Evidence for $B^+ \to \tau^+ \nu_\tau$ decays using hadronic $B$ tags

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We present a search for the decay $B^+ \rightarrow \tau^+ \nu_\tau$, using $467.8 \times 10^6 B \bar{B}$ pairs collected at the $\Upsilon(4S)$ resonance with the BABAR detector at the SLAC PEP-II B-Factory. We select a sample of events with one completely reconstructed $B^+$ in an hadronic decay mode ($B^- \rightarrow D^{(*)0} X^-$ and $B^- \rightarrow J/\psi X^-$). We examine the rest of the event to search for a $B^+ \rightarrow \tau^+ \nu$ decay. We identify the $\tau^+$ lepton in the following modes: $\tau^+ \rightarrow e^+ \nu_e \ell_-, \tau^+ \rightarrow \mu^+ \nu_\mu \ell_-, \tau^+ \rightarrow \pi^+ \ell_-$, and $\tau^+ \rightarrow \rho \ell_-$.

We find an excess of events with respect to expected background, which excludes the null signal hypothesis at the level of 3.5 $\sigma$ and can be converted to a branching fraction central value of $B(B^+ \rightarrow \tau^+ \nu_\tau) = (1.80^{+0.54}_{-0.51} \text{(stat.)} \pm 0.26 \text{(syst.)}) \times 10^{-4}$. 


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INTRODUCTION

The study of the purely leptonic decay is of particular interest as a test of the Standard Model (SM) and a search for physics beyond the SM. It is sensitive to the product of the $B$ meson decay constant $f_B$, and the absolute value of the Cabibbo-Kobayashi-Maskawa matrix element $|V_{ub}|$. In the SM the branching fraction is given by:

$$B(B^+ \to \tau^+ \nu) = f_B^2 |V_{ub}|^2 \frac{G_F m_B m_{\tau}^2}{8\pi} \left[ 1 - \frac{m_{\tau}^2}{m_B^2} \right] \tau_B^+, \quad (1)$$

where $G_F$ is the Fermi constant, $\tau_B^+$ is the $B^+$ lifetime, and $m_B$ and $m_{\tau}$ are the $B^+$ meson and $\tau$ lepton masses.

The process is sensitive to possible extensions of the SM. For instance, in two-Higgs doublet models and in minimal supersymmetric extensions of the SM it can be mediated by a charged Higgs boson. A branching fraction measurement can therefore also be used to constrain the parameter space of extensions of the SM. In a previously published analysis, based on a tagging technique using hadronic $B$ decays that is similar to that used in this paper and a smaller data set, the BABAR collaboration measured $B(B^+ \to \tau^+ \nu) = (1.8^{+0.4}_{-0.3}(\text{stat.}) \pm 0.4(\text{syst.})) \times 10^{-4}$, and using tagging based on reconstruction of semileptonic $B$ decays $B(B^+ \to \tau^+ \nu) = (1.3 \pm 0.8(\text{stat.}) \pm 0.2(\text{syst.})) \times 10^{-4}$.

The Belle collaboration measured, with a similar tagging technique used in this analysis, the branching fraction to be $B(B^+ \to \tau^+ \nu) = (1.79^{+0.56}_{-0.51}(\text{stat.})^{+0.40}_{-0.37}(\text{syst.})) \times 10^{-4}$, and using a tagging algorithm based on the reconstruction of semileptonic $B$ decays $B(B^+ \to \tau^+ \nu) = (1.54^{+0.38}_{-0.37}(\text{stat.})^{+0.29}_{-0.31}(\text{syst.})) \times 10^{-4}$.

