CUORE: A CRYOGENIC UNDERGROUND OBSERVATORY FOR RARE EVENTS

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(The CUORE COLLABORATION)

Abstract

CUORE is a proposed tightly packed array of 1000 TeO\textsubscript{2} bolometers, each being a
cube 5 cm on a side with a mass of 760 g. The array consists of 25 vertical towers, arranged in a square of 5 towers by 5 towers, each containing 10 layers of 4 crystals. The design of the detector is optimized for ultralow-background searches: for neutrinoless double beta decay of $^{130}$Te (33.8% abundance), cold dark matter, solar axions, and rare nuclear decays. A preliminary experiment involving 20 crystals $3 \times 3 \times 6$ cm of 340 g has been completed, and a single CUORE tower is being constructed as a smaller scale experiment called CUORICINO. The expected performance and sensitivity, based on Monte Carlo simulations and extrapolations of present results, are reported.

**Key words:** Underground Detectors, Double Beta Decay, Dark Matter, WIMPs, Axions

**PACS:** 23.40.-s; 95.35.+d; 14.80.Mz

1 Introduction

Neutrinoless double-beta decay, is a process by which two neutrons in a nucleus might beta decay by exchanging a virtual Majorana neutrino, and each emitting an electron. This would violate lepton number conservation ($\Delta L = 2$) \cite{1}, and would require neutrinos to be Majorana particles. There are many reviews on the subject \cite{2,3,4,5}. The decay rate for the process involving the exchange of a Majorana neutrino can be expressed as follows:

$$\frac{1}{\tau_{1/2}^{0\nu}} = G_{0\nu}^{0\nu}(E_0, Z) \frac{|< m_\nu >|^2}{m_e^2} \left| M_f^{0\nu} - (g_A/g_V)^2 M_{GT}^{0\nu} \right|^2.$$ \hspace{1cm}(1)

In equation (1), $G_{0\nu}^{0\nu}$ is the two-body phase-space factor including coupling constants, $M_f^{0\nu}$ and $M_{GT}^{0\nu}$ are the Fermi and Gamow-Teller nuclear matrix elements respectively, and $g_A$ and $g_V$ are the axial-vector and vector relative weak coupling constants, respectively and $m_e$ is the electron mass. The quantity $|< m_\nu >|$ is the effective Majorana electron neutrino mass given by:

$$|< m_\nu >| \equiv \left| \left| U_{e1}^L \right|^2 m_1 + \left| U_{e2}^L \right|^2 m_2 e^{i\phi_2} + \left| U_{e3}^L \right|^2 m_3 e^{i\phi_3} \right|,$$ \hspace{1cm}(2)

where $e^{i\phi_2}$ and $e^{i\phi_3}$ are Majorana CP phases ($\pm 1$ for CP conservation) and $m_{1,2,3}$ are the mass eigenvalues.

The electron neutrino, for example, is a linear combination of neutrino mass-eigenstates i.e.:

$$| \nu_e > = U_{e1}^L | \nu_1 > + U_{e2}^L | \nu_2 > + U_{e3}^L | \nu_3 >.$$ \hspace{1cm}(3)
The effective Majorana neutrino mass, $|<m_\nu>|$, is directly derivable from the measured half-life of the decay as follows:

$$|<m_\nu>| = m_e \frac{1}{\sqrt{F_N^{\nu/2}}} \ [eV],$$

(4)

where $F_N \equiv G^{0\nu}_M |M^{0\nu}_f - (g_A/g_V)^2 M^{0\nu}_{GT}|^2$. This quantity derives from nuclear structure calculations and is model dependent as shown later.

The most sensitive experiments thus far utilize germanium detectors isotopically enriched in $^{76}\text{Ge}$ from 7.8% abundance to $\sim 86\%$. This activity began with natural abundance Ge detectors by Fiorini et al. in Milan [6] evolving over the years to the first experiments with small isotopically enriched Ge detectors [7], and finally to the two present multi-kilogram isotopically enriched $^{76}\text{Ge}$ experiments: Heidelberg Moscow [8] and IGEX [9,10].

Where should the field of $\beta\beta$ - decay go from here? Suppose we consider the observed neutrino oscillations in the data from atmospheric neutrinos [11] and solar neutrinos [12]. These, coupled with the recent exciting results reported by the Sudbury Neutrino Observatory (SNO) Collaboration [13], gives clear evidence that solar neutrinos oscillate, and that the standard solar model is correct, but that solar electron neutrinos are oscillating to other flavors on their way from the sun, or in the sun. In addition, neutrino oscillation experiments have yielded the following values of $|U_{e\ell}|^2$: $|U_{e1}|^2 = (0.75^{+0.07}_{-0.12})$, $|U_{e2}|^2 = (0.25^{+0.12}_{-0.09})$, and $|U_{e3}|^2 = (< 0.026)$ with confidence levels of 3 $\sigma$.

A number of recent theoretical interpretations of these data [14,15,16,17,18,19] imply that the effective Majorana mass of the electron neutrino, $|<m_\nu>|$, expressed in Eq. (2), could be in the range 0.01 eV to the present bounds [8,10]. Considering this range, could a next generation $0\nu\beta\beta$ - decay experiment detect it? If so, what technique would be the best for a possible discovery experiment? We will address these questions in an effort to demonstrate that CUORE, an array of 1000, 760 g $\text{TeO}_2$ bolometers, is one of the best approaches presently available. It can be launched without isotopic enrichment nor extensive Research and Development (R & D), and it can achieve next generation sensitivity.

The CUORE project, discussed in Sec. 2 originates as a natural extension of the successful MI-DBD $^{130}\text{Te}$ experiment [20] where for the first time a large array of bolometers was used to search for $0\nu\beta\beta$ - decay. The good results obtained so far prove that the bolometric technique although novel is competitive and alternative to the traditional calorimetric Ge technique. In Sec. 2 details of the detectors of the CUORE array are discussed while in Sec. 3 the cryogenic system required to cool the array at the operating temperature of $\sim 10 \text{ mK}$ is described. Background issues are considered in
Sec. 4 while electronics, DAQ and data-analysis are discussed in Sec. 5 and Sec. 6. The background simulation and the predicted sensitivity for CUORE are analysed in Sec. 7 where we also discuss briefly the physical potential of CUORE regarding Dark Matter and solar axions searches. In Sec. 8 the enrichment option is discussed.

2 The CUORE project

The CUORE detector will consist of an array of 1000 $TeO_2$ bolometers arranged in a square configuration of 25 towers of 40 crystals each (Fig. 1). The principle of operation of these bolometers is now well understood [21]. Tellurium Oxide is a dielectric and diamagnetic material. According to the Debye Law, the heat capacity of a single crystal at low temperature is proportional to the ratio $(T/T_{\Theta})^3$, where $T_{\Theta}$ is the Debye Temperature of $TeO_2$. Thus, providing that the temperature is extremely low, a small energy release in the crystal results in to a measurable temperature rise. This temperature change can be recorded with thermal sensors and in particular using Neutron Transmutation Doped (NTD) germanium thermistors. These devices were developed and produced at the Lawrence Berkeley National Laboratory (LBNL) and UC Berkeley Department of Material Science [22], they have been made unique in their uniformity of response and sensitivity by neutron exposure control with neutron absorbing foils accompanying the germanium in the reactor [23].

The $TeO_2$ crystals are produced by the Shanghai Quinhua Material Company (SQM) in Shanghai, China and they will be the source of 760 g $TeO_2$ crystals for CUORE [24]. A single CUORE detector consists of a $5 \times 5 \times 5 \ cm^3$ single crystal of $TeO_2$ that acts both as a detector and source. The detec-
tors will be supported in a copper frame in the 25 tower configuration shown in Fig. 1. The frame, and dilution refrigerator mixing chamber to which it is thermally connected, forms the heat sink, while the PTFE (Polytetrafluoroethylene or TEFILON) stand-offs provide the thermal impedance which delays the re-cooling of the bolometers. The bolometers operate at $\sim 10 \text{ mK}$.

A single tower of CUORE is presently under construction. It will be attached to the mixing chamber of the same dilution refrigerator (DR) used in the Milano 20 crystal array experiment (MI-DBD) and run not only as a test bed for CUORE but will also be an experiment called CUORICINO [24,25] (which in Italian means small CUORE) designed to improve on the present sensitivity of $|\langle m_{\nu} \rangle| \,$ obtained with isotopically enriched Ge detectors [8,9]. CUORICINO will prove the feasibility of the extension of the MI-DBD technology to large arrays. The smaller array of 20, $3 \times 3 \times 6 \text{ cm}^3$ crystals was operated successfully for 31,000 hours $\times$ kg. The data yield a bound $\tau_{1/2}^{0\nu}(^{130}\text{Te}) > 2 \times 10^{28} \text{ yr}$, corresponding to $|\langle m_{\nu} \rangle| < (1 \text{ or } 2) \text{ eV}$, depending on the nuclear matrix element used [20].

