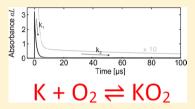
# Rate Constant and Thermochemistry for $K + O_2 + N_2 = KO_2 + N_2$

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Supporting Information

ABSTRACT: The addition reaction of potassium atoms with oxygen has been studied using the collinear photofragmentation and atomic absorption spectroscopy (CPFAAS) method. KCl vapor was photolyzed with 266 nm pulses and the absorbance by K atoms at 766.5 nm was measured at various delay times with a narrow line width diode laser. Experiments were carried out with O<sub>2</sub>/N<sub>2</sub> mixtures at a total pressure of 1 bar, over 748-1323 K. At the lower temperatures single exponential decays of [K] yielded the third-order rate constant for addition,  $k_{R1}$ , whereas at higher temperatures equilibration was observed in the form of double exponential decays of [K], which yielded both  $k_{R1}$  and the



equilibrium constant for KO<sub>2</sub> formation.  $k_{R1}$  can be summarized as  $1.07 \times 10^{-30} (T/1000 \text{ K})^{-0.733} \text{ cm}^6 \text{ molecule}^{-2} \text{ s}^{-1}$ . Combination with literature values leads to a recommended  $k_{R1}$  of  $5.5 \times 10^{-26} T^{-1.55} \exp(-10/T) \text{ cm}^6 \text{ molecule}^{-2} \text{ s}^{-1}$  over 250– 1320 K, with an error limit of a factor of 1.5. A van't Hoff analysis constrained to fit the computed  $\Delta S_{298}$  yields a K-O<sub>2</sub> bond dissociation enthalpy of 184.2  $\pm$  4.0 kJ mol<sup>-1</sup> at 298 K and  $\Delta_t H_{298}(KO_2) = -95.2 \pm 4.1$  kJ mol<sup>-1</sup>. The corresponding  $D_0$  is 181.5 ± 4.0 kJ mol<sup>-1</sup>. This value compares well with a CCSD(T) extrapolation to the complete basis set limit, with all electrons correlated, of 177.9 kJ mol<sup>-1</sup>.

#### INTRODUCTION

The high-temperature chemistry of alkali metal species has important implications for combustion. It is well established that the presence of alkali metal species may result in flame inhibition<sup>1,2</sup> and alkali-based flame inhibitors are of interest.<sup>3,4</sup> Potassium additives are also known to have an impact on gun muzzle flash.<sup>5</sup> Furthermore, most solid fuels contain alkali metals in minor quantities. Biomass such as wood and annual crops releases potassium to the vapor phase during pyrolysis and combustion, 6-8 mainly in the form of KCl. Once released, the alkali metal chlorides may be partially converted to alkali metal hydroxide or alkali metal sulfates.9 During cooling, the alkali metal components will condense, contributing to aerosol formation and/or cause operational problems, such as deposit formation and corrosion in boilers. 10,11 The fate of the alkali metal will depend on interactions with the sulfur and chlorine species of the gas.

Formation of potassium superoxide, KO2, is potentially important for both flame inhibition and the high-temperature K/S/Cl transformation in combustion. The ability of alkali metals to catalyze radical removal is well documented by data from laminar premixed flames 12-25 and flow reactor experiments.<sup>26</sup> Alkali-metal-based flame inhibitors are typically added as particulates<sup>3,4</sup> and heterogeneous effects have been proposed; however, the inhibiting effect of alkali metals is attributed mostly to gas phase radical removal reactions. The mechanism of inhibition is still in discussion. Under reducing conditions, results from flames 16,17,21 and from flow reactors 2 are consistent with the sequence (for K):  $KOH/KCl + H \rightarrow K$ 

+  $H_2O/HCl$ , K + OH + M  $\rightarrow$  KOH + M. In combustion systems, alkali metal chlorides and alkali metal hydroxides are rapidly equilibrated through the fast reaction KCl + H<sub>2</sub>O ≠ KOH + HCl. Under lean conditions, the inhibition mechanism is more uncertain. The chain-terminating recombination

$$K + O_2 + M \rightleftharpoons KO_2 + M \tag{R1}$$

has been suggested to be important. 18,27-29 However, it has been questioned whether potassium superoxide was sufficiently stable to play an important role under flame conditions.<sup>2,26</sup>

Formation of alkali metal superoxides (mainly KO<sub>2</sub>) may also play a role in the gas-phase transformation of alkali metal, sulfur, and chlorine species in solid fuel combustion. Provided KO<sub>2</sub> is sufficiently stable, it could promote oxidation of SO<sub>2</sub> to  $SO_3$  through the reaction  $SO_2 + KO_2 \rightarrow SO_3 + KO$ , which has been estimated to be fast.<sup>30</sup>

