INTERFACIAL PROPERTIES AND MECHANICAL BEHAVIOR OF TITANIUM ALUMINIDES

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ABSTRACT

The role of various interfaces in deformation and fracture behavior of two-phase TiAl-Ti₃Al alloys is analyzed on the basis of the specific interfacial and surface energies determined from ab initio calculations. The propensity of twinning observed in these alloys is consistent with the low true-twin boundary energy. The strong plastic anisotropy reported in TiAl polysynthetically twinned (PST) crystals is attributed partly to the localized slip along lamellar interfaces, thus lowering the yield stress for soft orientations. Interfacial fracture energies are estimated to be the highest for the α₂/γ lamellar boundary and the lowest for the 120° rotational γ/γ boundary. The fracture mode mixity plays an important role in the crack-tip plasticity by ordinary slip and true-twinning, leading to translamellar and interfacial fracture.

INTRODUCTION

The majority of structural materials successfully developed and used for high-temperature structural applications are two-phase or multiphase systems. This is because interfacial structures and properties resulting from phase separation or decomposition can offer many unique microstructural advantages in thermodynamic stability, directional alignment, and dispersion of component phases. One outstanding case in point is γ'/γ two-phase single crystalline nickel-base superalloys. Recently, another intermetallics-based system which has been the focus of extensive research and development is gamma titanium aluminides [1,2]. In this case of titanium-rich two-phase TiAl-Ti₃Al alloys, significant advances have been made in understanding the role of interfaces in deformation and fracture behavior of fully lamellar microstructure, due largely to the two significant contributions: (a) controlled experimental investigations using the so-called polysynthetically twinned (PST) crystals, e.g., [3,4] and (b) interpretive and predictive capability of computational approach for bulk, defect and interfacial properties, e.g., [5,6]. It is the latter which is the focus of this paper.

The purpose of this paper is, first, to summarize the calculated results of surface and interfacial (planar faults) energies of two-phase TiAl-Ti₃Al alloys and, second, to discuss the role of interfaces in deformation and fracture of PST TiAl crystals.

LAMELLAR MICROSTRUCTURE

Formation of lamellar microstructure in gamma titanium aluminides is best described with the aid of a partial Ti-Al phase diagram [7] as shown in Fig. 1. The single-phase α-field extends up to 1450°C in the near equiatomic composition. Because of this single phase field, in which aluminum is completely in solid solution with titanium of the h.c.p. structure, a variety of microstructure consisting of γ and α₂ phases can be obtained in the composition range of 43-50 at. % Al using different cooling rates [8]. The crystal structures of γ-phase TiAl (L₁₀ type) and α₂-phase Ti₃Al (D₀₁₅ type) are shown in Fig. 1. When a two-phase TiAl alloy of near-equatomic composition is
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prepared by usual ingot-metallurgy methods, the γ-phase precipitates from the α-phase producing a lamellar structure which is composed of the transformed γ and remaining α lamellae. Gamma lamellae are formed in such a way that the close-packed planes and directions in the γ-phase are matched parallel to the corresponding planes and directions in the α-phase, satisfying the so-called Blackburn relationship [9],

\[ \{111\}_\gamma // (0001)_\alpha \quad \text{and} \quad <110>_{\gamma} // <1120>_{\alpha} \]  

In the near-equiatomic composition, the ordering of α → α₂ usually occurs after the formation of a lamellar structure. However, nucleation and growth of γ lamellae can be preceded by the ordering of the α-phase when two-phase alloys with 40-44 at. % Al are cooled from the α single-phase field at fairly rapid cooling rates [10,11]. In this case, the γ lamellae precipitate out of the α₂ matrix. In any case, whichever the sequence of transformation is, the γ lamellae are observed to form by obeying the crystallographic habit relationship of Eq. (1). The microstructure of a PST crystal [3] is equivalent to that of a single-crystalline grain of fully lamellar polycrystals.

Figure 2(a) shows the atom stacking sequence of ABC on the (111) plane of the L1₀ structure viewed on the (111) plane, wherein the three different fault vectors, \( b_i \), are described. Figure 2(b) shows schematically how three different kinds of planar faults are created at three different types of γ/γ interfaces. When the angle of rotation, \( \theta \), and the fault shift vector, \( f \), are both zero, the top and bottom halves together constitute the reference state of a single crystal, i.e., the total internal energy is set to zero.