THE BABAR DETECTOR AND DATASET

The data used in this analysis were collected with the BABAR detector at the PEP-II storage ring. The sample corresponds to an integrated luminosity of 426 fb$^{-1}$ at the $\Upsilon(4S)$ resonance (on-resonance) and 44.5 fb$^{-1}$ taken at 40 MeV below the $B\bar{B}$ production threshold (off-resonance), which is used to study background from $e^+e^- \to f\bar{f}$ ($f = u, d, s, c, \tau$) continuum events. The on-resonance sample contains $(467.8 \pm 5.1) \times 10^6$ $B\bar{B}$ decays. The detector is described in detail elsewhere. Charged particle trajectories are measured in the tracking system composed of a five-layer silicon vertex detector and a 40-layer drift chamber (DCH), operating in a 1.5 T solenoidal magnetic field. A Cherenkov detector is used for charged $\pi-K$ discrimination, a CsI calorimeter (EMC) for photon and electron identification, and the flux return of the solenoid, which consists of layers of iron interspersed with resistive plate chambers or limited streamer tubes, for muon and neutral hadron identification.

In order to estimate signal selection efficiencies and to study physics backgrounds, we use a Monte Carlo (MC) simulation based on GEANT4. In MC simulated signal events one $B^+$ meson decays as $B^+ \to \tau^+ \nu$, and the other decays in any final state. The $B\bar{B}$ and continuum MC samples are equivalent to approximately three times and 1.5 times, respectively, the accumulated data sample. Beam-related background and detector noise are taken from data and overlaid on the simulated events.

SIGNAL SELECTION

We reconstruct an exclusive decay of one of the $B$ mesons in the event (which we refer to as the tag $B$) and examine the rest of the event for the experimental signature of $B^+ \to \tau^+ \nu$ (charged-conjugate modes are implied throughout the paper). We consider the most abundant $\tau$ decay modes $\tau^+ \to e^+ \nu_\tau$, $\tau^+ \to \mu^+ \nu_\tau$, $\tau^+ \to \pi^+ \nu$, $\tau^+ \to \rho^+ \nu$, totaling approximatively 70% of all $\tau$ decays. The signal region in data is kept blind until the end of the analysis chain when we extract the signal yield. We reconstruct the tag $B$ candidate in the set of hadronic decays $B^+ \to M^0 \pi^-$, where $M^0$ denotes a $D^{(*)0}$ or a $J/\psi$, and $X^-$ denotes a system of hadrons with total charge $-1$ composed of $n_1 \pi^\pm$, $n_2 K^\pm$, $n_3 \pi^0$, $n_4 K^{*0}$, where $n_1 + n_2 \leq 5$, $n_2 \leq 2$, $n_3$ and $n_4 \leq 2$. We reconstruct the $D^0$ as $D^{*0} \to K^-\pi^+, K^-\pi^+\pi^0, K^-\pi^+\pi^-\pi^0, K^0\pi^0, K^0\pi^+\pi^-\pi^0, K^0\pi^+\pi^-\pi^0, K^+K^-, \pi^+\pi^-$. We reconstruct the $D^{*0}$ meson as $D^{*0} \to D^{0}\pi^0, D^{0}\pi^0, D^{0}\pi^0$, and the $J/\psi$ meson as $J/\psi \to e^+e^-, \mu^+\mu^-$. The kinematic consistency of the tag $B$ candidates is checked with the beam energy-substituted mass $m_{\text{ES}} = \sqrt{s}/4 - p_B$ and the energy difference $\Delta E = E_B - \sqrt{s}/2$, where $\sqrt{s}$ is the total energy in the $\Upsilon(4S)$ center of mass system and $p_B$ and $E_B$ denote respectively the momentum and the energy of the tag $B$ candidate in the center of mass frame. The resolution on $\Delta E$ is measured to be $\sigma_{\Delta E} = 10 - 35$ MeV, depending on the decay mode; we require $|\Delta E| < 3\sigma_{\Delta E}$. Events with a candidate tag $B$ arise from two possible classes with different $m_{\text{ES}}$ distributions. Signal events with a correctly reconstructed tag $B$ and the other $B$ decaying as $B \to \tau \nu$, and background events from $\Upsilon(4S) \to B^+B^-$ with a correctly reconstructed tag