The CUORE detector then will be the final version of a three step development comprising: MI-DBD, CUORICINO, and finally CUORE. This, plus the fact that CUORE requires no isotopic enrichment, (the isotopic abundance of the $\beta\beta$ emitter $^{130}\text{Te}$ is 33.8%) puts CUORE ahead of other options of truly next generation $0\nu\beta\beta$ experiments. The technology, though novel, is developed and to a large degree proven.

2.1 The single CUORE detector

The single CUORE detector is a a $5 \times 5 \times 5 \text{ cm}^3$ single crystal of $\text{TeO}_2$ grown with ultrapure $\text{TeO}_2$ powders and optically polished on the surfaces. Crystals of $\text{TeO}_2$ have a tetragonal $<110>$ structure, and are grown along the (001) axis. The two axes normal to this axis are crystallographically equivalent, a fact relevant to their use in the search for solar axions discussed later [26]. The surface hardness is not the same for all sides, which complicates the crystal polishing. We have shown that repeated thermal cycling does not damage the crystals, as in the cases of crystals of other tellurium compounds, or those of tellurium metal. The Debye temperature of the $\text{TeO}_2$ crystals was specially measured for the CUORE project as 232 K [27]. This differs from the previous value of 272 K in the literature [28]. The specific heat of the $\text{TeO}_2$ crystals follows the Debye law down to 60 mK; the heat capacity of 760 g crystals extrapolated down to 10 mK is $2.3 \times 10^{-9} \text{ J/K}$.

The NTD thermistors are attached by epoxy to the crystal and are operated in the Variable Range Hopping (VRH) conduction regime with a Coulomb gap
The most important parameter characterizing the thermal response is the sensitivity, $A$, defined as follows:

$$A = \left| \frac{d \log R}{d \log T} \right| = \gamma \left( \frac{T_0}{T} \right)^\gamma.$$  \hspace{1cm} (5)

For our NTD thermistors this parameter ranges between 7 and 10. The resistance behavior follows the relation,

$$R = R_0 \exp(T_0/T)\gamma; \quad \gamma = 1/2.$$ \hspace{1cm} (6)

The VRH regime occurs in Ge when it is “doped” close to the Metal to Insulator Transition, which is $\sim 6 \times 10^{16}$ atoms/cm$^3$. This is achieved by thermal neutron radiation in a nuclear reactor, resulting in $(n, \gamma)$ reactions on $^{70,72,73,74,76}$Ge, followed by $\beta^-$-decay or electron capture. To first order, this produces (for a natural Ge sample) the following stable isotopes: $^{71}$Ga (18%), $^{73}$Ge (8.3%), $^{74}$Ge (36%), $^{75}$As (12%), and $^{77}$Se (0.8%). Beta minus and electron capture lead to n and p dopants, respectively. The sensitivity parameter, $A$, depends on the neutron irradiation dose. Therefore, each thermistor must be characterized at operating temperatures, as described for Si thermistors by Alessandrello et al. [32].

It is very important to optimize the neutron irradiation exposure and to make the exposures as uniform as possible. It is not possible to evaluate thermistor material directly from the reactor because of the long half life of $^{71}$Ge (11.43 days). A delay, of several months, is required to see if the Ge needs more exposure. To circumvent this difficulty, the Ge material is accompanied by foils of metal with long-lived $(n, \gamma)$ radioactive daughter nuclides. Accordingly, the neutron exposure of the Ge can be determined accurately, and uniformity of exposure is achieved. This technique was developed recently by the Lawrence Berkeley National Laboratory group of the CUORE Collaboration [23]. Following the neutron exposure and radioactive decay period, the NTD germanium is first heat treated to repair the crystal structure then cut into $3 \times 3 \times 1$ mm$^3$ strips. The thermistors are glued to the TeO$_2$ crystal by 9 spots of Araldit rapid, Ciba Geigy epoxy, of 0.4 to 0.7 mm deposited on the crystal surface by an array of pins. The height of each spot is 50 $\mu$m. This procedure was found to be reliable and reproducible in the MI-DBD experiment [20]. The heat conductance of the epoxy spots was measured in Milan and the phenomenological relation was found to be $\sim 2.6 \times 10^{-4} (T[K])^3$ watts per degree kelvin per spot.

The stabilization of the response of bolometers is crucial because of the unavoidable small variations in the temperature of the heat bath that change the detector gain (and consequently deteriorates the energy resolution). This
The problem is successfully addressed by means of a Joule heater glued on to each crystal. The heater is used to inject a uniform energy in the crystal, the thermal gain is monitored and corrected off-line (see Sec. 6). The heaters are $Si$ chips with a heavily doped meander structure with a constant resistance between 50 to 100 $k\Omega$. They are manufactured by the ITC - IRST company in Trento, Italy.

Electrical connections are made with two 50 $\mu m$ diameter gold wires, ball bonded to metalized surfaces on the thermistor. The gold wires are crimped into a copper tube, which is inserted into a larger one forming the electrical connection, and avoiding low temperature solder which contains $^{210}Pb$ and traces of radioisotopes. The larger copper tube, $\sim 14$ mm long and 2 mm in diameter, is glued to the copper frame that supports the crystals. This tube is thermally connected to the frame but electrically insulated.

The mounting of the $TeO_2$ crystals is crucial to detector performance, and must fulfil a number of sometimes contradictory criteria:

1. crystals must be rigidly secured to the frame to prevent power dissipation by friction caused by unavoidable vibrations, that can prevent the crystal from reaching the required temperature and can produce low frequency noise;
2. the thermal conductance to the heat sink (copper frame) must be low enough to delay the re-cooling of the crystal, following a heat pulse, such that the pulse decay time (re-cooling time) is much longer than the rise time;
3. however, the heat conductance must be high enough to guarantee efficient cooling;
4. the frame must compensate for the differences in thermal expansion coefficients of the various materials used;
5. and finally, only materials selected for low radioactivity can be used.

For CUORE, only two materials will be used, copper and PTFE; they can both be obtained with very low levels of radioactivity. Copper has a thermal conductivity and specific heat high enough to be an ideal heat bath, and has excellent mechanical properties; it machines well, and has excellent tensil, tortional and compressional strength.

PTFE is used between the copper frame and the crystals. It has low heat conductance and low heat leak [33]. It compensates for the differences between coefficients of thermal expansion of copper and of $TeO_2$. The heat conductance between the crystal and heat sink was measured in a similar configuration, but with a contact area larger by a factor of 2 [34].

The measurements of the temperature dependence of specific heats and thermal conductivities is crucially important for developing a model that explains
detector performance and that can be used to improve the detector design.

2.2 The detector model

A rough approximation of the NTD thermistor voltage pulse amplitude $\Delta V_{bol}$ produced by an energy deposition $E$ into the $TeO_2$ absorber can be obtained by:

$$\Delta V_{bol} = V_{bol} \cdot A \cdot \frac{\Delta T_{bol}}{T_{bol}} = V_{bol} \cdot A \cdot \frac{E}{C \cdot T_{bol}}$$  \hspace{1cm} (7)

where $V_{bol}$ is the bias of the NTD thermistor, $A$ is the sensitivity obtained from equation 5, $\Delta T_{bol}$ is the temperature increase and $C$ is the heat capacity of the absorber. Using the heat capacity discussed earlier, a one $MeV$ energy deposition into the $TeO_2$ absorber results in $\Delta T_{bol} = 7 \times 10^{-5} K$. Using equation 7, this results in $\Delta V_{bol} \sim 600 \mu V$; however, the observed pulses are lower by a factor $\sim 5$, therefore a more quantitative model is needed.

A semi-quantitative Thermal Model (TM) has been developed which describes the detector in terms of three thermal nodes with finite heat capacities of the $TeO_2$ crystal absorber, Ge thermistor lattice, and Ge thermistor electrons. For simplification, the lattice component of heat capacity is assumed to be negligible. The network describing the detector is shown in Fig. 2. The two heat capacities, and 4 thermal conductances, the parasitic power from the vibrations and power dissipated in the thermistor electrons, are the model parameters. A typical energy deposition of 1 $MeV$ in the crystal is used and it is assumed that it is instantaneously thermalized.

A computer code was developed in Milan to determine the static behavior. The required input data are: the heat sink temperature, the temperature behavior of the thermal conductances shown in Fig. 2, the parasitic power in the crystal, and a set of values of electrical joule power dissipated in the thermistor electrons. The code determines a complete solution to the static problem, for each power level, and yields the temperature of the three thermal nodes, the resistance of the thermistor, and the current through it. These parameters define the “operational point”. A set of operational points, with a fixed heat sink temperature, defines a “load curve”. Load curves are expressed as a set of voltage-current, or power resistance points. When the static operation point is determined, the time evolution of the pulse is computed. The main aim of the TM is to have a reliable prediction of the detector figure of merit on the basis of the known thermal parameters. To address this question it is necessary to solve the non trivial problem of how it is possible to compare the performances of two detectors The more sensitive thermistors yield larger amplitude pulses,
but they are also more sensitive to spurious noise, for example microphonics, crosstalk, and slow heat pulses from vibrations that excite the 1-5 $Hz$ portion of the noise spectrum. More gain at the heat sink temperature yields larger pulses at the price of higher resistance and more spurious noise.

