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# 2l - n'l' X-ray Transitions from Neonlike Charge States of the Row 5 Metals with $39 \leq Z \leq 46$

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## Abstract

X-ray spectra of 2l - n'l' transitions with  $3 \leq n \leq 12$  in the row five transition metals zirconium (Z=40), niobium (Z=41), molybdenum (Z=42) and palladium (Z=46) from charge states around neonlike have been observed from Alcator C-Mod plasmas. Accurate wavelengths ( $\pm .2$  mÅ) have been determined by comparison with neighboring argon, chlorine and sulphur lines with well known wavelengths. Line identifications have been made by comparison to *ab initio* atomic structure calculations, using a fully relativistic, parametric potential code. For neonlike ions, calculated wavelengths and oscillator strengths are tabulated for 2p-nd transitions in Y (Z=39), Tc (Z=43), Ru (Z=44) and Rh (Z=45) with  $n = 6$  and  $7$ . The magnitude of the configuration interaction between the  $(2p^5)_{\frac{1}{2}}6d_{\frac{3}{2}} J = 1$  level and the  $(2p^5)_{\frac{3}{2}}7d_{\frac{5}{2}} J = 1$  levels is demonstrated as a function of atomic number for successive neonlike ions. Measured spectra of selected transitions in the aluminum-, magnesium-, sodium- and fluorinelike isosequences are also shown.

## Introduction

Recently there has been considerable interest in x-ray transitions in high Z ions with charge states around the neonlike isosequence<sup>1-11</sup>. X-ray lasing<sup>12,13</sup> has been demonstrated in neonlike ions, and a need to understand the kinetics of this system has motivated development of very precise collisional-radiative modelling tools<sup>14</sup>. The identifications of many x-ray lines from neonlike ions allow high resolution experimental data to be used for benchmarking multi-electron atomic structure calculations<sup>15-19</sup>. Most of the work which has been

done in the past has been limited to 3-3, 2-3 and 2-4 transitions in the NeI isosequence and adjacent charge states. The high temperature, optically thin tokamak plasmas enable the measurement of many lines originating in transitions from levels having  $n \geq 5$ ; in fact, all of the transitions in the 2p-nd series in  $\text{Mo}^{32+}$  lying under the ionization potential have been measured<sup>10,11</sup>. The availability of a large number of transitions in several adjacent elements provides the opportunity to study the systematics of configuration interaction effects.

In this paper are presented spectra of selected 2p-nd transitions with  $n$  between 3 and 7 in near-neonlike Zr, Nb, Mo and Pd, obtained from Alcator C-Mod plasmas<sup>20</sup>. A comprehensive study of numerous transitions in these elements is given in Ref. (11). The 2p-nd transitions considered here are strongly split by the  $j$ -value (in  $jj$ -coupling) of the 2p hole in the ionic core. The splitting is very apparent in the neonlike ions, where the resonance transitions with upper states containing a  $2p_{\frac{1}{2}}$  hole are at much shorter wavelengths than the corresponding transitions with a  $2p_{\frac{3}{2}}$  hole. This splitting can lead to significant configuration interaction when a  $(2p^5)_{\frac{1}{2}}nd$  orbital is close in energy to a  $(2p^5)_{\frac{3}{2}}n'd$  ( $n' > n$ ) orbital. Interaction between the orbitals will perturb transition wavelengths and re-distribute oscillator strength within a class of transitions<sup>21</sup>. The magnitude of the configuration interaction between the  $(2p^5)_{\frac{1}{2}}6d_{\frac{3}{2}} J = 1$  level and the  $(2p^5)_{\frac{3}{2}}7d_{\frac{5}{2}} J = 1$  levels has been measured as a function of energy level spacing for the neonlike ions of Zr, Nb and Mo<sup>11</sup>. In this paper calculations are presented for these interacting levels in neonlike ions with  $39 \leq Z \leq 46$ .

