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EXPERIMENTS AND COMPUTER SIMULATIONS OF THE DYNAMIC CAVITY FORMED BY A PARTICULATED SHAPED-CHARGE JET IN SAND

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Experiments have been carried out to measure the dynamic cavity growth of dry sand during penetration by particulated jets from Viper 65-mm-diameter, Cu-lined conical shaped charges at 1000-mm standoff. The sand target was instrumented with foil switches, piezoelectric pins, and pressure transducers. Flash radiography at 450-keV was used to characterize the jets before impact and to image the target hole during jet penetration. We have developed a dry sand equation of state based on existing Hugoniot data as input to a porous material model incorporated in the 2-D arbitrary Lagrangian-Eulerian hydro-code CALE. We have carried out sand penetration simulations in which the particulated jet is modeled as hot copper rods. By varying parameters in the sand and copper descriptions we identify those features that affect the dynamic cavity formation.

INTRODUCTION

The design of warheads to attack mines or other deeply buried targets efficiently requires information on the dynamic growth of the cavity that forms around a penetrating projectile. Sand is an inexpensive, readily available material with a mass efficiency against shaped charge jets greater than 1.5 (Held, 1987). As such, it is likely to be encountered as overburden in buried target attack. We therefore undertook to study the evolution of the target cavity in dry sand undergoing penetration by a particulated jet. Sequential radiographic images of the target hole coupled with time-of-arrival and pressure data provided a detailed experimental record. To permit better understanding of the phenomena, the experiment was analyzed with a hydrodynamic simulation incorporating a porous sand model.

EXPERIMENTS

Two experiments were carried out for this purpose. The 65-mm-diameter, Cu-lined Viper precision shaped charge was used at a standoff distance of 1000 mm. The jet from this charge has a tip velocity of approximately 9.5 km/s. Particulation typically occurs when the tip reaches 800 mm.

In each experiment three 450-keV flash x-ray exposures were made at 10-μs intervals to record the progress of the jet and the growth of the hole. Experiment 1 (LLNL designation 1410-B9) recorded the jet before impact with the target on two exposures and the initial hole on the third exposure. Experiment 2 (1410-B10) recorded the hole development for a second jet on three exposures. The radiographs are reproduced in Figure 1.

The sand target for both experiments was 300 mm long, 60 mm high, and 40 mm wide. The sand used was #2 grit silicon dioxide, with a measured density of 1.66 g/cm³. The sides of the
Figure 1. Radiographs from Experiments 1 (r.) and 2 (l.). Times of the 450-keV radiographs are indicated, along with locations of piezoelectric crystal pins, foil switches, entrance to the sand box, and approaching Viper jet tip.
target, through which the radiographs were made, were constructed of 6-mm paper/foam sandwich material. The top and bottom were made of PMMA insulating plastic.

Foil switches formed the entrance and exit membranes, and foil switches were placed every 60 mm within the target to record the progress of the jet along the experiment centerline. Piezoelectric crystal pin switches were inserted in the sand to measure the time of arrival of the lateral compaction wave. The crystal pins were placed approximately 10 mm above and below the expected jet trajectory and every 60 mm along the length of the sand box, starting 20 mm behind the entrance plane.

In two locations in Experiment 1, polyvinyl difluoride (PVF₂) pressure transducers were placed against the sides of the box, 20 mm from the expected jet trajectory. In contrast to the crystal pins, these transducers have the potential for recording the amplitude of the pressure wave.

CALCULATIONS

We developed a dry sand equation of state based on existing Hugoniot data as input to an irreversibly compressible porous material model incorporated in the two-dimensional arbitrary Lagrangian-Eulerian hydrodynamic simulation CALE (Tipton 1995). We then carried out a sequence of sand penetration calculations in which the particulated jet was modeled as axi-symmetric, perfectly-aligned, hot copper rods with shapes, separations, and velocities consistent with the sequential radiographs of the Viper jet prior to target impact.

Sand Equation of State

In CALE there are two standard models that describe the compaction of porous materials. We chose a tabular form, which permits us to mimic the behavior of a model previously developed for the dynamic consolidation of powders (Reaugh 1987). We used that model to fit the measured Hugoniot of dry sand (van Thiel 1977), and extracted points from the compaction curve for the tabular input to CALE. This crush curve (pressure vs. porosity) is shown in Figure 2. The comparison of the model fit with the Hugoniot data is shown in Figure 3.

Figure 2. Sand pressure vs. porosity model adopted for CALE calculations.

Figure 3. Hugoniot data points for sand, compared with model curve.
In the CALE calculations, the equivalent stress is taken to be proportional to the pressure (with proportionality constant 1.0) up to a maximum pressure of 2.4 GPa, and it is set equal to that value for all higher pressure. The sand has no strength in tension. The maximum shear modulus is 10 GPa. Below 2.4 GPa the shear modulus is proportional to the pressure.

When the Hugoniot pressure exceeds the pressure at which all porosity is squeezed out, the details of the pressure-porosity curve do not matter. For our description of sand, this occurs at about 14 GPa, which corresponds to a particle velocity of 2 km/s. Above that pressure any thermodynamically consistent “snowplow” model (Hofmann et al., 1968) will reproduce the Hugoniot. Below that pressure, details of the crush curve will have an effect.