Recent experience shows that the best way to define a detector figure of merit is by fixing the heat sink temperature between 7 $mK$ and 11 $mK$ and by measuring a load curve. Using particle or heater pulses, the operation point on the load curve, corresponding to the highest signal, is determined. For each heat sink temperature, one determines a pair of points, thermistor resistance, $R$, and signal amplitude, $V$, usually expressed in microvolts per $MeV$, corresponding to the maximum pulse amplitude for a given heat sink temperature. One obtains a characteristic curve for that detector by plotting voltage vs resistance, which to a good approximation is a straight line on a log-log plot. This is called the Detector Merit Curve (DMC). Experience shows that a detector has very similar signal-to-noise ratio along a DMC. No large differences in performance are noted for heat sink temperatures of 8 $mK$ or 12 $mK$, because signal level and the spurious noise offset one another. It is better to avoid the extremities of the DMC that lead to higher spurious noise or low signals.

The best way to compare two different detectors is by using their DMCs. If the DMC of detector A lies systematically above that of detector B, the performance of detector A is superior. It provides the highest signals for a fixed thermistor resistance value. The main value of the TM is to predict the DMC given the temperature behavior of the thermal parameters discussed above.
As a test of the model, a typical detector of the MI-DBD 20-element array was simulated. These have different masses and geometries than the CUORE crystals. A DMC was then constructed using the model for this detector. It was then compared to the real DMC measured for the 20-detector array. A significant spread among the experimental points, for all 20-detectors was found. There were two reasons for this, intrinsic detector differences and the presence of points not corresponding exactly to the maximum signal. Nevertheless the simulated DMC lies inside of the experimental points and has the correct slope (see Fig. 3). The detector simulations are not distinguishable from a typical detector array.

The TM must correctly predict not only pulse amplitude, but also time constants. At a typical operating resistance (~ 100 MΩ) the predicted rise time (10%-90%) and decay time, are respectively 40 ms and 430 ms, and lie inside the distribution of these parameters for the 20-detector array. In Fig. 4, the simulated pulse is compared with real pulses collected with four detectors, randomly chosen among the 20 elements. It is evident that the pulse-shape of the simulated detector is very similar to that of a typical array of detectors. From this it was concluded that the TM is capable of explaining semi-quantitative performance of the 20-element array.
The TM can be used in parallel with specific low temperature experimental tests, to define the optimum properties of the CUORE element, and the results thus obtained imply the following optimum parameters for the CUORE elements:

1. $TeO_2$ absorber dimensions: $50 \times 50 \times 50 \text{ mm}$, of mass of $760 \text{ g}$;
2. NTD Thermistor # 31, $T_0 = 3.0 \text{ K}$, $R_0 = 1.5 \Omega$, dimensions $3 \times 3 \times 1 \text{ mm}$, with a contact distance of $3 \text{ mm}$, and with a resistance of $50 \text{ M}\Omega$ at $T = 10 \text{ mK}$;
3. absorber-thermistor coupling made with 9 epoxy spots, 0.5 to 0.8 mm in diameter, and 50 $\mu$m high;
4. gold connecting wires 50 $\mu$m in diameter, and 15 mm in length;
5. crystals mounted on PTFE blocks with a total PTFE-to-crystal contact area equal to about a few square mm.

2.3 The modular structure of the CUORE detector

The CUORE array comprises 1000 $TeO_2$ bolometers, grouped in 250 modules of 4 bolometers each. These are arranged in 25 towers of 40 crystals each, or a stack 10 modules high. The towers are assembled in a 5 by 5 matrix as shown in Fig. 1.
The structure of each four-detector module is shown in Fig. 5. The four crystals are held between two copper frames joined by copper columns. PTFE pieces are inserted between the copper and TeO$_2$, as a heat impedance and to clamp the crystals. There is a 6 mm gap between crystals with no material between them.

The four detectors are mechanically coupled; some of the PTFE blocks and springs act simultaneously on two crystals. Tests on this and a similar structure but with $3 \times 3 \times 6$ mm$^3$ crystals clearly demonstrate that the CUORE technology is viable. Noise reduction was achieved by replacing the $3 \times 1.5 \times 0.4$ mm$^3$ Ge thermistor by one with dimensions $3 \times 3 \times 1$ mm$^3$, which significantly improved the DMC shown in Fig. 6, and by utilizing cold electronics Fig. 7.

Reproducibility was tested on the MI-DBD array, which is a significant number of detectors (20) operating simultaneously. The reproducibility is satisfactory as shown in the load curves in Fig. 8. Four-detector modules of $50 \times 50 \times 50$ mm$^3$ crystals were also successfully tested, with pulse amplitudes spanning an interval from 50 to 150 µV/MeV at $\sim 100$ MΩ operation point, in agreement with the TM. The full width at half maximum FWHM is $\sim 1$ keV for low energy gamma peaks, and $\sim 5$ to 10 keV at 2.6 MeV. A stack of 10, 4-detector modules, will be connected by two vertical copper bars. The details of the wiring of the towers is still under development; however, the current plan is for 50 µm diameter twisted pairs of nylon coated constantane wire, running along the vertical copper bars. On the top of each tower, there would be 40 twisted pairs for the thermistors, and 4 for the heaters. Two more twisted pairs will be required for diagnostic thermometers, one on top, and one on the bottom of the tower.

The CUORICINO detector presently under construction consists of one of the 40 detector towers. CUORE is an array of 25 towers, each of which will be sus-
Fig. 6. Improvement in the Detector Merit Curve by increasing the thermistor size: $3 \times 3 \times 1 \, mm^3$ thermistors (stars) vs. $3 \times 1.5 \times 0.4 \, mm^3$ (diamonds).

Fig. 7. Noise Power Spectra without damping suspension (1), with damping suspension only (2) and with dumping suspension + cold electronics (3).
Fig. 8. Fifteen thermistor load curves for the 20 crystal array.

Figured independently from a large square copper plate, thermally connected to the mixing chamber of the DR. In this manner, tests of CUORICINO will be tests of the CUORE array. The array will be suspended from the mixing chamber by a vertical spring to decouple the detector from the vibrations of the dilution refrigerator. Tests were performed with piezo-electric accelerometers and vibrators to optimize the suspension (see Fig. 7). As a result a pendulum mechanical suspension was designed for the entire CUORE array.

The heavy shielding of CUORE will present non-trivial problems in the energy calibration with radioactive sources. The presently considered option is with radioactive metal wires encapsulated in PTFE tubes. The tubes would be placed vertically between the towers, and free to slide along a fixed tube to the appropriate calibration point. A vacuum tight sliding seal will allow the part of the tube containing wire to be inserted and extracted from the cryostat.

3 The cryogenic system

The CUORE bolometers will operate at temperatures between 7 and 10 \text{mK}. This will require an extremely powerful dilution refrigerator (DR). At these temperatures, the cooling power of a DR varies approximately as $T^2$. Estimates were made of the parasitic power the detector and DR would receive from: heat
transfer of the residual helium gas in the inner vacuum chamber (IVC), power radiated from the 50 mK shield facing the detector, and from vibrational energy (microphonic noise).

The estimated value is $\sim 1 \mu W$ at 7 mK, using reasonable values for the residual gas pressure and achievable surface quality for radiation transfer. The resulting estimate for the radiation contribution was negligible. CUORE will utilize a similar system to that of the Nautilus Collaboration that cools a 2-ton gravitational antenna. That system experienced a parasitic power of 10 $\mu W$ from unknown sources.

The CUORE detector will be cooled by a $He^3/He^4$ refrigerator with a cooling power of 3 $mW$ at 120 mK. Refrigerators with the required characteristics are technically feasible, one example is the DRS-700 DR model constructed by the Kamerling Omes Laboratory in Leiden. The unit is shown in Fig. 9, inserted in the dewar. One important design feature is the 50 mm diameter clear access to the mixing chamber to allow a rod, suspended from an external structure, to suspend the detector array to minimize vibrations from direct connection to the mixing chamber. The temperature of the rod will be controlled in stages along its length by flexible thermal contacts to avoid vibrations.

The dewar housing the DR will have a jacket of liquid nitrogen (LN), to avoid the need of superinsulation, which is not free of radioactivity. The system is
designed with several tubes passing through the LN bath, the liquid $He$ bath, and the IVC, to allow refilling with cryogenic liquids, and for sufficient feed through for electrical connections. Liquifiers will provide constant liquid levels for the two baths over long periods of operation.

The $He$ that evaporates from the main bath, and from the 1K-pot, will be recovered in a buffer tank and re-liquified with a helium liquifier with a capacity of several tens of $l/day$. The gas will be cooled to $\sim 70 \, K$, then to $10 \, K$, by a two stage Gifford-MacMahon cycle. This will be followed by a Joule-Thompson cycle that liquifies it, and injects it back into the main bath. The nitrogen liquifier, on the other hand, will require only a single stage Gifford-MacMahon cycle to cool a cold finger above the LN bath. It will condense the evaporated $N_2$ and let it fall back into the bath.