Crystallographic descriptions for each of \( \theta = 60, 120, \) and 180° γ/γ interfaces and their relative energies have been discussed by Rao et al. [12] on the basis of Bollman's O-lattice theory and an empirical Embedded Atom Method (EAM). The interfacial energies of these γ/γ variants were determined from first-principles local-density-functional (LDF) calculations including atomic relaxation near the interfaces.
Fig. 2(a). Atomic stacking (ABC) sequence on the (111) plane of the L1₀ structure, and (b) Schematic illustration of translation and rotation operations.

THEORETICAL METHODS

The interfacial energies were determined from first-principles local-density-functional (LDF) calculations. The full-potential linearized augmented plane-wave (FLAPW) method [13] was used to solve LDF equations. There is no shape approximation to the potential and charge density. The uniqueness of these features makes it possible to determine the energetics associated with shape deformations and lattice imperfections accurately. In this case for interfaces, angular momentum components up to l = 8 and approximately 60 plane waves per atom are used for expansion of wave functions. Relaxed structures of interfaces were optimized by calculating Hellmann-Feynman forces acting on the atoms.

For the calculation of γ/γ lamellar interfacial energies, supercell sizes of 5 x 5 (i.e., repeated layer stacking sequence of 5 layers of TiAl separating the interfaces) were used. For the calculation of antiphase boundary (APB) and complex stacking fault (CSF) energies in bulk TiAl, supercell sizes with 12 and 11 layer separating adjacent interfaces were used.

ENERGIES OF INTERFACES

γ/γ Interfaces

All the calculated interfacial energies in Table 1 are the values obtained after atomic relaxation. Fault energies calculated for the three kinds on the (111) plane, i.e., APB with \( f = \mathbf{b}_1 \cdot \mathbf{b}_3 \) or \( \mathbf{b}_2 \cdot \mathbf{b}_3 = <101>/2^* \), superlattice intrinsic stacking fault (SISF) with \( f = \mathbf{b}_3 = [112]/6 \), and CSF with

*The mixed <uvw> notation is used here to differentiate the first two indices from the third because of the tetragonality of the L1₀ structure.
### Table I. Interfacial Energies of $\gamma/\gamma$ Lamellar Boundaries in TiAl (in Units of mJ/m$^2$)

<table>
<thead>
<tr>
<th>Interface type</th>
<th>$\theta$</th>
<th>$f = 0$</th>
<th>$\frac{1}{2}&lt;101&gt;$ APB</th>
<th>$\frac{1}{6}[\overline{1}12]$ SISF</th>
<th>$\frac{1}{6}&lt;\overline{2}11&gt;$ CSF</th>
</tr>
</thead>
<tbody>
<tr>
<td>Bulk</td>
<td>0°</td>
<td>0</td>
<td>560</td>
<td>90</td>
<td>410</td>
</tr>
<tr>
<td>Pseudo-twin</td>
<td>60°</td>
<td>270</td>
<td>270</td>
<td>270</td>
<td>270</td>
</tr>
<tr>
<td>Rotational</td>
<td>120°</td>
<td>250</td>
<td>250</td>
<td>280</td>
<td>280</td>
</tr>
<tr>
<td>True-twin</td>
<td>180°</td>
<td>60</td>
<td>550</td>
<td>60</td>
<td>550</td>
</tr>
</tbody>
</table>

$f = b_1$ or $b_2 = <\overline{2}11>/6$, are listed in the first row ($\theta = 0$). In the APB, SISF, and true-twin boundary energies of $E_{\text{APB}} = 560$, $E_{\text{SISF}} = 90$, and $\Gamma_T = 60$ mJ/m$^2$ reported earlier [5], the relaxation effect was included only for the APB. Since there is no change in the nearest-neighbor atomic coordination at the SISF, superlattice extrinsic stacking fault (SESF), and true-twin interfaces, atomic relaxation at these fault interfaces is assumed to be negligibly small. The more refined recent calculation [14] gives an APB energy which is slightly increased from the previously reported value. With the inclusion of relaxation energy, the CSF energy is reduced from $E_{\text{CSF}} = 500$ mJ/m$^2$ to 410 mJ/m$^2$. Woodward et al [15] reported from their LDF calculations with the layered Korringa Kohn Rostoker (LKKR) method that $E_{\text{APB}}$, $E_{\text{CSF}}$, $E_{\text{SISF}}$, and $E_{\text{SESF}}$ energies are 670, 280, 110, and 110 mJ/m$^2$, respectively.