Hydrodynamic Modeling

The model of the jet used in the CALE calculations is based on the measurements of the particles in the experimental radiographs. The target was represented by a cylinder of sand with a radius \( r = 27.6 \text{ mm} \), giving the same area as in the rectangular target. The target sides were represented by a lucite shell 4.8 mm thick. Reflective boundary conditions were applied outside an air zone which was not reached by the expanding target during the course of the calculation. The density of sand was taken to be 1.60 g/cm\(^3\), which is slightly lower than the value of 1.66 g/cm\(^3\) measured. The reference density of silicon dioxide was 2.65 g/cm\(^3\).

CALE was used in a purely Eulerian mode for the penetration calculations. Within the region occupied by the hole, the grid size was 0.3 mm radially by 0.4 mm axially. Outside the hole radius the radial grid was allowed to expand gradually.

After the tip particle, the particle radii were all set to 0.9 mm, corresponding to the mean particle diameter of 1.86 \( \pm 0.26 \text{ mm} \). The lengths were set individually to the nearest full zone occupied by the particle, except that to allow for the narrowed ends of the actual particles, 0.4 mm was taken off each end of the modeled particles.

The density of the hot copper was taken to be 8.4 g/cm\(^3\), compared with a reference density of 8.93 g/cm\(^3\). This was based on hydrocode simulations of Viper jet formation, together with preliminary calculations using the reference density, which gave too rapid a rate of axial hole growth. The internal energy was set at 0.41 \text{kJ/g}, corresponding to a temperature of 800-1000 K. For the hot copper, the yield strength was set to an arbitrary low value of 0.1 GPa, and the shear modulus to 25 GPa. The jet strength plays only a minor role in this calculation.

The hole cavities that resulted from the CALE calculations are shown in Figure 4. The hole profiles are represented as cross sections of density. In each case we see a progression of particles down the axis, which correspond to the particles on the radiographs. Within the sand target we see the compression wave proceeding outward, followed by the growing hole.

Pressures were recorded at the locations of the foil switches, the crystal pins, and the PVF\(_2\) gauges.

**COMPARISON OF SIMULATION AND EXPERIMENT**

**Hole Cavity**

The agreement in hole depth between the simulation and the experiments is within 1 mm, or 0.5 percent. This indicates that the choice of relative densities and particle lengths in the simulation was well suited to the experiment.
The hole cavity, both as simulated with CALE and as observed in the experimental radiographs, develops as a series of scallop-shaped chambers, which are made by the individual particles. The chambers continue to grow in radius until the kinetic energy delivered by the jet particle is balanced by the work done against the target material.

In a preliminary CALE calculation, the maximum yield strength of the sand was taken to be 2.0 GPa. With this value, the calculated maximum radii of the chambers were about 10 percent too large for the radiographs in Experiment 2. In an effort to compensate, the maximum yield strength was raised by 20 percent to 2.4 GPa for the calculation shown here. The result was an improvement, and the calculated chamber radii now appear to be too large by only 5 percent.

The actual chamber growth is balanced by energy absorbed by material which experiences a wide range of conditions. Near the axis, a small amount of target material experiences large pressures of about 40 GPa, which quickly squeezes out the porosity and arrives on the Hugoniot. Far from the axis at later times much smaller pressures develop which involve larger amounts of material with less well understood energy absorption mechanisms. All of these contribute to determining the radius of the hole. With the simple model adopted here for the sand equation of state, the agreement within 5 percent may be considered good.

Figure 4. Hole cavities as calculated by CALE for the four sand radiographs shown in Figure 1.
The longer the spacing between particles, the more slowly the material in the narrow part of the hole, between the chambers, moves outward. Consequently, it may remain near enough to the axis to be encountered by later particles and caught up in their wakes. Evidence of this may be seen in the radiographs, particularly in Experiment 2, second and third radiographs (152.9 and 165.5 μs), at the location of the first foil switch, 60 mm from the entrance. This is a general phenomenon, seen at many locations, and it is evident in both the simulation and the experiment. It may even cause interference, as will be discussed in the next section.

Foil Switch Timing

The time of arrival of the jet tip at the locations of the foil switches is shown in Figure 5, for the experiments and for the CALE calculation. The foil switch in Experiment 1 at the entrance to the target was shorted about 0.16 μs early by a narrow precursor extending in front of the tip particle, which can be seen in Figure 1. There is evidence that a similar precursor was present at the tip of Experiment 2.

From the entrance switch through the fourth switch, the experiments agree with each other within ±0.65 μs, and CALE agrees within ±0.68 μs. At the fifth switch, Experiment 1 falls behind Experiment 2 by 3.77 μs, and it is late by 19.49 μs at the 1300-mm location. This seems to be the result of the bend in the Experiment 1 jet mentioned before, reaching from the tip back to 8.2 km/s. At a velocity of about 8.2 km/s, and extending to 7.8 km/s (particles no. 15-18), this portion of the jet did not contribute to deepening the hole. Finally, the jet emerged at a velocity of 7.0 km/s, whereas in Experiment 2 the exiting particle had a velocity of 7.9 km/s.