This complex cryogenic system will require a constant monitoring system. It must be capable of surveying the operating conditions to allow prompt intervention to correct malfunctions rapidly. In addition, the operating conditions of the entire cryogenic system must be recorded for future correlation with instabilities in the experimental data.

4 Radioactivity and shielding

Double-beta decay experiments, as well as dark matter searches and searches for rare events in general, require deep underground locations and ultra low radioactive environments. This latter requirement is usually accomplished by a severe selection of the materials used and by the realization of proper shielding surrounding the detectors. In the case that complicated structures like a dilution refrigerator are used, the problem of shielding and of using only low radioactive contamination materials is complex.

4.1 Shielding

In the case of CUORE, part of the bulk lead shielding will be placed inside of the cryostat, and part outside (Fig. 9). This will accomplish shielding against the dewar, and will reduce the total amount of lead required. A $4\pi$ layer of ultra-low background lead will constitute 3 cm thick walls of the cubic structure of the array. This layer will be Roman lead whose $^{210}Pb$ activity was measured to be less than 4 $mBq/kg$ [35]. The dilution refrigerator will be constructed from materials specially selected for low levels of radioactivity. Nevertheless, these levels might be higher than can be tolerated by the sensitivity requirements.
The top of the detector array will be protected by two layers 1 m by 1 m, with a 10 cm diameter central bore to accommodate the copper cold finger that supports the detector and the narrow neck of two radiation shields of the refrigerator that are at temperatures of 50 mK and 600 mK. The layer close to the detector will be 10 cm thick, made from high quality lead with an activity of 16 Bq/kg of $^{210}$Pb. The upper layer, also 10 cm thick, will be made of modern lead with an activity of $^{210}$Pb of 150 Bq/kg. Another layer of lead 17 cm thick, and 40 cm by 40 cm will be placed directly on the top face of the detector. It will be constructed from low activity lead of 16 Bq/kg of $^{210}$Pb. This configuration is designed so that the minimum path to the detector from the IVC and the dilution unit is 20 cm of lead. Finally, outside the dewar, there will be two 10 cm thicknesses of lead, 16 Bq/kg of $^{210}$Pb for the inner layer, and 150 Bq/kg for the outer layer. The lead shield will be surrounded with a 10 cm thick box of borated polyethylene that will also function as an hermetically sealed enclosure to exclude radon. It will be flushed constantly with dry nitrogen. The

The entire dewar, detector, and shield will be enclosed in a Faraday cage to exclude electromagnetic disturbances that also constitute a source of background, albeit at low energies, important to dark matter and solar axion searches. The addition of a muon veto surrounding the entire structure will be also considered.

4.2 Material selection and treatment

All the materials used to built the detectors, their mounting structure, the cryostat and the shielding themselves will be selected to ensure that only low radioactive contamination materials will be employed. A particular care will be obviously devoted to the detectors. The $TeO_2$ crystals will be grown from ultrapure $TeO_2$ powders to guarantee an extremely low level of bulk contamination (present limit on U and Th contamination is of the order of $\sim 10^{-13} g/g$). A particular care will be devoted to their surface treatment. Indeed the first crystals grown by SQM were polished in China with conventional cerium oxide polishing rouge. This resulted in a $^{238}U$ and $^{232}Th$ surface contamination of the crystals that contribute to the measured background in the $0\nu\beta\beta$ of the Mi-DBD first run. A re-polishing of the crystals in Italy with low contamination powders reduced that contamination in the Mi-DBD second run. A new polishing process studied in collaboration with SQM and a semi-automatic polishing system realised in LBNL was used for the surface treatment of the CUORICINO crystals (partially done in China and completed in Italy). Also copper and PTFE used to construct the CUORE array will be selected for their low contamination. Once machined all the copper and PTFE pieces will undergo a surface cleaning procedure that will guaran-
tee the required low level of surface radioactive contamination for those parts that directly face the detectors. The array will be assembled in a low \( Rn \) clean room to avoid contamination from \( Rn \) daughters.

4.3 Location

CUORE will be located in the underground halls of Laboratori Nazionali del Gran Sasso (L’Aquila - Italy) at a depth of 3400 m.w.e. where the muon flux is reduced to \( \sim 3 \times 10^{-8} \mu/cm^{-2}/s \) and the neutron flux to \( \sim 10^{-6} n/cm^{-2}/s \).

5 Electronics and Data Acquisition

The \( G\Omega \) front-end electronics furnishes a bias current to the NTD thermistors and receives and processes the resulting signal-bearing voltage. At the moment we are investigating two solutions that differ by the addition of a cold buffer stage inserted between the detector and the room temperature preamplifier in one case. The connection from the thermistors to the electronics is via shielded twisted pair from one to five meters in length, depending by the final solution adopted. The design of the electronics addresses four major issues. First, it should minimize the noise generated by the biasing circuitry and the preamplifier in the frequency band from \( 1 \sim Hz \) to a few tens of \( Hz \). Second, it should accommodate the broad spread of manufacturing characteristics that is typical of the bolometer/thermistor modules. For some modules, for example, the optimum bias current is as low as 150 \( pA \) and for others as high as 300 \( pA \). As a consequence the signal amplitude exhibits a corresponding spread. Third, it should enable in situ measurement of the bolometer characteristics. Fourth, the design should incorporate a high level of remote programmability in order that adjustments required during the observing period do not entail mechanical interventions in the vicinity of the bolometers. In the following subsections we give a brief discussion of the circuitry that we devised to address these issues. An extended discussion of the electronics appears in reference [36].

5.1 Thermistor biasing

We achieve thermistor biasing by the application of a programmable voltage across a series combination of the thermistor and two load resistors. If electronic system is operated only at room temperature, the load resistors are also at room temperature (\( R_L \) in Fig. 10). The contribution to 1/f noise of large resistors under bias and the minimization of this noise source is the subject
Fig. 10. Functional block diagram of the front-end electronics. Normally $R_L$ is 27 $G\Omega$. For determination of a bolometer I-V characteristic a command from the computer can reduce $R_L$ to 5.5 $G\Omega$.

of an independent report [37]. Under computer control we can reduce the biasing resistors from 27 $G\Omega$ to 5.5 $G\Omega$ which facilitates a measurement of the bolometer’s I-V characteristics at large bias. The impedance at the input of the electronics is sufficiently high that parasitic conductance in the circuit board is an issue that demands great attention. Precautions that we took to suppress parasitic conductance were a) segregation of inverting and non-inverting inputs by circuit board layer, b) strategic placement of guard traces around the solder junctions of high-impedance component leads, c) maintenance of a minimum spacing of 5 $\sim$ mm between high-impedance traces, and d) the placement of slots at critical locations on the circuit board to avoid conductance through minute amounts of soldering residue that sometimes escapes the standard cleaning procedures. Together these measures yield excellent results.

If a cold buffer stage will be adopted, the pair of load resistors $R_L$ of Fig. 10 will be moved close to the location of the buffer itself, at low temperature. Their value will be 27 $G\Omega$. In this case the rest of the biasing set-up will remain unchanged.

The application of bias voltage to the load resistors is the task of the programmable bias attenuator. This circuit is a five-bit R-2R ladder network with optical isolation of the digital input. Its outputs are the voltages $V_{b1}$ and $V_{b2}$ appearing in Fig. 10. They take the value

$$V_{b1} = -V_{b2} = \left( n/64 \right) (V_+ - V_-)$$

where $V_+$ and $V_-$ are derived from an Agilent Technologies 6627A system power supply common to all modules, $|V_+ - V_-|$ may be set as high as 60 V and $n$ can be set to any integer value between 1 and 64. Interposed between the programmable bias attenuator and the load resistors (but not shown in
Fig. 10) is a bistable DPDT relay, which provides for inverting the polarity of the bias voltage. By reversing the bias voltage during in situ DC characterization, we can account for the thermoelectric effect operating in the leads that connect the front-end electronics to the thermistors. Heavy filtering distributed through the biasing network reduces to a negligible level whatever noise originates from the power system or from the network itself.

5.2 Preamplifier

The design of our preamplifier was influenced by four paramount considerations. First, for the source impedance and signal characteristics that the bolometer presents, a voltage amplifier is the conventional approach [38]. Its performance is not superior to a charge or current configuration [39], but it allows its inputs to float. Floating inputs make biasing compatible with DC coupling. Second, the leads that connect the preamplifiers with the bolometers operating near 10 mK can extend between 1 m and 5 m in length. The drawback of these long leads is that they act as antennas for microphonic noise. We address this issue by making the preamplifier input differential. Compared with a single-sided input the amplifier noise power is double, but for the more troublesome microphonic noise originating in the leads, which is common mode, we achieve efficient suppression. The differential configuration also serves to suppress interchannel crosstalk. Third, the signal bandwidth of our bolometers extends from 1 Hz to about 10 Hz, and we ask that the amplifier noise, both series and parallel, be minimized in this frequency interval. Fourth, monitoring the baseline of each bolometer and correlating baseline shift with shifts in overall system gain require low thermal drift in the preamp.

In addition to the above features the use of a cold buffer stage can increase further the rejection to microphonism by minimizing the high impedance section of detector’s connecting leads.

