HIGH FREQUENCY ELECTROMAGNETIC TOMOGRAPHY

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Figure 2. Block diagram of the high frequency electromagnetic (HFEM) system.

\[ r \frac{\Delta \psi}{\omega} = \frac{\Delta \psi}{\omega_{0}} \]  

(1)

where:

- \( \Delta \psi \) = measured phase change
- \( \Delta \omega \) = angular frequency change (20 MHz)
- \( r \) = known ray path length
- \( \varepsilon_{r} \) = the electromagnetic permittivity of the rock
- \( \varepsilon_{0} \) = the electromagnetic permittivity of free space
- \( c \) = speed of light

we can obtain the line integral permittivity \( \psi_{k} \) along each ray. Equation (1) is valid for a homogeneous medium in the far field of the transmitting antenna.

DATA ANALYSIS

Image reconstruction is by an algorithm described by Dines and Lytle. The region in the plane between the boreholes is represented by the material parameters such as velocity \( v(x, y) \) or attenuation rate \( (x, y) \) which is to be calculated. Attenuation rate is a measure of how rapidly signal energy is dissipated with distance. However, work reported herein deals primarily with signal phase velocity, therefore we illustrate the analysis by writing the relation between it and total signal delay along the \( k \)th path \( D_{k} \):

\[ \tau_{k} = \sum_{i} \sum_{j} D_{ij} \text{ for } k = 1, 2, \ldots, K. \]  

(3)

where \( D_{ij} \) is the ray length of ray \( k \) through cell \( ij \) and it is understood that \( D_{ij} = 0 \) for all \( i \) and \( j \) not intercepted by a ray. Solution of Eq. (3) poses several problems. First the data \( \tau_{k} \) are necessarily inexact because of data noise which generally will make Eq. (3) inconsistent. Second, the number of independent equations can be insufficient so that the equations are underdetermined. Third, usually the number of equations is too large to be solved by direct inversion methods.

Iterative methods, especially suitable for computer solutions, have been devised which work well on underdetermined and inconsistent data. We have used the simultaneous iterative reconstruction technique (SIRT). It begins with an initial guess of \( v \) and calculates an estimate for the data \( \tau \). Then the difference between the data and calculated set is distributed along the ray paths. This leads to corrections in the estimated velocity function which, when applied, bring the estimate closer to the desired function. This process is repeated ray by ray and each cell is updated after all rays passing through a cell are considered. Ideally, these iterations continue until changes in the calculated \( \tau_{k} \) are of the order of the data noise. The algorithm is described in detail by Dines and Lytle. The resultant image can then be smoothed using a linear interpolation algorithm which averages over an effective length of about one cell dimension but produces an image with 9 times the number of cells actually used in reconstruction.

MEASUREMENT PRECISION

Both systematic and random measurement errors occur from several sources. In this section two of these potential error sources are discussed and an estimate made as to their impact on the HFEM results.

System Calibration. The measurement system was calibrated by subtracting, point by point, two phase characteristics; one when the antennas were placed adjacent to each other and the other for the measurement through the rockmass. In the first case \( r = 0 \) in Eq. (1) and therefore the system reference delay was adjusted to force \( \Delta \psi = 0 \) (see Eq. (1)). The difference between this phase characteristic and that measured through the rockmass provided a single calibration point for the system at \( r = 0 \).

One source of error introduced into each tomograph by this calibration is the seemingly simple requirement that the antenna separation is indeed zero. Actually, the requirement is that the separation be the same each time the calibration is performed. If it is not zero then the rockmass measurement of phase will be with respect to whatever separation is used. This fact works to our advantage because it allows removal of the
effects of the antenna casing (used to center the antennas in the boreholes) from the phase measurement. This is a problem because both antennas are in a casing designed to help center the antenna in the borehole and to remove the impedance mismatch between the air in the hole and the rockmass. The antennas slip a small amount in the casing during the experiment. Therefore, during the calibration procedure, placing the antenna casings adjacent to each other where the antennas were presumed to be, did not guarantee that the antennas were aligned. We estimate that the alignment error could have been as much as a few centimeters. Tests that we performed show that this type of alignment error would result in a typical uncertainty in the value of $\epsilon_r$ for the rockmass of 2% but an error always less than 5%.