\[ B(B^+ \to \tau^+ \nu) = \frac{f_B^2 |V_{ub}|^2 G_F m_B m_{\tau}^2}{8\pi} \left[ 1 - \frac{m_{\tau}^2}{m_B^2} \right] \tau_B^+, \quad (1) \]
\( B \) are characterized by an \( m_{ES} \) distribution peaked at the \( B \) mass. The other class of events consists of continuum background, \( e^+e^- \rightarrow q\bar{q} \ (q = u, \ s, \ldots) \) and \( e^+e^- \rightarrow \tau^+\tau^- \), and combinatorial background, \( \Upsilon(4S) \rightarrow B^0\bar{B}^0 \) or \( B^+B^- \) in which the tag \( B \) is misreconstructed: this class of events has a broad \( m_{ES} \) distribution that can be modeled by means of a phenomenological threshold function (ARGUS function) [9].

If multiple tag \( B \) candidates are reconstructed we select that with the lowest value of \( |\Delta E| \). The purity \( \mathcal{P} \) of each reconstructed \( B \) decay mode is estimated as the ratio of the number of peaking events with \( m_{ES} > 5.27 \text{ GeV} \) to the total number of events in the same range. We consider only events with the tag \( B \) reconstructed in decay modes with \( \mathcal{P} > 0.1 \). The yield in data is determined by means of an extended unbinned maximum likelihood fit to the \( m_{ES} \) distribution, as shown in figure 1. We use as probability density function (PDF) for the combinatorial and continuum background an ARGUS function, while for the correctly reconstructed tag \( B \) component we use as PDF a Gaussian function with an exponential tail (Crystal Ball function) [10]. Combinatorial and continuum backgrounds in any discriminating variable are estimated from a sideband in \( m_{ES} \) (5.209 GeV < \( m_{ES} < 5.260 \text{ GeV} \)) and extrapolated into the signal region (\( m_{ES} > 5.270 \text{ GeV} \)) using the results of a fit to an ARGUS function. The peaking \( B^+B^- \) background is determined from \( B^+B^- \) MC, after subtraction of the combinatorial component to avoid double counting by means of a similar fit.

![Graph](image)

FIG. 1: Fit to the \( m_{ES} \) distribution in data. Dots are data, the blue curve represents the fitted combinatorial and continuum background.

After the reconstruction of the tag \( B \), we apply a set of selection criteria on the rest of the event. We require the presence of only one well reconstructed charged track (signal track), with charge opposite to that of the tag \( B \). The \( \tau \) lepton is reconstructed in one of four decay modes: \( \tau^+ \rightarrow e^+\nu\bar{\nu}, \tau^+ \rightarrow \mu^+\nu\bar{\nu}, \tau^+ \rightarrow \pi^+\nu, \tau^+ \rightarrow \rho^+\nu \). We separate the event sample in four categories using particle identification criteria applied to the signal track. The \( \tau^+ \rightarrow \rho^+\nu \) sample is obtained by associating the signal track with a \( \pi^0 \) reconstructed from a pair of neutral clusters with invariant mass between 115 MeV/c^2 and 155 MeV/c^2. In order to remove the \( e^+e^- \rightarrow \tau^+\tau^- \) background we impose \( \tau \) mode dependent requirements, preserving 90% of the \( B^+ \rightarrow \tau^+\nu_e \) signal, on the ratio between the 2^{nd} and the 0^{th} Fox-Wolfram moments (R2) [11] calculated using all the charged tracks and neutral clusters of the event.

In order to reject the continuum and combinatorial background we use discriminating variables constructed from the kinematics of the tag \( B \) candidate. The first variable is the momentum in the CM frame (\( p^*_M \)) of the \( D^{(*)0} \) or \( J/\psi \) candidate reconstructed from the decay products of the tag \( B \). The second variable is the absolute value of the thrust [12] (\( |T_B| \)) of the tag \( B \). The third variable is the cosine of the angle between the thrust of the tag \( B \) and the thrust of the rest of the event (\( \cos\theta_{TB} \)). We combine \( p^*_M, |T_B| \) and \( \cos\theta_{TB} \) in a likelihood ratio

\[
L_C = L_S(p^*_M, |T_B|, \cos\theta_{TB}) / L_S(p^*_M, |T_B|, \cos\theta_{TB}) + L_B(p^*_M, |T_B|, \cos\theta_{TB}),
\]