Interfacial energies for the three different types, i.e., pseudo-twin ($\theta = 60°$), “rotational” ($\theta = 120°$), and true-twin ($\theta = 180°$), and true-twin ($\theta = 180°$), are listed in the first column ($f = 0$) of Table I. The pseudo-twin boundary energy of $\Gamma_P = 300$ mJ/m$^2$ [16] is reduced to 270 mJ/m$^2$ after relaxation. At the pseudo-twin ($\theta = 60°$) and rotational ($\theta = 120°$) boundaries, while both $E_{\text{APB}}$ and $E_{\text{CSF}}$ are reduced markedly, by factors of about two, as compared to those in the bulk, $E_{\text{SISF}}$ is increased by a factor of three. At the true-twin boundary, on the other hand, changes in the fault energies are relatively small, with slight increases in both $E_{\text{APB}}$ and $E_{\text{CSF}}$ and a decrease in $E_{\text{SISF}}$. These values are consistent with more frequent observation of true-twin type lamellar interfaces, in two-phase TiAl alloys of binary compositions, compared with the pseudo-twin and rotational types.

Degeneracies of fault energies noted in Table I are due to geometrically equivalent characteristic patterns of interfaces resulting from certain combinations of rigid-body translations and rotations according to the O-lattice theory [12]. An example of these degeneracies can be described with the aid of Fig. 3, where the C-layer of atoms have been rotated and translated with reference to the B-layer. Figure 3(b) shows the geometric pattern of interfaces by $\theta = 60°$ and $f = 0$, and Fig. 3(c) shows that by $\theta = 60°$ and $f = b_3$. These two operations result in a geometrically equivalent pattern between two atomic rows of the adjacent B and C layers. Because of the assumption that $c/a = 1$, the magnitude of $b_1 = b_2$ is equal to that of $b_3$, and the atomic lattices shown in Figs. 2 and 3 are equilateral triangles. With the actual value of $c/a = 1.02$ for $\gamma$-TiAl, this symmetry and the degeneracies are broken, thus giving rise to long-range coherency stresses and interfacial dislocations to accommodate the misfit strain across the interface.

**$\alpha_2/\gamma$ Interface**

At the coherent part of an $\alpha_2/\gamma$ interface with the crystallographic habit relationship of (0001)[1120]-Ti$_3$Al and (111)[110] TiAl, the interfacial energy is calculated to be 100 mJ/m$^2$ (the reference energy in this case is the sum of TiAl and Ti$_3$Al bulk energies). Significant reductions of $E_{\text{APB}}$ and $E_{\text{CSF}}$ in $\alpha_2$ phase to those (280 and 220 mJ/m$^2$, respectively) at the Ti$_3$Al/TiAl interface were reported recently [17], which are summarized in Table II.
Fig. 3. Degeneracy of the shear faults at a pseudo-twin interface: (a) reference state, (b) \( \theta = 60^\circ, f = 0 \), and (c) \( \theta = 60^\circ, f = b_2 \).

Table II. Calculated Shear Fault Energies at the TiAl/Ti\textsubscript{3}Al Interface (in Units of mJ/m\textsuperscript{2})

<table>
<thead>
<tr>
<th>Plane</th>
<th>APB</th>
<th>SISF</th>
<th>CSF</th>
</tr>
</thead>
<tbody>
<tr>
<td>(111) TiAl</td>
<td>560</td>
<td>90</td>
<td>410</td>
</tr>
<tr>
<td>(0001) Ti\textsubscript{3}Al</td>
<td>300</td>
<td>20</td>
<td>320</td>
</tr>
<tr>
<td>TiAl/Ti\textsubscript{3}Al</td>
<td>280</td>
<td></td>
<td>220</td>
</tr>
</tbody>
</table>