The importance of KO<sub>2</sub> in combustion depends on the rate constant for  $K + O_2 + M$  (R1) and on the thermal stability of  $KO_2$ . Values of  $k_{R1}$  have been measured directly in the temperature range 250–1100 K,<sup>31–34</sup> inferred from studies of lean premixed flames,<sup>27–29</sup> and calculated theoretically.<sup>35</sup> The direct measurements are in reasonably good agreement but deviate significantly from the values derived at high temperatures from flames. Also the thermochemistry of KO2 is in

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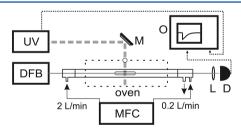
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discussion. Values for the bond dissociation energy  $D_0$  of KO<sub>2</sub> have been inferred from flame studies, <sup>18,36</sup> a molecular beam study, <sup>37</sup> time-resolved decay of atomic potassium, <sup>34</sup> and from theory. <sup>34,38–40</sup> Although recent theoretical studies imply a value of the BDE of approximately  $172 \pm 4$  kJ mol<sup>-1,38–40</sup> some data inferred from experiment indicate a substantially larger value. <sup>34,37</sup>

The objective of the present work is to extend the measurement range for the rate constant for  $K + O_2 + N_2$  to higher temperatures compared to previous direct studies, and to provide the first direct measurements of the bond dissociation energy of KO<sub>2</sub>. For this purpose we use the recently developed optical technique called collinear photofragmentation and atomic absorption spectroscopy (CPFAAS). This technique is based on the fragmentation of a precursor molecule and the detection of the fragment atoms via absorption spectroscopy. 41,42 It has been applied to monitor concentrations of the precursors KCl and KOH in combustion during combustion of solid biomass fuels,43 but to our knowledge the present work is its first application to chemical kinetics. Previous CPFAAS studies have focused on the maximum absorbance right after the photofragmentation that is proportional to the precursor molecule concentration. The decay process of the induced K atoms has been assumed to be exponential and was not studied in detail. In the present work, measurements analogous to CPFAAS experiments are performed to study the decay process of [K] in the temperature range of 748-1323 K and in atmospheres containing O<sub>2</sub> from 40 ppm to 21.4%.

#### EXPERIMENTAL SECTION

Potassium atoms were produced and detected using a measurement setup presented in Figure 1. The K atoms were



**Figure 1.** Experimental setup for the time-resolved detection of photoinduced potassium atoms: photofragmentation laser (UV); probe laser (DFB); mirror (M); lens (L); detector (D); oscilloscope (O); mass flow controller (MFC).

formed through photofragmentation of KCl molecules in an 80 cm long quartz sample tube having an inner diameter of 35 mm. The KCl powder was brought into the middle of the cell in a 10 cm long glazed combustion boat. The temperature of the sample tube was adjusted with a 50 cm long and 30 cm wide tube oven. The gas atmosphere in the tube was adjusted by flushing the tube for 5 min before each experiment with a gas mixture prepared by diluting dry synthetic air with nitrogen using a mass flow controller (5850S, Brooks Instruments). A gas flow of 2 standard liters per minute (L min<sup>-1</sup>) was brought to the tube from the entrance side of the probe laser and 0.2 L min<sup>-1</sup> from the exhaust side of the tube. The small flow at the exhaust side prevented the deposition of the KCl vapor on the inner surface of the exit window of the cell. The gas flows were

closed 2 min before recording the decay of the K atoms. The sample was at atmospheric pressure during the measurement.

The dissociation of the KCl molecules was performed by applying a fragmentation laser (FQSS 266-200, Crylas GmbH). It emitted 1 ns long pulses with a 20 Hz repetition rate at a wavelength of 266 nm. The laser pulses entered the sample tube through an 18 mm hole at the side of the oven and through the wall of the tube. The transmission of the wall material for the fragmentation wavelength was measured to be approximately 80%. The pulse energies of the fragmentation laser in the sample tube were adjusted to between 1 and 80  $\mu$ J, and the cross sectional 1/e diameter of the pulses was adjusted over the range of 3-10 mm, such that detected probe beam transmission did not drop to zero. The energy densities of the UV pulses in the tube were smaller than the saturation intensity of KCl.<sup>44</sup> The pulses were slightly focused with a lens prior to the entrance hole to increase the concentration of the released K atoms at the lower temperatures (<873 K) when the vapor pressure of KCl was small. The pulses traveled 10 mm above the top of the combustion boat and were dumped to the back wall of the oven.

