National Uranium Resource Evaluation

VOLUME 3 URANIUM ASSESSMENT FOR THE PRECAMBRIAN PEBBLE CONGLOMERATES IN SOUTHEASTERN WYOMING

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UNIVERSITY OF WYOMING Laramie, Wyoming February, 1981



PREPARED FOR U.S. DEPARTMENT OF ENERGY GRAND JUNCTION OFFICE, COLORADO

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INTRODUCTION

Uranium and thorium occur in Precambrian pebble conglomerate metasediments in the Sierra Madre and Medicine Bow Mountains of southeastern Wyoming as shown on Figure 1. The Geology Department of the University of Wyoming was asked to make a geostatistical assessment of the uranium endowment of these deposits as a part of the World Class core drilling operations of the Bendix Field Engineering Corporation. This study was to include (a) the development of optimum geostatistical methodology for assessing uranium endowment in areas of close drill control (1 mile or less centers) as well as in areas of distant drill control (5 mile centers or more), (b) the implementation of this methodology in assessing the uranium resources of the pebble conglomerates in southeastern Wyoming, and (c) the determination of the overall geostatistical uncertainty of the resource estimates. In addition, methods were to be studied for projecting the assessments into new areas, including prediction of estimate uncertainty.

The resource assessment consisted of four phases of activity. These were (a) a detailed geological study of the configuration, genesis, and structure of the deposits, (b) the statistical design of a sampling plan and the collection of rock samples from drill core and outcrops, (c) the geostatistical analysis of the assays of these samples, and (d) the integrated geological and statistical interpretation of these results to produce resource estimates and error predictions.



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Geostatistical sampling and analysis is somewhat different depending on whether the mineral resource is in the reconnaissance, exploration, development, or production phase of operations. Closely spaced drilling and sampling is characteristic of development and production operations. The sampling can be strongly controlled by statistical considerations with geological interpretations having reduced importance. In reconnaissance and early exploration effort, the geological interpretation is all important and statistics plays a supporting role. Actual data measurements may be quite sparse over large areas and, in the extreme situation of very sparse data, methods based on subjective probability and geological judgment may be the only available procedures.

In the assessment of the uranium endowment in southeastern Wyoming, enough data has been accumulated to form the basis for estimation with a modified version of optimal averaging called "kriging." This method takes into account spatial persistence of enrichment within the deposit and provides systematic procedures for predicting the errors in the resource estimates. In general, the kriging method assumes statistical stationarity over the zone for which the estimates are being prepared. In practical applications where trends are present, the analysis proceeds in three steps. These are (a) trend removal and various transformations to produce an approximate stationarity, at least, over sub-portions of the ore deposit, (b) the production of kriged estimates for the transformed endowment, and (c) the reverse transformation to estimate the resource in terms of the actual "in-place" endowment. Because the data available from outcrop and drill core is relatively sparse, modifications of the geostatistical procedures are required to remove trends and other

types of spatial changes in statistical behavior so that data from one area of the deposit can be used to make predictions for other portions of the deposit.

In the southeastern Wyoming study, the principal trend present was that associated with near-surface leaching of uranium by ground water. This varies with depth and possibly, with other mineralogical and physical properties of the host rock; hence, the adjusted values allow the use of surface and near-surface samples to estimate uranium endowment at depths below leaching horizons. The deposit was divided into small enough subzones so that horizontal spatial trends did not appear important. Thus, the analysis procedure consisted of an adjustment for leaching, the computation of kriged estimates, and the reverse transformation to predict the actual leached tonnages present in each depth interval.

If a large amount of data had been available from each depth interval (such as would be obtained from closely spaced production drilling on a tight grid), the entire leaching correction and reverse transformation process would be unnecessary. The unadjusted data from each depth interval would be used to predict the tonnage within that interval. In the present situation, the data consists of assays from a large number of outcrop transects perpendicular to formation strike, plus assays from as many drill holes as time and budget would permit. The drill hole data makes a significant and essential contribution to the assessment, particularly in evaluating leaching and geological continuity with depth, but the down-hole encounters of the enriched beds are much too widely spaced both in vertical and horizontal position to allow a simple average of data over each depth interval. Consequently, the three-step procedure of leaching adjustment, kriging, and reverse transformation appears to provide the most efficient use of the data in the resource assessment.

The uranium enrichment occurs in pebble conglomerate lenses (probably deposited as alluvial fans) scattered through a roughly tabular zone which crops out with an essentially linear strike and which dips fairly steeply (40 to 60 degrees). A convenient geometric model for such tabular deposits is that of a "mineable surface". That is, the thickness of the bed is temporarily ignored and attention is focused on a single bedding plane (i.e. mineable surface) of the formation.

This whole procedure of reducing the three-dimensional ore deposit to a two-dimensional mineable surface is sometimes called the "method of accumulation". It was originally developed for gold deposits in South Africa. It substantially simplifies the geostatistical computations without the loss of essential information.

The areas of the mineable surface within each depth interval provide basic input for the tonnage calculations for that depth interval. All data are projected onto the mineable surface. The total thickness of the beds with $U_{3}0_{8}$ exceeding 100 ppm along a given drill hole or surface transect is assigned to the point on the mineable surface where the drill hole or transect encounters the surface. The thickness must, of course, be corrected to true thickness as measured along a perpendicular to the mineable surface at that location.

The average ore grade is similarly projected along a perpendicular to the mineable surface, using bed thickness as weights. Average grade = $\frac{\Sigma(\text{bed thickness x ppm U}_{3}0_8)}{(1)}$

Σ bed thickness

The sum is restricted to those beds exceeding a $U_{30_{\rm R}}$ grade of 100 ppm.

Hence, relative to the mineable surface, the basic data can be reduced to an average thickness and an average grade at each piercement

of the mineable surface by drill hole or surface outcrop transect. In addition, the areas of the mineable surface are calculated for each depth interval for which resource estimates are required. The basic relation for resource tonnage is, then, of the general form:

> resource = mineable surface area x average thickness x average grade. (2)

The actual implementation of this relation is quite a bit more complicated, but the basic concept remains correct.

In order for the concept to remain valid, the sampling must be controlled so that the assays along a given transect or drill hole can be regarded as representing a channel sample through the tabular ore zone along a perpendicular to the mineable surface. In the case of uranium and other radioactive elements, the measured radioactivity provides a convenient method to guarantee that all zones with U_{308} exceeding 100 ppm have been completely sampled.

SUMMARY OF THE GEOLOGICAL DESCRIPTION OF THE DEPOSITS

The uranium-bearing quartz pebble conglomerate in southeastern Wyoming occur in two separate areas. One area lies on the Carrico Ranch in the northwestern Sierra Madre, while the other is in the northeastern Medicine Bow Mountains at the Onemile Creek and Threemile Creek localities. The two areas and some regional details are shown in Figure 1. The geology for each will be summarized separately.

Geology of the Sierra Madre Deposits

The Sierra Madre region of the Late Archean (greater than 2600 m.y.) and Early Proterozoic (2500-2000 m.y.) metasediments was evaluated for syngenetic fossil placer uranium deposits. The metasediments in the area fall into two major groups: (1) the Phantom Lake Metamorphic Suite, and (2) the Deep Lake Group (Graff, 1979; Houston and Karlstrom, 1980). These metasediments were deposited in epicontinental and miogeoclinal environments, near the southern margin of the Wyoming Archean Province.

Radioactive rocks have been identified near the base of each metasediment group. The Deep Gulch Formation is believed to be near the base of the Phantom Lake Suite and the Magnolia Formation is the base of the Deep Lake Group. The Magnolia Formation was found to be low-grade (less than 10-20 ppm U) over most of the Sierra Madre, so resource evaluation concentrated on the Deep Gulch Formation.

The Deep Gulch Formation is composed of four distinct lithologic units as follows:

(lowest) Unit I - Arkosic conglomerate - slightly radioactive

- Unit 2 Trough cross-bedded, subarkosic quartzite slightly radioactive
- Unit 3 Interbedded radioactive, pyritic, quartz-pebble conglomerate and subarkosic granular quartzite
- Unit 4 Planar cross-bedded, subarkosic quartzites nonradioactive.

Unit 3 is the major target for uranium resource evaluations in the Sierra Madre region. Unit 3 crops out in the northwestern Sierra Madre (see Figure 2) and the area of the unit (see Appendix B) was used as a basis for the calculation of uranium resources in the Sierra Madre.

Unit 3 varies in thickness, but in general, it averages 60-70 feet thick in the western area and gradually thickens to 100-110 feet in the eastern exposures.

It consists of 5-15 conglomerate "reefs" (coalesced conglomerate lenses forming mappable stratigraphic beds) which vary in thickness from 2 inches to 3 feet and in length from 50 feet to over a mile. The thickest "reef" may be continuous for up to four miles.

Radioactive units of the Deep Gulch Formation in the northwest Sierra Madre strike northeast, dip northwest and are overturned. The beds are part of the overturned limb of a large reclined isoclinal fold system plunging west. This structure is further complicated by intralimb reverse faults of unknown displacement.

Because of the complex structure, the subsurface extent of the Deep Gulch Formation is conjectural. For the present resource evaluation



the beds were projected to the depth of 5000 feet for the following reasons.

- Long outcrop trace suggests significant lateral continuity in a down-dip direction.
- Drill holes indicate uniform dips to depths of at least 500-1000 feet.
- 3. Information on the depth to the hinge of the syncline is not available and the uniform projection down dip is the most simple interpretation and perhaps the most reasonable guess, given the existing data.

Geology of the Medicine Bow Deposits

Although the depositional and structural history of the middle Precambrian metasedimentary sequences in the Sierra Madre and Medicine Bow Mountains are very similar, there are minor but important differences between the two areas.

In the Medicine Bows, the Phantom Lake Suite is metavolcanic in the lower part, with more typical quartzite and arkosic conglomerates occurring in the upper part of the suite. Reconnaissance and subsequent work (Karlstrom and Houston, 1979) indicates that although some weakly radioactive zones occur, quartz-pebble conglomerates are absent in the Phantom Lake Suite of the Medicine Bow Mountains. The Magnolia Formation of the Deep Lake Group, however, contains numerous quartzpebble conglomerates, and those in the Onemile Creek and the Threemile Creek areas exhibit substantial radioactivity.

The Magnolia Formation is about 500 m (1600 feet) thick in the Onemile Creek area and consists mainly of radioactive, muscovitic, granular quartzite and pyritic conglomerates, having much the same character

as those in the Sierra Madre, i.e. individual lenses which coalesce into a body of mappable proportions. Individual outcrops of these units are variable in thickness and radioactivity, but may be mapped as essentially continuous beds. Three of these units are significantly more radioactive than the others and were the targets for uranium resource evaluation. The extent of these units, designated as unit 1 (which is near the base of the Magnolia Formation) and units 5a and 5b (which are in the upper portion of the formation) is shown on Figure 3.

The major structure in the Onemile Creek area is a faulted and intruded overturned syncline in the Magnolia Formation. This syncline is documented by top and bottom criteria in the Magnolia quartzites (personal communication, Karlstrom, 1980). Uncertainties still exist in this interpretation. The plunge of the syncline is poorly known and evidence can support either an inclined or a reclined structure. These problems bear on the resource evaluation because a geometry based on the reclined synclinal model will have more extensive conglomerage units than one based on the inclined model. The geometries shown in Appendix B, have been based on a simple isoclinal, inclined fold system and the areas calculated are therefore conservative estimates of the area of radioactive zones in the Onemile Creek area.

The Threemile Creek area shown in Figure 4 is located about 1 1/2 miles south of the Onemile Creek area. Paraconglomerates rather than quartz-pebble conglomerates comprise most of the radioactive units in this area, and correlation with metasedimentary units to the north is difficult because of the less conglomeratic nature of the lithologies and because of the complex structure which separates the two areas. Additionally,



the contacts in the Threemile area are gradational. Karlstrom, Houston and others (Vol. 1, this report) conclude that the radioactive units here are basal Magnolia units rather than a facies of the typically paraconglomeratic Phantom Lake Suite but do not extend Onemile Creek stratigraphy into the Threemile Creek area.

Surface mapping and information from a single drillhole indicate that the principal radioactive zone occurs in beds which form the overturned limb of the Sand Lake Syncline. The geometry used as a basis for the resource estimation is similar to the overturned structures in the Onemile Creek area. (See Karlstrom, Houston and others, 1981, Vol. 1, this report for detailed discussion of geology).

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OUTCROP AND DRILL CORE SAMPLING PROCEDURES

Since the sampling procedures had to be designed early in the project when very little data was available, several weeks of intensive field measurement and mapping of surface radioactivity was initiated to provide a data base adequate to plan further sampling. The geostatistical characteristics needed were the variance, σ^2 , of the uranium endowment, the zone of influence, h_{c} , (defined as the distance of separation along the strike in a radioactive bed at which two uranium assays become uncorrelated), and the nugget effect, a^2 , (defined as the expectedsquare-difference between uranium assays taken from spatial locations near each other). The variance measures the dispersion of the uranium values, h_ characterizes spatial persistence, and a² indicates the amount of local discontinuities present; more detailed definitions and discussion of their importance in the technique of geostatistical kriging will be given in the next section. These three parameters, together with sample size, control the estimation error and are, therefore, needed in planning the number and placement of the samples to be collected.

Spectrometer readings with various separations in distance along radioactive conglomerate layers were used to make preliminary judgments concerning geostatistical characteristics of the radioactive beds. The sequences of readings were taken at 6-inch, 1-foot, and 6-foot spacings along a number of conglomerate layers. The measurement site was on

ridge 1 and 2 in the Sierra Madre on the Carrico Ranch. The spectrometers were calibrated at the Bendix offices in Grand Junction, Colorado.

The median zone of influence, h_o , was found to be 10 feet. The nugget-effect-to-variance quotient, a^2/σ^2 , had a median of 0.62. Finally, the average of the standard deviation-to-mean value quotient, σ/\overline{V} was 0.9. All these characteristics were determined for the uranium accumulation defined as

U accumulation = (estimates ppm U) x (bed thickness in inches). (3)

Outcrop Sampling Plan

These geostatistical characteristics provided a basis for the design of an outcrop sampling plan. A variety of possible sampling plans were studied. The method which appeared most appropriate consisted of the collection of samples for assay along transects perpendicular to the strike of the conglomerate beds, supplemented with certain radiometric readings to monitor the geostatistical character of the beds from area to area. The transect procedure for various spacings between lines of samples was studied by two methods. One method was by direct analysis via geostatistical formulas. The other method utilized digital simulation on the SIGMA 7 as based on a statistical model incorporating many of the geological characteristics of the formations. The two methods produced similar results.