SHEAR FAULT ENERGIES AND DEFORMATION MODES

**TiAl**

Plastic deformation of \(\gamma\)-TiAl by slip or twinning occurs primarily on \{111\} planes. An ordinary dislocation is expected to dissociate into a pair of Shockley partials, with Burgers vectors of \( b_1 = [211]/6 \) and \(-b_2 = [12\bar{1}]/6 \), forming a strip of CSF ribbon,

\[
[\bar{1}10]/2 \rightarrow [211]/6 + CSF + [\bar{1}2\bar{1}]/6.
\]  

The four-fold dissociation of a superdislocation consists of two sets of \( b_3 = [11\bar{2}]/6 \) and \(-b_2 = [12\bar{1}]/6 \) partial dislocations,

\[
[01\bar{1}] \rightarrow [11\bar{2}]/6 + SISF + [\bar{1}2\bar{1}]/6 + APB + [11\bar{2}]/6 + CSF + [\bar{1}2\bar{1}]/6.
\]  

Equilibrium widths of these two types of dislocation dissociation were determined [6] by using the calculated fault energies (Table I) and the calculated elastic constants [5]: \( w_c = 0.29 \) nm (screw) or 0.50 nm (edge) for Eq. (2), and \( w_1 = 5.2 \) nm, \( w_2 = 0.4 \) nm, and \( w_3 = 0.66 \) nm for SISF, APB, and CSF in Eq. (3), respectively, when the [011] superdislocation is in screw orientation.
The widths of an ordinary dislocation, Eq. (2), are still below the resolution limit of the conventional TEM technique and are in reasonable agreement with the atomistic simulation result of dislocation core spreading using the EAM [17]. The dissociation configuration of a screw superdislocation, Eq. (3), is asymmetric (w_l = 5.2 nm and w_c = 0.66 nm) because of the disparity between E_ssf = 90 mJ/m^2 and E_csf = 410 mJ/m^2. When a resolved shear stress is such that the leading partial dislocation in Eq. (3) is to extend the SISF ribbon further from the equilibrium width, this offers one possible dislocation mechanism for twin formation [6].

Crystallographic elements of true-twinning in TiAl by deformation are shown in Fig. 4. Deformation twinning occurs in the L1_0 structure by motion of twinning dislocations with b_3 = [112]/6 on successive (111) planes. The coherent twin boundary created by homogeneous shear process (Fig. 4) is equivalent to the true-twin interface obtained by f = 0 and \( \theta = 180^\circ \) (Fig. 2). Therefore, the twin boundary energy of \( \Gamma_t = 60 \text{ mJ/m}^2 \) applies equally to the coherent part of a twin boundary formed by deformation twinning.

![Fig. 4. Crystallography of deformation twinning in \( \gamma \)-TiAl. The filled circles (Ti atoms) are on the (110) plane of shear, and the open circles (Al atoms) are on the adjacent plane.](image)

**Ti_3Al**

Plastic deformation of \( \alpha_2 \)-Ti_3Al of the D0_19 structure is known to occur by three slip systems, viz., the prism slip, \( \{1100\}<11\overline{2}0> \), the basal slip, \( \{0001\}<1\overline{1}20> \), and the pyramidal slip, \( \{11\overline{2}1\}<1\overline{1}2\overline{6}> \). On the (0001) basal plane, a superdislocation of Burgers vector, \( \mathbf{a} = <\overline{1}20>/3 \), is dissociated into two superpartials with Burgers vector, \( \mathbf{b} = \mathbf{a}/2 = \mathbf{f} \), and each superpartial further splits into a pair of Shockley partials such that the following four-fold dissociation may occur,

\[
\frac{11\overline{2}0}{3} \rightarrow \frac{10\overline{1}\overline{0}}{6} + \text{CSF} + \frac{01\overline{1}0}{6} + \text{APB} + \frac{10\overline{1}0}{6} + \text{CSF} + \frac{01\overline{1}0}{6} .
\]