The relative concentration of the K atoms was measured by applying a narrow line width distributed feedback diode laser (Nanoplus GmbH), which emitted light at a wavelength of 766.5 nm (in air). The wavelength of the diode laser was locked to the absorption line of K atoms in a reference cell (SC-K-19 × 75-Q-W, Photonics Technologies). 42 The probe beam having a 1/e diameter of 1 mm was aligned to travel through the tube and to cross the volume affected by the fragmentation pulses. The optical path of the probe laser beam and the fragmentation pulses were perpendicular to each other in the tube. The short interaction region meant that the temperature was constant across it, despite any overall temperature gradients along the entire sample tube. The induced K atoms decreased the transmission intensity of the probe beam temporarily. The transmission waveform caused by the photofragmentation was detected using an amplified photodiode (PDA10A, Thorlabs) and a 12-bit oscilloscope (HDO6054, LeCroy).

An example waveform measured at a temperature of 1173 K in 2.67% of  $\rm O_2$  is presented in Figure 2a. The photofragmentation of KCl molecules took place at t=0, and it is seen as a fast dip in the photodiode (PD) voltage due to the temporarily increased absorption by the K atoms. The fragmentation was followed by recovery of the transmission as the induced K atoms reacted with ambient gas molecules and the distorted gas volume approached equilibrium.

To study the recovery process of the concentration of K atoms, the PD voltage was converted to the absorbance  $\alpha L$  by applying the Beer–Lambert law,

$$\alpha L = -\ln[I(t)/I(t<0)] \tag{1}$$

Figure 2b shows the corresponding absorbance curve calculated using eq 1. The absorbance is directly proportional to the sample concentration and the conversion can be done when absorption length and absorption cross section are known. The effective absorption length in this measurement was 1 cm (UV beam diameter) and the absorption cross section of K atoms at the wavelength in question is  $1.25 \times 10^{-16}$  m<sup>2</sup>, <sup>43</sup> which converts an absorbance equal to 1 to a K concentration of 130 ppb. At the lower end of the temperature range studied, the absorbance was observed to follow a single exponential decay,

$$\alpha L(t>0) = A_1 \exp(-k_1 t) \tag{2}$$

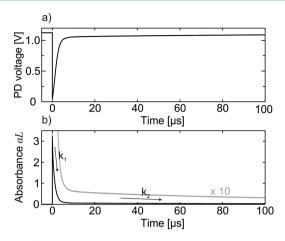


Figure 2. (a) Probe laser transmission curve. The dip is caused by the photofragmentation of KCl molecules. (b) Corresponding absorbance curve calculated from the transmission curve. The induced absorbance decays with two rate constants  $k_1$  and  $k_2$ . The second phase decay is emphasized in (b) by magnifying the decay curve by a factor of 10. The experiment was done at a temperature of 1173 K in 2.67% of  $O_2$  in  $N_2$ .

whereas at higher temperatures a double exponential decay process was observed,

$$\alpha L(t>0) = A_1 \exp(-k_1 t) + A_2 \exp(-k_2 t)$$
 (3)

### ■ RESULTS AND DISCUSSION

At 1073 K and below simple exponential kinetics were observed, in the form of eq 2, which may be interpreted in terms of the scheme

$$K + O_2 \xrightarrow{k_a} KO_2$$
 (a)

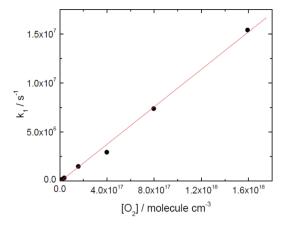
$$K \stackrel{k_d}{\to} loss$$
 (d)

 $k_{\rm a}$  represents the effective second-order forward rate constant for reaction R1 and  $k_{\rm d}$  accounts for loss of K atoms by processes that do not involve oxygen, such as diffusion. One would therefore expect the variation of potassium concentration with time t to follow eq 4,

$$[K] = [K]_0 \exp(-k_1 t) \tag{4}$$

where  $k_1 = k_a[O_2] + k_d$ . Figure 3 shows a plot of  $k_1$  vs  $[O_2]$ , from which it may be seen that the expected linear dependence on [O2] from reaction (a) is exhibited, and that the intercept is negligible, so that on the short time scale of these experiments  $k_{\rm d}$  is indistinguishable from zero. Details of  $k_1$  and  $[{\rm O}_2]$ measurements are provided in the Supporting Information (Table S1), and the results for the third-order rate constant  $k_{R1}$ derived as the slope  $k_a$  divided by  $[O_2] + [N_2]$  (corresponding to 1 bar total pressure) for 873-1073 K are listed in Table 1. Approximate, purely statistical, error limits were assessed via twice the standard deviation of the slopes of plots like Figure 3. At 748, 773, and 823 K single measurements of  $k_1$  were made, and divided by  $[O_2]$  and  $[{
m ilde O}_2]$  +  $[{
m N}_2]$  to obtain  $k_{
m RI}$ . We allow 25% error limits for these points, and also for a single measurement at 1323 K where black liquor (alkali-metal-rich waste product from pulp and paper processing) rather than KCl was the source of K atoms.