Another disadvantage with this calibration is that the phase change is measurable only relative to an unknown but constant value. This is because the antennas are electromagnetically loaded differently for calibration and for data acquisition with the result that each calculated permittivity is shifted some unknown but constant amount. Therefore the measured values of permittivity are relative only. However, the alternant tomographs, formed from differences in measured relative permittivity, contain reliable information on the changes in permittivity.

**Multipath signal propagation.** One of the objectives for the HFEM work is to evaluate the impact of high contrast anomalies (e.g., metallic heater canister or large diameter borehole) on the validity of the image reconstructions. Such anomalies can cause complex reflection and refraction of the waves, making the data difficult or impossible to interpret with the approximation of straight ray paths used by our inversion algorithm. Accurate determination of the effects of the heater would have required comparison of reconstructions from data sets taken before the heater hole was drilled and after it was drilled and the heater installed. However, other factors dictated that the heater hole was the first hole drilled. Therefore, our test for effects of interference from the heater had to be a comparison of reconstructions with the heater in place and with it removed. This test showed that reconstructions from data sets taken before the heater hole was drilled and after it was drilled and the heater installed. However, other factors dictated that the heater hole was the first hole drilled. Therefore, our test for effects of interference from the heater had to be a comparison of reconstructions with the heater in place and with it removed. This test showed that reconstructions in the image planes between Ne2a and Ne1, Ne3 and Ne4 (9.5 to 11.5 m) and between Ne4 and Ne5 (9.5 to 11.5 m) were least affected by scattering from the heater. In fact, in the half of each of these image planes furthest from the end of the heater (see Fig. 1), the effect was to change the pixel values of $\epsilon_r$ by less than 0.15.

**DATA INTERPRETATION**

The tomographs generated in this work are of electromagnetic permittivity of the rockmass. Of course, images of this parameter by itself are of little help in determining the near field environment of the canister. To be useful electromagnetic permittivity must be interpretable in terms of water content in the rock, because this is the property that has a bearing on the canister survivability.

A quantitative interpretation requires laboratory calibration of the electromagnetic properties of densely welded tuff, that is, measurement of their dielectric properties as a function of water content and temperature. This calibration then allows inference of in situ water content from tomographic dielectric

![Figure 3. Laboratory measured and model calculations of the relative permittivity as a function of water content. The points are laboratory measurement of the electromagnetic permittivity (real part) of densely welded Grouse canyon tuff of porosity 0.14. Reflection and transmission coefficients measured in a coaxial air line at 200 MHz were used to calculate the permittivity. Water from well J-13 was used as the pore fluid. The solid line is the relative permittivity as a function of water content for a multiphase dielectric mixture model. Spherical inclusions of air (\(\epsilon_r = 1\)) and thin needle inclusions of water (\(\epsilon_r = 81\)) are dispersed in a background of silicate material (\(\epsilon_r = 5\)) of total porosity 0.14. The dashed line is for the same model but with a water permittivity of 56 which is appropriate for pore water at 100 C.](image)
room temperature. The rock is considered a mixture of components, each having a specific electromagnetic property. To model an unsaturated rock, we consider a three-component mixture: solid matrix, pore water, pore air. Various theories, each with its characteristic approximations and assumptions, have been developed for such a dielectric mixture. Silhvoia and Kong* review some of these theories. We will use a multiphase formula where the n different inclusion phases are in the form of arbitrary ellipsoids. If the inclusion orientations are random so that the mixture is isotropic on a macroscopic scale, the effective permittivity is

\[
\varepsilon_{\text{eff}} = \varepsilon + \frac{1}{3} \sum_{m=1}^{n} \varepsilon_m + N_{\text{in}} \frac{\varepsilon - \varepsilon_m}{\varepsilon + N_{\text{in}} (\varepsilon - \varepsilon_m)}
\]