Table 3 lists the shear fault energies of Ti_3Al determined based on the LDF calculation [18]. In the case of (1\overline{1}00) prism planes, there are two different corrugated layers of atomic planes to be considered [19], and a lattice shift by the fault vector, \( \mathbf{f} = [1\overline{1}\overline{2}0]/6 \), creates two distinct APBs, viz., APB-I and APB-II in Table III, by

\[
[1\overline{1}\overline{2}0]/3 \rightarrow [1\overline{1}\overline{2}0]/6 + \text{APB} + [1\overline{1}\overline{2}0]/6 .
\]

The difference between the two APB energies for the (1\overline{1}00) plane listed in Table III is due to the fact that the introduction of an APB-II does not alter the nearest-neighbor coordination number of atoms at the APB interface. On the (1\overline{1}21) pyramidal plane, two possible fault vectors are \( \mathbf{f}_1 = [1\overline{1}00]/2 \) and \( \mathbf{f}_2 = [1\overline{1}26]/6 \). Nevertheless, they give rise to the same APB energy of 293 mJ/m^2 (Table 3). Therefore, a 2c+a = [1\overline{1}26]/3 type superdislocation is dissociated into two superpartials of \( \mathbf{b} = c+a/2 = f_2 \) type on the (1\overline{1}21) plane by
and each superpartial may undergo a further splitting by either a dissociation or a decomposition.

Table III. Calculated APB and CSF Energies of Ti3Al in Units of mJ/m²

<table>
<thead>
<tr>
<th></th>
<th>(0001)</th>
<th></th>
<th>(1100)</th>
<th></th>
<th>(1121)</th>
</tr>
</thead>
<tbody>
<tr>
<td>APB</td>
<td>CSF</td>
<td>APB-I</td>
<td>APB-II</td>
<td>APB</td>
<td></td>
</tr>
<tr>
<td>300</td>
<td>320</td>
<td>133</td>
<td>506</td>
<td>293</td>
<td></td>
</tr>
</tbody>
</table>

The equilibrium widths of two-fold dissociation, Eq. (5), on the (0001) plane, with $E_{APB} = 300$ mJ/m² are only 3 nm and 8 nm, respectively, for screw and edge orientations [6]. As listed in Table II, $E_{CSF}$ is reduced by 31% from 320 to 220 mJ/m². This indicates that the mobility of a Shockley partial pair, Eq. (4), is increased at or near the $\alpha_2/\gamma$ interface.

ROLE OF INTERFACES IN MECHANICAL BEHAVIOR

Deformation and microcracking characteristics of $\gamma$-TiAl and $\alpha_2$-Ti3Al have been reviewed recently [6]. In TiAl the habit planes of slip, twinning, and microcracking are common close-packed {111} planes. In Ti3Al, plastic deformation can occur by {100} prismatic, (0001) basal, and pyramidal slip systems. Deformation twinning is rarely observed in Ti3Al. Figure 5 shows a schematic drawing of a PST crystal, where the angle $\phi$ is between the lamellar habit planes, (111)$_\gamma$/(0001)$_{\alpha_2}$, and the applied stress axis. In reference to the (111) plane, there are a total of six different orientations (including opposite directions) of $\gamma$ lamellae, only three crystallographic variants of I, II, and III are indicated in Fig. 5.

Fig. 5. Schematic microstructural description of a PST crystal.
Experimental findings and theoretical analyses on how these interfaces affect deformation and fracture behavior of PST crystals are many [1,2], and also abundant are the records of alloy design efforts to try to obtain an acceptable balanced mechanical properties by tailoring this lamellar microstructure. In the remainder of this paper, we will discuss a few issues based on the results of first-principles calculations.