where the signal (S) and background (B) likelihoods are obtained from the products of the PDFs of the three discriminating variables:

\[
L_S(p^*_M, |T_B|, \cos\theta_{TB}) = P_S(p^*_M)P_S(|T_B|)P_S(\cos\theta_{TB}) \quad \text{and} \quad L_B(p^*_M, |T_B|, \cos\theta_{TB}) = P_B(p^*_M)P_B(|T_B|)P_B(\cos\theta_{TB}).
\]
The PDFs for the signal modes are obtained from the signal MC, whereas the PDFs for backgrounds are obtained from the $m_{	ext{ES}}$ sideband in data.

In order to further reject the background from correctly reconstructed tag $B$ events, we impose a requirement on center of mass momentum of the signal track for the $\tau^+ \rightarrow e^+ \nu \bar{\nu}$, $\tau^+ \rightarrow \mu^+ \nu \bar{\nu}$ and $\tau^+ \rightarrow \pi^+ \nu$ modes. For the $\tau^+ \rightarrow \rho^+ \nu$ mode we combine in a likelihood ratio ($L_R$) the following variables: the invariant mass of the signal track and the $\pi^0$, the total momentum in the CM frame of the pair $|p_{\pi^0}|$, the momentum in the CM frame of the $\pi^0$, and the missing mass of the event. The PDFs used in the likelihood ratio for the signal and background are determined from signal and $B^+B^-\text{MC}$, respectively.

The most discriminating variable is $E_{\text{extra}}$, defined as the sum of the energies of the neutral clusters not associated with the tag $B$ or with the signal $\pi^0$ from the $\tau^+ \rightarrow \rho^+ \nu$ mode, and passing a minimum energy requirement (60 MeV). Signal events tend to peak at low $E_{\text{extra}}$, background events, which contain additional sources of neutral clusters, tend to be distributed at higher values.

We optimize the selection requirements, including those on the purity $P$ of the tag $B$ and the minimum energy of the neutral clusters, aiming at the lowest expected uncertainty in the branching fraction fit. In order to estimate the uncertainty, which includes the statistical and the largest systematic uncertainties, we run 1000 toy experiments extracted from the background and signal expected shapes for a set of possible selection requirements, assuming a branching fraction of $1.4 \times 10^{-6}$\cite{13}.

The signal selection requirements are summarized in Table I. The $E_{\text{extra}}$ distribution with all the selection requirements applied is shown in Figure 2.

<table>
<thead>
<tr>
<th>Variable</th>
<th>$\tau^+ \rightarrow e^+ \nu \bar{\nu}$</th>
<th>$\tau^+ \rightarrow \mu^+ \nu \bar{\nu}$</th>
<th>$\tau^+ \rightarrow \pi^+ \nu$</th>
<th>$\tau^+ \rightarrow \rho^+ \nu$</th>
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<td>&gt; 10%</td>
<td>&gt; 10%</td>
<td>&gt; 10%</td>
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<td>cluster energy (MeV)</td>
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<td>&lt; 0.56</td>
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<td>&lt; 0.51</td>
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<td>&gt; 0.2</td>
<td>&gt; 0.3</td>
<td>&gt; 0.45</td>
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<td>&lt; 2</td>
<td>&gt; 1.4</td>
<td>&gt; 0.8</td>
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<tr>
<td>$L_R$</td>
<td></td>
<td></td>
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<td>&gt; 0.8</td>
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**TABLE I:** Optimized signal selection criteria for each $\tau$ mode.