The x-ray observations described here were obtained from the Alcator C-Mod<sup>20</sup> tokamak, a compact high field device with all molybdenum plasma facing components. For these measurements, the plasma parameters were in the range of  $7.7 \times 10^{13}/\text{cm}^3 \leq n_{e0} \leq 2.0 \times 10^{14}/\text{cm}^3$  and  $1500 \text{ eV} \leq T_{e0} \leq 3400 \text{ eV}$ . A laser blow-off impurity injection system<sup>22</sup>, which has been used to study impurity transport, was used to inject niobium, palladium and zirconium into Alcator C-Mod plasmas. The spectra presented here were recorded by a five chord, independently spatially scannable, high resolution x-ray spectrometer array<sup>23</sup>. Wavelength calibration<sup>23</sup> has been achieved by determining the instrumental dispersions in reference to H- and He-like argon, chlorine and sulphur lines and previously measured molybdenum<sup>10</sup> lines.

*Ab initio* atomic structure calculations for the aluminum- through fluorine-like isosequences (ground states  $2p^63s^23p$  to  $2s^22p^4$ , respectively) have been performed using the RELAC code<sup>24,25</sup>, which solves the Dirac equation by optimizing a parametric potential. RELAC has been used to calculate the full

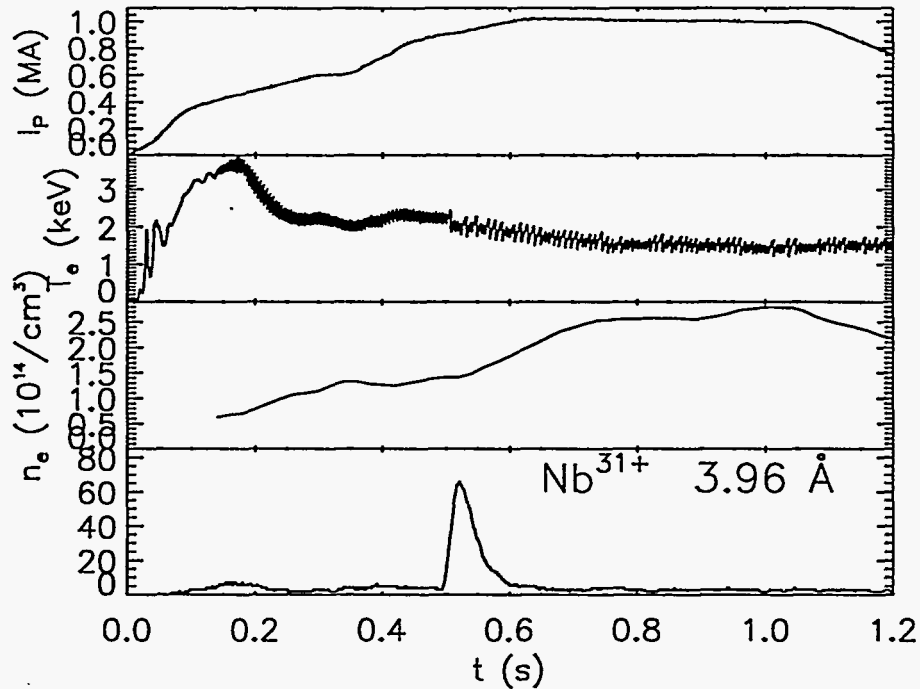


Figure 1: Plasma current, electron temperature, electron density and Nb x-ray (3.96 Å) brightness time histories in a discharge with a niobium injection at .5 sec.

multi-configuration transition wavelengths and oscillator strengths for all lines observed in this paper.

## X-ray Transitions

Shown in Fig.1 are the time histories of several quantities of interest for a typical Alcator C-Mod 5.3 T, deuterium discharge. There was a niobium injection into this particular discharge at 0.5 seconds, when the plasma current was 0.9 MA, the central electron temperature was 2200 eV and the central electron density was  $1.3 \times 10^{14}/\text{cm}^3$ . The niobium stayed in the plasma for about 100 ms; as shown by the bottom frame of the figure, indicative of anomalously fast impurity transport<sup>22</sup>. In Fig.2 is shown an x-ray spectrum taken during an injection which demonstrates the strongest niobium line which falls within the wavelength range of the spectrometer, the  $2p^6 - (2p^5)_{\frac{3}{2}}4d_{\frac{5}{2}}$  transition in neon-like  $\text{Nb}^{31+}$  at 3957.3 mÅ. Also apparent in this spectrum are some sodiumlike  $\text{Nb}^{30+}$  2p-4d lines at 4008.4 and 4011.3 mÅ, and some weaker lines from the magnesiumlike and fluorinelike charge states. A synthetic spectrum, generated

