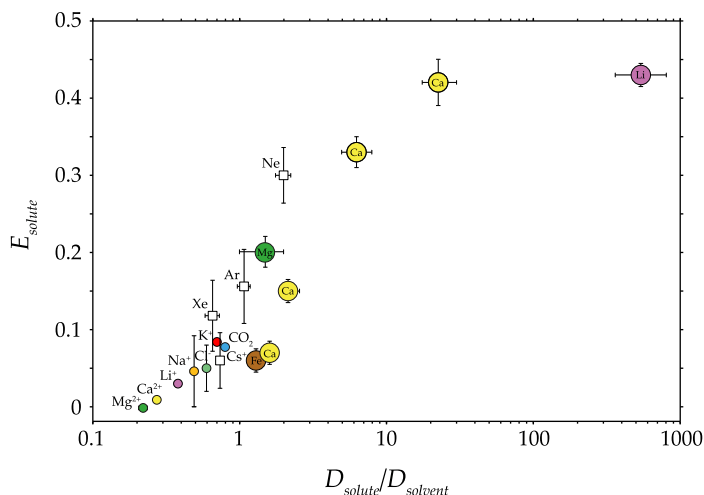


Fig. 5. The efficiency of isotope separation E in silicate liquids (large symbols) compared to E in aqueous solutions (small symbols). The subscript *solvent* refers to H_2O in aqueous solutions and Si (or SiO_2) in silicate liquids. Square symbols represent values obtained solely from molecular dynamics simulations (see Table 3 for complete summary).

Table 3

Summary of the values and associated references used in the compilation of Fig. 5.

Diffusing medium	Experiment No.	Description	Isotopic system	D_{solute} (m ² /s)	(+/-)	D_{solvent} (m ² /s)	(+/-)	E	(+/-)	References
Natural volcanic liquids	DF-9	basalt-rhyolite	⁴⁴ Ca/ ⁴⁰ Ca	3.60E-12	-	2.30E-12	-	0.07	(0.01)	Watkins et al. (2009)
	RB-2	basalt-rhyolite	⁴⁴ Ca/ ⁴⁰ Ca	1.30E-11	-	5.90E-12	-	0.15	(0.01)	Richter et al. (2003)
	RB-X	basalt-rhyolite	²⁶ Mg/ ²⁴ Mg	-	-	1.10E-11	-	0.10	(0.01)	Richter et al. (2008)
	RB-5	basalt-rhyolite	⁷ Li/ ⁶ Li	3.20E-09	-	5.90E-12	-	0.43	(0.01)	Richter et al. (2003)
	RB-X	basalt-rhyolite	⁵⁶ Fe/ ⁵⁴ Fe	1.40E-11	-	1.10E-11	-	0.06	(0.01)	Richter et al. (2009)
Simple silicate liquids	AB-AN	albite + anorthite	⁴⁴ Ca/ ⁴⁰ Ca	4.50E-11	-	2.00E-12	-	0.42	(0.03)	This study
	AB-DI	albite + diopside	⁴⁴ Ca/ ⁴⁰ Ca	2.50E-11	-	4.00E-12	-	0.33	(0.02)	This study
	AB-DI	albite + diopside	²⁶ Mg/ ²⁴ Mg	6.00E-12	-	4.00E-12	-	0.20	(0.02)	This study
Diffusing medium	Experiment No.	Description	Isotopic system					E		References
Liquid water (25 °C)	-	MD simulation	He	7.85E-09	(0.54)	2.40E-09	(0.10)	0.342	(0.056)	Bourg and Sposito (2008)
	-	MD simulation	Ne	4.78E-09	(0.37)	2.40E-09	(0.10)	0.300	(0.036)	Bourg and Sposito (2008)
	-	MD simulation	Ar	2.57E-09	(0.57)	2.40E-09	(0.10)	0.156	(0.048)	Bourg and Sposito (2008)
	-	MD simulation	Xe	1.57E-09	(0.11)	2.40E-09	(0.10)	0.118	(0.046)	Bourg and Sposito (2008)
Liquid water (75 °C)	-	Experiment	²⁵ Mg/ ²⁴ Mg	1.21E-09	(0.06)	5.50E-09	(0.10)	0.000	(0.003)	Richter et al. (2006); Bourg and Sposito (2007)
	-	Experiment	⁷ Li/ ⁶ Li	2.09E-09	(0.08)	5.50E-09	(0.10)	0.030	(0.004)	Richter et al. (2006); Bourg and Sposito (2007)
	-	Experiment	³⁷ Cl/ ³⁵ Cl	3.27E-09	(0.14)	5.50E-09	(0.10)	0.050	(0.030)	Richter et al. (2006); Bourg and Sposito (2007)
	-	MD simulation	Na	2.69E-09	(0.14)	5.50E-09	(0.10)	0.058	(0.044)	Bourg et al. (2010)
	-	Experiment	²⁴ Na/ ²² Na	-	-	-	-	0.046	(0.046)	Pikal (1972)
	-	MD simulation	K	3.85E-09	(0.17)	5.50E-09	(0.10)	0.098	(0.034)	Bourg et al. (2010)
	-	Experiment	⁴¹ K/ ³⁹ K	-	-	-	-	0.084	(0.004)	Bourg et al. (2010)
	-	MD simulation	Cs	4.04E-09	(0.20)	5.50E-09	(0.10)	0.060	(0.036)	Bourg et al. (2010)
	-	MD simulation	Ca	1.50E-09	(0.03)	5.50E-09	(0.10)	0.000	(0.022)	Bourg et al. (2010)
	-	Experiment	⁴⁴ Ca/ ⁴⁰ Ca	-	-	-	-	0.009	(0.001)	Bourg et al. (2010)
Liquid water (25 °C)	-	Experiment	¹³ CO ₂ / ¹² CO ₂	1.91E-09	(0.27)	2.40E-09	(0.10)	0.077	(0.004)	Jähne et al. (1987)
	-	Experiment	⁴ He/ ³ He	7.22E-09	(0.73)	2.40E-09	(0.10)	0.97	(0.18)	Jähne et al. (1987)