The target in a resource evaluation is to produce estimates of the ore reserve with controlled accuracy. One measure of this accuracy is the probable error (PE). The probable error is defined as the median of the absolute value of the error. Fifty percent of the time the error

magnitude will be less than PE and fifty percent of the time it will be larger. Thus, the probable error is a measure of what the error actually is.

In practice, it is more convenient to work with the relative probable error (PE%) as compared to the mean value of the deposit. If \overline{V} is the average grade of deposit and PE is the probable error of the estimate of grade, then

$$PE\% = \frac{PE}{\overline{V}} \times 100.$$
 (4)

The PE% value is related to h_{σ}^{2} , a^{2}/σ^{2} , and σ/∇ the geostatistical characteristics listed in the introduction. The following assumptions are made in the development of the formula.

- A linear deposit of length L requires a reserve estimate with relative probable error PE%.
- 2. The transect values are separated by more than a zone of influence h_0 , from one another. They need not be exactly equally spaced but should be roughly equidistant.
- The transect locations are <u>not</u> selected so as to "high-grade" the deposit.
- There is geological continuity between transects in a statistical sense.
- The average of the variograms along a transect remains about the same along the deposit.
- 6. The ore block averages being estimated are approximately normally distributed. Generally this will be true by a central limit theorem if the blocks are large, even if the local ore values have some other probability law (e.g., lognormal).

The formula then is, (with n = number of transects along L)

$$PE\% = 67.45 \ (\sigma/\overline{V}) \sqrt{\frac{1}{n} - (1 - \frac{a^2}{\sigma^2}) \left[\frac{h_o}{L} + \frac{1}{3} \left(\frac{h_o}{L}\right)^2\right]}$$
(5)

When $h_0 = 10$ feet, $\sigma/\nabla = 0.9$, and $a^2/\sigma^2 = 0.62$ are substituted into the formula, the equation reduces to

$$PE\% = 60.7 \sqrt{\frac{1}{n} - 3.8 \left[\frac{1}{L} + \frac{10}{3L^2}\right]}$$
 (6)

This relation is presented graphically in Figure 5. The basic question remains as to what PE% represents the best balance of accuracy and effort.

As an examination of the graph shows, greater accuracy requires more transects. For example, a 100-foot long deposit attains a PE% of 15% with 10 transects, but 15 transects are required if the PE% is to be reduced to 10%. Seven transects would give a 20% probable error for the same length.

For most regional resource valuations, a relative probable error of about 18 to 20% is usually acceptable. In development-type reserve estimates, at a mine site for example, a smaller PE% of 5% would be desirable. The more marginal the deposit is, the greater will be the accuracy needed to guarantee against loss if the property is mined. Everything considered, it appeared reasonable to design the Sierra Madre-Medicine Bow uranium estimates for a PE% = 20%.

The value of the length L depends on whether an estimate for the local area is desired, or a regional estimate is being made. For this study we looked only at the three favorable sites which contained the high-



Figure 5. Relationship between length of bed, number of transects and percent probable error.

est grade materials (Onemile Creek, Threemile Creek, and Carrico Ranch areas). Outcrops in high grade material will use an L of approximately 400 feet as the length of the outcrop, although several nearby outcrops may be linked if the outcrops are too short. The number of transects needed to give a PE% = 20% for that L is then 9, as read from the graph.

Transect sampling was carried out as follows. Spectrometer readings of total gamma radiation were made more or less continuously along the transect, to locate "hot" layers. These readings were not recorded individually, although an overall summary was written for general and special features present. Readings were recorded for extra-hot zones.

Attempts were made to sample all hot layers encountered. Thin layers, less than 8 inches, were sampled with one or two chunks of rock. Thicker layers were sampled at 3 or 4 places through the bed. The intent here was to approximate a channel sample of the "hot" bed as closely as possible. The samples for a single "hot" bed were bagged together and analyzed as a single combined sample which yielded an estimate of the average uranium in that bed at that location. Country rock, with radioactivity fairly uniform, was sampled at 2 or 3 locations along the transect.

Drill Core Sampling Plan

Assays of samples taken from drill core serve two important purposes. The assay values may be used to estimate reserves and they may be studied to lead to a more complete understanding of the geological processes present in the deposit. The sampling plan designed here was primarily directed to the first purpose - that of estimating reserves.

However, modifications have been introduced to allow the sampling plan to satisfy the second purpose reasonably well.

The accumulation for a core is defined as the integral of the ore value along the core. Let $V(\mathbf{Z})$ be the uranium concentration at vertical position \mathbf{Z} .

Accumulation =
$$\int_{z_{top}} V(z) dz.$$
(7)

Then the integral of the accumulation over the horizontal area of the deposit, after division by the volume of the deposit, gives the average value of the deposit.

Various elaborations, such as making the computations in zones or introducing statistical techniques like kriging, may be incorporated into the analysis. The procedure outlined above, however, illustrates the essential aspects of the method. To achieve this target, a three step procedure was used.

1. The core was scanned continuously with a spectrometer to locate "hot" zones accurately. The spectrometer scan was done in such a way as to give a continuous run of readings. This scan was confirmed by down-hole spectrometer measurements in the drill hole. As an operational definition, it appeared reasonable to define a "hot" zone as an interval of readings where the total gamma count is 20% greater than the nearby country rock average count. The location and length of the "hot" zones were carefully recorded for the collection of assay samples.

2. The "hot" zones were sampled for assay in intervals not exceeding one foot or the length of the "hot" zone, whichever was less. A lengthwise cut of the core, of uniform cross-section, running the full length of the interval, was crushed and split for the assay. If the "hot" zone was longer than one foot, several intervals were needed to cover the whole zone. The essential point is that the entire "hot" zone interval was covered by these interval samples.

In addition it was desirable to collect "point" samples at the bottom, middle, and top of the hot zones if the zones were of substantial thickness. As guided by geological judgment, it was desirable to sample any additional locations along the core where significant changes appeared to be present. These samples were largely intended to assist in geological interpretation, rather than reserve estimation.

3. The 'warm'' country rock surrounding the hot zones was sampled approximately every twenty-five feet. The root-mean-square percentage error in using a 25 foot sampling interval to estimate the country rock accumulation was found to be about 1%. Sampling at 80 foot intervals led to a 2.4% R.M.S. error. The 25-foot interval was suggested because it also offered some protection against unforeseen trends or variations in the uranium content of the country rock. It also has a quite acceptable accuracy. Since the overall accuracy of reserve estimation was planned for about 20%, the 1% error in vertical accumulation is quite satisfactory in not interfering with the horizontal (areal) outcrop sampling directed at achieving the 20% accuracy.

The samples for assay taken every 25 feet were point samples

(not interval or channel samples). In addition, extra samples were collected at locations along the core where the geologist believed that significant changes occur in the country rock.

OUTLINE OF GEOSTATISTICAL METHODOLOGY AND THE STATISTICAL PARAMETERS OF THE DEPOSIT

The Variogram

The basic characterization of spatial persistence used in mining geostatistics is the variogram function, sometimes called the semivariogram. It is a function of distance and direction of the separation or "lag" between two ore grades in the deposit. More specifically, the variogram, $\gamma(\underline{h})$, is defined as one-half of the average of the squareddifference between ore grades separated by the vector <u>h</u>. The difference between grades for each pair is squared. One-half of the average of these squared-differences would give an estimate of the variogram at lag <u>h</u>. This would have to be repeated at a number of different lag values to develop a clear delineation of $\gamma(\underline{h})$ for all <u>h</u> values. If the ore assays are established on some regular grid, the variogram can be estimated using neighboring pairs of grades for the shortest lag. Pairs separated by two grid spacing can be used for the next larger lag of averaging. Then 3 grid separations can be used, and so forth.

If the variogram does not vary with direction of lag but only depends on the distance of separation, the random field of data is said to be "isotropic." The variogram is then a function of the length, h, not the vector, \underline{h} .

For the uranium-bearing pebble conglomerates, the radioactivity appears to be isotropic within the mineable surface. Hence, the further

discussion will be restricted to this case. The theorems derived in Appendix A, however, are more general and are based on an anisotropic variogram with elliptical zone of influence over the mineable surface.

A typical isotropic variogram might have the shape shown in Figure 6. As the value of h becomes small, spatial persistence makes the grades increasingly similar to each other, and the γ (h) value approaches zero. The squared difference between grades of samples close together is small. As h gets large, the grade at one end of the separation becomes more and more unrelated to the grade at the other end. The squared difference gets larger. At some distance, called the zone of influence, h_o, the two grades are uncorrelated with each other and the average squared distance stays at about the same value for all larger h. It can be shown that for statistically stationary random fields of oregrade, the variogram will level off at a value equal to the variance, σ^2 , of the grade. Finally, one often encounters variograms with the appearance of Figure 7. If the Y(h) values at the shorter lags are extrapolated to zero, the line of extrapolation does not pass through zero, but gives $a^2>0$ where

$$a^{2} = \lim \gamma(h).$$

$$h \rightarrow 0 \qquad (8)$$

This means that there are abrupt changes in grade on a local scale (fractures, rich veins in waste, etc.). Thus, the average squared difference stays large even for spatial separations very small.

The variogram often motivates interesting geological conjectures concerning the deposit. Some other typical cases are given in Figure 8.



Figure 6. A typical isotropic variogram.



Figure 7. Typical variogram with variance, σ^2 ; zone of influence, h_o; and nugget effect, a².



spacings.
Variograms estimated from actual data have sample randomness and a much more jagged appearance than the idealized figures presented here. Some examples of actual variograms from the uranium data are shown below.

Another measure of spatial persistence useful in geostatistics is the covariance function. It can be defined as C(h), where

$$C(h) = \sigma^2 - \gamma(h)$$
(9)

for statistically stationary, isotropic random ore deposits.

Kriged Estimates

The geostatistical procedure of kriging (David, 1977; Journel and Huljbregts, 1978) can be based on either the covariance function or the variogram. In the following, the covariance function will be used. If all assay values are of equal important to the determination of the average grade in some depth zone, a reasonable estimate would be the arithmetic average of the assays. In mathematical terms, if $V(x_i)$ is the assay value at location x_i , and there are n assays available making an estimate of average grade for a zone B, then

$$\hat{\overline{V}}_{B} = \frac{1}{n} \sum_{i=1}^{n} V(x_{i})$$
(10)

where $\hat{\overline{V}}_{B}$ is the estimated average grade for the zone.

If all of the assays are not equally important to the determination of the average grade of zone B (for example, some assays may be within the zone and others may be some distance away), then a weighted average of the form

$$\hat{\overline{V}}_{B} = \sum_{i=1}^{n} a_{i} V(x_{i}), \qquad (11)$$

where
$$\Sigma = 1.0$$

i=1 (12)

may be more reasonable. For example, nearby values may be weighted more than those far away.

This raises the question, are there systematic procedures for determining the optimal or "best" choices of the weights, a_i . The answer is yes and the procedure is found to depend on the covariance function. The measure of optimality used is that the best weights, \hat{a} , are those which minimize the expected square difference between the actual average grade \overline{V}_B and the estimate of that value, $\hat{\overline{V}}_B$. The mathematical procedure for deriving these optimal weights is derived in theorem A-5 of Appendix A. Essentially the procedure reduces to the solution of a system of simultaneous equations whose coefficients and other constants are determined from the covariance function. The general technique is called kriging.

In the closely spaced sample collection of the production or development phases of mineral development, many samples are within a zone of influence of each other and the system of equations may become difficult to solve. However, in reconnaissance sampling the reverse is true. All samples are usually more than a zone of influence apart and the system of equations reduces to the very simple explicit solutions given in theorem A-6 of Appendix A. In fact if the zone of influence is small and the sample spacing is large, the weights are well approximated by l/n and

$$\hat{\overline{V}}_{B} = \frac{1}{n} \sum_{i=1}^{n} V(x_{i})$$
(13)

with error variance bounded by

$$\sigma_{\rm E}^2$$
 = Expected value of $(\hat{\overline{V}}_{\rm B} - \overline{V}_{\rm B})^2 \leq \frac{\sigma^2}{n} + c_{\rm BB}^2$, (14)

where C_{BB} can be computed from the geometry of the zone B and the covariance function. In particular, if the variogram is of the simple transitive isotropic form (definition A-1 with very small s(Θ) and $a = b = h_{O}$), a convenient upper bound for σ_{E}^{2} is

$$\sigma_{\rm E}^2 \le \frac{\sigma^2}{n} + \frac{\pi h_0^2 (\sigma^2 - a^2)}{3B}$$
(15)

where B denotes the area of zone B on the mineable surface.

The Sampling Relation in Figure 5

The equation used in Figure 5 was an even simpler version of the relation for σ_E^2 . All the equations can be simplified to one-dimensional space (i.e., samples along the strike of the outcrop). The simple transitive variogram becomes

$$\gamma(h) = \begin{cases} a^{2} + (\sigma^{2} - a^{2})|h|/h_{o}, \text{ if } |h| \leq h_{o} \\ \sigma^{2} , \text{ if } |h| > h_{o}. \end{cases}$$
(16)

and the covariance function is

$$C(h) = \begin{cases} (\sigma^2 - a^2) (1 - |h| / h_o), & \text{if } |h| \le h_o \\ 0, & \text{if } |h| > h_o. \end{cases}$$
(17)

Under the conditions that all samples are more than a zone of influence apart and are collected at an interior point of zone B more than a zone of influence from the nearest boundary of B, the expressions $C_{BB}^{}$ and $C_{Bi}^{}$ in theorem A-5 may be explicitly evaluated as

$$C_{Bi} = \frac{1}{L} \int_{B} C(x-x_{i}) dx$$
$$= (\sigma^{2}-a^{2})h_{o}/L$$
(18)

and

$$C_{BB} = \frac{1}{L^2} \int_{B} \int_{B} C(x-x') dx dx'$$

= $(\sigma^2 - a^2) (h_0/L) (1 - h_0/3L),$ (19)

where L is the length of the one-dimensional zone B. For this case, the values of a and μ resulting from the solution of the system of equations in theorem A-5 are

$$\hat{a}_i = 1/n \tag{20}$$

$$\hat{\mu} = (\sigma^2 - a^2)h_o/L - \sigma^2/n.$$
 (21)

Hence the expression for σ^2_E becomes

$$\sigma_{\rm E}^2 = c_{\rm BB} - \sum_{i=1}^{n} \hat{a}_i c_{\rm Bi} - \hat{u}$$

= $\frac{\sigma^2}{n} + (\sigma^2 - a^2) (h_o/L) (1 - h_o/3L) - 2 (\sigma^2 - a^2) (h_o/L).$ (22)

Since the probable error is

$$PE = .6745 \sigma_{E}^{},$$
 (23)

it follows that the probable error in % is given by

$$PE\% = 67.45 \sigma_{E} / \hat{\overline{V}} = 67.45 (\sigma / \hat{\overline{V}}) [1/n - (1 - a^{2}/\sigma^{2}) (h_{o} / L + h_{o}^{2}/3L^{2})]^{1/2}.$$
(24)

If $h_0 = 10$ feet, $\sigma/\overline{V} = 0.9$, and $a^2/\sigma^2 = 0.62$ as the preliminary radioactivity sampling seemed to indicate, the probable error becomes

$$PE\% = 60.7[1/n - 3.8(1/L + 10/3L^2)]^{1/2}.$$
 (25)

This equation was used to develop the graph in Figure 5.