We now turn to the measurements made at the higher temperatures where double-exponential decays of absorbance



**Figure 3.** Exponential decay coefficient for potassium atoms as a function of oxygen concentration at 923 K and a total pressure of 1 bar made up with nitrogen.

Table 1. Summary of Measurements for  $K + O_2 + N_2$ 

T/°C	T/K	$(k_{\rm R1} \pm 2\sigma)/10^{-30}$ cm <sup>6</sup> molecule <sup>-2</sup> s <sup>-1</sup>	comment
475	748	$1.47 \pm 0.37$	single point
500	773	$1.31 \pm 0.33$	single point
550	823	$1.24 \pm 0.31$	single point
600	873	$1.18 \pm 0.16$	exponential decays
650	923	$1.15 \pm 0.04$	exponential decays
700	973	$1.07 \pm 0.02$	exponential decays
750	1023	$0.998 \pm 0.027$	exponential decays
800	1073	$0.789 \pm 0.140$	exponential decays
800	1073	$0.978 \pm 0.152$	equilibrium mechanism
850	1123	$0.982 \pm 0.024$	equilibrium mechanism
900	1173	$0.969 \pm 0.032$	equilibrium mechanism
950	1223	$0.973 \pm 0.063$	equilibrium mechanism
1000	1273	$1.01 \pm 0.07$	equilibrium mechanism
1050	1323	$0.919 \pm 0.230$	single point, black liquor

were seen. Figure 4 shows a temporal K concentration profile upon photofragmentation of the KCl molecules at a temperature of 1223 K in 10.7%  $O_2$ . In agreement with the results of Figure 2, [K] is observed to recover to its original level in two steps. In the first phase [K] decreases fast and the 1/e relaxation time constant  $1/k_1$  is found to be 270 ns (Figure 4a). Figure 4b shows how [K] does not recover fully in the first phase and saturates to a nonzero level. Figure 4c presents how the second phase relaxation takes place on a time scale of the order of  $100~\mu s$ . The 1/e decay time constant for the second phase relaxation was, in the example signal,  $1/k_2 = 40~\mu s$ .

This double-exponential behavior, quantified in the form of eq 3, can be observed when reactants reversibly form an intermediate, and a reactant and/or intermediate is also lost irreversibly. In the absence of oxygen the lifetime of K was observed to be of the order of 1 ms, where K atoms are lost presumably mainly by diffusion out of the probe laser beam. This lifetime is too long to be significant on the time scale of the K atom profiles when O<sub>2</sub> is present. Accordingly, we have interpreted the results in terms of a simple mechanism

$$K + O_2 \xrightarrow{k_a} KO_2$$
 (a)

$$KO_2 \xrightarrow{k_{-a}} K + O_2$$
 (-a)

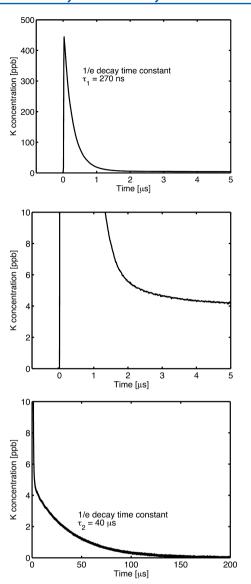


Figure 4. K relaxation after KCl photofragmentation at a temperature of 1223 K in 10.7%  $O_2$ : (a) first phase relaxation; (b) The concentration of K does not reach the original background level within first 5  $\mu$ s. (c) The thermodynamic equilibrium [K] is reached 200  $\mu$ s after the fragmentation. [K]<sub>0</sub> is the potassium concentration right after the photofragmentation, and [K]<sub>0</sub><sup>res</sup> is the concentration of the residual potassium atoms. This value is calculated by extrapolating the second phase recovery to t = 0.  $\tau_1 = 1/k_1$  and  $\tau_2 = 1/k_2$  are the recovery time constants in the fitting equation [K]<sub>t</sub> = ([K]<sub>0</sub> - [K]<sub>0</sub><sup>res</sup>) exp( $-t/\tau_1$ ) + [K]<sub>0</sub><sup>res</sup> exp( $-t/\tau_2$ ).