The bend in the Experiment 1 jet meant that the first part of the hole was not aligned with the straight part of the jet that came later. This, together with the tendency of target material to
remain near the axis where there is a large gap between particles, meant that the jet was likely to encounter target material midway down the hole. The largest gaps in the Experiment 1 jet are between particles no. 2 and 3 and between nos. 8 and 9. The target material corresponding to the gap between particles no. 2 and 3 is the likely candidate to have interfered with particles no. 15-18, as it deviates farthest from their trajectory.

**Crystal Pin and PVF₂ Gauge Timing**

In order to show the propagation of the pressure wave moving outward from the axis, relative timing data are presented in Figure 6. We have plotted the time difference between the arrival of the pressure wave at the pin location and the shorting of the preceding foil switch. The crystal pins were nominally 20 mm behind the foil switch and 10 mm from the axis. Actual locations were taken from the radiographs (as projected on the vertical plane). In both experiments, the jet passed closer to one set of pins than to the other. In Experiment 2, the jet's projected displacement was about 2 mm from the midpoint, as can be seen in Figure 1.

Three sets of locations were recorded in the CALE simulation, at radii of 8, 10, and 12 mm. As the response threshold of the piezoelectric pins is unknown, an arbitrary threshold value of 0.1 GPa was adopted in deriving the CALE times. However, the initial pressure rise occurs as much as 1 μs earlier for the later points.

The first set of points, near 1020 mm, represents the pressure wave from the tip particle. The propagation time is noticeably shorter than that for the remaining particles. The strength of the wave is larger there (about 4.5 GPa in the calculations vs. 0.3 GPa for the next location), and the axial offset is a smaller fraction of the particle size. Therefore, the propagation is dominated more by the compression phase and less by the succeeding rarefactions.

Despite these advantages, the first set of data points is hard to analyze. For Experiment 1, the cavity is asymmetrical and the jet tip is offset. Therefore, the delay between the CALE times and the experimental times may reflect geometrical variances as opposed to equation-of-state differences. For Experiment 2, the exact shape of the tip particle and the projected location of the undisturbed pins was not recorded.

The remaining sets of data, at 1090 mm, 1150 mm, etc., show longer delay times in accordance with the weaker shock from the remaining particles. Experiment 2 may be the more consistent set, as its jet appears to have been straight, even though offset from the experiment centerline. The mean time of arrival for Experiment 2 is about 1 μs earlier than the CALE points, although these times are subject to uncertainties of about 1 μs in simulating the calibration of the pins. Interpreting these as differences in the wave velocity is problematical, because this part of the equation of state, below about 2 GPa, is essentially unvalidated by the available data.

The PVF₂ data are similar to the crystal pin data, except with greater delays. Of the four gauges installed, signals were recorded only from the two that were the most sensitive, and for these the signal-to-noise ratio is small. For the gauge at 1150 mm, the time difference is 42.5 μs, and for the gauge at 1270 mm, the time difference is 34.6 μs. The results are somewhat inconsistent, as one would have expected the shorter time delay to be associated with the earlier pin. However, the signal shape may indicate response to the ionization associated with the passage of the jet. The derived pressures of 0.055 and 0.040 GPa (±20 percent) are consistent with expectations from the CALE calculations for similar locations behind preceding foil switches.
CONCLUSIONS

The experiments were successful in providing a record of the dynamic hole growth, and the hydrodynamic simulation aided in understanding the phenomena associated with particulated penetration.

The 40-mm-thick sand target provided sufficient contrast on the 450-keV flash radiographs to make the target interaction clearly visible. In particular, the constrictions that develop between the chambers that result from individual particles were revealed. Where longer intervals occur between succeeding particles, more target material remains near the axis. This is shown both in the radiographs and in the simulation. Where the jet is not well aligned, there is a potential for interference with later particles. This was observed in Experiment 1, which had a bent section extending from the tip back to a velocity of 8.2 km/s, and for which the jet from 8.2 to 7.8 km/s did not contribute to penetration.

The CALE calculation satisfactorily reproduced the observed dynamic target cavity growth with a few reasonable assumptions. The axial growth of the hole was matched at the times of the radiographs to 0.5 percent in depth and 1.5 percent in time by using a sand density of 1.60 g/cm$^3$ and a copper density of 8.4 g/cm$^3$. The particles were modeled as rods with lengths shortened front and rear by 0.4 mm to account for tapering. The growth of the hole in radius was also matched to 5 percent by the choice of a maximum yield strength of 2.4 GPa for the sand, combined with a compaction curve that fits the Hugoniot data. The two jets differed in the details of their particle distribution, and we recommend radiography of the actual jet that makes the hole being studied.

The use of foil switches on axis together with piezoelectric crystal pins and PVP$_2$ pressure gauges off axis permitted comparisons to be made between the compaction wave propagation in the experiments and the simulation. We observed agreement within 1 µs, but closer comparison would require better information about the instrument response functions and about the low-pressure end of the compaction curve.

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