weakly bound, as for Li^+ , it implies that the ion can move through the liquid as a single atom and therefore the mass dependence of the diffusivity is more strongly influenced by the relative mass difference of the isotopes. If a number of water molecules are strongly bound to the ion, the effective mass of the diffusing species is larger than that of the ion, and the mass dependence of the diffusivity is highly attenuated. Since the hydration shell is dynamic, the actual situation is that the ion spends part of the time isolated and part of the time bound to water molecules. If the hydration shell is massive enough, and the lifetime of the water molecules in the hydration shell long enough, the isotopic effect tends toward zero, as seems to be the case for aqueous Mg^{2+} . For the other ions the mass dependence of the diffusivity is non-zero, but much smaller than the inverse square root of the isotopic masses ($E = 1$). It should be noted that in the cases of Mg^{2+} , Ca^{2+} , K^+ , and Li^+ , the ratio of the diffusion coefficients for the isotopes has been measured experimentally, whereas the lifetime of water molecules in the hydration shell has been estimated using molecular dynamics models.

An important difference between aqueous solutions and silicate liquids is that ions in aqueous solution typically diffuse more slowly than H_2O , whereas elements in silicate liquids diffuse faster than Si. For aqueous solutions this effect may be due to charge balance constraints in addition to hydration, and the fact that water molecules are weakly bound to each other. In silicate liquids, Si is strongly bound in multi-atom complexes with O (as well as Al and other Si atoms), so it diffuses more slowly than other elements. The average size and lifetime of these Si–O complexes varies with liquid composition and could account for the variations in D_{Si} .

5.4. Other quantitative parameters

The parameter $D_{\text{solute}}/D_{\text{solvent}}$ is convenient in that it can be determined by experiment, but other parameters, particularly those at the molecular scale, may provide additional insight. Molecular dynamics simulations are increasingly used to study the structure and dynamics of silicate melts (Vuilleumier et al., 2009; de Koker and Stixrude, 2010; Karki, 2010). For example, solute diffusivity as well as the efficiency of isotope separation could be related to (1) the average lifetime of solute–matrix bonds ($\tau_{\text{solute-Si}}$, $\tau_{\text{solute-O}}$), (2) the mutual-diffusion coefficients (Wheeler and Newman, 2004) of the solute with individual elements of the Al–Si network such as AlO_4 tetrahedra, (3) the interconnectivity of the Al–Si network or relative proportions of Q^n species, where Q refers to an SiO_4 tetrahedron connected by a bridging oxygen atom to n adjacent SiO_4 tetrahedra, or (4) the dynamics of the Al–Si network itself, which could be approximated as the average lifetime of bridging oxygen bonds ($\tau_{\text{Si-O}}$) and would represent the exchange rate of Q^n species. Essentially, these parameters express the nanometer-scale coupling of solute and solvent motions on time scales that range from rapid solute–solvent collisions to slow reorganizations of the Al–Si network. Theoretical and MD simulation studies indicate that in simple (hard-sphere or Lennard–Jones) fluids and in liquid water, the efficiency of isotope separation E decreases as solute–sol-

vent coupling increases (Bhattacharyya and Bagchi, 2000; Bourg et al., 2010).