**Elastic Inhomogeneity**

Assuming that a bimaterial system of TiAl-Ti$_3$Al-TiAl as shown in Fig. 6 is composed of two elastically isotropic phases and using the calculated elastic moduli [6], one can estimate the magnitude of internal stresses due to the elastic incompatibility [20]. The induced stress in the $\alpha_2$ lamella was estimated to be -9% of an applied stress when the stress axis is perpendicular to the interfaces ([111] in Fig. 6) and +4% when the stress is applied in the parallel direction ([112] in Fig. 6). Since the yield stresses of PST crystals at room temperature are about 300 and 500 MPa [3] at two different hard orientations ($\phi = 0$ and 90°), the elastically induced stresses within the $\alpha_2$ lamellae are at most 45 MPa. This magnitude is relatively small compared to internal stresses caused by other sources, such as coherency stresses due to the lattice parameter mismatch and thermoelastic stresses due to the difference in thermal expansion. For instance, including the tetragonality of TiAl, Hazzledine et al. [21] estimated very large elastic stresses ($\approx 1$ GPa) at coherent $\alpha_2/\gamma$ interfaces. Appel and Wagner [22] observed generation of dislocations from lamellar interfaces during *in situ* TEM heating cycle of 300 $\rightarrow$ 994 $\rightarrow$ 300 K. The magnitude of internal stress for the dislocation generation is estimated to 140 MPa if one assumes the difference in thermal expansion coefficients [6] between $\gamma$ and $\alpha_2$ phases to be 20%. These internal stresses are much larger than the induced stresses due to the elastic incompatibility. Therefore, the elastic inhomogeneity between anisotropic $\gamma/\gamma$ interfaces and the $\alpha_2/\gamma$ boundary will be neglected in the ensuing discussion.

![Fig. 6. CSF energies and dissociation of screw [110]/2 dislocations in PST crystals.](image-url)
Inhomogeneous Slip and Plastic Anisotropy

According to the classical Peierls concept of dislocation mobility, the wider the planar dissociation configuration of a dislocation, the more mobile the dislocation is. In the case of \{111\}\(\{1\over 2\}10\) ordinary slip system in TiAl, Simmons et al. [17] found from their atomistic simulation study that the highest CSF energy caused the dislocation core to develop non-planar spreading, while the core structures associated with the lower energies were planar. Possible roles of various interfaces in the ordinary slip system can be discussed with the aid of Fig. 6 which schematically illustrates true-twin (TT, \(\gamma_1/\gamma_2\)), pseudo-twin (PT, \(\gamma_1/\gamma_3\)), rotational (RB, \(\gamma_1/\gamma_4\)), and \(\alpha_2/\gamma\) (Ti₃Al/TiAl) boundaries. Domain boundaries of other \(\gamma/\gamma\)-type that are roughly perpendicular to the (111) plane (Fig. 5) are neglected here for simplicity. Also neglected for now is the elastic inhomogeneity and anisotropy, and the presence of interfacial dislocations. The elastic constants of \(\gamma\)-TiAl were used throughout PST crystals for dislocation width calculations. The crystallographic orientation shown in Fig. 6 is with reference to the \(\gamma_1\) domain.

A screw ordinary dislocation of Burgers vector, \([1\over 2][1\over 1\over 1]\), is dissociated on either the (111) or (\overline{1}1\overline{1}) slip plane according to Eq. (2), where \(E_{\text{CSF}} = 410 \text{ mJ/m}^2\) in the \(\gamma_1\) bulk gives the equilibrium width of \(w_c = 0.29 \text{ nm}\) [6]. The calculated values of \(E_{\text{CSF}}\) at the \(\gamma/\gamma\)-type interfaces (the last column of Table I) and at the \(\alpha_2/\gamma\) interface (Table II) are shown in Fig. 6, which schematically depicts relatively wider dissociations at interfaces, the widest being at the \(\alpha_2/\gamma\) interface with \(w_c = 0.55 \text{ nm}\). According to the simple criterion for the ease of sliding that the wider the dissociation configuration of a dislocation, the more mobile the dislocation is, the mobility of \([1\over 2][1\over 1\over 1]\) screw dislocation is expected to be slightly reduced along a true-twin boundary, but significantly enhanced along all other types of the interfaces.

Because of more complex dissociation configuration involving all three types of the planar faults, Eq. (3), the role of interfaces in the relative mobility of superdislocations is more complicated than of ordinary dislocations. As listed in Table I, while \(E_{\text{APB}}\) and \(E_{\text{CSF}}\) in the bulk of \(\gamma\)-phase are both reduced, by about a half, at pseudo-twin and 120° rotational boundary interfaces, \(E_{\text{SISF}}\) is increased about threelfold.