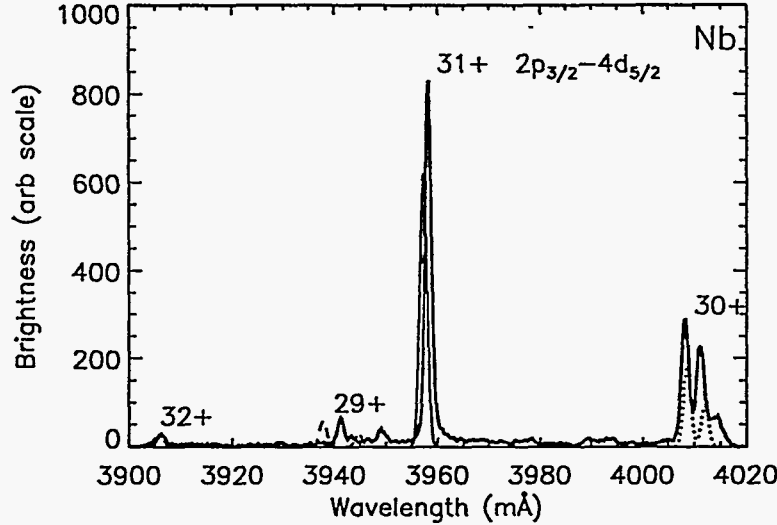


Figure 2: 2p-4d transitions in Nb<sup>29+</sup> - Nb<sup>32+</sup>. Theoretical lines for neonlike Nb<sup>31+</sup> (solid), Nb<sup>30+</sup> (dotted), Nb<sup>29+</sup> (dashed) and Nb<sup>32+</sup> (dash-dot-dash) are shown at the bottom, where the relative intensities within a given charge state are proportional to the oscillator strengths of each transition.

using calculated wavelengths<sup>11</sup>, typical instrumental and Doppler line widths, and line amplitudes proportional to the oscillator strengths<sup>11</sup> within a given charge state, is shown at the bottom of the figure. The observed niobium lines are within 1 mÅ of the calculated wavelengths<sup>11</sup>. Wavelength calibration was obtained from several nearby Ar<sup>16+</sup> lines<sup>26,27</sup>, S<sup>14+</sup> lines<sup>26</sup> and S<sup>15+</sup> lines<sup>28</sup>. A calibration spectrum showing several sulphur lines is shown in Fig.3. This spectrum includes the (unresolved) Lyman  $\beta$  doublet and the 1s<sup>2</sup>-1snp series in S<sup>14+</sup> with n between 5 and 13. Calculated wavelengths and radiative transition probabilities for this series are given in Table I.

Another strong neonlike Nb<sup>31+</sup> line, the 2p<sup>6</sup> - (2p<sup>5</sup>)<sub>1/2</sub>4d<sub>3/2</sub> transition at 3843.8 mÅ, is shown in Fig.4a. Also prominent in the figure are the 2p-4d lines at 3892.8 and 3822.9 mÅ, from sodium- and fluorinelike niobium, respectively. The corresponding 2p-5d transitions are shown in Fig.4b. At the bottom of each figure is a synthetic spectrum and the wavelength agreement is very good.