**BRANCHING FRACTION MEASUREMENT PROCEDURE AND RESULTS**

We use an extended unbinned maximum likelihood fit to extract the $B^+ \rightarrow \tau^+ \nu$ branching fraction. The likelihood function for the $N_k$ candidates reconstructed in one of the four $\tau$ decay modes $k$ is

$$L_k = e^{-(n_{i \tau} + m_{i \tau})} \prod_{i=1}^{N_k} \left( n_{i,k} P_{i,k}^*(E_{i,k}) + n_{b,k} P_{b,k}^*(E_{i,k}) \right)$$ \hspace{1cm} (2)

where $n_{i,k}$ is the signal yield, $n_{b,k}$ is the background yield, $E_{i,k}$ is the $E_{\text{extra}}$ value of the $i^{th}$ event, $P_{i,k}^*$ is the probability density function of signal events, and $P_{b,k}^*$ is the probability density function of background events. The background yields in each decay mode are permitted to float independently of each other in the fit, while the signal yields are constrained to a single branching ratio via the relation:

$$n_{i,k} = N_{B^+} \times \epsilon_k \times B$$ \hspace{1cm} (3)

where $N_{B^+} = (4.678 \pm 0.051) \times 10^6$ is the number of $B \bar{B}$ pairs in the data sample, $\epsilon_k$ is the $\tau$ decay mode dependent reconstruction efficiency, and $B$ is the $B^+ \rightarrow \tau^+ \nu$ branching fraction. The parameters $N_{B^+}$ and $\epsilon_k$ are fixed in the fit while $B$ is left floating. The reconstruction efficiencies $\epsilon_k$, which include the $\tau$ branching fractions, are obtained from MC simulation of the signal. Since the tag $B$ reconstruction efficiency is included in $\epsilon_k$ and is estimated from the signal MC, we apply a correction factor $R_{\text{data/MC}} = 0.926 \pm 0.010$ to take into account data/MC differences, taking the ratio of the peaking component of the $m_{\text{ES}}$ distribution of the hadronic tag $B$ in data and in MC simulation events.

We use histograms with a bin width of 60 MeV to represent the PDFs $P_{i,k}^*$ and $P_{b,k}^*$ for signal and background, respectively. The signal PDF is obtained from a high statistics signal MC simulation sample, corrected for data/MC.
FIG. 2: $E_{\text{extra}}$ distribution in data (dots with error bars) with all selection requirements applied and fit results overlaid. The hatched histogram is the background, the red dashed component is the signal. Plot (a) shows all $\tau$ decay modes fitted simultaneously. Lower plots show the projection of the simultaneous fit result on the four analyzed $\tau$ decay modes: (b) $\tau^+ \rightarrow e^+ \nu \bar{\nu}$, (c) $\tau^+ \rightarrow \mu^+ \nu \bar{\nu}$, (d) $\tau^+ \rightarrow \pi^+ \nu$, (e) $\tau^+ \rightarrow \rho^+ \nu$.

disagreement. Since a data sample of suitable statistics with exactly the same final states as our signal channels is not available, we use a sample of fully reconstructed events where in addition to the reconstructed tag $B$, a second $B$ is
reconstructed in an hadronic or a semileptonic decay mode, using charged tracks and neutral clusters not assigned to the tag $B$. In order to estimate the correction to the signal PDF, we compare the distribution of $E_{	ext{extra}}$ in this double tags sample from experimental data and MC simulation. The distributions are normalized to the same area and the comparison is shown in figure 2. We extract the correction function taking the ratio of the two distributions and fitting it with a second order polynomial.

We take the PDF of the combinatorial background from the $m_{	ext{ES}}$ sideband. The contribution of this component in the signal region is obtained by fitting the $m_{	ext{ES}}$ distribution after the selection has been applied. The shape of the peaking background is taken from $B^+B^-$ MC in the signal region, after the intrinsic combinatoric background has been subtracted by a fit to $m_{	ext{ES}}$, to avoid double counting. The two background components are added together in a single background PDF. We finally apply a smoothing procedure on the total background shape, excluding the first bins. We estimate the branching fraction minimizing $-2\ln \mathcal{L}$, where $\mathcal{L} = \prod_{k=1}^{n} \mathcal{L}_k$, and $\mathcal{L}_k$ is defined in equation (1). The projections of the fit results are shown in figure 2. We observe a significant excess of events with respect to the expected backgrounds and measure a branching fraction $B(B^+ \rightarrow \tau^+ \nu_\tau) = (1.80^{+0.57}_{-0.54}) \times 10^{-4}$, where the uncertainty is statistical. We evaluate the significance of the observed signal, including only statistical uncertainty, as $S = \sqrt{-2 \ln(\mathcal{L}_{\text{obs}}/\mathcal{L}_{\text{exp}})}$, where $\mathcal{L}_{\text{obs}}$ and $\mathcal{L}_{\text{exp}}$ denotes the obtained maximum likelihood value and the likelihood value assuming background only. We find $S = 3.6\sigma$. Table III summarizes the results from the fit.