To address these considerations the room temperature version of the front-end we adopted is the circuit shown in Fig. 11a. At the core of the design is the JFET pair J1 and J2, which accepts the differential input. We selected the transistor type for these JFETs with a view to minimizing the noise, especially at low frequency. The capacitance of the gate of the selected transistor is about 80 pF, which optimizes the tradeoff between low series noise, low parallel noise, and matching to the detector. To minimize parallel noise we establish for each of the JFETs VDS = I2Rg − (I1 − I2) Rs/2 at 0.8 V, the lowest value consistent with adequate gain. The connection of the outputs of the operational amplifiers (op-amp) A3 and A4 through the resistors Rf to the sources of the JFETs closes the feedback loop and establishes the gain at (Rf+Rs)/Rs. With Rf = 20 kΩ and Rs = 91 Ω the gain is 220 V/V. Neither
the input JFETs nor any of the op-amp circuits are individually compensated for thermal drift. We deal with this issue by trimming the circuit as a whole. One component of the current source in the thermal drift compensation circuit of Fig. 11 a is a diode that serves as a thermometer. The magnitude of the coefficient $\eta$ is proportional to the value of a single resistor, and placement of a shunt determines the sign of $\eta$. We operate the preamp in a temperature controlled chamber and trim $\eta$ to neutralize the uncompensated thermal drift. In this way we were able to reduce an uncompensated drift as large as 60 $\mu V/^{\circ}C$ to about 0.1 $\mu V/^{\circ}C$.

To minimize further the microphonic noise coming from the length of the leads, we have also realized, and are testing, a solution that uses an additional stage of amplification, operated cold, inserted near the 4.2 $K$ plate of the dilution refrigerator (and therefore much closer to the detectors). Each cold stage is a differential buffer composed by two Silicon JFETs that work in source follower configuration. This way the length of the leads that connect the detector to this additional buffer stage is reduced to about 1 m, while the remaining part of the wires toward the room temperature is driven by the low output impedance of the buffer. The buffer stage works at the optimum temperature for Silicon, around 110 $K$. Each cold buffer, together to the load resistors, is located on a boards that accommodates 6 channels. The boards are realized on a substrate made of PTFE 25% reinforced fibreglass. This solution allows obtaining two goals. From one side the small thermal conductance of the PTFE minimize the thermal power to be injected for increasing the temperature of the JFETs to the optimum one, starting from the heat sink at 4.2 $K$. On the other side the radioactivity level of PTFE 25% reinforced fibreglass is better by a factor of about 2 with respect to the pure fibreglass. In addition the printed circuit boards have a thickness of only 0.5 mm in order to reduce the amount of mass present. Thermally shielded metallic boxes have been realized that are each able to contain 2 of such boards. Inside the boxes the boards are suspended by means of nylon wires that have a small thermal conductance to the heat sink, at the 4.2 $K$. This solution allows a good reduction of noise (see Fig. 7) however it’s realization presents some technical difficulties.

The input offset of the preamplifier, for whatever configuration, is the sum of contributions from the asymmetry of the JFETs and the bias voltage of the NTD thermistor. The JFET asymmetry may contribute up to $\pm 20 \, mV$ to the offset. In normal operation thermistor biasing contributes no more than 20 $mV$, but for obtaining the thermistor I-V characteristic the bias voltage should be settable to both polarities and to a magnitude as high as 50$mV$. We designed the offset corrector circuit to compensate input offsets from -80 $mV$ to +80 $mV$ under control of the digital section. In a naive design for this circuit the central element would be a conventional CMOS digital-to-analog converter (DAC). Such a design, however, would generate excessive low-frequency noise. Our design incorporates a DAC8043A, which is less noisy than ordinary DACs.
because it omits the conventional output buffer. To derive adequate current from this device we place it in the feedback loop of a low-noise op-amp. We achieve further noise suppression by using the DAC8043A to swing the output through just $20 \text{ mV}$, i.e. $1/4$ of the maximum output excursion. A simple arrangement of two analog switches in series with low-frequency noise-free resistors provides the necessary additional $60 \text{ mV}$ of output swing.

5.3 Programmable gain amplifier

The outputs of the preamp drive the differential inputs of the programmable gain amplifier, which we show in Fig. 11b. The computer can set $R_b$ to any parallel combination of a set of five resistors, 31 possibilities. The resulting gain from preamp input to amplifier output takes values from 220 to 5000 $V/V$. The differential outputs travel on an analog bus to a filter circuit, which is followed by analog to digital conversion.

The supply voltage for the very front-end so far described has been designed for the purpose for having very good stability, of a few $\text{ppm}/C$, and large rejection ratio [40]. These implemented features provide great stability during a long time measurement. One such supply voltage is dedicated to 12 boards, or 24 complete channels.
5.4 Antialiasing filter and analog trigger

In this experiment it is feasible to apply optimal filtering algorithms to the detector signal in the off-line analysis, and signal shaping in hardware is thus inappropriate. To ensure adequate frequency response we implement in hardware only an antialiasing filter at the downstream end of the analog signal processing. This low-pass filter is an active six-pole Bessel design, which yields a roll-off of 120 dB/decade. To allow for adapting the bandwidth to the individual bolometer modules the cutoff frequency is settable from the computer to 8, 12, 16 or 20 Hz.

The trigger circuit input is AC coupled to the output of the antialiasing filter. Its gain is settable from the computer to 4.2, 12.5, 21 or 29 V/V. The AC coupling produces a negative excursion of the trigger circuit input that, if uncompensated, would result in a shift of the baseline. A baseline restoring section [41] in the trigger circuit suppresses this effect. Pulses from a bolometer exhibit a trailing undershoot because of the coupling of the inductive part of the bolometer’s dynamic impedance to the parasitic capacitance in shunt with it. After differentiation by the AC coupling, the undershoot of large pulses has the potential to retrigger. An RC network [42] within the trigger circuit cancels the effect of the undershoot and thus suppresses retrigerring. Its time constant is settable from the computer to 14, 27, 53, or 66 s. The final element in the trigger circuit is a two-pole Bessel low-pass filter. The cutoff of this filter tracks the cutoff of the antialiasing filter but is higher in frequency by 4 Hz. One trigger-Bessel module accommodates three channels.

5.5 Data acquisition and triggering

The analog trigger and antialiasing circuits are situated in a small Faraday cage close to the acquisition and triggering system to which they send their outputs. The data acquisition system (DAS) is based on the VXI standard. Its main goal is the implementation of a zero dead-time system based on the continuous analysis of a large circular memory buffer characterized by a very fast data transfer rate (DMA) with the ADC memories. The DAS consists of an embedded controller PC (DASC), and few trigger and ADC cards. Signals from the front-end electronics are sent both to a series of 16 bit ADC modules (where they are digitized) and, after proper differentiation, to simple threshold trigger modules. The ADC sampling interval is set to values in the range 1-10 ms depending on the observed characteristics of the signals. Because of these large sampling times, each ADC module is multiplexed and can serve a number of acquisition channels. Sampled data are continuously transferred to a large circular buffer of the DASC. When a trigger signal is also transferred
to the DASC the circular buffer is analyzed in order to recognize and extract the desired sampled interval without interfering with the ADC activities. In normal conditions such a logic does not require any DAQ dead-time. Synchronization between trigger and ADC modules and the DASC is, of course, of crucial importance. The trigger discriminating thresholds are settable in increments of 5 mV. This threshold adjustment in combination with the gain selection in the trigger circuit provides channel-by-channel fine control of the trigger level. Given the variability of the energy-to-voltage conversion among bolometers, the ability to tailor the trigger level to the bolometer module is a valuable feature particularly for what concerns dark matter searches for which the trigger level should be as low as possible.

5.6 Noise considerations

When the cold buffer stage is not present, the analog electronics chain just described produces noise at the level of 50 nV (FWHM) referred to the input over the 10 Hz bandwidth of the signal. The 27 GΩ load resistors produce 80 nV in this bandwidth. The combined noise is then about 100 nV (FWHM). When the cold buffer stage is present the series power noise is increased a factor of about 2, while parallel noise is decreased by a factor of at least 3, mainly by the use of the cold load resistors. This way the overall noise contribution becomes about 90 nV (FWHM). In both cases the noise is considerably below the 1.0 µV (FWHM) level of noise that we have observed from a reference bolometer that we consider to be an exemplar of good performance. On the basis of this assessment we believe that the analog front end is more than adequate for the needs of the experiment.

The two front-end solutions have the same level of noise, but the presence of the cold buffer stage, reducing the high impedance path, should further improve the common mode noise from the vibration of the leads. Unfortunately there is another source of microphonism, that is not a common mode, due to the mechanical friction between the detector and its mounting. If this source will result in noise much greater than that of the connecting leads, the use of a cold buffer stage will be not necessary. This fact will save a factor of two in the number of connecting leads (two for the readout and two for biasing for the case of the cold stage), and will save thermal power injection inside the fridge. The savings in parasitic capacitance that is obtained with shortening the high impedance path is not a concern with the foreseen very slow signals.
5.7 Digital control

A digital control system (DCS) enables the computer to manipulate all of the significant parameters of the analog front end. These parameters include the thermistor bias current, the input offset correction, the gain, and the application of test signals to the inputs. During data acquisition the DCS is generally idle. In this state even the DCS clock shuts down thus eliminating the possibility that DCS activity will contribute to noise on the analog outputs.

