LONGITUDINAL EMITTANCE MEASUREMENTS IN
THE FERMILAB RECYCLER RING

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Abstract
The Recycler Ring (RR) is a new 8GeV antiproton storage ring at Fermilab. Presently, this machine is being commissioned using protons from the Booster. It uses barrier buckets for stacking, unstacking and storing the beam. At any given time, the RR is capable of storing proton or antiproton beams in multiple segments azimuthally. These segments of the beam may have widely differing longitudinal emittance and beam intensities and bunch lengths. It is highly essential to be able to measure the longitudinal emittance and keep track of the longitudinal dynamics at various stages of the operation of the RR. In this paper, we discuss a few methods of longitudinal emittance measurements in barrier buckets and discuss their merits and demerits.

INTRODUCTION
The Recycler Ring at Fermilab[1] is the world's largest antiproton storage ring built mainly using permanent magnets. For stacking the antiprotons in the RR, the beam will be transferred either from the Fermilab Accumulator Ring (cold beam) or from the Tevatron (used hot beam) via the Main Injector (MI). The hot and cold beams are stored in the RR in separate regions and cooled further. When beam is needed for the Tevatron collider operation, the cold beam from the RR will be extracted in the form of small bunches and transferred to the MI and accelerated to 150 GeV before injection into the Tevatron. All of these rf manipulations in RR are carried out using barrier buckets.

During the last year we had several antiproton stores in RR to understand the transverse and longitudinal dynamics, effectiveness of stochastic cooling system, beam life-time etc. We have also transferred the antiproton beam from the Recycler into the Main Injector and accelerated to 150 GeV.

The RR and the MI share the same underground tunnel. The MI acceleration cycles have significant effects on the longitudinal and transverse beam emittance of the stacked beam in the RR. After identification of this problem we have taken several measures to mitigate these effects and to minimize the emittance growth.

Over the past three years we have used different methods of emittance measurement to learn about the longitudinal dynamics at various stages of operation of the Recycler. In this paper, we review the methods used for longitudinal emittance measurements in barrier buckets and discuss their merits and demerits. We also illustrate the use of Monte Carlo methods to estimate the longitudinal emittance in case of a complex beam distribution.

BARRIER BUCKETS AND LONGITUDINAL EMITTANCE

Use of rf barrier buckets is not new at the Fermilab accelerators. Sinusoidal rf barriers were invented[2] to be used in the antiproton De-blocking and Accumulator rings to produce longitudinal gaps in the stored beam.

A barrier bucket is characterized by barrier pulse shape V(t), pulse duration \( T_1 \) and gap between +ve and -ve pulses \( T_2 \). The general Hamiltonian for an arbitrary barrier rf bucket can be written as [3],

\[
H = -\frac{\eta}{2\beta^2 E_0} (\Delta E)^2 - \int_0^T eV(\tau)d\tau \\
\]

where \( \eta \) is the slip-factor of the synchrotron, \( \Delta E \) is energy deviation from synchronous energy \( E_0 \), \( T_0 \) is the revolution period of the charged particle, \( e \) is the electronic charge. The half bucket height is given by,

\[
\Delta E_b = \sqrt{\frac{2\beta^2 E_0}{|\eta|} \int_{T_2}^{T_1 + T_1} eV(\tau) d\tau} \\
\]

Here, we assume that the +ve and -ve pulses are symmetric about the center of the bucket. It is important to note that all physical quantities depend basically on \( \int eV(\tau)d\tau \) not on the exact shape of the wave form if it had some symmetry about the bucket center.