### SYSTEMATICS

The dominant source of systematic uncertainty is the background PDF, due the finite statistics of the $B^+B^-$ MC simulated sample, used to estimate the $B^+B^-$ background PDF, and of the $m_{\text{ES}}$ data sideband, used to estimate the combinatorial and continuum backgrounds. In order to estimate the systematic uncertainty we repeat the fit of the branching fraction with 1000 variations of the background PDF, varying each bin within the statistical error, and assign 12% as systematic uncertainty.

The systematic uncertainty due to the signal $E_{\text{extra}}$ distribution correction function obtained from data/MC comparisons using control samples is obtained by varying the parameters of the second order polynomial within their uncertainty and repeating the fit to the $B^+ \rightarrow \tau^+ \nu_\tau$ branching fraction. We observe a 1.7% variation that we take as the systematic uncertainty on the signal shape.

Uncertainty in the differences between data and MC in the tracking and neutral reconstruction efficiencies reflects in the uncertainty in the central value of the branching fraction. The difference of the tracking efficiency is estimated with a control sample of high momentum tracks from $e^+e^- \rightarrow \tau^+\tau^-$ events to be 0.5% per track. Since there is only one signal track candidate in all four $\tau$ decay modes in the $B^+ \rightarrow \tau^+ \nu_\tau$ signal, we use this value as the uncertainty due to tracking efficiency. We accept events with one extra low $p_T$ charged track. Comparing the multiplicity of low $p_T$ charged tracks from the double tags sample in data and in MC, we estimate the systematic uncertainty to be 1.3%. Adding in quadrature the two uncertainties we estimate the the systematic error to be 1.4%.

Other systematic uncertainties on the efficiency stem from the finite signal MC statistics (0.8%), the uncertainty in the tag $B$ efficiency correction (5.0%), the electron identification (2.6%), and muon identification (4.7%). The systematic uncertainties are summarized in Table III. The total systematic uncertainty is obtained by combining all sources in quadrature.
FIG. 3: $E_{\text{extra}}$ distribution for double tags. The second $B$ is reconstructed in hadronic decays (left plot) or semileptonic decays (right plot). Points are data, histograms are MC simulation.

<table>
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<th>BF uncertainty (%)</th>
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<td><strong>Total</strong></td>
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TABLE III: Contributions to systematic uncertainty on the branching fraction.

CONCLUSIONS

In summary, we have measured the branching fraction of the decay $B^+ \rightarrow \tau^+ \nu_\tau$ using a tagging algorithm based on the reconstruction of hadronic $B$ decays using a data sample containing $467.8 \times 10^6 B\bar{B}$ pairs collected with the BABAR detector at the PEP-II $B$-Factory. We measure the branching fraction to be $B(B^+ \rightarrow \tau^+ \nu_\tau) = (1.80^{+0.57}_{-0.54}\,(\text{stat.}) \pm 0.26(\text{syst.})) \times 10^{-4}$, excluding the null hypothesis at the level of 3.6 standard deviations using statistical uncertainties only, and at the level of 3.3 standard deviations including the systematic uncertainties. This result supersedes our previous result using the same technique \[3\]. Combining this result with the other BABAR measurement of $B(B^+ \rightarrow \tau^+ \nu_\tau)$ derived from a statistically independent sample \[4\], we obtain a single BABAR result $B(B^+ \rightarrow \tau^+ \nu_\tau) = (1.76 \pm 0.49) \times 10^{-4}$, where the uncertainty includes both statistical and systematic uncertainties.

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