6 Off line analysis

When the output voltage of one detector exceeds the trigger threshold, the acquisition system saves a number of converted points of the corresponding channel. Accordingly, for each electronic-pulse, the wave form corresponding to a time window of \( \sim \) two seconds is sampled and acquired. The existence of a pre-trigger interval guarantees that a small fraction of the number of points acquired are measurements of the DC level of the detector, or it’s temperature, just prior to the production of the pulse.

The fact that for each trigger an entire wave form is sampled and recorded, implies that off-line analysis of a large body of data will require a significant effort. Nevertheless, this effort will be justified because of the useful information that can be extracted from the signal waveform. The following are important goals for the analysis:

(1) maximization of the signal to noise ratio for the best estimate of the pulse amplitude. This is accomplished by means of the optimum filter (OF) technique \([43]\);
(2) ability to correct the effects of system instabilities that change the response function of the detectors;
(3) ability to reject spurious triggered pulses by means of pulse shape analysis;
(4) capability of identifying and rejecting radioactive background pulses by means of coincidence analysis.

The optimum filter (OF) technique is frequently used with bolometers to evaluate the amplitude of a signal superimposed on stochastic noise. This algorithm has proven to provide the best estimate of the pulse amplitude under general conditions. Relative to a simple maximum-minimum algorithm, this technique allows the evaluation of the signal amplitude with much higher efficiency resulting in an improvement in energy resolution by as much as a factor of two. To use the OF technique, the following information is necessary: the
response function i.e., the shape of the signal in a zero noise condition, and the noise power spectrum. Once these are known, the OF function is determined. It is then used as a software filter for the acquired pulses. The role of the OF function is to weight the frequency components of the signal to suppress those frequencies that are highly influenced by noise. The amplitude of the pulse is then evaluated using optimally filtered pulses. Some pulse shape parameters can be deduced from the comparison of the filtered pulses with the filtered response function.

In processing the data off line, the following parameters are evaluated and recorded to disk for each digitized pulse:

(1) the channel number i.e., the ADC channel that exceeded the trigger threshold;
(2) the absolute time at which the pulse occurs with a precision of 0.1 ms;
(3) the OF amplitude i.e. that of the optimally filtered signals
(4) the baseline, obtained by averaging a proper number of points from the pre-trigger interval. It is a direct measurement of the DC level at the output of the detector just prior to the production of the pulse, and therefore it provides a measurement of the detector temperature at the creation of the signal;
(5) the signal rise and signal decay times;
(6) the pulse shape parameters, obtained by comparison between the pulse and the expected response function of the bolometer. The algorithms used to make this comparison, and to produce a numerical evaluation of it, are based on two main techniques: the comparison of the wave forms of the pulse and response function after OF, or Adaptive Filtering. A third powerful technique is based on artificial neural networks;
(7) the pile-up fraction, pile up is usually efficiently rejected using pulse shape analysis; however, this does not guarantee the identification of the rejected event as one from a pile-up. To improve this rejection, and to be able to evaluate the fraction of piled-up events, the Wiener-Filter algorithm is implemented [34].

The next step in the off line analysis is gain instability correction. The OF amplitudes are corrected to reduce or cancel the effects of system instabilities responsible for the variation of the ratio between the energy, \( E \), absorbed by the crystal and the amplitude \( \Delta V \) of the corresponding electrical pulse. In a very naive model (see Eq.7) of bolometers the following relation exists:

\[
\Delta V = G_e A V_{bol} \frac{E}{C T_{bol}} = G_e A V_{bias} \frac{R_{bol}}{R_{bol} + R_{load}} \frac{1}{C T_{bol}} E
\]  

(8)

Where \( G_e \) is the total gain of the electronic chain, \( A \) = thermistor sensitivity, \( V_{bias} \) = total bias, \( V_{bol} = V_{bias} (R_{bol}/R_{bol} + R_{load}) \), \( R_{load} \) = load resistance,
$R_{bol} = \text{bolometer resistance},\ C_{bol} = \text{crystal heat capacity},\ T_{bol} = \text{temperature of the crystal}.$

There are three instabilities that can modify the ratio $\Delta V/E$: a variation in the electronic gain ($G_e$), a variation in the bias ($V_{bias}$), and finally a variation in the temperature ($T_{bol}$) of the crystal. The electronic system is designed to guarantee a stability of $G_e$ and of $V_{bias}$ within 0.1%. It is however, much more difficult to maintain stability within 0.1% of the detector temperature on long time scales. At a temperature of 10 mK this would require maintaining the temperature of 1000 crystals to an accuracy of 10 $\mu K$ for a period of several days.

To overcome this problem, a silicon resistor glued to each crystal is used as a heater to produce a reference pulse in the detector. It is connected to a high precision programmable pulser that produces a fast voltage pulse every few minutes dissipating the same amount of energy ($E_{ref}$) into the crystal each time. These voltage pulses mimic pulses produced in the crystal by particle interactions and are used to measure the value of the ratio $\Delta V/E$. Any variation of the amplitude of the reference pulse is due to variations of the $\Delta V/E$ ratio. The OF amplitude of the reference pulse is therefore used to measure, every few minutes, the actual value of $\Delta V/E$ while the baseline of the reference pulse provide the contemporary measurement of the value of $T$. A fit is then used to obtain the values of $\Delta V/E$ for each temperature value. Therefore, in this step of the off line analysis, the OF amplitude of each pulse is corrected according to the value assumed by the $\Delta V/E$ for the detector temperature at which the pulse has been generated. This technique has been proven to be efficient in the MI-DBD experiment, where a typical temperature fluctuation over a day ranged from a few tenths to $\sim 100 \mu K$. After correction, these fluctuations were reduced to less than 1 $\mu K$ [44].

Pulse shape analysis is very useful in rejecting spurious signals produced by microphonics and electronic noise. A confidence level is determined for each pulse shape parameter and for the rise and decay time of each pulse. Signals falling within these intervals are defined as “true” pulses, and signals having one or more of their parameters outside of the relevant interval are rejected as noise. The use of more than one pulse shape parameter results in better reliability of the rejection technique.

The linearization of the detector response is critically important for energy calibration. The final step in data processing is the conversion of the OF amplitudes into energy values. The naive bolometer model previously used assumes linearity; however, several parameters depend on the crystal temperature, rendering the corresponding equation non-linear. Accordingly, the relation between $\Delta V$ and $E$ will be obtained periodically by the use of radioactive calibration sources. The ratio $\Delta V/E$ will be measured for several
gamma lines, and the data will be fit to the model previously described, but taking into consideration the fact that the bolometer resistance and the crystal heat capacity are temperature dependent. This will provide the calibration function of $E$ as a function of $\Delta V$, that will then be used to convert the OF amplitudes into energy values.

Finally, the close packed array of the crystals will allow the rejection of events that left energy in more than one single crystal. This will be particularly useful in rejecting a very high energy gamma rays that enter from outside of the array. The small angle Compton scattering in a single crystal can mimic a double beta decay event, a dark matter scattering, or a solar axion. The probability that this photon would escape the rest of the array without a second interaction is small. In addition, background events from radioactivity within the structure of the array will also have a significant probability of depositing energy in more than one crystal. This will also be true for high and intermediate energy neutrons. In the final stage of off-line analysis these coincidence events can be identified from the data which will contain the detector number, signal time, pulse energy, and pile-up parameter.

7 Simulation and predicted performances

The goal of CUORE is to achieve a background rate in the range 0.001 to 0.01 $\text{counts/(keV kg y)}$ at the $0\nu\beta\beta$ transition energy of $^{130}\text{Te}$ ($2528 \text{keV}$). A low counting rate near threshold (that will be of the order of $\sim 5 \text{ keV}$) is also foreseen and will allow CUORE to produce results in the Dark Matter and Axions research fields. In Sec. 7.1 we present a very conservative evaluation of the background reachable with CUORE; this is mainly based on the status of the art of detector design and of radioactive contaminations. This rather pessimistic approach in background evaluation is the only one that presently guarantees a reliable prediction. However CUORE construction will require about five years, there will therefore time enough for an R&D dedicated to background reduction as it is foreseen in most next generations experiments. In Sec. 7.2 we discuss this possibility.

7.1 Background simulations

Radioactive contaminations of individual construction materials, as well as the laboratory environment, were measured and the impact on detector performance determined by Monte Carlo computations.

The code is based on the GEANT-4 package; it models the shields, the cryo-
Table 1
Bulk contamination levels in picograms per gram.

