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**Superconducting Super Collider
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Abstract

The location of a liner inside the beam tube is one of the options considered for the Super Colliders (SSC–Superconducting Super Collider and LHC–Large Hadron Collider). The liner could serve as a synchrotron radiation intercept and also help enhance the vacuum. A definite distribution of holes or slots is required to be located on the liner for pumping out the desorbing gases. There will be wake fields propagating within the liner due to diffraction at discontinuities (holes, slots, bellows, *etc.*) following the incident beam fields. The effect of these wake fields can be minimized by adopting the least number of pumping holes/slots required and through an optimal choice of hole/slot shape and size. The effect of the wake fields on the beam may be expressed through coupling impedances defined proportional to the corresponding forces integrated through distance per unit charge. It is necessary to compute the impedance of holes and slots and determine the scaling of the impedance with the dimensions of the hole/slot and the liner, in order to optimize the choice of pumping holes/slots. The coupling impedances of slots and holes have been calculated here using the code MAFIA and the scaling assessed. The results compare favorably with existing analytical results.

1.0 INTRODUCTION

The introduction of a liner inside the beam tubes of super colliders (the Superconducting Super Collider–SSC, and the Large Hadron Collider–LHC) serves many purposes. The liner could serve as a synchrotron radiation intercept. If the liner could be maintained at a high temperature, the incident energy could be removed efficiently. The discontinuities in the liner will result in wake fields propagating inside the liner. These fields will act on successive bunches and could result in bunch lengthening, instabilities and emittance growth. The liner will help enhance the vacuum; one needs to provide an appropriate number and distribution of slots/holes on the surface of the liner for removing the desorbing gases. We have the advantage of optimizing and minimizing the number of holes and thus minimize the effect of the wake fields on the beam.

The effect of the wake fields on the beam bunches may be expressed quantitatively through the longitudinal or transverse coupling impedances of the slots or holes, which are defined proportional to the integrated force (longitudinal or transverse) per unit charge.^{1–4} The coupling impedance of round holes on the liner of LHC and SSC have been studied analytically by Gluckstern⁵ and Kurennoy³ for low frequencies, where the dimension of the hole is much smaller than the wave length of the incident field. Kurennoy⁶ has obtained a formula for the coupling impedance of slots using the expressions of magnetic and electric polarizabilities from McDonald.^{7,8} We have computed here the coupling impedances of slots and holes of various dimensions using the code MAFIA.⁹ We have obtained scaling relations for the coupling impedances and compared them with the values obtained using expressions from Gluckstern and Kurennoy.^{3,5,6}

2.0 DESCRIPTION OF THE PROBLEM

A schematic of the beam pipe and the liner is shown in Figure 1. The liner of inner radius a and thickness Δ is located inside the beam tube of radius b . A slot of length w and width d is located on the liner. The center of the slot is situated at $z = 0.0$. In the case of round holes we will denote the diameter of the hole by d . The coordinate system is shown in Figure 1. The longitudinal impedance is defined as follows:³

$$Z(\omega) = -\frac{1}{q} \int_{-\infty}^{\infty} E_z(r=0, \theta=0) e^{jkz} dz \quad (1)$$

where $k = \frac{\omega}{c}$.

TIP-03612

Figure 1. Slot details and coordinate system.

The calculations for wake fields were done using Version 31f of the code T3310 in the MAFIA group (see Appendix for sample input). T3310 was run exclusively on an IBM 560 workstation. The impedances were calculated on a Sun SPARC station with the in-house post-processor MW2FFT designed to read the wake fields, sigma, beta, offsets, length and time variables for calculating the Z directly from the T3310 print file with the T3310 input file prepended. The dataset name and the number of holes is entered interactively and then the impedance is calculated and the output stored for plotting. Details of calculation of the impedance from MAFIA output can be found in Reference 11.

An example of the geometry for the cases run is shown in Figure 1(a). The inner radius of the liner $a = 1.65$ cm, the thickness of the liner $\Delta = 1$ mm, the radius of the beam tube $b = 2.15$ cm and the total length of the structure is 20 cm. The mesh size was 0.5 mm in

all cases. The beam modeled for all cases was Gaussian with a $\sigma = 0.25$ cm extending up to 5σ 's in the positive and negative z directions. In the case of the transverse impedance, the beam was offset 1 mm from the axis in the positive x and y directions. In the case of the longitudinal wakes alone, one quarter of the structure was modeled and the length increased to 50 cm. For the cases where the radius a of the liner was varied, the thickness Δ was maintained at 1 mm and the air gap between the liner and the beam tube was maintained at 4 mm.