As far as ordinary dislocations are involved, the enhanced mobility along these lamellar interfaces supports the notion of “channeled dislocation motion” [23] or “supersoft deformation mode” [12] in lamellar TiAl, which may be a contributing factor to the strong orientation dependence of yield strength in PST TiAl crystals [3]. Recent experimental results of offset displacement of the fiducial lines on deformation inhomogeneities [24] and in situ TEM observation of deformation-induced interface migration [25] are consistent with the inhomogeneous interfacial deformation.

Slip-Twin-Interface Interactions

Interlayer distances of three different types are marked in Fig. 5 as \(d_L\), \(d_D\), and \(d_A\), respectively, for \(\gamma/\gamma\) lamellae, \(\gamma/\gamma\) domains, and \(\alpha_2\) lamellae. The initial state of internal stresses are created due to the distributions of interfacial misfit dislocations resulting from lattice parameter misfits at various semicoherent interfaces. These intrinsic interfacial dislocations have their Burgers vectors which are usually related to smallest partial dislocations in Eqs. (2-6). In the case of \(\gamma/\gamma\) interfaces, interfacial dislocations form a network of screw character [26]. As illustrated in Fig. 6, after a screw \((1\overline{1}1)[1\overline{1}0]/2\) dislocation moves into \(\alpha_2/\gamma\), RB, or PT interface by cross-slip, it can interact with these intrinsic interfacial dislocations such a way that an extensive interfacial slip and/or migration occur.

When dislocations of edge or mixed types are involved in a dislocation pileup against these interfaces, stress concentrations at the interfaces may reach a level sufficiently high for either initiation of slip or twinning into the adjacent domain leading to a Hall-Petch type relationship, or crack nucleation by the Stroh mechanism. This occurs mainly due to an accumulation of dislocation reaction products associated with the head of a pileup. These deformation-induced extrinsic interfacial dislocations (edge type) can alter the internal stresses significantly. Using Hall-Petch and Stroh mechanisms, Hazzledine and Kad [26] discussed the orientation dependent yield
and fracture stresses reported in PST TiAl crystals [3]. The highest yield strength achieved in \(\gamma\)-TiAl-based alloys, by refining the lamellar microstructure, is 971 MPa at room temperature [27]. To interpret this result based on Hall-Petch relationship, Sun [28] introduced a dislocation multiple pileup model based on \(d_{L}\) and \(d_{G}\), the grain size. The intermediate lengths of \(d_{D}\) and \(d_{A}\) (Fig. 5) and lamellar colony size have not been taken into consideration.

**Translamellar and Interfacial Fracture**

Once a microcrack is initiated on a (111) plane of \(\gamma\)-phase, which is of the lowest surface energy \(\gamma_{s} = 2.25 \text{ J/m}^2\) in TiAl [29], it may propagate across a series of \(\gamma/\gamma\) interfaces under the influence of mode-II and mode-III components of external loading applied to the coplanar (111)[112] twinning (edge) and (111)[110] ordinary slip (screw), leading to translamellar fracture. The effect of this mode mixity was illustrated in terms of crack-tip stress fields [20] and directly observed in an electron microscopy study [30].

Using the ideal cleavage energies, \(G_c = 2\gamma_{s}\), calculated earlier [29] and the interfacial energies, \(\Gamma_i\), given in Table I, one can evaluate interfacial fracture energy by using the relationship,

\[
G_i = G_c - \Gamma_i - E_m, 
\]

where \(E_m\) is the misfit energy estimated using the Frank and van der Merwe method [31] and the available lattice parameters of TiAl and Ti₃Al [6]. The calculated results are summarized in Table IV. Because of the approximations involved in determining the interfacial and misfit energies, the final interfacial fracture energies are only estimates. Nevertheless, these results give us a relative measure of interfacial fracture mode, indicating that fracture is easiest along 120° rotational \(\gamma/\gamma\) interfaces and most difficult along \(\alpha_2/\gamma\) boundaries.