$$KO_2 \xrightarrow{k_b} loss$$
 (b)

 $k_{\rm a}$  represents the effective second-order rate constant for K atom addition to  ${\rm O_2}$  at a given total pressure,  $k_{\rm -a}$  is the effective first-order dissociation rate of  ${\rm KO_2}$ , and  $k_{\rm b}$  is the effective first-order rate of loss of  ${\rm KO_2}$  by pathways that do not regenerate K atoms. These include diffusive loss of  ${\rm KO_2}$  although presumably this is even slower than the neglected diffusive loss of K atoms. Assuming  ${\rm [O_2]} \gg {\rm [K]_0}$ , the integrated rate law may be written as  ${\rm Assuming} = {\rm [O_2]} \approx {\rm [K]_0}$ .

$$[K] = \frac{[K]_0}{\lambda_1 - \lambda_2} ((Q + \lambda_1) e^{\lambda_1 t} - (Q + \lambda_2) e^{\lambda_2 t})$$
(5)

with

$$Q = k_{-a} + k_{b} \tag{6}$$

$$\lambda_1 + \lambda_2 = -Q - k_a[O_2] \tag{7}$$

$$\lambda_1 \lambda_2 = k_b k_a [O_2] \tag{8}$$

By comparing terms with the empirical eq 3, we see that the three rate constants may be derived via

$$[K]_0 = A_1 + A_2 (9)$$

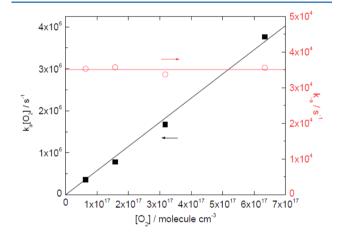
$$Q = k_1 + \frac{A_1(k_2 - k_1)}{[K]_0}$$
 (10)

$$k_{a}[O_{2}] = k_{1} + k_{2} - Q \tag{11}$$

$$k_{\rm b} = \frac{k_{\rm l}k_{\rm 2}}{k_{\rm a}[{\rm O}_2]}$$
 (12)

$$k_{-a} = Q - k_{\rm b} \tag{13}$$

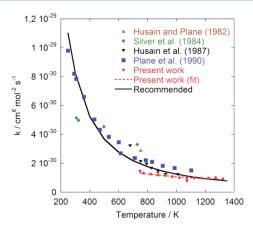
This analysis was applied to the double exponential data obtained over 1073-1273 K. A check on the consistency of the analysis is that the  $k_{\rm a}[{\rm O_2}]$  term should vary linearly with  $[{\rm O_2}]$  and  $k_{\rm -a}$  should be independent of  $[{\rm O_2}]$ . Figure 5 shows the



**Figure 5.** Effective first-order rate constants at 1223 K for K addition to  $O_2$  (solid black squares, left axis, linear fit constrained to pass through the origin) and for  $KO_2$  dissociation (open red circles, right axis, linear fit constrained to have zero slope).

results at 1223 K, and it may be seen that these conditions are met. A second check is that at 1073 K, low  $[O_2]$  led to double-exponential behavior whereas at high  $[O_2]$  the equilibrium is shifted sufficiently toward products that the back-reaction is negligible, leading to single exponential decays of [K]. Data obtained both ways are tabulated for comparison, but unfortunately, at this temperature neither method works very well because  $k_a[O_2]$  and  $k_{-a}$  are not well-separated. The results are given in Table S1 (Supporting Information) where we report the slope of  $k_a[O_2]$  vs  $[O_2]$  plots constrained to pass through the origin, and the mean of the  $k_{-a}$  values. Again,  $k_{R1}$  is obtained by dividing  $k_a$  by  $[N_2] + [O_2] \approx [N_2]$  and is listed in Table 1.