Figure 1(a). 3D plot of the slot distribution, 20-cm liner with 32 2×12 slots, randomly distributed.

All the wake fields were calculated with irregular distributions of holes or slots. For the case of longitudinal wake fields and impedances 184 holes were modeled except for the 2×12 mm and 2×20 mm cases, where only 60 slots were simulated. For the transverse wake fields and impedances, 80 openings were simulated for all but the cases with the two longest slots where only 32 slots were used. The strategy was to incorporate as many openings as possible for the strongest possible signal with the length in z as long as could be accommodated within the limitations of the code.

2.1 The Longitudinal Coupling Impedance of Round Holes

The expression for the longitudinal coupling impedance of holes at low frequencies obtained by Gluckstern and Kurennoy^{5,6} is:

$$Z = \frac{jZ_0 k d^3}{6\pi^2 a^2} \quad (2)$$

where, $Z_0 = 120\pi \Omega$ is the impedance of free space. In order to check the variation of the longitudinal impedance of holes with the radius of the liner a , computations were carried with MAFIA, with randomly distributed 4-mm holes with the liner radii of 1.35, 1.65 and 1.95 cm. The impedance varies linearly with the frequency in the range 0–5 GHz (Figure 2). The impedances at a frequency of 5.27 GHz are shown in Table 1. The values in the fourth column of Table 1 calculated with a a^{-2} dependence compare favorably with the values in the third column obtained from MAFIA. The impedance results for round holes are shown in Figure 3 and Table 2. It should be remembered that the round hole is approximated by a polygon with maximum number of sides possible within the limitations of the code and the computer memory. The impedance is again found to vary linearly with the frequency in the range 0 to 5 GHz. The impedance was scaled with a d^3 dependence with the impedance of the 3-mm hole as a reference and the resulting values are shown in column 4 of Table 2. These compare favorably with the MAFIA results in column 3. The values in column 4 were obtained with the Gluckstern/Kurennoy formula, Eq. (2) and are about two times higher. The difference can be explained by the fact that Eq. (2) is valid only for a very thin wall. The thickness corrections have been calculated for round holes by Gluckstern,⁵ and they reduce the impedance values from those for the case of a thin wall. The last column of Table 2 shows the impedance using Eq. (2) with thickness corrections applied. The MAFIA results are in good agreement with these corrected impedance values. Also shown in Figure 3 are experimental values of the longitudinal coupling impedance for a 3-mm hole.¹⁰ These values are found to be marginally higher than those obtained from MAFIA computations.

Figure 2. Variation of the longitudinal impedance with the liner radius.

Table 1. Variation of the Longitudinal Impedance with the Radius of the Liner.

Liner I.D. (cm)	Frequency (GHz)	Impedance (mohms)	$Z = Z_{1.35}(\frac{1.35}{d})^2$ (mohms)
1.35	5.270	18.32	18.32
1.65	5.270	12.02	12.26
1.95	5.270	8.936	8.780

Figure 3. Longitudinal coupling impedance of holes.

Table 2. Longitudinal Coupling Impedance of Holes.

Hole Dia. (mm)	Freq. (GHz)	Imped. (mohms)	$Z = Z_{3 \text{ mm}}(\frac{d}{3})^3$ (mohms)	Imped. Eq. (2) (mohms)	Corrected Imped. (mohms)
2	4.977	1.560	1.391	2.447	1.390
3	4.977	4.696	4.696	8.260	4.870
4	4.977	11.38	11.13	19.58	12.100
5	4.977	22.76	21.74	38.24	25.200

2.2 The Longitudinal Coupling Impedance of Slots

Kurennoy⁶ has obtained the following analytical expressions for the longitudinal coupling impedance of a slot. From the general expressions of References 3, 5:

$$Z = jZ_0 k \frac{(\alpha_m + \alpha_e)}{4\pi^2 a^2}, \quad (3)$$

using the magnetic and electric polarizabilities α_m, α_e from McDonald,^{7,8} the longitudinal coupling impedance of a rectangular slot with length w and depth d for the case $w > d$ is

$$Z = jZ_0k \frac{d^3(0.1814 - 0.0344d/w)}{4\pi^2a^2}. \quad (4)$$

When the slot ends are rounded the expression for impedance becomes

$$Z = jZ_0k \frac{d^3(0.1334 - 0.0500d/w)}{4\pi^2a^2}. \quad (5)$$

For the case of a rectangular slot with $d > w$, the following equations apply.