For higher n transitions in neonlike systems, the upper levels of certain lines in the 2p<sup>6</sup> - (2p<sup>5</sup>)<sub>3/2</sub>nd<sub>5/2</sub> series and the 2p<sup>6</sup> - (2p<sup>5</sup>)<sub>1/2</sub>nd<sub>3/2</sub> series can have nearly identical energies, giving rise to significant configuration interaction. In particular, the effect is seen in the enhancement of the intensity of the 2p<sup>6</sup>

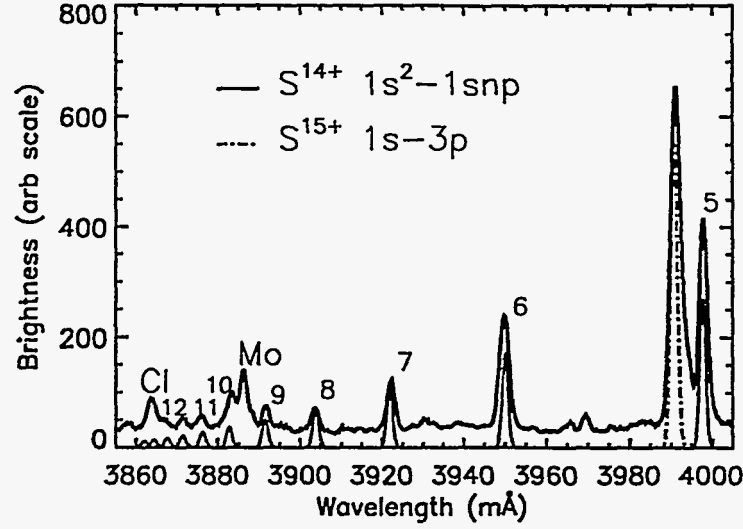


Figure 3:  $1s^2-1snp$  transitions in  $S^{14+}$  with  $n$  between 5 and 12. Also apparent is the Lyman  $\beta$  doublet of  $S^{15+}$ , a  $2p-4s$  line of  $Mo^{32+}$  at 3886.3 mÅ, and a satellite of  $Cl^{15+}$   $K_{\beta}$  at 3863.7 mÅ.

Table 1: Calculated  $1s^2-1snp$  transition wavelengths and radiative transition probabilities for heliumlike  $S^{14+}$ .

Transition	wavelength (mÅ)	$A (10^{12}/s)$
$1s^2 \ ^1S_0 - 1s4p \ ^1P_1$	4088.46	7.28
$1s^2 \ ^1S_0 - 1s5p \ ^1P_1$	3997.73	3.63
$1s^2 \ ^1S_0 - 1s6p \ ^1P_1$	3950.10	2.07
$1s^2 \ ^1S_0 - 1s7p \ ^1P_1$	3921.92	1.29
$1s^2 \ ^1S_0 - 1s8p \ ^1P_1$	3903.84	.860
$1s^2 \ ^1S_0 - 1s9p \ ^1P_1$	3891.54	.602
$1s^2 \ ^1S_0 - 1s10p \ ^1P_1$	3882.79	.438
$1s^2 \ ^1S_0 - 1s11p \ ^1P_1$	3876.34	.328
$1s^2 \ ^1S_0 - 1s12p \ ^1P_1$	3871.45	.252
$1s^2 \ ^1S_0 - 1s13p \ ^1P_1$	3867.66	.198