The present rate constants can be summarized as  $k_{\rm R1}=1.07 \times 10^{-30} (T/1000~{\rm K})^{-0.733}~{\rm cm}^6~{\rm molecule}^{-2}~{\rm s}^{-1}~{\rm over}~750-1320~{\rm K}.$  They are in reasonable accord with the prior determinations up to 1100 K plotted on Figure 6 but the rate coefficients do not



**Figure 6.** Arrhenius plot for the reaction K + O<sub>2</sub> + N<sub>2</sub>  $\rightleftharpoons$  KO<sub>2</sub> + N<sub>2</sub>. The symbols denote the experimental data from Husain and Plane, Silver et al., Husain et al., Plane et al. and from the present work. The dashed line shows a best fit to the present data ( $k_{\rm Rl} = 1.07 \times 10^{-30} (T/1000 \ {\rm K})^{-0.733} \ {\rm cm}^6 \ {\rm molecule}^{-2} \ {\rm s}^{-1} \ (750-1320 \ {\rm K}), \ {\rm and the solid line shows the recommended} \ k_{\rm Rl} \ {\rm of } 5.5 \times 10^{-26} T^{-1.55} \ {\rm exp}(-10/T) \ {\rm cm}^6 \ {\rm molecule}^{-2} \ {\rm s}^{-1} \ {\rm over } 250-1320 \ {\rm K}.$ 

extrapolate well to lower temperatures. An overall fit to the data of the present work together with those of Husain and Plane, <sup>32</sup> Husain et al., <sup>33</sup> and Plane et al. <sup>34</sup> leads to a recommended  $k_{\rm R1}$  of  $5.5 \times 10^{-26} T^{-1.55} \exp(-10/T) \, {\rm cm}^6$  molecule <sup>-2</sup> s <sup>-1</sup> over 250 – 1320 K. An error limit of a factor of 1.5 includes most of the present and past measurements.

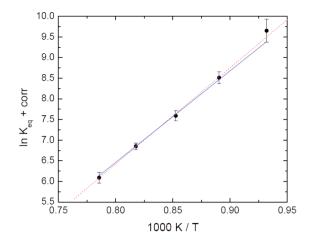
The ratio  $k_a/k_{-a}$  equals the concentration equilibrium constant  $K_{c}$ , which is listed in Table 2, along with the

Table 2. Equilibrium Constants Derived from Forward and Reverse Kinetics (See Text)

T/K	$K_c/10^{-16}$ cm <sup>3</sup> molecule <sup>-1</sup>	$K_{ m eq}$ std state 1 bar	correction	$ln(K_{eq}) + corr$	$\sigma^b$
1073	23.5	$1.59 \times 10^{4}$	-0.016	9.65	0.28
1123	7.87	$5.08 \times 10^{3}$	-0.017	8.51	0.14
1173	3.28	$2.03 \times 10^{3}$	-0.021	7.59	0.12
1223	1.64	971	-0.027	6.85	0.08
1273	0.799	455	-0.031	6.09	0.13
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"Equal to  $(\Delta H_{\rm T}-\Delta H_{298})/RT-(\Delta S_{\rm T}-\Delta S_{298})/R$ . "Statistical uncertainty in  $\ln(K_{\rm eq})$ .

thermodynamic equilibrium constant  $K_{\rm eq}$  based on unit activity for a standard pressure of 1 bar. A van't Hoff plot for  $K_{eq}$  yields thermodynamic information for reaction R1. A potential complication is the temperature dependence of  $\Delta H$  and  $\Delta S$ . A correction term to  $\ln K_{\rm eq}$  of  $(\Delta H_{\rm T} - \Delta H_{298})/RT - (\Delta S_{\rm T} \Delta S_{298}$ )/R was added so that the slope and intercept of the van't Hoff plot in Figure 7 correspond to  $-\Delta H_{298}/R$  and  $\Delta S_{298}/R$ , respectively. This small correction was derived via statistical mechanics from the experimental properties of K and  $O_2$ , <sup>46</sup> the  $KO_2$  vibrational frequencies of 1109, 307, and 304 cm<sup>-1 47</sup> and the ab initio  $C_{2\nu}$  geometry of Vasiliu et al., <sup>40</sup> a K-O distance of  $2.40 \times 10^{-10}$  m, and a OKO angle of 32.5°. The correction varied from -0.016 at 1073 K to -0.031 at 1323 K. The unconstrained linear fit corresponds to a second-law analysis and yields  $\Delta S_{298} = -101.7 \pm 9.9 \text{ J K}^{-1} \text{ mol}^{-1}$  and  $\Delta H_{298} =$  $-193.8 \pm 11.9$  kJ mol<sup>-1</sup>. The error limits are  $2\sigma$  and are purely the statistical uncertainty of the fit. A third-law analysis constrains the intercept to the separately estimated  $\Delta S_{298}$  = 93.6 J K<sup>-1</sup> mol<sup>-1</sup> and yields  $\Delta H_{298} = -184.2 \pm 0.5$  kJ mol<sup>-1</sup>.