$$Z = jZ_0k \frac{d^3}{4\pi^2a^2} \left(\frac{0.132}{\ln(1 + 0.66\frac{d}{w})} - \frac{\pi}{16} \left(\frac{w}{d} \right)^2 \left(1 - 0.57\frac{w}{d} + 0.14 \left(\frac{w}{d} \right)^2 \right) \right). \quad (6)$$

For a slot with rounded ends and with $d > w$,

$$Z = jZ_0k \frac{d^3}{4\pi^2a^2} \left(\frac{0.187 + 0.052\frac{w}{d}(1 - \frac{w}{d})}{\ln(1 + 2.12\frac{w}{d})} - \frac{\pi}{16} \left(\frac{w}{d} \right)^2 \left(1 - 0.77\frac{w}{d} + 0.19 \left(\frac{w}{d} \right)^2 \right) \right). \quad (7)$$

MAFIA computations were carried out for various slots of widths w and depth d . The results for $d = 2$ mm and $w = 2, 6, 12$, and 20 mm are shown in Figure 4. The impedance is almost independent of the width w and this favorably compares with the predictions of Eqs. (4) and (5) which show very weak dependence on w . The impedances for $w = 2$ mm and $d = 2, 3, 4$, and 5 mm are shown in Figure 5 and Table 3. Shown in column 4 of Table 3 is the scaling exponent n obtained from $Z = Z_{3 \text{ mm}}(\frac{d}{3})^n$. Column 5 gives the values of the impedance calculated using Eq. (6). These values are about two times the values from MAFIA computations. This difference can again be explained by thickness corrections which are not included in Eq. (6). While the impedance is almost independent of w , it is found to vary as d^n with n being approximately equal to 2.8, as evidenced by the values in column 4. The impedances for slots with $w = 4$ mm and $d = 1, 2$, and 4 mm are shown in Figure 5 and Table 4. The impedances from Eq. (4) are again higher than the MAFIA results. Column 4 of Table 4 gives the scaling exponent obtained from $Z = Z_{2 \text{ mm}}(\frac{d}{2})^n$. The exponent is approximately 3.0 for $w = 4$ mm.

The effect of rounding the edges of slots is shown in Figure 6 using slots of $d = 2$, $w = 6$ mm and $d = 2$, $w = 12$ mm. The rounding of the edges of slots results in a decrease of impedance by a factor of about 1.3 and this is also born out by Eqs. (4) and (5).

Figure 4. Longitudinal impedance of slots with various widths, w .

Figure 5. Longitudinal coupling impedance of slots with various depths, d .

Table 3. Longitudinal Coupling Impedance of Slots ($w = 2$ mm).

Slot Dimns. (mm)	Freq. (GHz)	Imped. (mohms)	n	Imped. Eq. (6) (mohms)
2×2	4.977	2.139	2.845	4.360
3×2	4.977	6.779		13.030
4×2	4.977	14.98	2.756	28.070
5×2	4.977	26.46	2.666	50.270

Table 4. Longitudinal Coupling Impedance of Slots ($w = 4$ mm).

Slot Dimns. (mm)	Freq. (GHz)	Imped. (mohms)	n	Imped. Eq. (4) (mohms)
1×4	4.977	2.261	3.35	6.314
2×4	4.977	2.308		4.803
4×4	4.977	18.53	3.005	34.40

Figure 6. Longitudinal impedance for rectangular and rounded slots.

2.3 The Transverse Coupling Impedance of Slots

The transverse coupling impedance is defined as follows:³

$$\begin{aligned} \vec{Z}_t(\omega, \vec{r}, \vec{r}) = \lim_{r \rightarrow 0} \frac{j}{qr} \int_{-\infty}^{\infty} dz e^{jkz} \Big(\hat{n}_a (E_r - Z_0 H_\phi)(r, \phi, z; \omega) \\ + \hat{n}_\phi (E_\phi - Z_0 H_r)(r, \phi, z; \omega) \Big). \end{aligned} \quad (8)$$

The transverse impedance per round hole reduces from Eq. (8) to

$$Z_t = j \frac{Z_0}{24\pi^2} \frac{d^3}{a^4}. \quad (9)$$

In the case of slots with $w > d$ Eq. (8) reduces to

$$Z_t = j \frac{Z_0}{2\pi^2} \frac{d^3}{a^4} \left(0.1814 - 0.0344 \frac{d}{w} \right). \quad (10)$$

The transverse impedances (per hole or slot) computed from MAFIA for holes and slots are shown in Figures 7 and 8.

The d^3 dependence and k^0 dependence indicated by Eqs. (8) and (9) are corroborated by the MAFIA results.

