Hydrodynamic Modeling of Tissue Ablation with a Free-electron Laser


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Hydrodynamic modeling of tissue ablation with a free-electron laser

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ABSTRACT

The Vanderbilt University free-electron laser (FEL) provides a continuously tunable ($\lambda = 2 - 10 \mu m$) source of pulsed IR radiation with a pulse structure unlike those of conventional lasers (a macropulse of $5 \mu s$ consisting of a train of $1 \text{ ps}$ micropulses at a frequency of $3 \text{ GHz}$). A numerical hydrodynamic code at Lawrence Livermore National Laboratory, known as LASTISSD, was used to model the ablation of tissue using the FEL. This study investigates the role of the FEL pulse structure by comparing the results from simulations using a time-averaged energy deposition and a pulsetrain energy deposition.

Keywords: free electron laser, tissue ablation, hydrodynamic modeling

1. INTRODUCTION

The Vanderbilt University free electron laser is a continuously tunable source of pulsed mid-IR radiation with a wavelength range of $\lambda = 2 - 10 \mu m$. Previous studies have suggested that by tuning the FEL to the vibrational mode of the amide-II bonds in protein ($\lambda = 6.45 \mu m$) the FEL is well suited for precise tissue cutting and ablation with minimal collateral damage.\textsuperscript{1} This original study has been followed by several investigations into the role of the FEL wavelength in tissue ablation,\textsuperscript{2-5} however, none of these studies have considered the effect of the FEL pulse structure in tissue ablation. Previously reported\textsuperscript{6} experimental results have been largely inconclusive, in part due to the ultrashort duration of the micropulses.

A diagram of the pulse structure of the FEL is seen in Figure 1. It consists of a macropulse of $4-6 \mu s$ at a repetition rate of up to $30 \text{ Hz}$. The macropulse is the envelope of a high frequency ($3 \text{ GHz}$) train of micropulses with a duration of about $1 \text{ ps}$, separated by approximately $350 \text{ ps}$. This pulse structure results in a laser that is capable of both high peak ($10 \text{ MW}$) and average ($100 \text{ kW}$) powers. If a laser pulse is shorter than the time necessary for heat to diffuse out of an irradiated volume, it is said to be thermally confined. Likewise, if the pulse is shorter than the time necessary for a stress wave to propagate out of the irradiated volume, it is said to be inertially confined. A diagram of these confinement conditions for many common laser systems appears in Figure 2. In it, the penetration depth $\delta$ is plotted against the pulse duration $\tau_L$ for the pulses of some common laser systems. The condition for thermal confinement is given by the line $\tau = \delta^2/4\alpha$, where $\alpha$ is the thermal diffusivity of the medium. As the pulse duration is further decreased, the condition for inertial confinement given by the line $\tau = \delta/\sigma$, where $\sigma$ is the speed of sound in the medium. It can be seen from Figure 2 that the FEL macropulse is thermally confined at all penetration depths except those below $\approx 1 \mu m$, which is only seen at wavelengths near the strong water absorption peak at $\lambda = 3.0 \mu m$. Further, both the FEL micropulses ($1 \text{ ps}$) and the micropulse separation ($350 \text{ ps}$) are short compared to the inertial confinement time for all penetration depths. This raises the possibility that large amplitude stress waves may be generated by the FEL micropulse structure.

In order to investigate the effects of the micropulse structure on a sufficiently short time scale, we turned to theoretical modeling using a numerical hydrodynamic code called LATISSD that is being developed at Lawrence Livermore National Laboratory (LLNL). The current study investigated the effect of the FEL micropulse structure on the laser-induced stress waves. We hypothesize that the results of ablation with the FEL can not be solely attributed to wavelength tunability and specific absorption in amide bands.

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Figure 1. Pulse structure of the FEL.

