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NEW EQUATION OF STATE MODELS FOR HYDRODYNAMIC APPLICATIONS

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Two new theoretical methods for computing the equation of state of hot, dense matter are discussed. The ab initio phonon theory gives a first-principles calculation of lattice frequencies, which can be used to compare theory and experiment for isothermal and shock compression of solids. The ACTEX dense plasma theory has been improved to allow it to be compared directly with ultrahigh pressure shock data on low-Z materials. The comparisons with experiment are good, suggesting that these models will be useful in generating global EOS tables for hydrodynamic simulations.

INTRODUCTION

An equation of state (EOS) is required for any continuum mechanics simulation, and for processes involving high energy densities, the EOS needs a large range of the density and temperature. There is a longstanding need for more accurate EOS generation models and tabular representations. In this paper we discuss two new models which will be useful in generating accurate EOS tables for hydrodynamic codes.

New data on compressed states of matter are available from the diamond anvil cell and from strong shockwave sources. These data are now numerous enough to stimulate improvements in theory and detailed comparisons between experiments and theory. Two useful new theoretical methods are ab initio phonons and ACTEX.

AB INITIO PHONONS

Ab initio phonon theory is a method for computing lattice phonon frequencies within the electron band structure formalism. For a periodic atomic displacement corresponding to a given lattice wave vector, a self-consistent electron band-structure calculation using the perturbed Hamiltonian yields the harmonic energy and the corresponding lattice mode frequencies. We have carried out this calculation for carbon diamond using the plane wave method with the local density approximation. We have computed a small set of phonons over a range of densities and have averaged them into a density-dependent Einstein frequency. The sum of the vibrational free energy and static lattice energy provide a complete equation of state for solid diamond.

Comparison of theory and experiment is shown in Fig. 1 for the diamond room temperature isotherm and in Fig. 2 for the principal shock Hugoniot. The model predicts a normal density about 1% too large, and this gives a slight offset to the predictions. Remarkably, the model is in good agreement with shock data up to 6 Mbar, where diamond is predicted to melt. Hotter shock states can be obtained from porous diamond with starting densities below the normal density of 3.51 g/cc and the agreement here is also good. Evidently diamond is very nearly a harmonic solid with negligible contributions from anharmonic and electronic terms.

One of the remarkable results from the ab initio phonon theory is the first-principles prediction of the Grüneisen gamma function. This function is frequently used as an empirical parameter, since it is only poorly known from experiments. The ab
initio phonon theory has now made it possible to compute the Grüneisen function with much more confidence. The Grüneisen function for diamond is shown in Fig. 3.

FIGURE 1. Experimental room temperature isotherm for diamond (points) compared with ab initio phonon theory (curve).

FIGURE 2. Experimental shock Hugoniot for diamond (points) compared with ab initio phonon theory (curve).

FIGURE 3. Ab initio phonon theory prediction of the density dependence of Grüneisen gamma for diamond.

Ab initio phonon theory can be applied with confidence to low-Z sp-bonded materials where the plane wave technique works well. The use of pseudopotentials allows application of the theory to some higher-Z and d-bonded materials. The theory should be helpful in generating accurate Grüneisen functions for simple metallic, molecular, covalent, and ionic materials for use in constructing approximate Grüneisen functions for more complex solid materials.

ACTEX

ACTEX (Activity Expansion) is a dense plasma model based on the Abe cluster expansion of the partition function for a Coulomb gas of nuclei and electrons, combined with quantum corrections and a renormalization which includes a representation of atomic species in various states of ionization (5). The ACTEX EOS predictions are exact for weakly coupled plasmas at very high temperature, and become less accurate as the condensed matter regime is approached. ACTEX includes the electron shell ionization region which occurs as a density maximum on the Hugoniot. Recently published ultrahigh pressure Hugoniot data from nuclear explosion and pulsed laser sources overlap...
the region of validity of ACTEX and a detailed comparison between the two is now possible.

The comparison has been made for D, Be, CH, H₂O, Al, and SiO₂(6). The best overall comparison is with Al, for which nuclear explosion-driven shock experiments have been performed up to 4000 Mbar, where K and L shell ionization is occurring(7). The comparison is shown in Fig. 4. The ACTEX curve shows two large density maxima which correspond to the ionization of the K and L electron shells. The data have large errors and so the test of the theory is not rigorous, but the theory shows the expected form and appears to be semiquantitative in the 10 - 100 Mbar region.

New shock data on liquid deuterium using high energy pulsed lasers have revealed a sharp density maximum in the Hugoniot(8). This feature provides a very strong constraint on any theory of dense, dissociating hydrogen. ACTEX is compared with the data in Fig. 5. The agreement is very good in that ACTEX closely approximates the density and pressure of the experiment near the Hugoniot maximum. Since the ACTEX model does not include the diatomic molecular fluid, it cannot make predictions for the lower part of the Hugoniot curve. Fig. 5 also shows other model predictions for the shock Hugoniot of deuterium. It is clear that there are major discrepancies between theoretical models, largely due to our limited understanding of dissociation in dense fluids.

DISCUSSION

The ab initio phonon theory is accurate for the solid state and can be extended with corrections into the liquid state, but is valid only when the electronic excitations are negligible, i.e., T < T_F. ACTEX is a plasma theory valid for conditions where condensed matter interactions are small, i.e., T > T_F. At present we lack a single theory which covers the entire temperature range from cold solid to hot plasma. A possible candidate for such a theory is the hot band structure model, in which the thermally excited states of the condensed phase are included in the self-consistent LDA calculation. This model should pass smoothly from the T = 0 limit to the T = ∞ (one-component plasma) limit. Work on this model is underway at Livermore.

The two theories described here increase the precision of theoretical EOS modeling. The application of this work to hydrodynamic code calculations can best be done by incorporating the results into simpler global EOS generators such as QEOS(1) by using adjustable parameters to fit the
theoretical data as if it were experimental. Then smooth and consistent global EOS tables can be generated which incorporate the most accurate physics.

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