**Figure 7.** van't Hoff plot of  $K_{\rm eq}$  for  $K + O_2 \rightleftharpoons KO_2$ . A second-law fit is shown as the dashed red line and a third-law fit is shown as the solid blue line.

The thermodynamic parameters agree between both methods, but as expected, the third-law method is more precise. Combined with  $\Delta_i H_{298} = 89.0 \pm 0.8 \text{ kJ mol}^{-1}$  for atomic potassium, <sup>46</sup> the corresponding heat of formation of KO<sub>2</sub> is  $\Delta_i H_{298} = -95.2 \pm 4.1 \text{ kJ mol}^{-1}$ . The experimental vibrational frequencies for KO<sub>2</sub> yield  $H_{298} - H_0 = 12.14 \text{ kJ mol}^{-1}$ , and together with  $H_{298} - H_0$  of 6.20 and 8.68 kJ mol $^{-1}$  for K and O<sub>2</sub>, respectively, <sup>46</sup> we obtain the 0 K bond strength  $D_0(\text{K}-\text{O}_2)$  as 181.5 kJ mol $^{-1}$ . This value is compared with experimental and theoretical results from the literature in Table 3.

Table 3. Reported Bond Dissociation Energies for KO<sub>2</sub> and Comparison with the Present Values

reference	$D_0/\mathrm{kJ}~\mathrm{mol}^{-1}$	method
Jensen <sup>36</sup>	$170 \pm 30$	flame study
Figger et al. <sup>37</sup>	$188 \pm 10$	molecular beam study
Hynes et al. <sup>18</sup>	$174 \pm 20$	flame study
Plane et al. <sup>34</sup>	≥203	time resolved decay (LIF)
Plane et al. <sup>34</sup>	154	theory
Partridge et al. <sup>38</sup>	$170 \pm 8$	theory
Lee and Wright <sup>39</sup>	$168 \pm 3$	theory
Vasiliu et al. <sup>40</sup>	173	theory
Present work	$181.5 \pm 4$	CPFAAS
Present work	177.9	theory

There remains the issue of systematic error. A rough-and-ready approach is based on the ca. factor of 1.5 differences between literature determinations of  $k_{\rm a}$  which, if propagated as a factor of 1.5 variation in  $K_{\rm eq}$  imply a variation of  $\pm 4$  kJ mol<sup>-1</sup> in  $\Delta H_{298}$ . With this as an uncertainty limit, the 298 K bond strength is 8.7 kJ mol<sup>-1</sup> above that calculated by Vasiliu et al.<sup>40</sup> and is therefore significantly different.

#### **AB INITIO ANALYSIS**

It is common to exclude core electrons from the correlation treatment in ab initio analysis. For a potassium atom, these would be the 1s, 2s, 2p, 3s, and 3p orbitals. However, in an ionic compound like  $KO_2$  the potassium loses its only valence 4s electron so the remaining interactions involve the core electrons. Indeed, the 3s and 3p atomic orbitals may be higher in energy than the oxygen orbitals. For this reason it has become standard practice in calculations on alkali metals to

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Table 4. Computed Reaction Enthalpies at 0 K in the KO<sub>2</sub> System, with Contributions from Each Term, in kJ mol<sup>-1</sup>

reaction	$\Delta(CCSD(T)/aug\text{-}cc\text{-}pwCVQZ)$	$\Delta(CCSD(T)/aug\text{-}cc\text{-}pwCV5Z)$	$\Delta E_{ m inf}$	$\Delta E_{ m zpe}$	$\Delta E_{ m rel}$	$\Delta E_{ m final}$
$D_0(ions)$	555.32	556.27	557.27	-3.92	0.91	553.35 <sup>a</sup>
$D_0$	175.64	177.96	180.39	-1.11	-1.36	177.92
IP(K)	416.58	416.67	416.76	0.00	1.39	418.15
$-EA(O_2)$	-36.91	-38.36	-39.88	-2.81	0.88	$-42.73^{a}$
<sup>a</sup> Includes empirical $-0.91$ kJ mol <sup>-1</sup> correction to the energy of $O_2^-$ for splitting in its $^2\Pi$ ground state. <sup>53</sup>						

incorporate some of these inner orbitals in the correlation space<sup>48</sup> and, in particular, Vasilu et al.<sup>40</sup> included the 3s and 3p electrons in their correlation treatment at the coupled cluster level, CCSD(T), for potassium compounds.