The graph served only as a guide for sampling purposes. Subsequently more extensive data arrays were used to refine and adjust the variogram parameters. For example, it was decided to use in the probable error computations of the final resource estimate, the values $a^2 = 0$ and $h_0 = 60$ feet since these gave conservative bounds for the error. Almost all of the estimated variograms gave values which actually predict smaller probable errors than $a^2 = 0$ and $h_0 = 60$ feet.

Lognormality of $U_{3}^{0}0_{8}$ and Th_{2}^{0}

The correction of the near-surface tonnage estimates to produce leached uranium endowments, depends critically on the probability law for the population of the larger U_3^{0} values. Previously published investigations have usually found that uranium grade is lognormal. It appeared reasonable to expect lognormal behavior for the Medicine Bow and Sierra Madre deposits.

The grade values which enter the computations consist of the thickness-weighted averages of the grade along each outcrop transect or drill hole as it pierces the mineable surface. The averages are only computed for exceedances of 100 ppm $U_3^0 0_8$. Let m denote the number of the transects or drill holes which fail to encounter an (unleached) $U_3^0 0_8$ value exceeding 100 ppm. If there are n transects and drill

holes, then (n-m) of the piercements of the mineable surface encounter exceedances of 100 ppm. Let

$$\ln U_{m+1} \le \ln U_{m+2} \le \ln U_{m+3} \le \dots \le \ln U_n$$
(26)

represent the averages of the logarithm of the grade for those layers exceeding 100 ppm unleached. The fraction of the piercements with value less than or equal to $\ln U_r$ is r/n. This is sometimes called the empirical distribution function,

$$F_{E}(U_{k}) = r/n, \text{ for } m < r \le n$$
(27)

and is regarded as a prediction of the distribution function for the uranium values when uranium = U_r . However, this estimate has the defect that

$$\hat{F}_{E}(U_{n}) = 1.0$$
 (28)

and this value cannot be plotted on lognormal probability paper since 1.0 on the probability scale corresponds to $U = \infty$ for these types of probability. This problem can be circumvented in several ways. One of the best is advocated by Gumbel (1954) who points out that if F(u) is the distribution function for the U population, then

$$\{\text{Expected value of } F(U_r)\} = r/(n+1).$$
(29)

With this plotting formula (i.e. $\hat{F}_{*}(U_{r}) = r/(n+1)$), the largest value observed, ln U_{n} , is plotted versus

$$\hat{F}_{*}(U_{n}) = n/(n+1)$$
 (30)

on the probability scale. This point can be placed on lognormal paper with no difficulty.

Thus the procedure used in testing the transect and drill hole accumulated grades for lognormality was as follows. The width-averaged values of the ln $U_{3}O_{8}$ (as corrected approximately to their unleached values) for all exceedances of 100 ppm were ranked in increasing order:

r rank	Average In U ₃ 08	$\hat{F}_{*}(U_{r}) = r/(n+1)$
m+1	ln U _{m+1}	(m+1)/(n+1)
m+2	۱n U _{m+2}	(m+2)/(n+1)
m+3	ln U _{m+3}	(m+3)/(n+1)
•		
•	•	•
•	•	•
n	ln U	n/(n+1).

If the graph of $\ln U_r$ versus r/(n+1), on normal probability paper is approximately a straight line, then the grade accumulations of exceedances of 100 ppm behave approximately like the upper tail of the lognormal.

This procedure was followed for the Medicine Bow and Sierra Madre $U_3^{0}_8$ and Th0₂ values. The resulting graphs are shown in Figure 9. In each case a straight line appears reasonably consistent with the data. The lognormal parameters, μ and σ^2 , can be estimated from the straight lines by the following conventions

$$\mu$$
 = value of ln where p = 50 (31)

$$\hat{\sigma}$$
 = (value of in where p = 84.13) $-\hat{\mu}$, (32)

where p is % probability.



Figure 9. Lognormal probability plots for uranium and thorium, Sierra Madre and Medicine Bow Mountains.

The predicted values for μ and σ are listed with each graph in Figure 9. These values will be used later in the section on the leaching formulas and associated resource adjustments.

The Variogram Parameters

As more data was accumulated, additional information became available for computing variogram parameters. The assay values could not be used for this purpose since they were always more than a zone of influence apart. However, additional radioactive count data was collected at close enough spacing to allow the determination of a^2/σ^2 and the zone of influence, h_. Some examples are shown in Figures 10, 11, and 12. In addition, there were many cases where only upper bounds to the parameters could be determined. A number of such estimates are summarized in Tables 1 and 2. Upper bounds are very relevant, because often they can be used to develop corresponding upper bounds for the probable error. In the resource data analyzed so far, a zone of influence of 60 feet and a nugget effect of 0 appears to give reasonable upper bounds. Actually, the probable errors were computed for both $h_{o} = 30$ and $h_{o} = 60$ feet with only slight changes in results. Thus, the error analysis is quite insensitive to h_0 and a^2 for the range of values in the data studied.



Figure 10. Variogram typical of conglomerate h, Sierra Madre.



Figure 11. Variogram typical of conglomerate k, Sierra Madre.



Figure 12. Variogram typical of Onemile Creek area conglomerates.

Rank	Zone of influence, h _o feet (ranked)	nugget-to-variance ratio a ² /σ ² (ranked)
1	3	.0
2	3	.03
3	5	.27
4	5	. 28
5	6	.55
6	10	.61
7	10 median value	.62 median
8	14	.63
9	26	. 79
10	36	. 80
11	45	.81
12	75	.91
13	117	.99

Table 1. Variogram parameters for radioactivity, Carrico Ranch, Sierra Madre. (Note: parameters are ranked separately in increasing size. Average variance of count = 55000 ppm²).

	Conglomerate	Zone of influence (ft)	Sill Value	Nugget effect
NO	G	shows trend		
REG	н	40	220(ppmTh) ²	1.0(ppmTh) ²
MADI		40	2200(ppmTh) ²	0.0(ppmTh) ²
SIERRA CARRICO RA	J	shows trend		
	К	90	3350(ppmTh) ²	200(ppmTh) ²
	L	25	350(ppmTh) ²	100(ppmTh) ²
z	Case 1	<10	***	••••••••••••••••••••••••••••••••••••••
3EG1(2	40	35000(cps) ²	0(cps) ²
OW EEK I	3	< 10		
NE B(E CRI	4	<10		
MILE	5	30	80000(cps) ²	0(cps) ²
MEI	6	20	18000(cps) ²	6000(cps) ²
	7	< 10		

Table 2. Variogram parameters values for data from various portions of the areas in the Sierra Madre and Medicine Bow Mountains

PREDICTION EQUATIONS FOR LEACHING

It appeared reasonable to assume that (1) below some particular depth, the uranium and thorium maintained some fixed functional relation with each other, and (2) above that depth the functional relation required that depth be introduced as an additional variable.

Multivariate stepwise regression was used to search for the critical depth and for the functional relationships. Calculations were made for ln U and ln Th as well as U and Th as measured. The logarithms of the assay values gave substantially better curve fits. After much trial-and-error, the following basic equation was determined to best represent the general features of the relation between ln U, ln Th, and depth, d:

$$ln U = (a_{0} + a_{1}e^{-cd} + a_{2}e^{-2cd} + a_{3}e^{-3cd}) + (b_{0} + b_{1}e^{-cd} + b_{2}e^{-2cd} + b_{3}e^{-3cd}) ln Th + random error.$$
(33)

This basically assumes that at any depth, there is a linear relation between In U and In Th. However, the intercept and slope of the linear relation are a cubic polynomial of the variable exp(-cd). This allows considerable freedom for the curve to follow the data as it varies with depth. Also, by choosing various values of c, the leaching could be made to reach either great depths or only affect very shallow portions of the deposit.

The general method of analysis consisted of fixing a value of c, and then determining the best coefficients $(a_0, a_1, a_2, a_3, b_0, b_1, b_2, b_3)$ to fit the data by stepwise-multiple regression. The goodness-offit, as measured by the fraction of scatter "explained" by the curve fit (a quantity called R² in statistical parlance) was then noted for that c value. This was done for many different c values and a graph of R² versus c was prepared. The value of c at the maximum R² would then be judged as the value most consistent with the data. Based on the R² criterion, the value c = .03 was chosen for both the Sierra Madre and the Medicine Bow Areas. Let d_0 be the depth at which the variable exp(-cd) dies off to one percent of what it is at d = 0. Then d_0 would be the solution to

$$e^{-.03d_0} = .01$$
 (34)
or
 $d_0 = 154$ feet. (35)

Thus, the c = .03 value implies that the leaching is negligible below d = 154 feet. The functional relations, for d>154 feet would approximately be

$$\ln U = a_0 + b_0 \ln Th + error.$$
(36)

With c = .03, the stepwise regression gave quite adequate curve fits with the formulas:

$\frac{\text{Sierra Madre}}{\text{In U} = (-.573 + .158 e^{-.09d})}$ $+ (.738-1.050 e^{-.03d} + .906 e^{-.06d}) \text{ In Th}$ (standard deviation of error of fit = .717);

Medicine Bow

In both equations, the regression explained about 60 percent of the scatter. Thus the equations represent reasonably good trend lines, but there is still substantial scatter (40 percent) about the trend. It should be clearly noted that these equations do not function as prediction equations giving the In U value for a particular sample as a function of the In Th and depth for that sample. Rather they establish the surface or trend about which the data scatter.

The equations at substantial depth (>154 feet or so) reduce to the relations for no leaching of:

Sierra Madre (d = ∞)
ln U =
$$-.573 + .738$$
 ln Th (39)
and
Medicine Bow (d = ∞)
ln U = $1.608 + .663$ ln Th. (40)

These equations can be manipulated to the more conventional form of the uranium to thorium ratio of:

$$\frac{\text{Sierra Madre}}{(U/\text{Th})} = e^{-.573} \text{Th}^{-.262}$$

$$= .56 \text{Th}^{-.26}$$
(41)

and

$$\frac{\text{Medicine Bow}}{(U/\text{Th})} = e^{1.608} \text{Th}^{-.337}$$
(42)

This result was somewhat surprising. The exponent on thorium is quite similar for the two areas (on the order of -.3), but the multiplier is nine times larger in the Medicine Bow area than in the Sierra Madre. It is conjectured that this difference is probably due to the different ages of the formations and some substantial associated depositional or mineralogical differences. Mineralogical analyses performed by Houston (and reported in Volume I, this report) indicate that, although the Medicine Bow deposits have several mineral phases bearing both uranium and thorium, the Sierra Madre units lack any major uranium-bearing minerals.

The relation clearly delineates the observed relationship in the assays that most of the radioactivity in the Carrico Ranch area (Sierra Madre) is due to thorium content, while the Medicine Bow areas have more uranium for the same level of thorium.

Tha amount of leaching at any depth, as stated in terms of difference in logarithms of unleached uranium and leached uranium follows the trend given by subtracting the shallow or depth-dependent relation from the unleached relation holding at depth.

Sierra Madre

log increment for leaching =
$$-.158 e^{-.09d}$$

+ (1.050 e $^{-.03d}$ -.906 e $^{-.06d}$) In Th (43)

Medicine Bow

log increment for leaching = +9.786 e^{$$-.03d$$}-8.471 e ^{$-.09d$}
+ .0947 e ^{$-.03d$} ln Th. (44)

Along the outcrop transects where the major portion of assay data used in the resource calculation was obtained, the log increment for leaching (at d=0) reduces to:

log increment for leaching = 1.315 + .0947 ln Th. (46)

Another surprising aspect of the leaching relationships was discovered in the zone between d = zero and d = 30 feet. In planning the analysis, it was more or less assumed that the leaching would be largest at d = zero and decrease along some curve with increasing depth. The formula used in the curve-fitting permits other behavior, however, if the data requires it. A careful examination of the log increment for leaching shows that for larger values of thorium, the amount of leaching increases with depth for about the first 30 feet or so and then begins to decrease steadily with increasing depth. This happens in both the Sierra Madre and in the Medicine Bow areas. Scatter plots of uranium versus depth show that this is a real behavior and not some peculiarity of the analysis procedure. The values at the surface outcrops are slightly richer on the average than those at shallow depths. However, the number of assays in this 10 to 30 foot zone is quite restricted and the main curve behavior is controlled primarily by the average surface values (d = zero) and the trend of the values between 50 feet and 150 feet.

It has been conjectured that the leaching may be strongly affected by the length of time the moisture stays in contact with the ore as it percolates downward. Surface moisture would move down rapidly at first and then slow down somewhat with increasing depth. Thus, the contact time might be less at d = zero than at d = 20 feet. However, this is pure speculation.

The leaching adjustments and subsequent tonnage correction procedures were carefully designed so that they would not be sensitive to whether this maximum leaching at 30 feet is actually present or not. The data available at the surface (d=0) and below 50 feet (d>50 feet) were quite adequate to provide satisfactory accuracy in the determination of the leaching trend. However, the sparsity of the data for 0<d<50 feet suggests that the magnitude of the maximum occurring in that interval may, in part, be related to the well known tendency of polynomial curve fits to oscillate to unrealistic extremes where data is absent. As a reasonable approximation to what is probably present, the leaching curves given in equation (43) and (44) were modified for 0<d<50 feet by replacing the curve with a straight line interpolation between the values at d=0 and at d=50 feet. The resulting modified curve was averaged over the intervals (0,100) and (100, 200) to obtain the leaching

correction used in the resource computation. This computation yielded the results shown in Table 3. Greater depths were essentially unleached, so the adjustments or corrections were small or zero.