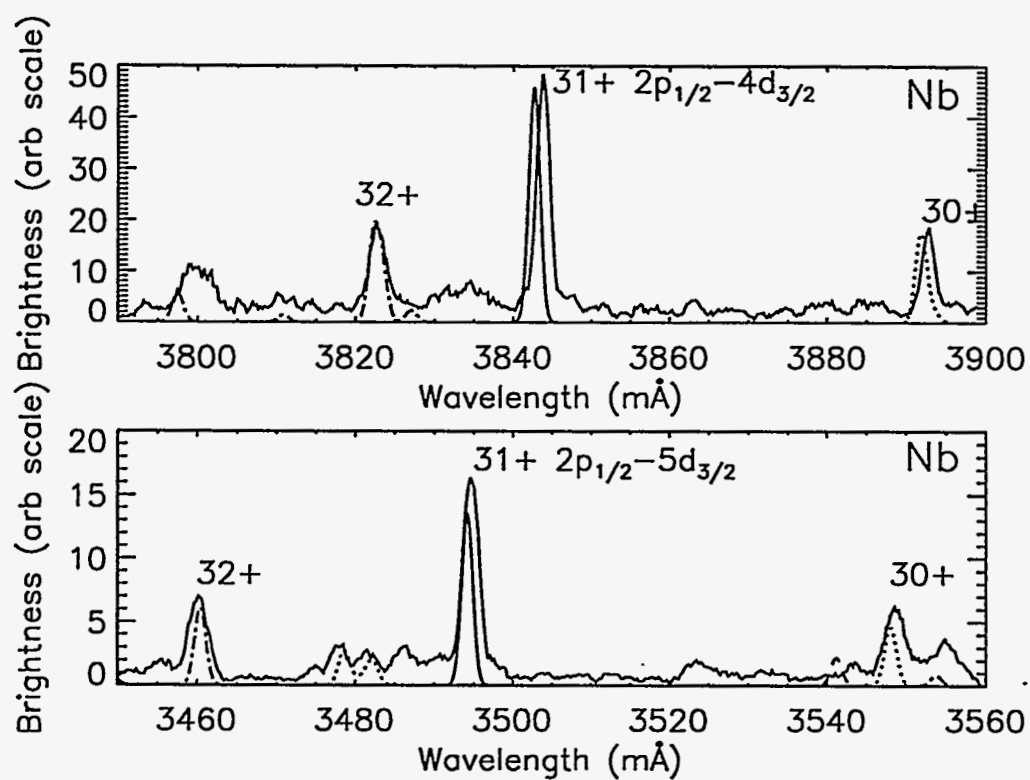


Figure 4: (a) 2p-4d and (b) 2p-5d transitions in neonlike  $Nb^{31+}$  (solid),  $Nb^{30+}$  (dotted) and  $Nb^{32+}$  (dash-dot dash).



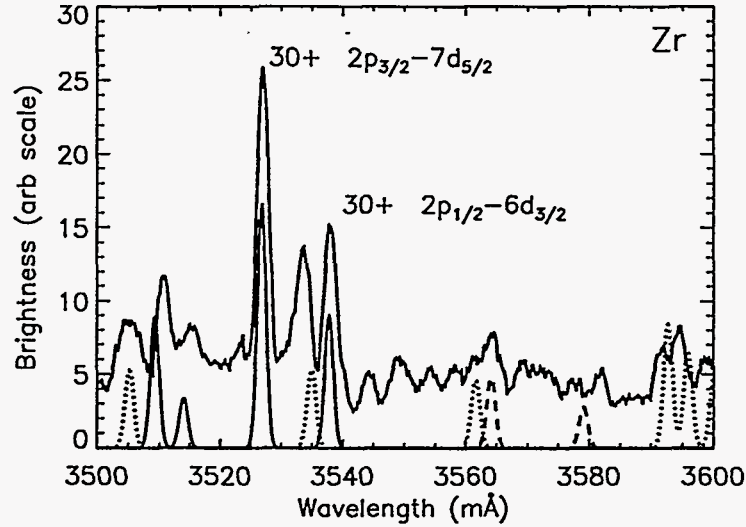


Figure 5:  $2p_{3/2} - 7d_{5/2}$  and  $2p_{1/2} - 6d_{3/2}$  transitions in neonlike  $Zr^{30+}$ , and the calculated neonlike (solid), sodiumlike (dotted) and fluorinelike (dashed) lines. Also shown are  $2s-5p$  transitions in  $Zr^{30+}$  (solid) at 3510.3 and 3515.1 mÅ.