Figure 7. Transverse impedance of holes.

Figure 8. (a) Transverse impedance of slots. (b) Transverse impedance of slots.

3.0 CONCLUSIONS

MAFIA computations were carried out for the longitudinal and transverse coupling impedances of slots/holes on the liners of super colliders. The impedances of round holes scale as d^3 and a^{-2} . The impedances of slots scale approximately as $d^{2.8}$ for $w = 2$ mm and $d^{3.0}$ for $w = 4$ mm and w^0 . Rounding the edges of slots results in a further decrease in impedance. One should obviously choose randomly placed slots of least d and maximal w and also round the edges of the slots, if this does not pose fabrication problems. The total number of slots will be determined from the required pumping area. There is good agreement between MAFIA calculations and analytical results with thickness corrections taken into account.

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APPENDIX
Input File

Following is the input file for m310 for calculating the longitudinal wakes for 60 2x12 slots using a quarter geometry.

```
#file t m a o stat=unk name=m ex
#file t p a o stat=unk ex
#file t l a o stat=unk ex
#general
text(1)='50cm liner with 60 2 x 12 slots, randomly distributed, July 1993'
text(2)='quarter geometry; bunch sigma=0.25cm'
#general scale=0.01
#mesh
xm 0.0 s43 2.15
ym 0.0 s43 2.15
zm -25.0 s 500 0.00 s500 25.0 ex
#brick
mat=1 vol= 0.0 +2.15 0.0 +2.15 -25.0 +25.0 ex
#ccyl
mat=0 fill=diag ori=z range=-25.0 +25.0 center 0. 0. rad=2.15
part=quarter which=+x+y ex
mat=1 center=0. 0. rad=1.75
part=quarter which=+x+y ex
mat=0 rad=1.65
part=quarter which=+x+y ex
#brick
mat=3 vol 0.000 0.100 1.650 1.750 -21.100 -19.900 ex
mat=3 vol 0.000 0.100 1.650 1.750 -18.900 -17.700 ex
mat=3 vol 0.000 0.100 1.650 1.750 -16.550 -15.350 ex
mat=3 vol 0.000 0.100 1.650 1.750 10.200 11.400 ex
mat=3 vol 0.000 0.100 1.650 1.750 -13.700 -12.500 ex
mat=3 vol 0.000 0.100 1.650 1.750 15.900 17.100 ex
mat=3 vol 0.000 0.100 1.650 1.750 18.100 19.300 ex
mat=3 vol 0.000 0.100 1.650 1.750 -5.250 -4.050 ex
mat=3 vol 0.000 0.100 1.650 1.750 -1.600 -0.400 ex
mat=3 vol 0.000 0.100 1.650 1.750 -11.500 -10.300 ex
mat=3 vol 0.000 0.100 1.650 1.750 -9.300 -8.100 ex
mat=3 vol 0.000 0.100 1.650 1.750 5.100 6.300 ex
mat=3 vol 0.000 0.100 1.650 1.750 0.600 1.800 ex
mat=3 vol 0.000 0.100 1.650 1.750 2.800 4.000 ex
mat=3 vol 0.000 0.100 1.650 1.750 7.300 8.500 ex
$
mat=3 vol 1.650 1.750 0.000 0.100 -13.600 -12.400 ex
mat=3 vol 1.650 1.750 0.000 0.100 11.050 12.250 ex
mat=3 vol 1.650 1.750 0.000 0.100 8.300 9.500 ex
mat=3 vol 1.650 1.750 0.000 0.100 -9.650 -8.450 ex
mat=3 vol 1.650 1.750 0.000 0.100 4.250 5.450 ex
mat=3 vol 1.650 1.750 0.000 0.100 -4.950 -3.750 ex
mat=3 vol 1.650 1.750 0.000 0.100 17.600 18.800 ex
mat=3 vol 1.650 1.750 0.000 0.100 -2.750 -1.550 ex
mat=3 vol 1.650 1.750 0.000 0.100 -17.600 -16.400 ex
mat=3 vol 1.650 1.750 0.000 0.100 -7.450 -6.250 ex
mat=3 vol 1.650 1.750 0.000 0.100 -0.550 0.650 ex
mat=3 vol 1.650 1.750 0.000 0.100 19.800 21.000 ex
mat=3 vol 1.650 1.750 0.000 0.100 1.650 2.850 ex
mat=3 vol 1.650 1.750 0.000 0.100 13.250 14.450 ex
mat=3 vol 1.650 1.750 0.000 0.100 -21.100 -19.900 ex
$
stop
```