	Depth	Interval		
Area	<u>0-100</u>		100-200	
Medicine Bows	1.406 + .0344 In Th	.1542 -	+ .0015 ln	Th
Sierra Madre	0401 + .1357 In Th		.0162 ln	Th

Table 3. Modified averaged log increment for leaching.

The general leaching adjustments proceeded as follows. The log increment for leaching was added to the logarithm of the measured uranium and the value of .165 was added to this to adjust the grade to values for the equivalent logarithm of $U_3^{0}_{8}$. The leaching correction procedure really only affected the top 150 feet of the resource so that in terms of the total deposit only a small portion was involved. However, it allowed the surface outcrop assays to become reasonable predictors of the unleached $U_3^{0}_8$ grades holding at depth.

All the assay data, as adjusted to unleached equivalent grade, then could be used to compute accumulations or thickness-averaged grades for those uranium bearing beds with exceedances of 100 ppm. These accumulations are tabled in Appendix D. Finally, these accumulated grades were kriged to produce resource estimates in terms of unleached $U_3^0 0_8$. The exact details of the kriging will be outlined in the next seciton. However, it is appropriate to discuss the tonnage correction used to convert to leached resource estimates in this section because it is controlled in part by the leaching relations.

As discussed previously, the logarithm of the unleached $U_3^{0}{}_8$ accumulations appear to behave according to lognormal probabilities. This implies that the $U_3^{0}{}_8$ will also be lognormal. Also, if B^{*} represents the

subset of the region B where exceedances of 100 ppm are encountered, then the fraction of B^* with grade exceeding some other value, say 200 ppm, can be computed from the lognormal behavior.

For example, as shown in Figure 13, let the area under the curve to the right of ln 100 be area A. This would represent the fraction of B with unleached average grade exceeding 100 ppm. The unleached average grade which would become equal to 100 ppm after leaching would be obtained from:

unleached equivalent = $\ln 100 + \frac{\log increment}{\text{for leaching}}$ (47) for any particular selected depth. This value on the horizontal axis of Figure 13 is schematically indicated by the downward arrow. Let area A^{*} be the area under the lognormal curve to the right of the vertical arrow. The two areas, A and A^{*}, can be interpreted, respectively, as the fraction of B with unleached grade greater than 100 ppm and the fraction of B^{*} with leached grade greater than 100 ppm. The lognormal curve is characterized by $\hat{\mu}$ (the middle or balance point of the curve) and $\hat{\sigma}$ (the standard deviation parameter). If these values are known, the areas A and A^{*} to area A. The basic relation is:

fraction of B [^] with leached grade>100 ppm	= tonnage correction	x	fraction of B with equivalent unleached grade>	(78)
			IUU ppm.	(40)



Figure 13. Probability distribution curve illustrating the basis for the tonnage correction.

The Basic Kriging Relation

The resource determination formula then becomes

tons Uz08 fraction of leached mineable surarea of average х х in a given mineable thickness face with depth interal surface unleached grade>100 ppm

average unleached tonnage / 11900000. grade for х exceedances of 100 ppm (49)

The fraction of the mineable surface with unleached grade>100 ppm is the area of B^* divided by the area of B. This in turn is approximated by the total number of drill holes and outcrop transects which encountered beds whose adjusted unleached equivalent grade exceeded 100 ppm, divided by the total number drill holes and transects piercing the mineable surface. For example in the Sierra Madre, only two drill holes and two outcrop transects passed through beds with unleached equivalent grade greater than or equal to 100 ppm. There were a total of 31 drill holes or transects that encountered the mineable surface. Then the fraction would be 4/31. That is 27/31 of the mineable surface does not experience any exceedances of 100 ppm unleached.

The value 11,900,000 makes the conversion from ppm to tons of resource. It is based on 11.9 cubic feet per ton, which in turn is the appropriate value for country rock with a specific gravity of 2.7.

The assumptions under which this resource formula is equivalent to kriging will now be discussed. Let $V^*(\underline{x})$ be the equivalent unleached grade of the deposit at location $\underline{x}(x_1, x_2, x_3)$. From geological considerations and from the limited data available $V^*(\underline{x})$ appears to behave as a stationary random function. Let the adjusted random function $V(\underline{x})$ be defined as

$$V(\underline{x}) = \begin{cases} V^{*}(\underline{x}), & \text{if } V^{*}(\underline{x}) \ge 100 \text{ ppm} \\ 0, & \text{otherwise.} \end{cases}$$
(50)

The resource in mathematical terms is

resource = correction ×
$$\int \int \int V(\underline{x}) d\underline{x}$$
,
Deposit (51)

where the correction is the depth dependent value which adjusts ppm to tons and makes the tonnage correction for the depth interval involved. In the present study a further modification was introduced in that the inside integral was taken as a perpendicular to the mineable surface and an accumulation was defined as

$$A(x_1, x_2) = \int V(\underline{x}) dx_3.$$

along \perp
to mineable surface (52)

Then the resource formula becomes the integral over the mineable surface, B, of A(x₁, x₂). Thus, resource = correction $\times \int_{B} \int A(x_1, x_2) dx_1 dx_2$. (53)

It was convenient to think in terms of average grade, $\overline{A}(x_1, x_2)$, and total thickness of beds with exceedances of 100 ppm unleached equivalent, $T(x_1, x_2)$. These are mathematically related as

$$\overline{A}(x_1, x_2) = A(x_1, x_2) / T(x_1, x_2).$$
(54)

Thus the resource becomes

resource = correction × (area of B) × (area of B^{*}/area of B)
× (1/area of B^{*})
$$\int_{B^*} \int T(x_1, x_2) \bar{A}(x_1, x_2) dx_1 dx_2$$
. (55)

The integration can be reduced to being over B^* because $\overline{A}(x_1, x_2) = 0$ for the rest of B.

This whole process has reduced the problem to that of estimating the average accumulation over B^* :

average accumulation =
$$\frac{1}{B^{\star}} \int A(x_1, x_2) dx_1 dx_2$$

= $\frac{1}{B^{\star}} \int f(x_1, x_2) \tilde{A}(x_1, x_2) dx_1 dx_2.$ (56)

This is precisely what kriging as discussed in Appendix A is designed to estimate. The estimate is a weighted average of \overline{TA} over the outcrop and drill hole transects where the weights are determined to minimize the estimate error as shown in Appendix A. Thus the resource estimate becomes

kriged
resource = correction₁ × (area B) × area B^{*}/area B
estimate (57A)
× (kriged estimate of accumulation over B^{*})
= correction
$$_2$$
 × area B × (kriged estimate of
accumulation over
B). (57B)

The resource can be regarded either as a correction times the kriged average over B^{\star} or as a different correction times the kridged estimate over B.

The kriged accumulations are developed in terms of $U_{3}^{0}{}_{8}^{0}$ itself, rather than $\ln U_{3}^{0}{}_{8}^{0}$. Actually, it is acceptable practice to use either approach. Kriging based on $\ln U_{3}^{0}{}_{8}^{0}$ is called lognormal kriging. However, this study was based on $U_{3}^{0}{}_{8}^{0}$ because it was believed that the kriged estimates represent averages over large volumes for this case. The small zones of influence found (certainly less than 100 feet) would indicate that it is equivalent to average a number of independent random quantities. By the central limit theorem of statistics, the average of a number of lognormal variables will be normally distributed, and not lognormal. Thus the probability behavior for the overall resource values can, in this case, be based on regular normality, even though the original input data is lognormal. Actually, the central limit theorem behavior dominates very quickly. The average of even three of four independent lognormal variable will, to a very good appproximation, behave as a normal variable.

Computation of Probable Error

As shown in the theorem A-6 in Appendix A, the variance of estimate error, for the kriged estimate over B, is

$$\sigma_{\rm B}^2 \le \frac{\sigma^2}{n} + \pi h_{\rm O}^2 (\sigma^2 - a^2) / 3B.$$
 (58)

The corresponding probable error would be

$$PE = .6745\sigma_{B}$$
 (59)

and the percentage probable error is

PE% $\stackrel{\sim}{=}$ 67.45 $\hat{\sigma}_{B}$ /(kriged estimate of acccumulation over B). (60) The probable error is interpreted as the median error due the randomness of grade and thickness as evidenced by the measured data. Thus, it is a statistical error, not a geological uncertainty factor. Judgments concerning geological uncertainty will be discussed later.

In order to apply (58) to the resource estimates in the present model, values have to be assigned to the σ^2 , h_o , and a^2 constants; the quantities n and B, (representing the number of transects or drill hole piercements of the mineable surface, and the mineable surface area of the region which is being averaged, respectively) are known from the sampling plan and the assumed geological model.

The estimate of σ_B^2 is quite insensitive to a^2 and h_o . Hence it appears reasonable to accept conservative values for these parameters and obtain a reasonable upper bound for σ_B^2 . If a^2 is set to zero, the right-hand side of (58) is made as large as it can get relative to the variation of a^2 . From the measured data, it appears quite likely that the overall value of h_o is less than 60 ft. Thus, a^2 =0 and h_o =60 ft. appear to be reasonable choices.

The value of σ^2 is important to the error estimation. In the resource model used, the accumulation, as a function of position on the mineable surface, was taken to be zero if the unleached grade was less than 100 ppm, and was assigned the measured value if the unleached grade exceeded or equaled 100 ppm. Let p be defined as the fraction of the mineable surface with unleached grade \geq 100 ppm (see eg. (49)).

Then the accumulation is a random function over the mineable surface which is zero on p-fraction of the surface and has an average value of mean measured accumulation as determined for those transects or piercements with value \geq 100 ppm. Let Acc denote this last average, and let A (x₁, x₂) be the overall random function which is zero when the accumulations drop below 100 ppm (see eq. (52)). Also let Acc² denote the average of the squared values over this same region.

As shown in eqs (49)-(57), the kriged values reported in the resource estimate may be considered as regional averages of A (x_1, x_2) . Several questions need to be answered before the probable error formulas given earlier can be applied. These are: (1) Is A (x_1, x_2) stationary? and (2) What is the mean and variance of A (x_1, x_2) ?

The accumulations without the 100 ppm cutoff are assumed to be covariance stationary after correction for leaching, with expected lagged product L(h₁, h₂), mean μ_0 and expected square s₀.

We note that:

$$\mu_{A} = E[A (x_{1}, x_{2}0] = p\mu_{0}, \qquad (61)$$

$$\sigma_A^2 = E[A^2(x_1, x_2)] = ps_0,$$
 (62)

$$E[A(x_1, x_2) A(x_1+h_1, x_2+h_2)] = p^2L(h_1, h_2).$$
(63)

These values do not vary with spatial position, so covariance stationarity is verified. It follows from the above that reasonable estimates for the mean and variance of A (x_1, x_2) are: $\hat{\mu}_A = \text{est. mean A} = p \ \overline{\text{Acc}},$ (64)

$$\hat{\sigma}_{A}^{2} = \text{est.variance A} = p \ Acc^{2} - (p \ Acc)^{2}.$$
 (65)

This last quantity is the reasonable data-derived value to

use as
$$\sigma^2$$
 in eq. (58). Thus

$$PE\% \leq 67.45 \sqrt{\{pAcc^2 - (pAcc)^2\} \{\frac{1}{n} + \pi h_0^2 / 3B\}}$$
(66)
 $pAcc$

These probable error values are listed in the resource tables.

Probable errors for intervals and overall estimates are estimated from the same formula. The area B is changed in each case to contain the mineable surface area for that region.

The combination of probable errors from several different (and assumed independent) regions requires a different formula. Let R_1 , R_2 , ..., R_n be n regions with mean values μ_1 , μ_2 , ..., μ_n and probable errors (PE)₁, (PE)₂, ..., (PE)_n. Then the square probable error of the overall average is the weighted average of the individual square probable errors.

P.E. of overall average =
$$\begin{bmatrix} n & & \\ \Sigma & \mu_{1} & (PE)^{2} \\ \frac{i=1}{n} & & \\ \frac{\Sigma & \mu_{1}}{i=1} & & \end{bmatrix}^{1/2} .$$
(67)

The Resource Computations

The resource calculations are summarized in Tables 4 to 8 for leached $U_3 O_8$. The left column gives the depth interval. The next three

columns list the area of mineable surface in each depth interval, the leaching correction as based on the value of the integral of the interval, and the tonnage correction. The fifth column summarizes the resource estimates in terms of equivalent unleached tonnage exceeding 100 ppm. The tonnage correction is multiplied times this to give the sixth column which is the final estimate of the resource endowment for $U_3 0_8$ with grade exceeding 100 ppm. This grade represents an estimate of the in-place, leached tonnage of the ore deposit.

The final column of the table gives the percent probable error as based on the conservative choices of $h_0^{=60}$ feet and $a^2=0$. The probable errors for the $U_3^{0}{}_8$ reserves in the Sierra Madre (Table 4) are unexpectedly rather large. However, an examination of the underlying data reveals the probable reason. There were only 4 of 31 transects or drill holes which encountered exceedances of 100 ppm unleached $U_3^{0}{}_8$. Among these four, three encountered relatively thin and low grade uranium concentrations, while one was substantially thicker and richer. Thus, the variance of accumulation (thickness X value) was quite substantial and this large variance produced a corresponding large probable error. Because of the small number of encounters (i.e., only four), the estimate of probable error in this case should be regarded as somewhat unreliable and used only as a general indication of magnitude of error.