-  $(2p^5)_{3/2} 7d_{5/2}$  transition at the expense of the  $2p^6 - (2p^5)_{1/2} 6d_{3/2}$  transition<sup>10,11</sup> in  $Mo^{32+}$ , where the difference in the upper state energy levels is 3.5 eV, and the interaction is quite large. A spectrum of these two lines in  $Zr^{30+}$  is shown in Fig.5. In the case of zirconium, the separation is 11 eV (11 mÅ) and there is little configuration interaction at all (the two lines are within a factor of 2 in intensity). This effect is summarized in Fig.6a where the calculated oscillator strengths of the  $2p^6 - (2p^5)_{3/2} 6d_{5/2}$ , the  $2p^6 - (2p^5)_{1/2} 6d_{3/2}$ , the  $2p^6 - (2p^5)_{3/2} 7d_{5/2}$  and the  $2p^6 - (2p^5)_{1/2} 7d_{3/2}$  lines are plotted as a function of atomic number. The oscillator strengths of the  $2p^6 - (2p^5)_{3/2} 6d_{5/2}$  lines and the  $2p^6 - (2p^5)_{1/2} 7d_{3/2}$  lines are relatively insensitive to atomic number. The magnitude of the configuration interaction between the  $2p^6 - (2p^5)_{1/2} 6d_{3/2}$  level and the  $2p^6 - (2p^5)_{3/2} 7d_{5/2}$  level is quite apparent; as the atomic number increases from Y to Mo, the  $g^*f$  value of the  $7d_{5/2}$  line increases while the value of the  $6d_{3/2}$  line decreases. At technetium ( $Z=43$ ), this effect dramatically switches; for Tc and above, the  $2p^6 - (2p^5)_{1/2} 6d_{3/2}$  line is at shorter wavelength and the  $2p^6 - (2p^5)_{3/2} 7d_{5/2}$  line is the *weaker* of the two. The wavelength differences between the two levels is shown in Fig.6b.

For the electron temperatures of Alcator C-Mod, palladium can just reach the neonlike state, and the lower charge states are present in abundance.

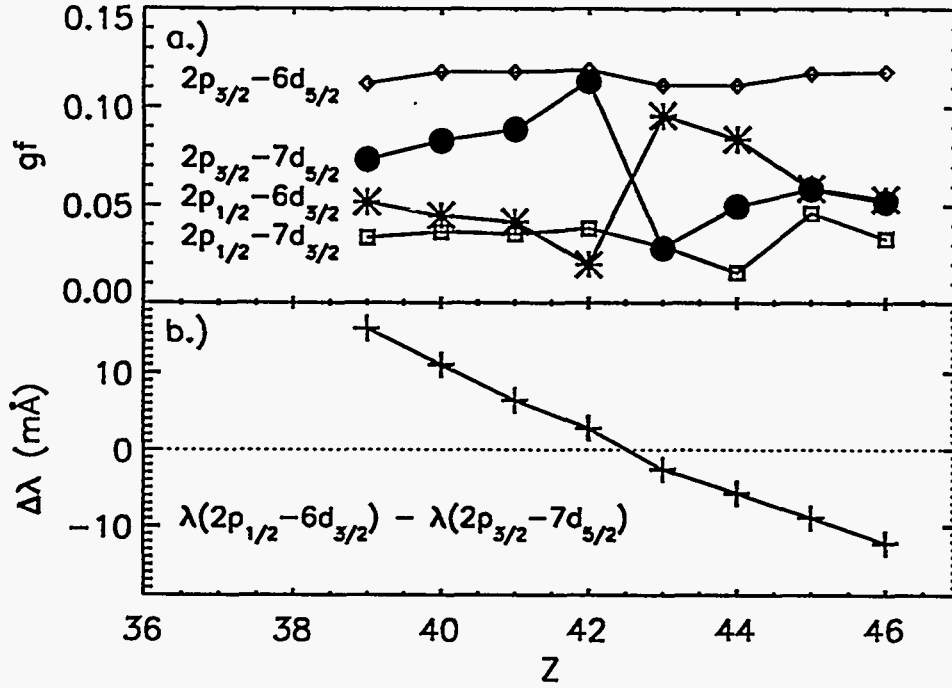


Figure 6: Calculated oscillator strengths (a) of 2p-6d and 2p-7d transitions and calculated wavelength differences (b) between  $2p_{\frac{1}{2}} - 6d_{\frac{3}{2}}$  transitions and  $2p_{\frac{3}{2}} - 7d_{\frac{5}{2}}$  transitions as a function of atomic number  $Z$ .

Table 2: Calculated neonlike 2p-nd E1 transition wavelengths and oscillator strengths for  $n = 6$  and  $7$  in  $Y^{29+}$ ,  $Tc^{33+}$ ,  $Ru^{34+}$  and  $Rh^{35+}$ . The upper level designations in the first column are indicated by three  $jj$ -coupled orbitals where '-' indicates  $l - s$  coupling and '+' indicates  $l + s$  coupling: the first two orbitals show the occupancy of the  $2p_{\frac{1}{2}}$  and  $2p_{\frac{3}{2}}$  subshells, respectively, and the third orbital is where the 2p-electron has been promoted.