The Recycler uses a wide-band (10kHz-100MHz) RF system capable of generating many barrier buckets of

Figure 1: A schematic of RR beam phase-space distribution (a) in a rectangular barrier bucket and, (b) its projection along the time axis.
any shape[4]. The maximum height of a barrier pulse is
set to about +/−2kV each. The width of a pulse can be
varied. The pbar beam from the antiproton Accumulator
will have 2.5 MHz rf structure and that from the Recycler
to MI can have 2.5 MHz or 7.5 MHz rf structure. The rf
system can also produce 2.5 MHz/7.5 MHz rf buckets in
between barrier buckets. For a given peak rf voltage a
wave form of rectangular shape gives maximum value of
\[ \int V(t)dt \]. Hence, we adopted a rectangular barrier bucket.
The pulse width is selected to be \( \approx 908 \) nsec.

A schematic view of RR barrier waveform with its
bucket boundary (an equal Hamiltonian contour defining
the bucket) and beam in it is shown in Figure 1. For the
beam penetrating in the barrier the beam half height is
given by

\[
\Delta E_\beta = \sqrt{\frac{2 \beta^2 E_\beta eV_b T_1}{\eta T_0}\\}
\]

(3)

The longitudinal emittance \( \varepsilon_I \) is given by,

\[
\varepsilon_I = 2T_2 \Delta E_\beta + \frac{8\pi \eta}{3 \omega_c \beta^2 E_\beta eV_b} (\Delta E)^3
\]

(4)

where \( \omega_c=2\pi/ T_0 \) and \( \beta \) is ratio of velocity of the beam to
velocity of the light. \( \eta = 0.0087, E_\beta=8.938 \text{GeV}, T_0 = 11.12 \mu \text{sec} \) for the Recycler.

TECHNIQUES FOR MEASUREMENT OF
\( \varepsilon_I \) AND \( \Delta E \)

An accurate measurement of longitudinal emittance of
particle beams in any synchrotron is not a trivial task. The
knowledge of correct longitudinal emittance is key to the
understanding the longitudinal beam dynamics. This in-
turn helps to improve the proton-antiproton luminosity
in the Tevatron. So far, we have used four different
measurement techniques in the Recycler. They can be
broadly classified into two categories: beam destructive
techniques and non-destructive techniques. The
destructive techniques are mainly one-time measurements. Their use in a storage ring like the
Recycler is very limited. On the other hand, the non-
destructive techniques are used as the major beam
diagnostics in daily operations. Here, we describe both of
these approaches for completeness.

Destructive Techniques

Two different methods of this type are illustrated here.
The first method is based on matching the bucket area to
bunch area. After the beam is captured in a barrier bucket
the height of the rf pulse is adiabatically reduced while
the width is held constant until the beam area fills the
bucket. To determine the rf voltage, \( V_b \), where the beam
just fills the bucket a gated current integrator (GCI) [5] is
used to measure the beam captured between the barriers.
A schematic view of this method is shown in Figure 2
(left). Knowing the \( V_b \) and \( T_1 \) in equations 3 and 4, the
beam energy spread and the beam area are measured. This
technique was used in the early detection of the
longitudinal emittance growth in the Recycler arising
from the MI high energy cycles. Similar measurements
can be made if we change the width of the barrier pulse
keeping the pulse height constant. For barrier buckets
with non-rectangular barrier pulses this method would be
less useful.

The second method requires an ability to turn-off the
barrier pulses much faster than the synchrotron period of
the beam in the barrier bucket. Then the beam energy
spread \( \Delta E \), the fractional change in orbiting time \( \Delta T \) and
total de-bunching time \( T \) are related according to

\[
\frac{\Delta E}{E} = \frac{\eta}{\beta^2} \frac{\Delta T}{T}
\]

(5)

In the RR, the synchrotron oscillation period is about
0.6 sec for a barrier bucket with \( T_2=1.6 \mu \text{sec} \) and the beam
rf voltage can be turned-off in <1msec. Figure 2 (right
inset) illustrates an example of measuring \( \Delta E \) by fast de-
bunching method. The de-bunching time (from bottom to
the top) and fractional increase in orbiting time is
measured using digitized wall-current monitor data.