Following is the input file for t3310 for calculating the longitudinal wakes for 60 2x12 slots using a quartergeometry.

```
printscreen
#file act=op type=log status=unknown name=t ex
  type=print act=op stat=unk ex
  type=maf act=op stat=old ex
#boun
  xboun=mag,elec yboun=mag,elec, zboun=waveguide,waveguide
#mat
  mat=1 type=elec
  mat=0 eps=1
  mat=3 eps=1
  show
#beam
  sigma=0.0025 xpos=0.00 ypos=0.00 charge=1.0 bunch=gauss return
#monitor
  symb=wz/bun field=wz
  xlo=0.00 xhi=0.00 ylo=0.00 yhi=0.00 slo=0.00 shi=0.512 ex
  show
#time
  mt = 4 nend=@integer00
  menu
#control
  check dumsave=no map=3
  execute
end
```


Following is the input file for p310 for calculating the longitudinal wakes for 60 2x12 slots using the whole geometry.

```
#file act=op type=log status=unknown name=p ex
  type=print act=op stat=unk ex
  type=maf act=op stat=old ex
#list
  sym=general ex
  items=1024 symb=wz/bun ex
stop
```

Following is the input file for m310 for calculating the transverse wakes for 32 2x12 slots using the whole geometry.

```
#file t m a o stat=unk name=m ex
#file t p a o stat=unk ex
#file t l a o stat=unk ex
#general
text(1)='20cm liner with 32 2 x 12 slots, randomly distributed, Oct. 1993'
text(2)='whole geometry; bunch sigma=0.25cm'
#general scale=0.01
#mesh
xm -2.15 s43 0.0 s43 2.15
ym -2.15 s43 0.0 s43 2.15
zm -10.0 s 200 0.00 s200 10.0 ex
#brick
mat=1 vol= -2.15 +2.15 -2.15 +2.15 -10.0 +10.0 ex
#ccyl
mat=0 fill=diag ori=z range=-10.0 10.0 center 0. 0. rad=2.15
part=full ex
mat=1 center=0. 0. rad=1.75
part=full ex
mat=0 rad=1.65
part=full ex
#brick
mat=3 vol -0.100 0.100 -1.750 1.750 -5.250 -4.050 ex
mat=3 vol -0.100 0.100 -1.750 1.750 -7.000 -5.800 ex
mat=3 vol -0.100 0.100 -1.750 1.750 -1.600 -0.400 ex
mat=3 vol -0.100 0.100 -1.750 1.750 -9.300 -8.100 ex
mat=3 vol -0.100 0.100 -1.750 1.750 5.100 6.300 ex
mat=3 vol -0.100 0.100 -1.750 1.750 0.600 1.800 ex
mat=3 vol -0.100 0.100 -1.750 1.750 2.800 4.000 ex
mat=3 vol -0.100 0.100 -1.750 1.750 7.300 8.500 ex
$
mat=3 vol -1.750 1.750 -0.100 0.100 8.300 9.500 ex
mat=3 vol -1.750 1.750 -0.100 0.100 -9.550 -8.350 ex
mat=3 vol -1.750 1.750 -0.100 0.100 4.250 5.450 ex
mat=3 vol -1.750 1.750 -0.100 0.100 -4.950 -3.750 ex
mat=3 vol -1.750 1.750 -0.100 0.100 -2.750 -1.550 ex
mat=3 vol -1.750 1.750 -0.100 0.100 -7.450 -6.250 ex
mat=3 vol -1.750 1.750 -0.100 0.100 -0.550 0.650 ex
mat=3 vol -1.750 1.750 -0.100 0.100 1.650 2.850 ex
$
stop
```

Following is the input file for t3310 for calculating the transverse wakes for 32 2x12 slots using the whole geometry.

```
printscreen
#file act=op type=log status=unknown name=t ex
  type=print act=op stat=unk ex
  type=maf act=op stat=old ex
#boun
  xboun=elec,elec yboun=elec,elec, zboun=waveguide,waveguide
#mat
  mat=1 type=elec
  mat=0 eps=1
  mat=3 eps=1
  show
#beam
  sigma=0.0025 xpos=0.001 ypos=0.001 charge=1.0 bunch=gauss return
#monitor
  symb=wz/bun field=wz
    xlo=0.001 xhi=0.001 ylo=0.001 yhi=0.001 slo=0.00 shi=0.512 ex
  symb=wx/bun field=wx ex
  symb=wy/bun field=wy ex
  show
#time
  mt = 4 nend=@integer00
  menu
#control
  check dumsave=no map=3
  execute
end
```