To our knowledge, there are no MD studies on silicate liquids in which isotope-specific diffusivities have been reported. Additionally, due to computational constraints (cf. Karki, 2010) most MD simulations on silicate liquids are carried out at temperatures that far exceed those of our experiments (typically 3000–6000 K). It is nevertheless worthwhile to consider how MD studies may provide a more detailed understanding of the mechanisms of diffusive isotope separation in silicate liquids.

In a study that simulates relatively low temperatures (1827–3727 °C; $P \approx 1$ GPa), Horbach et al. (2001) investigated the structure and dynamics of Na-silicate melts ($\text{Na}_2\text{Si}_2\text{O}_5$, $\text{Na}_2\text{Si}_3\text{O}_7$, and SiO_2). Na was found to diffuse rapidly and the ratio $D_{\text{Na}}/D_{\text{Si}}$ was large for all conditions studied (≈ 100 at 1827 °C and down to ≈ 5 at 3727 °C). The diffusivity of Na, Si, and O were compared to the average lifetime of chemical bonds ($\tau_{\alpha-\beta}$) between atoms of type α and β . The mobility of Na atoms is not correlated with the lifetime of Na–O or Na–Si bonds, but rather with the lifetime of Na–Na bonds, suggesting that the elementary diffusion step for Na is the breaking of Na–Na bonds (Horbach et al., 2001). This conclusion is consistent with a model where Na atoms diffuse by site-hopping among Na “sites” in a static Si–O matrix. In this end-member regime we would expect E_α to be large. The behavior of Si was found to be more complicated; there is no direct relationship between D_{Si} and the lifetime of Si–O or Si–Si bonds (Horbach et al., 2001). The data in Fig. 4 indicate that $D_{\text{O}}/D_{\text{Si}}$ and E_α co-vary, but we cannot discern whether they are responding to differences in the relative lifetimes of chemical bonds (e.g., $\tau_{\text{Si-Si}}/\tau_{\alpha-\text{Si}}$), other parameters such as Q^n speciation, or a combination.

5.5. Geological implications

It is now recognized that discernible isotope effects can be produced by chemical diffusion in molten silicates. This result and the recent discovery of temperature-induced fractionations (Richter et al., 2008, 2009; Huang et al., 2010) suggest that there is considerable stable isotopic variability in igneous systems. A number of recent studies have documented these effects and have used them to assess the role of diffusion and extent of isotopic disequilibrium during crystallization (Teng et al., 2008a), subsolidus cooling (Barrat et al., 2005; Beck et al., 2006; Dauphas et al., 2010), thermal migration (Lundstrom, 2009) and wallrock contamination (Teng et al., 2006, 2008b; Chopra et al., 2009). Future studies will undoubtedly uncover additional isotopic heterogeneity in igneous rocks, and interpreting these effects quantitatively will require simplified physical models and knowledge of the magnitude of E_{solute} and how it varies with temperature, pressure, and composition (e.g., Beck et al., 2006; Dauphas et al., 2010).

The correlation of E_{solute} with $D_{\text{solute}}/D_{\text{solvent}}$ offers a useful empirical relationship for predicting where there may be large isotope effects in nature. An important conclusion is that $D_{\text{solute}}/D_{\text{solvent}}$, and E_{solute} are likely to be greater in high- SiO_2 liquids than in low- SiO_2 liquids and with decreas-

ing temperature toward the glass transition (Dingwell, 1990). Watson and Müller (2009) modeled the expected effects of diffusive isotopic fractionations of trace elements incorporated during the growth of magmatic crystals. They show the expected isotopic profiles within and around crystals for different values of E , crystal growth rate and fluid velocity. For $^{44}\text{Ca}/^{40}\text{Ca}$, a diffusivity difference of 1% ($E = 0.21$), which may be a reasonable value for a rhyolitic liquid, can lead to fractionations of 4‰ for a cm-sized crystal in a stagnant fluid. This value assumes that equilibrium as well as surface reaction effects are negligible, which may or may not be the case. Models such as this provide a useful foundation for future comparison to actual measurements; at present there are few (if any) on mass-dependent isotope effects in igneous minerals at the sub-grain scale. Our experimental results also indicate that even for a given bulk composition, different cations may have significantly different values of E and therefore different isotope pairs may be sensitive as recorders of crystallization conditions during different stages of magmatic differentiation.