Since the data was available and may be of interest at some future date, resource estimates were also made for the tons of thorium oxide (ThO₂) exceeding 100 ppm. For this case, the whole leaching adjustment

Depth Interval	Area per depth interval of mineable surface (ft. ²)	Leaching correction for ^{1n U} 3 ⁰ 8	Tonnage correction (adjusted to leached resource)	Unleached tons>100 ppm per depth interval	Resource tons>100 ppm after correction for leaching	% Probable error
0- 100	3,343,000	0.7063	0.2158	8.9	1.9	52.7
100- 200	3,360,000	0.0891	0.8457	9.0	7.6	52.7
200- 300	3,360,000	0	1.000	9.0	9.0	52.7
300- 400	3,360,000	0	1.000	9.0	9.0	52.7
400- 500	3,029,000	0	1.000	8.1	8.1	53 .5
500-1000	16,236,000	0	1.000	43.4	43.4	52.7
1000-1500	16,965,000	0	1.000	45.4	45.4	52.7
1500-2000	16,965,000	0	1.000	45.4	45.4	52.7
2000-3000	33,931,000	0	1.000	90.8	90.8	52.7
3000-4000	33,931,000	0	1.000	90.7	90.7	52.7
4000-5000	33,931,000	0	1.000	90.7	90.7	52.7
				Tota	442.0 tons	52.7%

Table 4. Summary of Uranium Resource Calculations for Sierra Madre Unit #3.

*These probable errors are unexpectedly rather large. However, an examination of the underlying data reveals the probable reason. There were only 4 of 31 transects or drill holes which encountered exceedance of 100 ppm unleached $U_3 O_8$. Among these four, three encountered relatively thin and low grade uranium concentrations, while one was substantially thicker and richer. Thus, the variance of accumulation (thickness x value) was quite substantial and this large variance produced a corresponding large probable error. Because of the small number of encounters (i.e., only four), the estimate of probable error in this case should be regarded as somewhat unreliable and used only as a general indication of magnitude of error.

Depth Interval	Area per depth interval of mineable surface (ft.2)	Leaching correction for 1nU ₃ 0 ₈	Tonnage correction (adjusted to leached resource)	Unleached tons>100 ppm per depth interval	Resource tons>100 ppm after correction for leaching	% Probable error
0- 100	903,500	1.5484	0.0673	120.0	8.1	17.3
100- 200	831,700	0.1604	0.9302	110.5	102.8	17.3
200- 300	795,600	0	1.000	105.7	105.7	17.3
300- 400	704,100	0	1.000	93.5	93.5	17.4
400- 500	633,100	0	1.000	88.1	88.1	17.6
500-1000	2,243,700	0	1.000	298.1	298.1	16.7
1000-1500	589,200	0	1.000	78.3	78.3	17.7
				Tota	774.6 tons	17.3%

Table 5. Summary of Uranium Resource Calculation for Medicine Bow Unit #1.

Depth Interval	Area per depth interval of mineable surface (ft. ²)	Leaching correction for ln U ₃ 0 ₈	Tonnage correction (adjusted to leached resource)	Unleached tons>100 oon per depth interval	Resource tons>100 ppm after correction for leaching	% Probable error
0- 100	825,900	1.5942	0.0569	109.7	6.2	17.3
100- 200	825,900	0.1624	0.9292	109.7	102.0	17.3
200- 300	859,300	0	1.000	114.2	114.2	17.3
300- 400	798,900	0	1.000	106.1	106.1	17.3
400- 500	783,700	0	1.000	104.1	104.1	17.3
500-1000	1,596,400	0	1.000	212.1	212.1	16.8
1000-1500	147,000	0	1.000	19.5	19.5	21.2
				Tota	664.2 tons	17.8%

Table 6. Summary of Uranium Resource Calculations for Medicine Bow Unit #5a.

Depth Interval	Area per depth interval of mineable surface (ft.2)	Leaching correction for InU ₃ 0 ₈	Tonnage correction (adjusted to leached resource)	Unleached tons>100 ppm per depth interval	Resource tons>100 ppm after correction for leaching	% Probable error
0- 100	702,200	1.5962	0.0509	93.3	4.7	17.4
100- 200	694,200	0.1625	0.9292	92.2	85.6	17.6
200- 300	725,400	0	1.000	96.4	96.4	17.4
300- 400	621,700	0	1.000	82.6	82.6	17.4
400- 500	286,200	0	1.000	3 8 .0	38.0	19.1
500-1000	378,600	0	1.000	50.3	50.3	18.4
				Tota	1 357.6 tons	17.9%

Table 7. Summary of Uranium Resource Calculations for Medicine Bow Unit #5b.
Depth Interval	Area per depth interval of mineable surface (ft. ²)	Leaching correction for InU ₃ 08	Tonnage correction (adjusted to leached resource)	Unleached tons>100 ppm per depth interval	Resource tons>100 ppm after correction for leaching	% Probable error
0- 100	675,600	1.5498	0.0670	89.7	6.1	17.6
100- 200	675,700	0.1605	0.9302	89.8	83.5	17.6
200- 300	675,700	0	1.000	89.8	89.8	17.6
300- 400	671,200	0	1.000	89.2	89.2	17.6
400- 500	669,000	0	1.000	88.9	88.9	17.6
500-1000	3,325,800	0	1.000	441.8	441.8	16.6
1000-1500	3,163,300	0	1.000	420.2	420.2	16.6
1500-2000	2,992,400	0	1.000	397.5	397.5	16.7
				Tota	1 1617.0 tons	17.2%

Table 8. Summary of Uranium Resource Calculations for Threemile Creek area, Medicine Bow Mountains.

and tonnage correction was unnecessary, since thorium is relatively unaffected by leaching. These somewhat smaller tables for the tonnage of ThO₂ exceeding 100 ppm are given in Tables 9 to 13.

Since there may be some interest in what was the maximum value of $U_3^{0}{}_8$ unleached equivalent values which were encountered in the drill holes where the values did not rise above 100 ppm, the maximum values encountered in these holes are summarized in Tables 14 and 15. Finally the overall resource estimates for the Deep Gulch Formation in the northwestern Sierra Madre and for the Onemile Creek area of the north-eastern Medicine Bow Mountains are tabulated in Table 16 and 17 for $U_3^{0}{}_8$ and Th 0_2 respectively.

Judgements Concerning Geological Uncertainty

Any evaluation of uranium resources is strongly dependent on a geologic understanding of the geometry of the mineralized bodies. The geostatistical resource estimate presented in this report reflects our current understanding of the structure and stratigraphy of the Onemile Creek area and the Carrico Ranch area, based on surface mapping at a scale of 1:1200 and on subsurface, drill-core data. In both areas, the mineralized units have been folded at least twice, faulted, and intruded by mafic magmas. As a consequence of this complex deformational history (and in spite of detailed mapping and reconnaissance drilling) there are still geologic uncertainties in extrapolating outcrop information into areas of poor outcrop and into the subsurface. For this report, we have evaluated what we consider to be the most reasonable geometry of the

Depth Interval	Area per Depth Interval of Mineable Surface	Resource Tons >100 ppm	% Probable Error
0- 100	3,343,000	126.6	16.0
100- 200	3,360,000	126.7	16.0
200- 300	3,360,000	126.7	16.0
300- 400	3,360,000	126.9	16.0
400- 500	3,029,000	114.2	16.0
500-1000	16,236,000	612.5	15.8
1000-1500	16,965,000	640.0	15.8
1500-2000	16,965,000	639.7	15.8
2000-3000	33,931,000	1230.0	15.8
3000-4000	33,931,000	1280.0	15.8
4000-5000	33,931,000	1280.0	15.8
	Total	6353.3 Tons	15.9%

Table 9. Summary of Thorium Resource Calculations for Sierra Madre Unit #3.

Depth Interval	Area per Depth Interval of Mineable Surface (ft. ²)	Resource Tons>100 ppm	% Probable Error
0- 100	903,500	62.6	15.2
100- 200	831,700	57.6	15.4
200- 300	795,600	55.1	15.4
300- 400	704,100	48.8	15.5
400- 500	633,100	45.9	15.5
500-1000	2,243,700	155.4	14.8
1000-1500	589,200	40.8	15.6
	Tota	466.2 tons	15.3%

Table 10. Summary of Thorium Resource Calculations for Medicine Bow Unit #1.

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Depth Interval	Area per Depth Interval of Mineable Surface (ft. ²)	Resource Tons>100 ppm	% Probable Error
0- 100	825,900	57.2	15.4
100- 200	825,900	57.2	15.4
200- 300	859,300	59.5	15.2
300- 400	798,900	55.3	15.4
400- 500	783,700	54.3	15.4
500-1000	1,596,400	110.6	14.9
1000-1500	147,000	10.2	18.7
	Total	404.3 Tons	15.8%

Table 11. Summary of Thorium Resource Calculations for Medicine Bow Unit #5a.

Depth Interval	Area per Depth Interval of Mineable Surface (ft. ²)	Resource Tons >100 ppm	% Probable Error
0- 100	702,200	48.6	15.5
100- 200	694,200	48.1	15.5
200- 300	725,400	50.2	15.5
300- 400	621,700	43.0	15.6
400- 500	286,200	19.8	16.8
500-1000	378,600	26.2	16.3
	Total	235.9 Tons	15.9%

Table 12. Summary of Thorium Resource Calculations for Medicine Bow Unit #5b.

Area per depth interval of Mineable Surface (ft. ²)	Resource tons>100 ppm	% Probable error
675,600	46.8	15.5
675,700	46.8	15.5
675,700	46.8	15.5
671,200	46.5	15.5
669,000	46.3	15.5
3,325,800	230.4	14.6
3,163,300	219.1	14.6
2,992,400	207.3	14.8
Total	890.0 tons	15.2%
	Area per depth interval of <u>Mineable Surface (ft.²)</u> 675,600 675,700 675,700 671,200 669,000 3,325,800 3,163,300 2,992,400 Total	Area per depth interval ofResource $tons>100 ppm$ Mineable Surface (ft.2) $tons>100 ppm$ 675,60046.8675,70046.8675,70046.8675,70046.5669,00046.33,325,800230.43,163,300219.12,992,400207.3Total890.0 tons

Table 13. Summary of Thorium Resource Calculations for Threemile Creek area, Medicine Bow Mountains.

Unit # Drill Core	Unit 1 Unt Th	Unit 2 Unt Th	Unit 4 Unt Th
SM-1	3.7 20	29 130 ⁽²⁵⁰⁾	18 56
SM-1A	64.0 400	35.0 26 ⁽²³⁰⁾	14 140
SM-2	no encounter	15 110 ⁽¹²⁰⁾	12.2 17 ⁽⁶⁴⁾
SM-3	21 28	36 100 ⁽²²⁰⁾	no encounter
JP-1	4.6 9	27 97	26 220
JP-2	29 220	26 150	22 20 ⁽³⁴⁾
JP-3	4.2 15	no encounter	no encounter
JP-4	42 170	no encounter	14 22

Table 14. Highest uranium and thorium values from units 1, 2, 4 from drill cores in the Sierra Madre. *Value in parentheses indicates highest spot sample.

prill Hole pritransect	1 ^U 3 ⁰ 8 ^{Th0} 2	2 U3 ⁰ 8 ^{Th0} 2	3 ^U 3 ⁰ 8 ^{Th0} 2	4 ^U 3 ⁰ 8 ^{Th0} 2	5 U3 ⁰ 8 Th02
EMB-1	C(1) C(1)	C(1) C(1)	C(1) C(1)	24.8 21.6	NE
EMB-2	NE	NE	NE	E-ND	E-ND
EMB-3	NE	NE	NE	NE	NE
EMB-4	NE	NE	NE	NE	NE
EMB-6	NE	NE	NE	E-ND	C(2,3) C(2,3)
EMB-7	NE	NE	NE	C(2) C(2)	C(2,3) C(2,3)
EMB-8	NE	NE	NE	E-ND	C(3) C(3)
EMB-9	NE	NE	NE	NE	C(3) C(3)
EMB-10	NE	NE	NE	NE	C(3) 84.2
EMB-11	NE*	NE*	NE*	NE*	NE*
MB-16	C(1) C(1)	C(1) C(1)	34.8 29.6	NE	NE
T1A	C(1) C(1)	C(1) C(1)	NE	NE	NE
T1B	C(1) C(1)	C(1) C(1)	NE	NE	NE
TIC	C(1) C(1)	C(1) C(1)	NE	NE	NE
Т2	C(1) 96.7	C(1) C(1)	20.8 92.2	14.0 51.2	NE
T3	NE	NE	NE	NE	C(3) C(3)
т4	NE	NE	NE	C(2) C(2)	NE
T 5	NE	NE	NE	C(2) C(2)	C(2,3) C(2,3)
т6	NE	NE	NE	87.6 61.8	75.8 C(3)
Т7	NE	NE	NE	NE	C(3) C(3)
т8	NE	NE	NE	C(2) C(2)	C(2,3) C(2,3)

Lithologic Units

NE - Not encountered by drill hole or transect NE*- Units encountered do not correlate with these lithologic units C(1)- Used in resource calculation; number indicates which resource geometry includes this unit: 1- Unit 1, Onemile Creek area 2- Unit 5a, Onemile Creek area 3- Unit 5b, Onemile Creek area 03⁰8 and ThO₂ are reported in ppm and maximum ThO₂ may not be from same sample as maximum U₃O₈.

Table 15. Maximum uranium and thorium values <100 ppm encountered in Magnolia Formation lithologic units, Medicine Bow Mountains.

	Deep Gulch Northweste Madre Mou	Formation rn Sierra ntains	Magnolia 1 Northea Medicine Bow	Formation astern v Mountains
Depth Interval (feet)	Tons U ₃ 0 ₈ >100 ppm	Probable Error %	Tons U ₃ 0 ₈ >100 ppm	Probable Error %
0- 100	1.9	52.7*	25.1	16.6
100- 200	7.6	52.7	378.9	16.7
200- 300	9.0	52,7	406.0	16.7
300- 400	9.0	52.7	371.4	16.7
400- 500	8.1	53.5	319.1	16.7
500-1000	43.4	52.7	1002.2	16.5
1000-1500	45.4	52.7	518.0	16.6
1500-2000	45.4	52.7	397.5	16.7
2000-3000	90.8	52.7		
3000-4000	90.7	52.7		
4000-5000	90.7	52.7		
Total	442.0 tons	52.7%	3418.2 tons	16.7%
Average grade for U ₃ 0 ₈ exceeding 100 ppm	130.	2 ppm	305	.7 ppm
Average total thickness of beds with U ₃ 0 ₈ exceeding 100 ppm	1.	5 feet	6	.l feet
Thickness per bed	0.	6 feet	0	.95 feet
Map area	12 s	q. miles	2	.5 sq. miles

Table 16. Resource summary for tons U308 with grade exceeding 100 ppm for the listed areas, together with other basic statistics.

*See footnote on Table 4.