In this work the geometries of O<sub>2</sub>, O<sub>2</sub>, and KO<sub>2</sub> were obtained using coupled cluster theory and the large aug-ccpwCVQZ atomic basis set for oxygen<sup>49</sup> and specially constructed for potassium by Peterson and co-workers, 50 with all the electrons correlated. The optimized O-O distances in the three molecules are 0.121, 0.135, and 0.135 nm, consistent with a K<sup>+</sup>O<sub>2</sub><sup>-</sup> species where there is charge transfer to the oxygen. In KO<sub>2</sub> the computed K-O distance is 0.240 nm. Then single-point energies were derived with CCSD(T)/aug-ccpwCV5Z theory, <sup>50</sup> again with all electrons correlated, followed by a scalar relativistic correction Erel (mass-velocity plus Darwin terms) performed at the CISD/aug-cc-pwCVQZ level of theory. These calculations were made with the Molpro 2010 program, 51 and the results are listed in Table S2 (Supporting Information). The CCSD(T) results with  $\zeta = 4$  and 5 were extrapolated to the infinite basis set limit via the relation:<sup>52</sup>

$$E_{\rm inf} = (125 \cdot E_5 - 64 \cdot E_4)/61 \tag{14}$$

Vibrational zero-point energies  $E_{\rm zpe}$  were derived from experimental data (KO<sub>2</sub>; <sup>47</sup> O<sub>2</sub> and O<sub>2</sub><sup>-53</sup>). The final energies ( $E_{\rm inf}+E_{\rm rel}+E_{\rm zpe}$ ) were employed to derive 0 K enthalpy changes for the reactions in Table 4, which are coupled via the Hess cycle

It may be seen that that the ionization potential of K is close to converged with the aug-cc-pwCVQZ basis set and that the final extrapolation is very small, only 0.09 kJ mol<sup>-1</sup>, and with the relativistic correction we compute  $IP(K) = 418.15 \text{ kJ mol}^{-1}$ , which is 0.66 kJ mol<sup>-1</sup> below the experimental value of 418.81 kJ mol<sup>-1.56</sup> Similarly, the dissociation enthalpy of KO<sub>2</sub> to ions is nearly converged with the  $\zeta$  = 4 basis set. The other two processes involve extrapolations of only ca. 2 kJ mol<sup>-1</sup> so application of different extrapolation strategies would have little impact on  $\Delta E_{\text{final}}$ . The direct calculation of  $D_0$  yields 177.9 kJ mol<sup>-1</sup>, which is somewhat larger than the 172.8 kJ mol<sup>-1</sup> derived by Vasiliu et al.<sup>40</sup> using a similar computational method. The critical difference may be the use of a frozen inner core of electrons in the prior work vs the all-electron calculations here. The 5 kJ  $\text{mol}^{-1}$  increase in  $D_0$  more closely brings theory and experiment,  $184.2 \pm 4.0 \text{ kJ mol}^{-1}$ , into accord. The electron affinity of oxygen is reproduced well at the present level of theory, which yields EA(O<sub>2</sub>) about 0.7 kJ mol<sup>-1</sup> too low when compared to the experimental value of 43.38  $\pm$  0.18 kJ  $\text{mol}^{-1.54,55}$  A similar modest error might exist in KO $_2$  where a superoxide moiety is present. An alternative assessment of  $D_0$  is thus equal to  $D_0(ions) - IP(K) + EA(O_2)$ . With experimental values for the latter two items, this also yields  $D_0 = 177.9 \text{ kJ}$ 

 $\text{mol}^{-1}$ , confirming the calculation via neutrals. The errors in IP(K) and  $\text{EA}(O_2)$  have canceled.

#### CONCLUSIONS

The collinear photofragmentation and atomic absorption spectroscopy (CPFAAS) method has been applied to generate and monitor atomic potassium in the presence of oxygen. Rate constants for the third-order addition process were determined over 748–1323 K, which compare well with prior data obtained at up to 1100 K. The short time scale of the detection method permits direct observation of equilibration in the K +  $O_2$  =  $KO_2$  system for the first time. A third-law analysis yields the K $O_2$  bond dissociation enthalpy, which is 9 kJ mol $^{-1}$  greater than the most recent ab initio calculations in the literature. We find that correlating all the electrons in coupled cluster/infinite basis set calculations roughly halves the discrepancy.

### ASSOCIATED CONTENT

## S Supporting Information

Supplementary Table S1 reports the results of the kinetic analyses for K atom loss in the presence of oxygen in a nitrogen bath gas. Supplementary Table S2 summarizes ab initio energies of K,  $O_2$ ,  $KO_2$ ,  $K^+$ , and  $O_2^-$ . This material is available free of charge via the Internet at http://pubs.acs.org.

## AUTHOR INFORMATION

# Notes

The authors declare no competing financial interest.

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