![Figure 2: A schematic of the method which adopts varying rf voltage at a fixed pulse width in RR (left). Typical data from the fast de-bunching method in the RR (right).](image)

Non-destructive Techniques

We are using two different methods of non-destructive
type in the Recycler beam longitudinal emittance studies.
The first of these is a variation on the traditional method
of measuring the beam profile using a wall current
monitor (WCM). A detailed account of use of WCM in
longitudinal emittance measurement is given in ref.6. The
second method is based on Schottky signal detection.

A. Resistive Wall Current Monitor

A WCM is a device which measures the image charge
that flows along the vacuum chamber following the beam
and hence reproduces the longitudinal profile of the beam.
We have a 4 GHz bandwidth pickup WCM[7] in the Recycler Ring. By knowing the exact location of the barrier pulse and their shapes one measures the beam penetration into the barrier pulse to measure the $\Delta E$. For a beam confined in a rectangular barrier bucket the beam penetration is symmetric with respect to the center of the bunch. However, any asymmetry in the shape of the pulse or non-zero rf voltage in the gap between +ve and -ve barrier pulse (which might arise due to rf hardware or software systems) will result in an asymmetric beam penetration in the barrier. The WCM then measures different amounts of penetration in the barrier (later we illustrate an example of this type). The WCM data is very sensitive to small distortions in the barrier pulse. In particular, when the longitudinal emittance of the beam is small the WCM allows detection of distortion of the baseline between the barrier pulses.

The Recycler WCM signals are sent to a digitizing scope RDT720. The rf fan-out signals are also processed along with the WCM signals to measure the relative position of the barrier pulse in the ring. A special trigger module is developed to trigger the scope at different times of rf manipulation. Then the data is collected using a software program[8].

Figure 3: WCM data for antiproton stacking.

Figure 3 illustrates a case of pbar beam stacking in the Recycler. “New Beam” in this figure has 2.5MHz bunch structure. Knowing the bunch length and the peak rf voltage one can measure the longitudinal emittance of the beam at injection. Measuring the penetration of the beam into the barrier pulses and using equations (3) and (4) the longitudinal emittance of the beam in barrier buckets at various stages are estimated. The errors in the measured emittance mainly come from detector response, estimating the beam penetration into the barrier and the measured rf voltage.

B. Schottky Signals

Using Schottky signals for beam emittance measurements in a storage ring is an excellent method[9]. For a coasting beam, the energy spread $\Delta E$ and the frequency spread of the Schottky spectrum $\Delta f$ are related according to

$$\frac{\Delta E}{E} = \frac{\beta^2 \Delta f}{\eta f}$$

where $f = n f_0$, $f_0$ is the revolution frequency of the synchronous particles and $n$ is the harmonic number. Measuring the maximum energy spread using a Schottky detector resonating at a reasonable harmonic number ($n \sim 100$) and a spectrum analyzer is straightforward.

In case of a sinusoidal bunched beam, the beam particles execute synchrotron oscillations. The time of passage of a particle in front of the detector is modulated according to synchrotron oscillation amplitude. Thus, the time coordinate $t \rightarrow t + \tau \sin(\Omega t + \phi)$ as compared to a coasting beam. The quantities $\tau$, $\Omega$, and $\phi$ are synchrotron amplitude, frequency and phase, respectively. Then the beam current for a single particle in frequency domain will take the form

$$i(t) = i f_0 + 2i f_0 \sum_{k=1}^{\infty} J_k(n a \Omega t + k \phi)$$

(7)

where $J_k$ is the Bessel function of order $k$. Hence, in the case of bunched beam with some energy spread, each revolution frequency band at frequency $nf_0$ (as seen in the coasting beam) is replaced by a central line with an infinite number of satellites. Further, the satellites of order $k$ with different values of $n$ are correlated which gives rise to coherence. This feature of the bunched beam Schottky spectrum makes it more complicated to interpret for longitudinal emittance measurements. Fortunately, for sufficiently large $n$, (at high frequency), the equation (6) is an excellent approximation for all types of beams.