(4)

where \( N_{\text{in}} \), \( N_{\text{in}} \), and \( N_{\text{in}} \) are the depolarization factors of the \( k \)th phase, \( \varepsilon_{\text{eff}} = \varepsilon_{\text{eff}} \) is the fractional volume of the \( i \)th phase and \( \varepsilon_{\text{eff}} \) is the background permittivity. In our model, the background dielectric is the silicate matrix and the two inclusion phases are the two pore fluids in a partially saturated rock—water and air. If the permittivities are complex, we have a model of a lossy mixture since \( \varepsilon = \varepsilon_r - j\varepsilon_i \) where \( j = \sqrt{-1} \) and \( \varepsilon_r = \sigma/\omega\varepsilon_0 \). The real component \( \varepsilon_r \) describes the phase velocity which is approximately \( \sqrt{\varepsilon_r/\varepsilon_0} \). The imaginary component describes energy dissipation from both dielectric (e.g., orientation of dipole moments) and ohmic losses (e.g., motion of charge carriers). Therefore, \( \sigma \) contains both dielectric and the more familiar ohmic conductivity. The angular frequency is \( \omega \). Notice that the assumption of noninteracting inclusions is not really valid. That is, the inclusions are not isolated so that their perturbations on the field are independent. The effect of this on the calculated effective permittivity is not known. Unfortunately, we find no mixture theory capable of accounting for interacting inclusions.

For our dielectric mixture model, we need the permittivity of each component. The relative permittivity of water is known to be a very nearly constant value of 81.2 (at 17°C) between 0 and 600 MHz. To demonstrate the use of Eq. (4), we assume \( \varepsilon_w = \varepsilon_{\text{water}} = 80 \) and \( \varepsilon_s = \varepsilon_{\text{silicate}} = 1 \). To obtain the permittivity of the rock matrix, \( \varepsilon_{\text{eff}} \) in Eq. (4)), we use our 200 MHz laboratory measurements of the dielectric permittivity of G-tunnel tuff (see Fig. 3). An automatic network analyzer was used to measure the transmission and reflection coefficients of a tuff sample machined to fit in an air line and from these the sample permittivity was calculated. When the sample was dry, the calculated relative permittivity was 4.35. This value is not representative of the silicate matrix because it incorporates the effects of the 14 volume percent pore space. To calculate the silicate permittivity, we can use Eq. (4) with \( \varepsilon_s = 4.35 \) and solve for \( \varepsilon_{\text{eff}} \). We model the rock as a single inclusion mixture; the pores as spherical inclusions (\( N_{\text{in}} = N_{\text{in}} \) = \( N_{\text{in}} = 1/3 \)) of volume fraction \( f = 0.14 \) and \( \varepsilon_{\text{in}} = 1 \) for air. We find that the silicate matrix relative permittivity is about 5.

Now, using the background permittivity \( \varepsilon_{\text{eff}} = 5 \) in Eq. (4), we can estimate the rock permittivity as a function of porosity and saturation. Figure 3 shows the model results assuming the air component are spherical inclusions and the water component are randomly oriented thin needles (prolate spheroids, depolarization factors 0, 1/2, 1/2). This model was chosen because it is a reasonable representation to the measured data and is also a reasonable model for water held by capillarity along the pore wall and air filling the remaining central part of the pore. (It turns out that the results do not differ more than 10% if we assume randomly oriented disk shaped inclusions [oblate spheroids with depolarization factors 1, 0, 0] to model the water.)

This model should represent the rock at about 20°C but does not account for the fact that the permittivity of many materials depends on temperature. We have measured the permittivity of dry tuff and found that it is independent of temperature between 20 and 70°C. We conclude from this that the silicate matrix and air inclusion components of our mixture do not require a temperature dependent model. However, the relative permittivity of water has a well documented temperature dependence given by Eisenberg and Kauzmann\(^4\) as \( \varepsilon_w = 87.740 - 0.47T + 9.398 \times 10^{-4} T^2 \). This temperature dependence is included for water in Eq. (4), the effective permittivity of the mixture decreases with temperature as shown in Fig. 3.