6. SUMMARY AND CONCLUSIONS

Superliquidus diffusion-couple experiments using simplified synthetic silicate liquids were carried out to investigate why the efficiency of isotope separation by diffusion varies between cations and in liquids of different composition. Two diffusion experiments were conducted using combinations of the mineral constituents albite, anorthite and diopside. For both experiments, a simplified chemical diffusion model was used to estimate cation diffusivities (D_{cation}) and the efficiency of isotope separation (E).

The experimental results indicate that a relationship exists between the efficiency of isotope separation E and the normalized diffusivity – the ratio of the mobility of the cation (D_{cation}) to the mobility of the liquid matrix (D_{Si}). Where $D_{\text{cation}} \leq D_{\text{Si}}$, isotope separation by diffusion is less efficient because the cation is likely to be more strongly bound to the aluminosilicate matrix, and hence, the mass difference between isotopes is effectively reduced because the cation is associated with a larger complex that includes Si, and its motion in the liquid is correlated with the motions of many other atoms. Conversely, where $D_{\text{cation}} \gg D_{\text{Si}}$, isotope separation by diffusion is more efficient because it is likely that the element is not strongly bound to the aluminosilicate matrix and is diffusing mostly as an isolated atom through a quasi-stationary aluminosilicate framework.

Our results and interpretive model offer a plausible explanation for why diffusive isotope effects are greater in silicate liquids at 1450 °C than in aqueous solutions at 25–75 °C. In silicate liquids, the solvent is mainly silicon in the form of silica tetrahedra, which are generally less mobile than the other cations; that is, $D_{\text{cation}}/D_{\text{solvent}}$ is generally greater than unity. In aqueous solutions, by contrast, the solvent water molecules are generally more mobile than the diffusing ions owing to relatively strong interactions between ions and their surrounding water molecules.

The correlation of E_{solute} with $D_{\text{solute}}/D_{\text{solvent}}$ offers a useful empirical relationship for estimating diffusive isotope ef-

fects in geological liquids. The parameter $D_{\text{solute}}/D_{\text{solvent}}$ is convenient in that it can be determined by experiment, but it is only a proxy for how strongly bound a cation is to the liquid matrix. Other parameters may also be important, and molecular simulations should be used to further investigate isotope separation in silicate liquids.

Our empirical result also provides a context for discussing diffusive isotope effects in natural geologic environments. It is now recognized that kinetic isotope separations can be relatively large, even at the high temperatures associated with molten silicates, and our results indicate that these effects for common cations like K, Ca, Mg, Fe and Li, are likely to be greater in high-SiO₂ liquids than in low-SiO₂ liquids. At present there are only a few documented instances of diffusive isotope effects in natural rocks – mostly in mafic systems – and future stable isotope studies will doubtless uncover much more isotopic variability. Quantifying these effects will require a combination of experiments and molecular-scale modeling in order to better understand and/or characterize the efficiency of isotope separation for different isotope pairs under different conditions. This information in turn will be useful for assessing the effects of diffusion and extent of isotopic disequilibrium during crystallization, mineral dissolution, and chemical alteration on the differentiation of silicate liquids that solidify to form igneous rocks.

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APPENDIX A

A.1. Additional comments on relating diffusivity to mass

The simplest treatment of isotopic diffusion applies to particles in an ideal (i.e., monatomic and dilute) gas because the identity of the diffusing species is known and potential interactions between particles can be neglected. From kinetic theory the diffusivity D is the product of the root mean speed v_{rms} of particles and the mean free path l between collisions:

$$D = l \cdot \underbrace{\left(\frac{3RT}{m}\right)^{1/2}}_{v_{\text{rms}}} \quad (\text{A1})$$