<u></u>	Deep Gulch Formation		Magnolia Fo	ormation
	Northweste Madre Mou	rn Sierra ntains	Northea Medicine Boy	∍stern Mountains
Depth Interval (feet)	Tons Th02 >100 ppm	Probable Error %	Tons Th0 >100 ppm	Probable Error %
0- 100	126.6	16.0	215.2	14.8
100- 200	126.7	16.0	209.6	14.8
200- 300	126.7	16.0	211.7	14.8
300- 400	126.9	16.0	193.6	14.8
400- 500	114.2	16.0	166.4	14.8
500-1000	612.5	15.8	522.5	14.5
1000-1500	640.0	15.8	270.1	14.6
1500-2000	639.7	15.8	207.3	14.8
2000-3000	1280.0	15.8		
3000-4000	1280.0	15.8		
4000-5000	1280.0	15.8		
Total	6353.3 tons	15.9%	1996.4 tons	14.7%
Average grade for Th0 ₂ exceeding 100 ppm	265.	5 ppm	284	+.5 ppm
Average total thickness of beds with ThO, exceedin	α .			
100 ppm ²	<i>э</i>	.5 feet	-	3.5 feet
Thickness per bed	0	.6 feet	C).8 feet
Map area	12	mi∠	2	2.5 mi ²

Table 17. Resource summary for tons ThO, with grade exceeding 100 ppm for the listed areas, together with other basic statistics.

mineralized units. However, in this section it is fruitful to examine other feasible geologic interpretations which could result in either larger uranium reserve estimates (terms "optimistic" interpretations) or smaller reserves estimates ("pessimistic" interpretations).

For the Medicine Bow areas, there are three major uncertainties in interpreting the subsurface extent of mineralized units in the Magnolia Formation. The first two, the plunge of the major syncline and the shape and extent of the mafic intrusive bodies, involve outcropping Magnolia Formation of both the Onemile Creek and the Threemile Creek areas. The third deals with the possibility of subcropping Magnolia Formation unconformably underlying the Cascade Quartzite east of Onemile Creek.

The major structure in the Onemile Creek area is a faulted and intruded, tight to isoclinal overturned syncline. Figure 14 shows two possible plunges for this syncline. Figure 14a, an inclined syncline, is consistent with the macroscopic pattern of the Magnolia Formation which can be traced through the Threemile Creek area over a distance of 6 miles to the southwest, into an area of open, upright folds with subhorizontal fold axes. Figure 14b, a reclined syncline, is suggested by mesoscopic fold configurations in the Onemile area. We have used the inclined fold geometry of 14a in our resource estimate because it explains regional relationships better and because we believe the mesoscopic fold structures are related to a superposed fold system which is well documented by stereonet plots of bedding foliations and lineations. Nevertheless, if the reclined fold plunge of 14b were used, the resources estimate would change. Figure 15 and 16 show schematic east-west cross-sections of part of the Onemile syncline using both interpretations. With the reclined



Figure 14. Schematic diagrams of possibe styles of folding in the Onemile Creek area: a) inclined, b) reclined. Heavy dashed line with arrow shows plunge of fold.

b.



a. Inclined fold with mafic sill.



b. Reclined fold with mafic sill.





a. Inclined fold with vertical dike.



b. Reclined fold with vertical dike.

Figure 16. Possible fold geometries with mafic bodies modelled as vertical dikes.

syncline 14b, mineralized zones would extend to greater depths (averaging 2000 feet instead of 1000 feet) and the reserve figure would be increased by a factor of about 2, if extended to the required depth of 5000 feet. Projection of the Threemile Creek geometry as an inclined syncline to 5000 feet was considered unsupported by our subsurface information but this projection would also double the reserve figure.

The problem of the shape of mafic intrusive bodies is also illustrated in Figures 15 and 16. We believe that the bodies are mainly sill-like and that they were intruded along bedding planes and faults which parallel the axial plane of the fold. However, the bodies could either thicken or thin with depth or remain fairly uniform in thickness. Figure 15, which represents our favored interpretation of sill-like shapes, gives a reasonably optimistic uranium resource estimate, Figure 16, showing geologically unreasonable vertical mafic dikes, would give a pessimistic estimate. If the latter were used, the resource number could be decreased by a factor of .5.

The third problem, of the possibility of subcropping Magnolia east of Onemile Creek, is difficult to evaluate and we have neglected such a possibility in our resource estimate. However, Figure 3 (map) shows the hinge of the major syncline to be offset left laterally into this area so there may be mineralized Magnolia in the subcrop. If so, it is conceivable that the resource estimate should be increased by a factor of 1.5 or 2.

Table 17 summarizes what we consider to be the extremes of optimistic versus pessimistic geologic interpretations in the Medicine Bow area and how they would affect the present resource number (R) reported earlier.

Possible optimistic geometry	 <u> </u>
Reclined folds	 2R
Buried Magnolia Formation	 2R
Most optimistic	 4R
Present geometry used	
Inclined folds, no buried	
Magnolia Formation, mafic sills	 R
Most likely	 R
Most pessimistic geometry	
Vertical mafic dikes	 .5R
Most pessimistic	 -5R

TABLE 18

We believe our present interpretation is geologically most reasonable but other geologic interpretations could increase the estimate by a factor up to 4 times or decrease it by about one-half.

For the Sierra Madre area, geologic uncertainties in interpreting the structure of the Deep Gulch Formation of the Carrico Ranch area involve the subsurface projection of the unit. The unit maintains a fairly uniform overturned dip of about 50 degrees for a lateral distance of at least four miles and drill data indicate these dips remain uniform in the subsurface at least to depths of 500 - 1000 feet. Therefore, we have projected it farther, to depths of 5000 feet, in our reserve estimate.

However, the overturned beds are part of a large overturned reclined syncline, plunging west, which has only been partly defined; we have not found the equivalent beds in the upright limb of the syncline on the surface and we believe there are large reverse faults parallel to the

axial planes of the folds. As a consequence, it is possible that the mineralized unit is truncated at levels shallower than 5000 feet, (Figure 17B), decreasing the reserve estimate, or is repeated by folding, (Figure 17A), increasing the estimate. Figure 17 shows these two possibilities plus the interpretation used in our resource estimate (17C). The pessimistic interpretation could decrease the estimate by a factor of .2; the optimistic interpretation could increase the estimate by a factor of 2 or 3. The present, optimistic and pessimistic estimations for the Sierra Madre are summarized in Table 19.

T	A	В	L	Ε	1	9
		_	_	~		~

Optimistic	Present	Pessimistic
Repeated Folding-2 or 3R	Continuous Dip-R	Reverse Faulting2R
Most optimistic-2R to 3R	Most likely-R	Most Pessimistic2R

A quantitative statistical version of this geological uncertainty, as based on a careful consideration of the factors previously outlined is shown in Table 20.

Geologists Subjective Probability			
Actual Resource	Sierra Madre Area	Medicine Bow Area	
R/2	.15	.05	
R	.75	. 50	
2R	.05	.25	
3R		20	
Expected Actual			
Resource	1.075R	1.625R	

Table 20. Estimated (subjective) probabilities the actual resource is less or more than that derived from the geostatistical analysis.



Figure 17. Optimistic (A), pessimistic (B) and favored (C) interpretations of the subsurface extent of the Deep Gulch Formation in the Northwest Sierra Madre. 1= basement gneiss; 200 = Deep Gulch Formation; 2=quartzites and metavolcanic rocks of the Phantom Lake metamorphic Suite. This may be interpreted in words as suggesting that geological judgment gives very little chance for much more resource being found in the Sierra Madre, but there may be as much as 62 percent more tonnage than estimated in the Medicine Bow Mountains. This all is, of course, very speculative but it does provide some measure of the geological uncertainties involved in the interpretations.

SUMMARY AND CONCLUSIONS

- The uranium endowment in Precambrian pebble conglomerate metasediments in the Sierra Madre and Medicine Bow Mountains of southeastern Wyoming was determined through an investigation which carefully coordinated geology with mining geostatistics.
- 2. The resource assessment consisted of four phases of activity. These were (a) a detailed geological study of the three-dimensional geometry of the uranium-bearing rocks, (b) the collection of samples from outcrop transects and drill core according to planned systematic geostatistical procedures, (c) the transformation of the assay values to unleached equivalents, the development of resource estimates by kriging, and the reverse transformation to leached uranium endowment, and (d) the integrated geological and statistical interpretation of these results to produce final resource estimates and error predictions.
- 3. Leaching was carefully studied so that the outcrop assay data could be converted to unleached equivalent U_{308}^{0} content and then be used to predict the uranium endowment at depth where little data was available. Leaching was found to be negligible at depths greater than 154 feet. The amount of leaching in outcrop samples was found to be somewhat less than that at 50 feet or so.
- 4. The geostatistical methodology used in the assessment is outlined in detail. The only trend found to be significant in the deposits was that due to leaching. This nonstationarity was removed by transformation to equivalent unleached U₃0₈. The resulting

stationary regionalized variable was analyzed by a type of optimal weighed averaging called kriging. This produced estimates of the average accumulation over the test area and predictions of the probable error of these averages. The sampling was so designed that the kriging procedure reduced to ordinary arithmetic averaging. Upper bounds to the estimate error was determined by the kriging mathematics. Derivations of the mathematical formulas used are given in Appendix A.

- 5. As an interesting additional resource assessment, the endowment of thorium for exceedances of 100 ppm was also calculated for the study areas. The same geostatistical procedures were used, except that the leaching adjustment and reverse transformation was unnecessary.
- 6. The uranium endowment was computed as 442 tons \pm 53% for the Deep Gulch Formation in the Sierra Madre, and as 3,418 tons \pm 17% for the Magnolia Formation of the Medicine Bow Mountains. The corresponding thorium endowment was 6,353 tons \pm 16% for the Sierra Madre and 1,996 tons \pm 15% for the Medicine Bow Mountains. The errors stated here are probable errors. The actual error has a probability of 50% of being larger than this and 50% of being smaller. A 90% confidence interval would be 2.96 times this probable error.
- 7. The geological model used in the analysis involved subjective interpretations of the various sources of geological information. In general, the interpretations made were chosen to be slightly

conservative. A careful analysis of the amount the resource might change under various alternative interpretations is outlined. The basic conclusions are presented in Tables 18, 19, and 20. In the Medicine Bows, under the most pessimistic interpretation the resource could be about half the value calculated in the current investigation and under the most optimistic interpretation, it might be four times larger than that calculated. Similarly in the Sierra Madre, the most pessimistic interpretation would yield a reduction by 80% of the current reserve estimation, and the most optimistic version would increase the estimation up to a factor of 3.

8. The relations developed from the study of leaching have significant bearing on various geological questions concerning the two areas. The substantial difference between the leaching relations suggest that mineralogical differences, age differences, depositional history, or other factors may distinguish the two areas.

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APPENDIX A

Mathematical Derivations

APPENDIX - DERIVATIONS

Definition A-1

A radial, transitive variogram with elliptical zone of influence is defined as

$$\gamma(h_1, h_2) = \sigma^2$$
, for $h_1^2 + h_2^2 > h_0^2$ (0) (A-1)

and

$$\begin{split} \gamma(h_1, h_2) &= a^2 \{1 - \exp[-(h_1^2 + h_2^2)/2 \ s^2(\theta)] \} \\ &+ (\sigma^2 - a^2) \sqrt{h_1^2 + h_2^2} / h_0(\theta), \end{split} \tag{A-2} \end{split}$$
 for $h_1^2 + h_1^2 \le h_0^2(\theta),$

where

$$\theta = \arctan \left(\frac{h_2}{h_1} \right)$$
 (A-3)

$$s^{2}(\theta) = A^{2}B^{2}/[A^{2} \sin^{2}(\theta - \psi) + B^{2} \cos^{2}(\theta - \psi)]$$
 (A-4)

$$h_{o}^{2}(\theta) = a^{2}b^{2}/[a^{2}\sin^{2}(\theta-\phi) + b^{2}\cos^{2}(\theta-\phi)]$$
 (A-5)

and $s(\theta)$ is small compared with the scale of measurement of h_1 , and h_2 . Both $s(\theta)$ and $h_0(\theta)$ define ellipses with long axes in the ψ and ϕ angular directions in (h_1, h_2) space.

The covariance function corresponding to this variogram is zero for $h_1^2 + h_2^2 > h_0^2$ (0) and

$$C(h_{1}, h_{2}) = a^{2} \exp[-(h_{1}^{2} + h_{2}^{2})/2s^{2}(\theta)] + (\sigma^{2} - a^{2}) [1 - \sqrt{h_{1}^{2} + h_{2}^{2}}/h_{0}(\theta)]$$
(A-6)

for
$$h_1^2 + h_2^2 \le h_0^2(\theta)$$
.

Definition A-2

Let V(x, y) be some resource variable of economic interest at location (x, y). Let B specify some area within which the average value of V(x, y), denoted by \overline{V}_{B} , is of importance.

Stated in formulas

$$\overline{V}_{B} = (1/B) f_{B} f V(x, y) dx dy$$
 (A-7)

where B is also interpreted as the area of B where that is appropriate. The expression, V (x, y), will be considered a stationary random function with variogram $\gamma(h_1, h_2)$, covariance C(h_1, h_2), and mean μ .