<table>
<thead>
<tr>
<th>Contaminant</th>
<th>$^{232}Th$</th>
<th>$^{238}U$</th>
<th>$^{40}K$</th>
<th>$^{210}Pb$</th>
<th>$^{60}Co$</th>
</tr>
</thead>
<tbody>
<tr>
<td>TeO$_2$</td>
<td>0.5</td>
<td>0.1</td>
<td>1</td>
<td>10 µBq/kg</td>
<td>0.2 µBq/kg</td>
</tr>
<tr>
<td>copper</td>
<td>4</td>
<td>2</td>
<td>1</td>
<td>0</td>
<td>10 µBq/kg</td>
</tr>
<tr>
<td>Roman lead</td>
<td>2</td>
<td>1</td>
<td>1</td>
<td>4 mBq/kg</td>
<td>0</td>
</tr>
<tr>
<td>16 Bq/kg lead</td>
<td>2</td>
<td>1</td>
<td>1</td>
<td>16 Bq/kg</td>
<td>0</td>
</tr>
</tbody>
</table>

The background sources considered are:

1. bulk and surface contamination of the construction materials in $^{238}U$, $^{232}Th$ chains and $^{40}K$ and $^{210}Pb$ isotopes;
2. bulk contamination of construction materials due to cosmogenic activation;
3. neutron and muon flux in the Gran Sasso Laboratory;
4. gamma ray flux from natural radioactivity in the Gran Sasso Laboratory;
5. background from the $2\nu\beta\beta$ decay.

For bulk contaminations the main contributions to background come from the heavy structures near the detectors (the copper mounting structure of the array, the Roman lead box and the two lead disks on the top of the array) and from the detectors themselves (the TeO$_2$ crystals). The radioactivity levels used in the computations for these materials are given in Table 1. The $^{232}Th$, $^{238}U$, $^{40}K$ and $^{210}Pb$ contamination levels of TeO$_2$, copper and lead as well as the $^{60}Co$ cosmogenic contamination of copper are deduced from the 90% C.L. upper limits obtained for the contaminations measured in MI-DBD experiment and with low activity Ge spectrometry [45]. In both cases no evidence of a bulk contamination is obtained with the achievable sensitivity and only upper limits could be obtained. The $^{60}Co$ cosmogenic contamination of TeO$_2$ is on the other hand evaluated according to the time required to produce TeO$_2$ powder from the ore, grow the crystals and store them underground. The results of the Monte Carlo simulations using these contamination levels are given in Table 2 for the $0\nu\beta\beta$ decay and the low energy (10-50 keV) regions. The threshold assumed is 10 keV and only values after reduction by anti-coincidence between detectors are there indicated. These values have to be considered as upper limits on the possible contribution of bulk contaminations to the CUORE background; they prove that with the already available materials background
Table 2
Computed background in the $0\nu\beta\beta$ decay and in the low energy regions for bulk contaminations in the different elements, the Cu structure accounts for the detector mounting structure and the 50 mK shield.

<table>
<thead>
<tr>
<th>Simulated element</th>
<th>$TeO_2$ crystals</th>
<th>Cu structure</th>
<th>Pb shields</th>
<th>TOTAL</th>
</tr>
</thead>
<tbody>
<tr>
<td>$0\nu\beta\beta$ decay region $counts/(keV kg y)$</td>
<td>$1.6 \times 10^{-3}$</td>
<td>$1.5 \times 10^{-3}$</td>
<td>$7.0 \times 10^{-4}$</td>
<td>$3.8 \times 10^{-3}$</td>
</tr>
<tr>
<td>dark matter region $counts/(keV kg d)$</td>
<td>$2.3 \times 10^{-2}$</td>
<td>$9.6 \times 10^{-4}$</td>
<td>$5.0 \times 10^{-5}$</td>
<td>$2.4 \times 10^{-2}$</td>
</tr>
</tbody>
</table>

lower than $\sim 4 \times 10^{-3}$ $counts/(keV kg y)$ in the $0\nu\beta\beta$ decay region and $\sim 3 \times 10^{-2}$ $counts/(keV kg d)$ in the low energy (10-50 keV) region are ensured.

Surface contaminations contribute to background only when they are localized on the crystals or on the copper mounting structure directly faced to them. Background contributions in the two regions of interest are summarized in Table 3. There U and Th contaminations with an exponential density profile and a $\sim 1 \mu m$ depth (in agreement with the contaminations observed in the MI-DBD experiment) are considered, while the contamination of this surface layer is assumed to be: for crystals $\sim 100$ times lower and for copper $\sim 50$ times lower than the corresponding contamination in MI-DBD experiment. As discussed in Sec. 4 the MI-DBD crystals were contaminated during the polishing procedure due to the use of highly contaminated powders. Polishing powders with a radioactive content 1000 times lower are however commercially available [46] and have already been used for Cuoricino, an improvement of the surface contamination of a factor 100 is therefore fully justified. A similar situation is that of copper; in the MI-DBD experiment the copper surfaces were treated with an etching procedure [47] shown to reduce impurities on surfaces before the sputtering process. This procedure allowed to obtain a good improvement of the surface quality of copper however it is not optimized from the point of view of background. The use of low contaminated liquids (water and inorganic acids are available with U and Th contaminations lower than 0.1 pg/g) in a low background environment will allow an improvement of one to two orders of magnitude in the surface contamination of copper.

Concerning the other background sources i.e. cosmogenic activation as well as muons, neutrons and gamma rays from the Laboratory environment these should produce minor contributions to the $0\nu\beta\beta$ background thanks to the underground storage of construction materials and the optimization of the lead and neutron shields. In particular the only cosmogenically produced long lived isotope contributing to $0\nu\beta\beta$ background is $^{60}Co$ whose presence has
been already included as a bulk contamination of both TeO$_2$ and copper (see Table 1 and Table 2). The situation is a little bit different for what concerns the low energy region. A preliminary evaluation of the non-intrinsic background rates near threshold results in a counting rate similar to that due to bulk contaminations. A complete and detailed study of the non-intrinsic background rates is underway.

Using the present upper limits for the $^{130}$Te $2\nu$ half-life, the unavoidable background produced by the $2\nu\beta\beta$ decay is lower than $10^{-4}$ counts/(keV kg d) (using the predicted energy resolution).

In summary, in a very conservative approach where the CUORE-tower mechanical structure is assumed identical to the structure used in CUORICINO, with the presently achieved quality of low contamination materials and considering the worst possible condition for bulk contaminations (i.e. all the contamination equal to the present 90%/C.L. measured upper limits (Table 1), the CUORE background will be $\sim 0.007$ counts/(keV kg y) at the $0\nu\beta\beta$ transition and $\sim 0.05$ counts/(keV kg d) near threshold.

### 7.2 Background R&D for CUORE

CUORE construction will require about five years; during that period we plan to spend much effort in trying to further reduce the achievable background. There are indeed several points on which it is possible to work. Concerning the crystals, their $1.8 \times 10^{-3}$ counts/(keV kg y) contribution to the $0\nu\beta\beta$ region is dominated by the $^{60}$Co cosmogenic contamination. This could be lowered by one order of magnitude by producing the crystals in a shallow depth laboratory. For U and Th impurities we have only upper limits of order $10^{-13}$ g/g. However we know that before crystallization the TeO$_2$ powder is much more contaminated, therefore the selection of a lower contamination powder together with the efficient reduction of impurities by the crystallization procedure should guarantee a contamination of $10^{-14}$ g/g. The situation for copper is a little bit different as not only it is possible to work on the

<table>
<thead>
<tr>
<th>Simulated element</th>
<th>$TeO_2$ crystals</th>
<th>$Cu$ mounting structure</th>
<th>TOTAL</th>
</tr>
</thead>
<tbody>
<tr>
<td>$0\nu\beta\beta$ decay region</td>
<td>$8.5 \times 10^{-4}$</td>
<td>$2.0 \times 10^{-3}$</td>
<td>$2.8 \times 10^{-3}$</td>
</tr>
<tr>
<td>counts/(keV kg y)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>dark matter region</td>
<td>$6.8 \times 10^{-4}$</td>
<td>$5.3 \times 10^{-4}$</td>
<td>$1.2 \times 10^{-3}$</td>
</tr>
<tr>
<td>counts/(keV kg d)</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
selection of low contamination copper but it is also possible to reduce the amount of copper used for the mounting structure of the detectors. This is particularly true in the case of the two copper frames (see Fig 5) that hold the crystals in the four-detector module, presently in CUORICINO (and also in our simulation) they are over sized from both the thermal and the mechanical points of view. A reduction of at least a factor 2 of their mass and surface is possible with a consequent reduction of the bulk and surface contribution to background. The background coming from surface contaminations is dominated, in the $0\nu\beta\beta$ region, by the copper contribution and mainly by the 4-crystal copper frames. This contribution could be reduced not only by the reduction of the frame mass but also by covering the copper surfaces with cleaner materials. If successful this R&D would then result in a reduction of background to the level of 0.001 counts/(keV kg y) at the $0\nu\beta\beta$ transition energy and to 0.01 counts/(keV kg d) at threshold.

7.3 CUORE $0\nu\beta\beta$ sensitivity

The connection between the effective electron neutrino mass and the nuclear structure factor $F_N$ is given in equation (4). The values of $F_N$ calculated for $^{76}Ge$ and $^{130}Te$ are given in Table 4 for 11 different nuclear structure models.