Since D varies inversely with the square root of particle mass m , one might anticipate from Eq. (A1) that the ratio

of isotopic diffusion coefficients is proportional to the square root of the inverse mass ratio between the isotopes:

$$\frac{D_2}{D_1} = \left(\frac{m_1}{m_2}\right)^{1/2}. \quad (\text{A2})$$

This is referred to as the square-root-of-mass law and is only valid for systems in which the assumptions of kinetic theory apply. In other systems such as non-dilute gases, liquids, and solids, Eq. (A2) serves as a useful reference from which to compare the mass dependence on diffusion coefficients. For example, there is a substantial literature on isotopic diffusion in solids (Schoen, 1958; Rothman and Peterson, 1965; Le Claire, 1966; Mundy et al., 1966; many others), and deviations from the square-root-of-mass law are combined with theories of lattice or vacancy diffusion to infer diffusion mechanisms (cf. Section 1.3 in Watkins et al., 2009).

In contrast to theories of diffusion in the gas or solid phase, there is no simple scaling law that describes the relationship between diffusivity and mass in liquids because isotopic substitution affects translational and rotational mobility differently (McLaughlin, 1960). When rotation does not contribute significantly to momentum transfer, molecular motion can be described by the linear equation of motion:

$$F_x = m \frac{dv_x}{dt}, \quad (\text{A3})$$

where F_x is the net central force acting on a molecule due to the potential field of its neighbors and v_x is the linear velocity. For spherically symmetric molecules such as cyclohexane and methane, and in which only central forces matter, Eq. (A3) is expected to adequately describe molecular motion and the ratio of transport coefficients has been shown to be in agreement with the square-root-of-mass law (McLaughlin, 1960). If, on the other hand, rotational motion is important for momentum transfer, the angular equation of motion is needed for describing changes in momentum due to non-central forces:

$$G_x = I_{x\beta} \frac{d\omega_\beta}{dt}, \quad (\text{A4})$$

where G_x is the torque on a molecule from forces due to neighboring atoms, $I_{x\beta}$ is the inertia tensor, and ω_β is the angular velocity. Rotational and translational motions of molecules are not independent; a change in torque can arise from translation of a nearby molecule or a change in force can arise from rotation of nearby molecule. This translational-rotational coupling is associated with molecular anisotropy and its effect on transport coefficients depends on intermolecular forces, which are theoretically complex (Weingartner et al., 1989). Broadly speaking, however, it is clear that isotope substitution will affect m and $I_{x\beta}$ differently and the resulting influence on diffusion coefficients will vary depending on the importance of rotational motion. For anisotropic molecules such as water and benzene, the ratio of isotope-specific molecular diffusion coefficients does not agree with the square root of mass law but is in better agreement when mass is replaced with the principal moments of inertia (McLaughlin, 1960; Weingartner et al., 1989):

$$\frac{D_2}{D_1} = \left(\frac{I_{1,\gamma}}{I_{2,\gamma}}\right)^{1/2}, \quad (\text{A5})$$

where γ refers to any of the principal axes x , y , and z .

In cases where Eq. (A5) might apply, one first needs detailed information on the structure of the diffusing species. The principal moments of inertia are known or can be calculated for simple organic molecules (e.g., Holz et al., 1996) and self diffusion NMR measurements show that the isotope effect on translational and rotational diffusion tends more towards a square-root of the moment of inertia law when there is strong translation-rotation coupling (e.g., Holz et al., 1996; Hardy et al., 2001). In silicate liquids, however, the picture is not as simple because diffusion occurs through rapid chemical exchanges instead of molecular mechanisms of motion (Stebbins, 1995). In other words, even the definition of speciation in silicate liquids is ambiguous. This motivates several of the questions addressed in this study: (1) How and why does the mass dependence on diffusivity vary between cations in molten silicates? (2) How and why does the mass dependence on diffusivity depend on liquid composition? (3) Can the physical mechanisms of diffusion be inferred from the mass dependence on diffusivity in molten silicates? (4) Can the magnitude of diffusive isotope effects be predicted for a cation or liquid composition?

A.2. Additional comments on multicomponent diffusion models

When the multicomponent diffusion equation is cast in vector notation, the diffusion coefficients that relate fluxes to gradients are housed in a diffusivity matrix where the off-diagonal terms represent diffusive coupling. Since the Al, Si, and Na gradients are relatively small in the AB-AN and AB-DI experiments, explicitly accounting for the off-diagonal terms and their mass-dependence would add additional free parameters without changing our interpretation or the overall pattern shown in Fig. 4.