Theorem A-3

The theoretical mean of \overline{V}_{B} is given by

$$\sigma_{B}^{2} = \text{Variance } [\overline{V}_{B}] = (1/B)^{2} f_{B} f_{B} f C(x-x', y-y') dx dy dx' dy'.$$
(A-8)

Proof

$$E[\overline{V}_{B}] = E[(1/B) f_{B}f V(x, y) dx dy]$$

= (1/B) f_{B}f \mu dx dy = \mu. (A-9)

Variance $[\overline{V}_B] = E[\{(1/B) f_B f V(x, y) dx dy - \mu\}^2]$

$$= E[(1/B)^{2} f_{B} f_{B} f \{V(x, y) - \mu\} \{V(x', y') - \mu\} dx dy dx' dy']$$

$$= (1/B)^{2} \int_{B} \int_{B} \int_{B} C(x-x', y-y') dx dy dx' dy'.$$
 (A-10)

Definition A-4

Suppose that the value of V(x, y) is known by sampling at the points $(x_1, y_1), (x_2, y_2), \ldots, (x_n, Y_n)$. A reasonable estimate $\hat{\overline{V}}_B$ of the quantity \overline{V}_B is provided by a linear combination of the sample values

$$\hat{\overline{V}}_{B} = \sum_{i=1}^{n} a_{i} V(x_{i}, y_{i}). \qquad (A-11)$$

It seems reasonable to require that $\hat{\overline{V}}_B$ be an unbiased estimate. This condition implies that

$$\sum_{i=1}^{n} a_i = 1.0$$
 (A-12)

because

$$\mu = E[\hat{\overline{V}}_B] = \prod_{i=1}^{n} a_i E[V(x_i, y_i)] = \prod_{i=1}^{n} a_i \mu. \quad (A-13)$$

Theorem A-5 (David, 1977; Journel and Huljbregts, 1978)

The constants \hat{a}_i ; i= 1, 2, ..., n, which minimize the estimation error variance, σ_E^2 , defined by

$$\sigma_{\rm E}^2 = {\rm E}[(\hat{\overline{V}}_{\rm B} - \overline{V}_{\rm B})^2], \qquad (A-14)$$

subject to the side condition

$$\sum_{i=1}^{n} \hat{a}_{i} = 1.0$$
 (A-15)

are the solution to the matrix equation

$$\begin{bmatrix} c_{11} & c_{12} & c_{13} & \cdots & c_{1n} & 1 \\ c_{21} & c_{22} & c_{23} & \cdots & c_{2n} & 1 \\ c_{31} & c_{32} & c_{33} & \cdots & c_{3n} & 1 \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ c_{n1} & c_{n2} & c_{n3} & \cdots & c_{nn} & 1 \\ 1 & 1 & 1 & \cdots & 1 & 0 \end{bmatrix} \times \begin{bmatrix} \hat{a}_{1} \\ \hat{a}_{2} \\ \hat{a}_{3} \\ \vdots \\ \hat{a}_{3} \\ \vdots \\ \hat{a}_{3} \\ \vdots \\ \vdots \\ \hat{a}_{n} \\ \hat{u} \end{bmatrix} = \begin{bmatrix} c_{B1} \\ c_{B2} \\ c_{B3} \\ \vdots \\ \vdots \\ \vdots \\ \hat{a}_{n} \\ \hat{u} \end{bmatrix}$$
(A-16)

where

$$C_{ij} = C(x_i - x_j, y_i - y_j)$$
 (A-17)

and

$$C_{Bi} = (1/B) \int_{B} \int C(x - x_{i}, y - y_{i}) dx dy$$
 (A-18)

An estimate of the estimation error variance is given by

$$\hat{\sigma}_{E}^{2} = C_{BB} - \hat{\Sigma}_{i} \hat{a}_{i} C_{Bi} - \hat{u} \qquad (A-19)$$

where

$$c_{BB} = \sigma_B^2 \tag{A-20}$$

defined in (A-3).

Proof

By the method of Lagrangian multipliers, \hat{a}_i , will be the result of minimizing Q where

$$Q = \sigma_{E}^{2} + 2u(\sum_{i=1}^{n} a_{i} - 1.0)$$
 (A-21)

with the added condition that

$$\sum_{i=1}^{n} a_{i} = 1.0.$$
 (A-22)

Now

$$Q = E[\{i_{j=1}^{n} a_{j} \forall (x_{i}, y_{j}) - (1/B) f_{B} f \forall (x, y) dx dy\}^{2}] + 2u(i_{j=1}^{n} a_{j} - 1.0)$$

$$= E[\{i_{j=1}^{n} a_{j} < \forall (x_{i}, y_{j}) - \mu > - (1/B f_{B} f < \forall (x, y) - \mu > dx dy)^{2}] + 2u(i_{j=1}^{n} a_{j} < 1.0)$$

$$= i_{j=1}^{n} j_{j=1}^{n} a_{i}a_{j}c_{ij} - 2 i_{j=1}^{n} a_{j}c_{B} + c_{BB} + 2u(i_{j=1}^{n} a_{j} - 1.0). \qquad (A-23)$$

Consequently

$$\frac{\partial Q}{\partial a_k} = 2 \sum_{i=1}^n a_i C_{ki} - 2C_{Bk} + 2u.$$
 (A-24)

If \hat{a}_i and \hat{u}_i are the values which make $\partial Q/\partial a_k = 0$, then

$$\sum_{i=1}^{n} C_{ki} \hat{a}_{j} + \hat{u} = C_{Bk}$$
 (A-25)

for K = 1, 2, ..., n. This system of simultaneous equations corresponds to the matrix equation stated in the theorem. The value of Q when \hat{a}_i and \hat{u} are substituted into the formula gives a reasonable estimate of σ_E^2 as

$$\hat{\sigma}_{E}^{2} = \sum_{i=1}^{n} \sum_{j=1}^{n} \hat{a}_{i} \hat{a}_{j} \hat{c}_{ij} - 2\sum_{i=1}^{n} \hat{a}_{i} \hat{c}_{Bi} + \hat{c}_{BB}. \qquad (A-26)$$

This formula can be simplified by multiplying both sides of eq. (A-25) by \hat{a}_k and summing over k=1, 2, ..., n. This gives

$$k^{\Sigma}_{21} i^{\Sigma}_{k} i^{a}_{i} i^{a}_{k} + u^{C}_{k} i^{a}_{j} i^{a}_{k} = k^{\Sigma}_{k} i^{a}_{k} k^{C}_{Bk}.$$
(A-27)

Since $\sum_{k=1}^{n} a_{k} = 1.0$, the previous equation can be substituted into eq. (A-26) to yield

$$\hat{\sigma}_{E}^{2} = C_{BB} - \hat{\Sigma}_{I} \hat{a}_{I} C_{BI} - \hat{u}.$$
 (A-28)

Theorem A-6

Suppose that

~

$$C_{ij} = \{ \begin{array}{c} \sigma^2, & \text{if } i=j \\ \sigma, & \text{if } i\neq j \end{array}$$
 (A-29)

and that the indices i = 1, 2, ..., n can be divided into two sets, $S_1 = \{i; 1 \le i \le m\}$ and $S_2 = \{i; m < i \le n\}$ such that

$$C_{Bi} \neq o$$
, if $i \in S_1$ (A-30)

$$C_{Bi} = 0$$
, if i εS_2 (A-31)

where the symbol " ϵ " should be read as "belongs to". That is samples more than a zone of influence away have subscripts in S₂, while those within a zone of influence of the block being estimated will have subscripts in S₂. Under these assumptions, the solution to the martix equation in A-5

is

$$\hat{a}_{i} = \begin{cases} (1/n) + C_{Bi}/\sigma^{2} - \frac{m}{k^{\Sigma}} C_{Bk}/n\sigma^{2}, & \text{if } i \in S_{1} \\ (1/n) - \frac{m}{k^{\Sigma}} C_{Bk}/n\sigma^{2} , & \text{if } i \in S_{2} \end{cases}$$
(A-32)

$$\hat{u} = (1/n) \sum_{k=1}^{m} c_{Bk} - \sigma^2/n$$
 (A-33)

and

$$\sigma_{\rm E}^2 = \sigma^2 / n + c_{\rm BB} - (2/n) \sum_{k=1}^{m} c_{\rm Bk} - \sum_{k=1}^{m} c_{\rm Bk}^2 / \sigma^2 + (\sum_{k=1}^{m} c_{\rm Bk})^2 / n \sigma^2.$$
 (A-34)

Proof

The inverse of



The theorem then follows from theorem A-5.

Theorem A-7

For the variogram in Definition (A-1), assuming $s(\theta)$ is small enough so that the exponential can be ignored,

$$0 \le C_{B1} \le \pi ab (\sigma^2 - a^2)/3B;$$
 (A-35)

$$c_{BB} < \pi ab (\sigma^2 - a^2)/3B.$$
 (A-36)

An upper bound for $\hat{\sigma}_{\rm E}^2$, providing $C_{\rm B}^{}/\sigma^2$ is negligible, is

$$\hat{\sigma}_{\rm E}^2 < (\sigma^2/n) + \pi ab(\sigma^2 - a^2)/3B.$$
 (A-37)

Proof

If the elliptical base for the variogram is entirely enclosed within B, then

$$\int_{B} \int C(x - x', y - y') dx dy = \pi ab(\sigma^{2} - a^{2})/3.$$
 (A-38)

The rest of the relations follow from theorem A-6.

is
Appendix B

Detailed Tabulations of Deposit Geometry

Sierra Madre, Unit #3

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	0-5000	48375	80600.		191692	53095	52573	135450	56250	25726	105200	86061	161564	1120	122277	33875		120176	944525	120236	92226	165738	145473	114200		
	001 000	175 36	17 80		ig2 12	6 56(11 82	50 9	50 16	'26 2 4	00	61 15	i64 8	50 16	EI 11:	375 58		11 921	525 15	36 8	9861	738 15	4	500 I 4		
	3000-4	36483	17009		12316	9530	11525	9354	16562	24257	3052	15860	8615	16317	1322	58338		11201	1944	8202	9757	19657	4451	14142		
	2000-3000	3648375	1700908	•	1231692	9 23095	1152573	935450	1656250	2425726	305200	1586061	861564	1631750	1322277	5833875		1120176	1944525	820236	975798	1965738	445473	1414200		
	. ft.) 1500-2000	1824187	840454		615804	476547	576286	467725	828125	1212863	152600	793030	430782	815875	1322277	2916937		560088	972262	410118	48784	982869	222736	207100		
SUMMARY OF AREAS PER DEPTH INTERVAL FOR SIERRA MADRE	1000-1500	1824187	850454		615804	476547	576286	467725	828125	1212863	152600	793030	430782	815875	661138	2916937		560088	972262	410118	487899	983869	222736	707100		
	<u>500 -1000</u>	1094512	850454		615804	476547	576286	467725	828125	1212863	152600	793030	430782	815875	861139	2916937		560088	972262	410118	487899	982869	222736	707100		
	400 - 500	0	170085	,	123165	95306	115322	93545	165625	242598	30525	158618	86163	163187	132232	583406		112014	194459	81983	97583	982869	44549	141425		
	300 -400	331775	1 70085		123165	95306	115322	93545	165625	242598	30525	158618	86163	163187	132232	583406		112014	194459	81983	97583	196581	64549	141425		
	200 300	331775	170085		123165	95306	115322	93545	165625	242598	30525	158618	86163	163187	132232	583406		112014	194459	81983	97583	196581	64544	141425		
	100 - 200	331775	170085		123165	95306	115322	93545	165625	242598	30525	158618	86163	163187	132232	583406		112014	194459	81983	97583	196581	44549	141425		
	23015 feet	282523	104708	:	107744	104739	100695	104839	130625	342428	26972	150625	119730	163125	152073	552875		146616	193737	103664	11422	944691	44549	127130		
	<u>ngth = .</u> V. El	7685	7670	_	2/11	7870	7883	7957	7855	7762	7805	7821	8003	8041	7987	7948	_	2960	7849	7197	7167	7962	8060	7995		
: : : : : :	Segment	Carrico Ridge #1	r: Inferred Geometry	A, Between Carrico Ridge #1 and #2	Inferred Geometry B, Between Corrico	Carrico Ridge	#4 Inferred Geometry	Between Carrico Ridge #2 and #3 Carrico Ridge	#3 Inferred Geometry	Between Carrico Ridge #3 and Fault Deep Gulch #5	Deep Gulch #4	Deep Gulch #3A	Deep Gulch #38	Inferred Geometry	Deep Gulch #1	Inferred Geometry	Between Deep Gulch #1 and Manning Ridge #1	Manning Ridge #1	Inferred Geometry	Between Manning <u>Ridge #1 and #2</u> Manning Ridge #2A	Manning Ridge #28	Inferred Geometry	Between Manning <u>Ridge #2 and #3</u> Manning Ridge #3	Inferred Geometry	Between Manning Ridqe #3 and Fault	

Tabie B-i / OF AREAS PER DEPTH INTERVAL FOR SIERR



Figure B-1





Figure B-3



Sierra Madre Unit # 3 Figure B-4



Figure B-5



Figure B-6







Figure B-9



Sierra Madre Unit #3

Figure B-10





Sierra Madre Unit #3 Figure B-11

SEGMENT	AVE.	-			200-400		E00-1000	1000-1500
NUMBER	Eact Limb	0-100	100-200		300-400	400-500	. 500-1000	1000-1500
	8850	43750	43750	43750	56250	71320	20350	
2	8770	64500	64500	64500	64500	64500	191350	
2	8710	89250	89250	89250	89250	144375	212250	
у Ц	8700	95625	95625	95625	95625	147250	2,22,00	
5	8640	42500	42500	42500	42500	42500	213900	5625
6	8600	63000	63000	63000	63000	63000	107250	45150
° 7	8420	60000	60000	60000	60000	60000	68000	
, 8	8500	70000	70000	70000	87500	26250		
9	8535	78000	78000	78000	78000	40000	43750	
Unit 5a:	Eastern	Syncline, S	trike Length	= 1475 feet				
1	8420	52500	52500	52500	52500	37365		
2	8450	25000	25000	25000	26200			
3	8480	54375	54375	87812				
4	8510.	39375	39375	39375	39375	39375	303750	46250
5	8510	48000	48000	48000	48000	48000	435840	49890
(Unit 5a	totals inc	clude both (east limb and	eastern svi	ncline portio	ons)	· · · · ·	
Total are	a	005075	005075	050010	700700		1 For LLO	
for inter	vals	8258/5	825875	859312	/98/00	/83935	1596440	146915
Cumulativ	е агеа	8258/5	1651/50	2511062	3309762	4093697	5690137	5837052
Unit 5b:	East Lim	b, Strike L	ength = 3100	feet				
ł	8800	36000	36000	36000	12750			
2	8825	38750	38750	38750	46500			
3	8760	52000	52000	52000	52000	52000	17500	
4	8707	78750	78750	78750	78750	28500		
5	8670	58750	58750	58750	38750			
6	8640	26000	26000	26000	26000	33250	90250	
7	8530	102000	105000	150000	180000			
8	8500	89250	78750	57750				
9	8500	25250	25250	34500				
<u>Unit 56:</u>	Eastern	Syncline, S	trike Length	= 1620				
1	8660	27500	25900	24000	22385	16250	52650	
2	8595	60000	60000	60000	60000	60000	152500	
3	8555	25000	25000	27400	27400	27400	31620	
4	8530	36000	36000	36000	36000	36000	27600	
5	8510	32750	32750	39300	39300	32725	6507	
ъ 	0590		15312	6250	1875			
(Unit 5b Total are	totals ind	clude both	east limb and	d eastern sy	ncline portio	on)		
for inter	vals	702170	694212	725450	621710	286125	378627	
Cumulativ	e area	702170	1396380	2121830	2743540	3029665	3408292	

Table B-2 SUMMARY OF AREAS PER DEPTH INTERVAL FOR MEDICINE BOW Area per depth interval (sq. ft.)