It is evident from the values in Table 4 that for a given half-life sensitivity, a $^{130}Te$ detector can be between a factor of $\sim 2$ and $\sim 4.6$ as efficient in probing...
the Majorana mass parameter, \( < m_\nu > \) as a \(^{76}\text{Ge} \) detector. However, because of the ratio of the molecular weights, the ratio of the isotopic abundances in the detector materials, there are 5.41 times as many \(^{76}\text{Ge} \) atoms in a kg of \( \text{Ge} \) metal isotopically enriched to 86\% in \(^{76}\text{Ge} \), as there are \(^{130}\text{Te} \) atoms in a kg of natural abundance \( \text{TeO}_2 \). If we average the ratios of the values in Table 4, and drop the two highest, and two lowest values, we find \( < F_N^{(130}\text{Te}) / F_N^{(76}\text{Ge}) > \approx 6.2 \). Considering the uncertainty in this procedure, we estimate that a detector of \( \text{TeO}_2 \) of natural abundance is equivalent in decay rate to one of 86\% \(^{76}\text{Ge} \) of the same mass.

CUORE will have 206 kg of \(^{130}\text{Te} \) which will contain \( 1.19 \times 10^{27} \) atoms of \(^{130}\text{Te} \). If we assume, from our discussion of backgrounds, a counting rate of 0.01 \( \text{counts/(keV kg y)} \) and an energy resolution of \( \sim 5\text{ keV} \) there will be less than 60 background counts/y to a 95\% kg in the 5 keV window. The half-life sensitivity would be:

\[
T_{1/2}^{0\nu}(^{130}\text{Te}) \geq (8.25 \times 10^{26}) \cdot \left( \frac{t}{2\sqrt{BG}} \right) \text{ y}.
\]  

The total number of background counts expected in the 5 keV window in 10 years is \( \sim 460 \). The 1\( \sigma \) statistical fluctuation, \( \sigma = \sqrt{n} \), is \( \sim 21 \) and the 2\( \sigma \) C.L. is 42. The half-life sensitivity is then \( \sim 2 \times 10^{26} \text{ y} \). Using equation 4, we quote the sensitivities of the Majorana mass parameter in Table 4 in the last column.

In the case a background of 0.001 \( \text{counts/(keV kg y)} \) would be reached the 10 year sensitivity would be \( \sim 3.5 \times 10^{26} \text{ y} \) (at 95\% C.L.) and the corresponding sensitivities of the Majorana mass parameter will be \( \sim 1.8 \) times higher than those quoted in Table 4 (i.e. in the range 11 – 56 meV).

7.4 CUORE dark matter and axion sensitivity

The sensitivity of CUORE in WIMP detection is shown in Fig 12 where the one year projected exclusion plots for background counting rates of 0.05 and 0.01 \( \text{counts/(keV kg d)} \) and a threshold of 10 keV are shown. Thanks to the large mass of the detector, CUORE will be also able to give results on the dark matter modulation signal as discussed in reference [61]. Concerning solar axion detection the sensitivity of CUORE will depend strongly on the threshold reached. In the case of a 5 keV threshold and a 2 keV FWHM low energy resolution the \( g_{\gamma\gamma}^{\text{lim}} \) sensitivity is of about \( 0.7 \times 10^{-9} \text{ GeV}^{-1} \) [26].
Fig. 12. Exclusion plots for a background of 0.05 and 0.01 counts/(keV kg d).

8 The enrichment option

CUORE is the only future proposal for a 0νββ decay experiment that plans the use of non-enriched material. Indeed as already the high isotopic abundance of $^{130}$Te allows excellent high sensitivities even using the much cheaper natural abundance material. This obviously implies that the construction of a larger array would be not only technically possible but also fiscally acceptable. On the other hand the high natural abundance of $^{130}$Te allows a much simpler and less expensive enrichment procedure than that for other double beta decay candidates. Moreover $TeO_2$ crystals made with $^{130}Te$ isotopically enriched material have been already tested during the MI-DBD experiment with results compatible with those obtained for the natural crystals both from the detector performances and detector background point of view. An enriched CUORE with a background of 0.001 counts/(keV kg y) would have a 10 years half-life sensitivity of $\sim 10^{27}$ y (at 95% C.L.) implying a sensitivity on the Majorana mass parameter in the range $9 - 46$ meV.

9 Conclusions

It is quite straightforward to demonstrate how the determination of the effective Majorana mass of the electron neutrino constrains the lightest neutrino
mass eigenvalue. This was done recently by Barger, Glashow, Marfatia and Whisnant [59]. However it is very convenient to use the approximation that $\sin \theta_2 \simeq 0 \equiv s_2$ and $\cos \theta_2 \simeq 1$. With the further assumption $\delta m_2^2 \ll \delta m_{AT}^2$ in the normal hierarchy case we obtain:

$$|<m_{\nu}| \leq m_1 \leq \frac{|<m_{\nu}|}{\cos(2\theta_3)}$$

where $\cos(2\theta_3) \simeq 0.5$. Similarly in the case of inverted hierarchy:

$$\sqrt{|<m_{\nu}|^2 - \delta m_{AT}^2} \leq m_1 \leq \frac{\sqrt{|<m_{\nu}|^2 - \delta m_{AT}^2 \cos(2\theta_3)}}{\cos(2\theta_3)}$$

A related quantity, $\Sigma \equiv m_1 + m_2 + m_3$ has great importance in cosmology. It is related to the quantity $\Omega_\nu$, the fraction of the critical density, $\rho_0$ (that would close the universe) that is in the form of neutrinos, where:

$$\Sigma = (93.8\, eV) \, \Omega_\nu \, h^2$$

and $h$ is the dimensionless Hubble constant. It was shown in reference [59] that $\Sigma$ obeys the following inequality with respect to $|<m_{\nu}|$:

$$2|<m_{\nu}| + \sqrt{|<m_{\nu}|^2 + \delta m_{AT}^2} \leq \Sigma$$

$$\leq \frac{2|<m_{\nu}| + \sqrt{|<m_{\nu}|^2 + \delta m_{AT}^2 \cos(2\theta_3)}}{\cos(2\theta_3)}$$

where the + and − signs refer to normal and inverted hierarchy respectively, and $\cos(2\theta_3) \equiv 0.5$. If this relation is written as two equalities, and each side is solved for $|<m_{\nu}|$ in terms of $\Sigma$, quadratic equations results with the constant terms $(\Sigma^2 \mp \delta m_{AT}^2)$. Values of $\Sigma^2$ of cosmological interest are much larger than $\delta m_{AT}^2 \leq 0.005\, eV$ (99.73% C.L.). Accordingly the above inequality reduces to the trivial form:

$$|<m_{\nu}| \leq \Sigma/3 \leq 2|<m_{\nu}|$$

This clearly demonstrates the direct connection between neutrinoless double beta decay and neutrino dark matter. Cosmic microwave background and galaxy cluster surveys have set the bound $\Sigma \leq 1.8\, eV$ [60]. It is expected that the MAP satellite will produce data that will result in a sensitivity $\Sigma \simeq 0.5\, eV$. In the case of Majorana neutrinos, the CUORE experiment is projected to have a sensitivity of $\Sigma \simeq (0.035 - 0.103)\, eV$ depending on the nuclear matrix element used to analyze the data.
One interesting scenario results in the case the MAP satellite, for example, observes a clear signal well above their limiting sensitivity, and CUORE (as well as other next generation experiments) have a negative results at sensitivities of Σ far below that of the satellite data. This would be a clear indication that the phenomenon causing the density fluctuations implied by the CMB data was not caused by Majorana neutrino dark matter. In addition a positive measurement of the mass \( m_{\nu_e} \) by KATRIN \(^3\)He beta end-point spectrum measurement would have to yield \( m_{\nu_e} \geq 0.35 \text{eV} \). The CUORE experiment will have a far greater sensitivity and if it would find a negative result, the mystery of Dirac or Majorana character of neutrinos will be solved.

It should be abundantly clear from the forgoing discussion that the most important remaining issue in neutrino physics is that of the determination of the neutrino mass scale. Neutrino oscillation experiments have clearly demonstrated that:

1. neutrinos have mass and that their mass eigenstates mix
2. the mixing matrix elements have values that imply that next generation \( 0\nu\beta\beta \) decay experiments should be able to determine the scale of neutrino mass in the case of Majorana neutrinos.

The main advantage of CUORE is that it will utilize \( \text{TeO}_2 \) crystals of natural abundance Te, while this technology has yielded energy resolutions approaching those of intrinsic Ge detectors. Energy resolution is crucially important for an actual observation of \( 0\nu\beta\beta \) and a measurement of \( |< m_\nu >| \).

References


[23] E. Norman and R. J. McDonald - Presentation made to the CUORE collaboration, Milan Italy, 11 December 2000 (Private communication).


[37] C. Arnaboldi et al., IEEE Transactions on Nuclear Science, to be published October 2002 ”Low Frequency Noise Characterization of Very Large Value Resistors”.