**Table IV. Interfacial Fracture Energies in Two-Phase TiAl**

(in Units of J/m²)

<table>
<thead>
<tr>
<th>Interface</th>
<th>(G_c)</th>
<th>(\Gamma_i)</th>
<th>(E_m)</th>
<th>(G_i)</th>
</tr>
</thead>
<tbody>
<tr>
<td>(\gamma/\gamma)</td>
<td>4.5</td>
<td>0.27</td>
<td></td>
<td>-4.2</td>
</tr>
<tr>
<td>PT (60°)</td>
<td>4.5</td>
<td>0.25</td>
<td>0.03</td>
<td>4.2</td>
</tr>
<tr>
<td>RB (120°)</td>
<td>4.5</td>
<td>0.06</td>
<td></td>
<td>-4.4</td>
</tr>
<tr>
<td>TT (180°)</td>
<td>4.65</td>
<td>0.10</td>
<td>0.07</td>
<td>4.5</td>
</tr>
<tr>
<td>(\alpha_2/\gamma)</td>
<td></td>
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</tbody>
</table>

At room temperature, single-phase \(\gamma\)-TiAl is very brittle, but fracture toughness (\(K_O\)) of two-phase TiAl alloys is measured to be reasonably good, e.g., the critical stress intensity factor for Mode I crack of \(K_{IC} = 16-23 \text{ MPa\sqrt{m}}\) from fully lamellar microstructure [32], \(K_O = 10-32 \text{ MPa\sqrt{m}}\) from a variety of microstructures [33], and \(K_O > 50 \text{ MPa\sqrt{m}}\) from fine \((d_L = 0.1 - 0.4 \mu m)\) lamellar microstructures [34]. According to Booth and Roberts [35], the average stress intensity factor of \(\gamma\)-TiAl single crystals is \(K_{IC} = 1.0 \text{ MPa\sqrt{m}}\), which is close to the theoretical values of \(k_{IC} = 0.89\) and 1.04 MPa\sqrt{m} for the \{100\} and \{001\} surfaces at 0 K, respectively [20]. In single-phase \(\gamma\)-TiAl, experimental evidence of crack-tip slip and twinning (\(K_O > 7 \text{ MPa\sqrt{m}}\)) was analyzed in Ti-54 at. % Al [36], and grain-boundary toughening (\(K_O = 10 \text{ MPa\sqrt{m}}\)) was reported in Ti-50 at. % Al [33]. Obviously, in two-phase TiAl alloys, the presence of various lamellar interfaces influences the crack-tip plasticity, which is strongly orientation dependent [4,37], and therefore affecting translamellar and interfacial microcracking in the crack-tip region. Based on the
calculated energies of surfaces and interfaces (Table IV), the tendency for translamellar (\(G_\varepsilon = 4.5\) J/m² for \{111\} crack in \(\gamma\)-phase) or interfacial microcracking along the \(\alpha_2/\gamma\) boundaries (\(G_i = 4.5\) J/m²) is the same. It is the mode mixity of the stress state at a head of the main crack that dictates the fracture toughness of a lamellar microstructure. The inverse relationship between the fracture toughness and the lamellar spacing (\(d_L\) and/or \(d_A\)) has been reported [32], and the coherency stresses may become significantly large at fine lamellar microstructure to an extent that they tend to prevent crack propagation across \(\alpha_2\) lamellae [38].

**SUMMARY**

More common observation of the true-twin type interfaces in the lamellar microstructure and the propensity of deformation twinning, in two-phase TiAl-Ti₃Al alloys, are consistent with the low value, \(\Gamma_T = 60\) mJ/m², of true-twin boundary energy. Planar fault energies at pseudo-twin and 120° rotational interfaces are markedly different from their counterparts in the bulk of \(\gamma\)-phase, i.e., approximately, \(E_{APB}\) and \(E_{CSF}\) decreases by a half and \(E_{SSF}\) increases by a threefold. Enhanced mobility of ordinary dislocations along \(\alpha_2/\gamma\) and \(\gamma/\gamma\) interfaces (except true twin boundaries) is predicted based on the reduced \(E_{CSF}\) values. Though the differences are not large, interfacial fracture energies are estimated to be the highest for the \(\alpha_2/\gamma\) lamellar boundary and the lowest for 120° rotational \(\gamma/\gamma\) boundary. The mode mixity plays an important role in the crack-tip plasticity by ordinary slip and true-twinning, leading to translamellar and interfacial fracture.

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