Figure 2. Confinement regions as a function of pulse duration for various laser pulses including the FEL macropulse. Modified from Welch et al. [7]
2. MODELING METHODS

LATIS3D is a subset of Kull, a larger simulation code at LLNL. Kull is a comprehensive physics package, based on finite volumes and written in the computer language C++, that includes light transport, fluid flow, materials response, and heat transfer modeling. The current study only considers the hydrodynamic response of the material, which is calculated using the standard thermodynamic conservation equation for mass, momentum, and energy:

\[
\frac{\partial p}{\partial t} = -\rho \mathbf{\nabla} \cdot \mathbf{v}, \quad (1)
\]

\[
\frac{\partial \rho v^k}{\partial t} = -\frac{\partial P}{\partial x^k} - \rho v^k \mathbf{\nabla} \cdot \mathbf{v} + \rho \mathbf{a}_k, \quad (2)
\]

\[
\frac{\partial \rho e}{\partial t} = -P \mathbf{\nabla} \cdot \mathbf{v} - \rho e \mathbf{a} \mathbf{\nabla} \cdot \mathbf{v}. \quad (3)
\]

We used a tabular equation of state of water to model the tissue and only sub-threshold fluences were initially used. The stress waves in the medium are generated by a time-dependent energy source deposition with a Beer's Law absorption distribution. Only one dimensional propagation is considered by making the laser spot radius \( r \) much larger than the penetration depth \( \delta \). Two types of laser irradiation schemes were considered: 1) a pulsetrain energy deposition that is similar the pulse structure of the FEL and 2) a time-averaged energy deposition that had an equivalent total energy as the pulsetrain, but delivered at a constant power level. These two pulse deposition schemes can be seen in Figure 3. For both cases, the laser spot radius \( r = 100 \) \( \mu \)m, and the penetration depth \( \delta = 10 \) \( \mu \)m, which is approximately the penetration depth of water at \( \lambda = 6.45 \) \( \mu \)m. The total energy delivered to the sample in both the pulsetrain deposition (Figure 3a) and the time-averaged deposition (Figure 3b) was \( E_{\text{tot}} = 50 \) \( \mu \)J which was deposited over the same pulse duration \( \tau_p = 50 \) ns. For the pulsetrain deposition, it is assumed that the individual micropulse are absorbed instantaneously, that is, the micropulse duration is short compared to the inertial confinement time. The energy contained within one micropulse was \( E = 0.3 \) \( \mu \)J, with a delay between micropulses \( \tau_d = 333 \) ps and a total of \( n = 150 \) pulses delivered. The numerical mesh consisted of 20 zones/\( \mu \)m.

3. RESULTS

The results from the model simulations appear in Figures 4, 5, and 6. Figure 7 shows the stress waves generated from both the pulsetrain and time-averaged energy deposition described in section 2. For both schemes, we see that the peak stress amplitudes are comparable, however in the pulsetrain deposition, it appears that there is a high frequency noise imposed on the stress waves. By looking at an expanded scale (Figure 5), we can see that the high frequency noise is well correlated with the pulsetrain. There are 150 pressure transients present and time delay between them is exactly the same as the delay between subsequent pulses (333 ps).

This correlation between the pressure transients and the delivered pulses is more clearly seen in Figure 6. In it, the total energy was the same as the previous simulations (\( E_{\text{tot}} = 50 \) \( \mu \)J) which was delivered on over the same duration (\( \tau_p = 50 \) ns). However, the number of pulses was reduced to \( n = 50 \) and the delay between pulses was increased to \( \tau = 1 \) ns. Again, we see that the pressure transients are well correlated with the pulses delivered, both in the total number (50) and in the delay between each pulse (1 ns).
Figure 4. Pressure amplitude as a function of tissue depth at multiple times for both the pulsetrain and time-averaged energy deposition schemes. The numerical grid is 200 \( \mu m \) deep.

Figure 5. Pressure amplitude as a function of tissue depth at multiple times for both the pulsetrain and time-averaged energy deposition schemes. The numerical grid is 100 \( \mu m \) deep.
4. DISCUSSION

In comparing the results from the pulsetrain and time-averaged energy depositions, we see that the peak stress wave amplitudes generated are the same, which is exactly what one would expect given that the average radiant exposure ($E_{\text{rad}}/t_0$) is constant for both cases. However, for the pulsetrain deposition, we see that large local pressure transients are generated. These local pressure transients create large pressure gradients that are on the order of $\frac{d\sigma}{dx} = 300 \text{ bar/\mu m}$. Such large pressure gradients, which have both a compressive and tensile component, may effect tissue on a cellular level by tearing cell membranes and other microstructures.

The data that has been presented shows that the micropulse structure has an effect on the stress waves that are generated by laser exposure. This suggests that the results of ablation with the FEL can not be solely attributed to wavelength its tunability and the selective absorption of multiple tissue components.

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