To illustrate this point, Fig. A1 compares data from the AB-AN experiment to model profiles calculated assuming a hypothetical, non-unique 3×3 diffusivity matrix. Model 1 assumes no mass dependence on the off-diagonal diffusivities for Ca whereas Model 2 assumes a mass dependence on the off-diagonal diffusivities that is equivalent to that imposed on the diagonal term. Although the multicomponent diffusion problem offers a more detailed description of the chemical fluxes in space and time and better fits to the major-element data, the isotopic profiles are similar for the AB-AN experiment regardless of the mass-dependence on the off-diagonal terms (Model 1 versus Model 2).

The EBD approach for Ca and Mg is ultimately justified by (1) the initial conditions of the AB-AN and AB-DI experiments, (2) the simplicity of the EBD model and (3) the quality of the fits to the Ca and Mg data in Figs. 1-3, which show that the EBD model provides an accurate representation of the Ca and Mg chemical and isotopic fluxes and the evolution of the diffusion profiles in space and time.

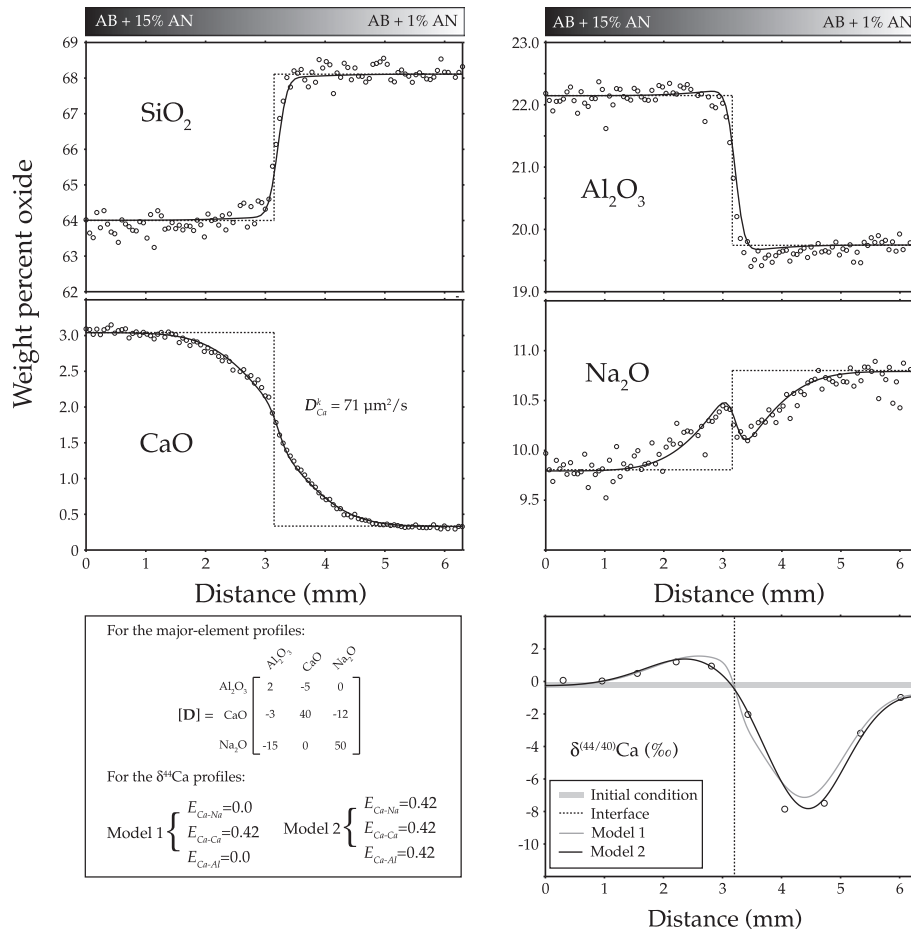


Fig. A1. Major-element profiles from the AB-AN experiment compared to model diffusion profiles (solid lines) using a hypothetical diffusivity matrix. $[D]$ ($\mu\text{m}^2/\text{s}$) was estimated from smoothed profiles of the data as inputs in MultiDIFLUX (Dayananda, 2005), and refined by trial-and-error. The lower right panel shows that the isotopic profiles are relatively insensitive to a mass-dependence on the off-diagonal terms in $[D]$ (Model 1 versus Model 2).

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