Figure 4: Typical Schottky spectra taken with two detectors. Left ($n=882$) and right ($n=19500$).

The beam bunched in barrier buckets can be described in terms of a sum over harmonics of the synchrotron frequency, but the synchrotron frequency spread is so big that the signal from a beam bunched in barrier is very similar to a truly coasting beam.

At the Recycler, we have used three Schottky detectors with frequencies 79MHz, 1.5GHz and 1.75GHz. They have $n = 882, 16700, 19500$, respectively. In Figure 4, we illustrate a typical longitudinal Schottky spectrum from two detectors with widely different harmonic
numbers. The data are taken for the same beam in a barrier bucket. The data shown on left are obtained with 79MHz Schottky detector and show in addition to the Schottky signal a prominent coherent peak at revolution harmonic. Hence, unambiguous determination of $\Delta E$ is difficult. The figure on the right hand side shows data with the 1.75GHz Schottky detector and does not show coherent peak. We find that the maximum energy spread is about 5.6MeV for the case illustrated here.

It is important to note that the measured $\Delta E$ using Schottky spectrum is independent of rf voltage wave form if spectrum does not show any coherent peak. However, the Schottky technique does not distinguish between captured beam or an un-captured beam. It can be gated to measure different parts of the beam.

C. Comparison between WCM and Schottky Methods

We have carried out a number of experiments to measure longitudinal emittance of the beam in Recycler Ring using Schottky signals and by using WCM. Here we illustrate two examples from these measurements.

Figure 5: (a) WCM data for bunched beam in the Recycler, (b) 1.75GHz Schottky spectrum for the same beam.

Fig. 5 shows data from WCM and 1.75GHz Schottky detector for beam in four 2.5MHz buckets. The 2.5MHz rf voltage was about 2kV and average bunch length (90% by area) is about 260 nsec. We find that the measured emittance for assumed elliptical distribution to be 20eVs and $2\Delta E=12$MeV (<20%). For the same beam the Schottky spectrum gives about $2\Delta E=9$ MeV.

Data taken for the beam in a typical barrier bucket are shown in Figure 6. In this case $T_2=1.6$ $\mu$sec. The measured $e_i=14$eVs and $\Delta E=8$MeV from the WCM measurements can be compared to $e_i=9$eVs and $\Delta E=8$ MeV from Schottky measurements.

Figure 6: (a) WCM data for the beam in a rectangular barrier bucket, (b) 1.75GHz Schottky spectrum for the same beam. $T_1=908$ nsec, $T_2=1.6$msec and $V_0=2$kV.

D. Some Special Cases

The perfect rectangular barrier pulse discussed above is not reality in the Recycler. Typically, a rectangular barrier pulse in the Recycler will be have rounded edges. In between barrier pulses there may be a small slope of a few percent of the total pulse amplitude. Besides, as one adds a number of barrier pulses around the accelerator ring the adjacent barrier pulses are found to be distorted at a few percent level. This phenomenon makes the measurement of longitudinal emittance more difficult.

Figure 7 illustrates a case with non-symmetric Vrf between barrier pulses. Figure 7(a) shows a WCM data for cooled pbar beam. We have made an attempt to simulate the WCM data using a multi-particle beam dynamics code (a Monte Carlo program), ESME[10]. In our model we have assumed a damping oscillating rf wave with a Vrf $(max)=2.5\%$ of 2kV between the barrier pulses which starts at the negative barrier pulse. This method predicts the longitudinal emittance to be about 51eVs and $\Delta E_{max}=8$ MeV. The energy spread estimated here can be compared with the Schottky signal method of 6.4MeV (at -10dB).
In summary we have measured the longitudinal emittance of the beam in the Recycler Ring by using four different techniques, two destructive and two non-destructive techniques. The WCM and Schottky spectrum methods are very promising, and are suitable for future applications in Recycler during routine operation. A more detailed understanding of the measurement errors is the subject of future effort.

REFERENCES

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