SEGMENT NUMBER	AVE. EL.	0-100	100-200	200-300	300-400	400-500	500-1000	1000-1500	1500-2000
Unit 1:	West Lim	b, Strike	Length = 29	75					
1	8700	94375	56790	15900					
2	8600	57000	60125	62405	64920	67375	156740	12145	
3	8660	56170	56170	71750	45920	51250	189000		
4	8620	91875	91875	91875	88200	82232	323415		
5	8580	75600	73375	60480	51300	47300	125850		
Unit 1:	Southern	Limb, Str	ike Length	= 3430					
1	9250	78750	78750	78750	67500	58500	188175		
2	9230	87500	87500	87500	75000	67500	275000	162500	
3	9260	70000	70000	70000	60000	52000	178125	53200	
4	9215	51000	51000	51000	51000	51000	90250		
5	9205	30625	30625	30625	31500	17500	13125		
6	9200	37500	37500	37500	30000	30000	78125		
7	9150	20000	20000	20000	20800	16000	77350		
8	9120	20400	20400	20400	20400	21250	90100	38400	
9	9040	60000	60000	60000	60000	60000	262500	156250	
10	8985	37500	37500	37500	37500	41250	196875	166775	
Unit 1:	Normal L	imb, Strik	e Length =	<u>575</u>					
1	9190	4000							
2	9180	17500							
3	9170	13750							
(Unit 1 Total au	totals in	clude the	west limb,	southern li	mb, and nor	mal limb po	ortions)		
for inte	ervals	903545	831610	795685	704040	663160	2243630	589270	· · · · · · · · · · · · · · · · · · ·
Cumulati	ive area	903545	1735155	2530840	3234880	3898040	6141670	6730940	
Three Mi	le Creek:	Strike L	ength = 602	5					
1	9280	123750	123750	123750	119350	117150	566500	518415	508100
2	9360	121000	121000	121000	121000	121000	605000	577730	600220
3	9390	109200	109200	109200	109200	109200	546000	573200	52 9 300
4	9360	128700	128700	128700	128700	128700	643500	597575	539925
5	9400	93600	93600	93600	93600	93600	468000	434600	385400
6	3980	99450	99450	99450	99450	99450	497250	461760	429490
Total ar	ea ervals	675650	675650	675650	671250	669050	3325750	3163280	2992435
Cumulati	ive area	675650	1351300	2026950	2698200	3367250	6693000	9856280	12848715

Table B-2 (continued) SUMMARY OF AREAS PER DEPTH INTERVAL FOR MEDICINE BOW Area per depth interval (sq. ft.)









Figure B-13. Structure contours on top of mineable Unit 1, overturned southern limb of Onemile Creek syncline, Onemile Creek area, Medicine Bow Mountains.



Explanation as on Unit 1, overturned west limb Contour interval 200 feet

> Figure B-14. Structure contours on top of principal radioactive unit in Threemile Creek area, Medicine Bow Mountains.

EXPLANATION FOR STRUCTURE CONTOUR MAPS



area, Medicine Bow Mtns.



Structure contours on top of mineable unit 5b, east limb of Onemile Creek Syncline, Onemile Creek area. Explanation as on sheet for eastern syncline.



Figure B-16



Structure contours on top of mineable unit 5a, east limb of Onemile Creek Syncline, Onemile Creek area. Explanation as on sheet for eastern syncline.

T 18N R78W

Sec. 6 Sec. 5 Sec. 7 Sec. 8

Appendix C

Graphical Presentation of Placement and True Thickness of Ore Beds in the Outcrop Transects and the Drill Holes.

Sierra Madre Unit #3

	Figure C-l	۲ Transect #1, #2, #3	age 128
	C-2	Transect #4, #5, #6, #7	129
	C-3	Transect #8, #9, #10, #11	130
	C-4	Transect #12, #13, #14	131
	C-5	Transect #15, #16, #17	132
	C-6	Transect #18, #19, #20	133
	C-7	Transect #21A, #21B, #22A	134
	C-8	Transect #22B, #23, #24	135
	C-9	Core SM-1, SM-2, JP-1	136
	C-10	Core JP-2, JP-4	137
Med	licine E	Bows	
	C-11	Transects #TIA, #TIB, #TIC	138
	C-12	Transects #T2	139
	C-13	Transects #T3, #T4	140
	C-14	Transect #T5	141
	C-15	Transect #T6	142
	C-16	Transect #T7	143
	C-17	Transect #T8	144
	C-18	Core, EMB-1	145
	C-19	Core, EMB-6	146
	C-20	Core, EMB-7	147
	C-21	Core, EMB-8	148
	C-22	Core, EMB-9, EMB-10	149
	C-23	Core, MB-16	150
	C-24	Core, EMB-11	51







Figure C-2. Thickness and U, Th values of Unit 3, Deep Gulch Conglomerate from transects 4, 5, 6 and 7, Carrico Ranch, northwest Sierra Madre. ND = NO DATA AVAILABLE



Figure C-3. Thickness and U,Th values of Unit 3, Deep Gulch Conglomerate from transects 8, 9, 10 and 11, Carrico Ranch, northwest Sierra Madre.



Figure C-4. Thickness and U,Th values of Unit 3, Deep Gulch Conglomerate from transects 12, 13 and 14, Carrico Ranch and Deep Gulch, northwest Sierra Madre. ND = NO DATA AVAILABLE



Figure C-5. Thickness and U, Th values of Unit 3, Deep Gulch Conglomerate from transects 15, 16 and 17, Deep Gulch, northwest Sierra Madre.

ND=NO DATA AVAILABLE











ND = NO DATA AVAILABLE SS = SPOT SAMPLE

Figure C-9



Sierra Madre Unit # 3 Figure C-10

ND = NO DATA AVAILABLE SS = SPOT SAMPLE














Unt Th (ppm)(ppm)

Figure C-16. Thickness and U, Th values of radioactive conglomerates from surface transect T7, Onemile Creek area, Medicine Bow Mtns.











Figure C-21. Thickness and analysis for beds exceeding IOOppm U_3O_8 in core from drill hole EMB-8, Onemile Creek area, Medicine Bow Mtns.



Figure C-22. Thickness and analysis for beds exceeding 100 ppm U_3O_8 in core from drill holes EMB-9 and EMB-10, Onemile Creek area, Medicine Bow Mtns.





Appendix D

Average Grade and Total Bed Thickness for Outcrop Transects and Drill Holes

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Table	D-	1
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Sierra Madre Accumulations of $U_3^0 0_8$ in exceedance of 100 ppm

Transect or Drill Hole	Average ^U 3 ⁰ 8	Average (U ₃ 0 ₈)2	Average In U ₃ 08	Total Thickness	Average Thickness
Transect #5	109.9	12077	4.70	.7	•7
Transect #16	116.03	13464	4176	.5	•5
SM-1 Core	110.6	12232	4.71	•7	•7
SM-2 Core	184.29	43423	5.12	4.2	.60

Unit #3

Transect or Average Average Average Total Average Bed (U₃0₈)² U308 InU308 Drill Hole Thickness Thickness Unit 1: 164.04 34145 8.4 Transect TIA 4.99 1.20 48501 8.4 Transect TIB 207.20 5.27 0.65 Transect TIC 403.02 5.69 8.4 1.05 327435 83880 1.00 Transect T2 245.24 5.32 5.0 EMB-1 Core 5.12 175.31 33142 9.2 0.92 MB16 Core 392.60 255433 5.66 15.2 0.95 Unit 5a: 0.63 145567 1.9 Transect T4 379.51 5.93 369.23 5.86 9.4 3.13 Transect T5 151538 Transect T8 416.26 268186 5.71 3.0 1.00 5.82 11.8 1.48 EMB-6 Core 424.77 276813 5.10 8.3 0.52 EMB-7 Core 195.73 71319 Unit 5b: 2.8 175.97 95542 4.82 1.40 Transect T3 6.26 0.6 0.60 278678 Transect T5 527.94 6.18 1.00 485.40 235613 1.0 Transect T7 42608 1.00 204.80 5.31 3.0 Transect T8 5.76 15.4 0.96 538639 EMB-6 Core 508.19 259.86 82586 5.45 6.7 0.37 EMB-7 Core 0.69 4.8 218.73 53081 5.32 EMB-8 Core 0.50 269.30 97202 5.39 1.0 EMB-9 Core 1.8 0.36 EMB-10 Core 170.68 30032 5.12 Threemile Creek Area: 0.54 60521 5.34 2.7 226.2 EMB-11 Core

Table D-2 Medicine Bow Accumulations of $U_3 O_8$ in exceedance of 100 ppm

Table D-3

Sierra Madre Accumulations of ThO_2 in exceedance of 100 ppm

Transect or Drill Hole	Average Th0 ₂	Average (ThO ₂) ²	Average InTh0 2	Total Thickness	Average Thickness
Transect #1	591.70	350118	6.38	2.0	2.0
Transect #2	423.40	193168	6.00	4.3	2.15
Transect #3	235.85	68743	5.35	5.5	1.83
Transect #4	162.24	27903	5.06	5.8	2.90
Transect #5	341.35	116533	5.82	.7	.7
Transect #6	216.20	46742	5.36	1.3	1.3
Transect #7	257.75	67550	5.54	2.3	1.15
Transect #9	130.47	17057	4.86	1.5	۰75
Transect #10	202.75	44259	5.26	5.5	2.75
Transect #11	131.37	17291	4.87	4.4	2.20
Transect #13	156.20	26378	5.00	1.1	. 37
Transect #14	125.16	16832	4.80	1.0	.33
Transect #16	217.07	49381	5.35	1.3	. 43
Transect #18	286.74	95090	5.57	1.5	.50
Transect #19	294.33	87149	5.68	1.5	.75
Transect #21A	204.81	43386	5.30	1.3	. 32
Transect #21B	146.3	21641	4.97	.7	. 35
Transect #22A	329.99	108894	5.79	1.0	1.0
Transect #22B	227.57	51792	5.42	.9	.45
Transect #23	329.98	119252	5.74	.9	.45
Transect #24	466.53	217658	6.13	.6	.6
SM-1 Core	341.36	116532	5.82	.73	.73
SM-2 Core	287.72	113536	5.5	8.96	.64

Unit #3

lable D-4

Medicine Bow Accumulations of ${\rm Th0}_2$ in exceedance of 100 ${\rm ppm}$

Transect or Drill Hole	Average Th0 ₂	Average (Th0 ₂) ²	Average In ThO ₂	Total Thickness	Average Bed Thickness
<u>Unit l</u> :	<u>+</u>				· · ·
Transect TIA	215.70	49540	5.33	2.3	0.77
Transect T1B	170.09	34774	5.04	2.3	0.38
Transect TIC	307.83	116724	5.56	1.9	0.95
Transect T2	307.28	94392	5.72	1.0	1.00
EMB-1 Core	256.79	69967	5.51	3.0	1.00
MB-16 Core	182.06	36658	5.14	3.2	0.80
<u>Unit 5a</u> :					
Transect T4	555.17	326314	6.29	1.9	0.63
Transect T5	188.51	37128	5.21	6.7	1.12
Transect T8	464.26	315377	5.78	5.0	1.00
EMB-2 Core	159.30	25376	5.07	1.0	1.00
EMB-6 Core	387.81	191748	5.83	8.0	1.33
EMB-7 Core	270.97	88583	5.49	4.4	0.55
<u>Unit 5b</u> :					
Transect T3	147.92	21882	4.99	0.5	0.50
Transect T5	297.27	125548	5.48	1.6	0.80
Transect T6	100.13	100027	4.61	0.2	0.20
Transect T7	364.12	132589	5.89	1.0	1.00
Transect T8	261.72	71603	5.54	3.0	1.00
EMB-6 Core	255.64	86390	5.44	10.5	1.17
EMB-7 Core	300.54	117203	5.56	6.4	0.40
EMB-8 Core	256.85	78249	5.46	9.6	0.74
EMB-9 Core	642.90	567455	6.23	1.0	0.50
<u>Threemile</u> Creek Area:					
EMB-11 Core	165.26	31371	5.04	1.7	0.43

Table D-5

SUMMARY OF AVERAGE ACCUMULATIONS AND VARIANCES FOR $U_3^0 _8$

Unit	Average accumula- tion of U ₃ 0 ₈ above 100 ppm (ppm x ft.)	Average of accumulations squared (ppm x ft.) ²	Accumulation variance (ppm x ft.) ²	Number of transects with encounters of > 100 ppm U ₃ 08 (k)	Total number of transects (n)	
Sierra Madre unit 3	246.60	153596	18806	4	31	
Medicine Bow unit l	2551.73	9350811	3304805	6	6	
Medicine Bow unit 5a	2415.49	8377562	2960192	5	9	
Medicine Bow unit 5b	1455.88	7389445	4585649	9	10	
Medicine Bow units 1, 5a and 5b combined						
(Onemile Creek area)) 2024.53	8224884	3901555	20	25	
Medicine Bow Threemile Creek area	a 610.74	373003	57969	ſ	1	
All Medicine Bow units	1957.21	7850985	3842177	21	26	

Unit	Average accumula- tion of ThO ₂ above 100 ppm (ppm x ft.)	Average of accumulations squared (ppm x ft.) ²	Accumulation variance (ppm x ft.) ²	Number of transects with encounters of >100 ThO (k) ²	Total number of transects (n)
Sierra Madre unit 3	608.79	739051	344310	23	31
Medicine Bow unit l	522.07	294759	54267	6	6
Medicine Bow unit 5a	1515.53	3194760	1058781	6	ģ
Medicine Bow unit 5b	1048.37	2042130	941041	9	10
Medicine Bow units 1, 5a and 5b combined (Onemile Creek area) 1007.01	1847084	830330	21	25
Medicine Bow Threemile Creek are	a 280.94	78928	10275	1.	1
All Medicine Bow unit	s 974.01	1766713	815667	22	26

Table D-6 SUMMARY OF AVERAGE ACCUMULATIONS AND VARIANCES FOR ThO $_{\rm 2}$