Upper level	$Y^{29+}$		$Tc^{33+}$		$Ru^{34+}$		$Rh^{35+}$	
	$\lambda_T$ (mÅ)	$g^*f$	$\lambda_T$ (mÅ)	$g^*f$	$\lambda_T$ (mÅ)	$g^*f$	$\lambda_T$ (mÅ)	$g^*f$
$(2p_-)^2(2p_+)^36d_+$ J=1	3856.8	.112	3055.4	.111	32894.1	.111	2744.3	.117
$(2p_-)(2p_+)^46d_-$ J=1	3765.6	.0516	2967.1	.0955	2806.7	.0836	2657.7	.0587
$(2p_-)^2(2p_+)^37d_+$ J=1	3749.9	.0733	2969.7	.0280	2812.4	.0494	2666.6	.0583
$(2p_-)(2p_+)^47d_-$ J=1	3663.0	.0334	2885.7	.0289	2729.4	.0155	2584.3	.0460

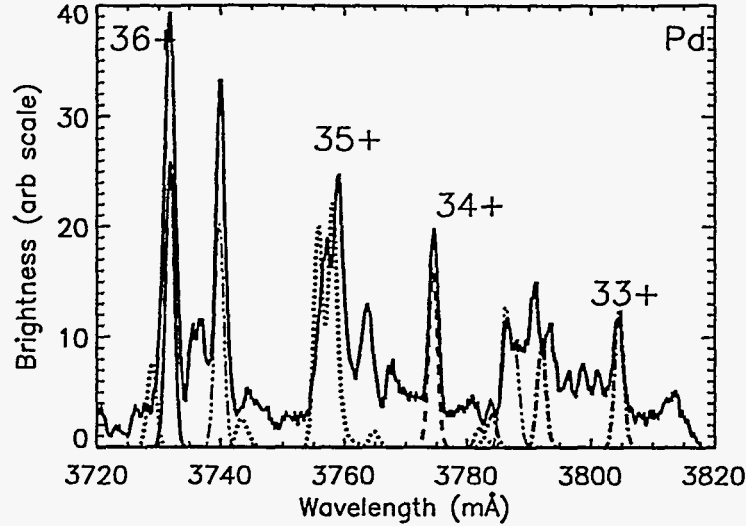


Figure 7: 2p-3d transitions in  $\text{Pd}^{33+}$  -  $\text{Pd}^{36+}$ . Theoretical lines for neonlike  $\text{Pd}^{36+}$  (solid),  $\text{Pd}^{35+}$  (dotted),  $\text{Pd}^{34+}$  (dashed) and  $\text{Pd}^{33+}$  (dash-dot-dash) are shown at the bottom, where the relative intensities within a given charge state are proportional to the oscillator strengths of each transition. Molybdenum transitions are shown by the thin dash-dot-dot-dot-dash lines.

Shown in Fig.7 is a spectrum of Pd 2-3 transitions in the vicinity of the  $2p^6 - (2p^5)_{\frac{1}{2}}3d_{\frac{3}{2}}$  line at 3731.7 mÅ. The corresponding lines in  $\text{Pd}^{35+}$ ,  $\text{Pd}^{34+}$  and aluminumlike  $\text{Pd}^{33+}$  are clearly identified.

## Conclusions

X-ray transitions in the magnesiumlike through fluorinelike charge states in zirconium, niobium, molybdenum and palladium have been observed from Alcator C-Mod plasmas. Line identifications have been made by comparison to the results of *ab initio* calculations and overall wavelength agreement is very good. The magnitude of the configuration interaction between the  $(2p^5)_{\frac{1}{2}}6d_{\frac{3}{2}}$  level and the  $(2p^5)_{\frac{3}{2}}7d_{\frac{5}{2}}$  level has been calculated as a function of atomic number for  $39 \leq Z \leq 46$ . 2p-3d transitions in aluminumlike  $\text{Pd}^{33+}$  have also been identified.

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