These models demonstrate several concepts important to interpreting the permittivity tomographs. First, over the range of parameters of interest, the permittivity is nearly linearly related to the water content. This fact can be used to interpret the alternant tomographs, using the slope of the curves to infer changes in water content. Second, the fractional volume of pore filled by air contributes very little to the rock mass permittivity. This is because the silicate matrix and especially the water have such high permittivities compared to that of air. In fact, for practical considerations, the contribution of the air could be neglected and the system could be modeled with a single inclusion (water) in the background (silicate). Third, the effect of temperature on the water permittivity could be important to accurate determination of water content. For a saturated porosity of 15 volume% at 100°C, the water content could be underestimated by about 20% using the room temperature model. Also, \( \varepsilon_{\text{eff}}/df\) will decrease about 28% between room temperature and 100°C. Ignoring this effect when interpreting an alternant tomograph would lead to an overestimate in the amount of dehydration during heating. Therefore, we will use the airline data in Fig. 3, \( \varepsilon_{\text{eff}}/df\), to interpret changes in rock mass moisture content at or near room temperature but will assume a 28% smaller slope to interpret changes in moisture at 100°C.
RESULTS AND DISCUSSION

Ray Data. The data shown in Fig. 4 is the measured relative permittivity along rays for which the transmitter and receiver were at common depths in their respective boreholes. Each point is a measure of the right hand side of Eq. (1) divided by the ray path length. For example, the point at 11.0 m depth represents the average permittivity (as a function of time) for the rock along a line which connects the transmitter and receiver at 11.0 m depth. We present this data first because it is part of the input to the reconstruction algorithm. Of course in this format the spatial information generated by the reconstruction is absent, but the artifacts generated by the reconstruction are also absent so that quantitative interpretation of the results should be more reliable.

Figure 4 shows an example of this data between Ne4 and Ne5. This plane is parallel to the heater, 0.7 m to one side and below the heater in elevation. Between August 26th, 1988 and March 29th, 1989 the relative permittivity decreased by approximately 3.8 (changes in $\varepsilon''$ of about 0.5). Of course, the rockmass is not homogeneous, therefore, this is a rough average over a region with extremes in permittivity changes from 4.5 to 1.8. If the rockmass was at 20 C during the period, a 3.8 variation would represent a change in fractional water content of about 0.13 (from the measured data in Fig. 3). If we assume the rockmass was always at 100 C the calculated water content change would be 28% higher or 0.17. The actual change in water content is likely between these values. Either figure represents a substantial drying of the rockmass at a distance of more than one meter from the end of the heater.

The overall dehydration measured between Ne4 and Ne5 appears not to be monotonic. The initial permittivity decrease was followed by an increase recorded on September 26th. This may correspond to a saturation halo preceding the drying front. If so the data indicate an increase in fractional moisture content up to 4.5 over initial conditions. The increase between January 19th and February 27th is of similar magnitude but both are of the order of the system calibration error and so that their interpretation is uncertain.

Cross borehole ray data between holes Ne2a to Ne6 and Ne6 to Ne7 (not shown here) indicate that before the experiment started there was a higher water content in the rockmass below the heater than above. These two data sets are from the uppermost and lowest parts of the rock where HFEM measurements were made. Because of the proximity of the heater to Ne6, data from the full length of that hole cannot be used for reliable calculation of permittivity values. However, data at the extremes of the range measured show that above the heater (between Ne6 and Ne7) the typical relative permittivity is about 7.8 while below the heater (between Ne2a and Ne6) the permittivity is typically about 10.0 (remember that these absolute values are not accurate because of uncertainties in system calibration but their relative magnitudes should be reliable). If these data are representative of the rockmass adjacent to the experiment, the upper part of the rock may be dryer than that below (lower fractional water content of 0.08). We have no way of knowing if this was a pristine condition. On the other hand, a possible external source of such a moisture gradient is the drill water used for the 11 boreholes used in the experiment.

Tomographs. Over the course of the 10 month experiment, data was acquired for more than 100 tomographs; each data set required the collecting of from 81 to 441 individual data points, depending on the region sampled. Figure 5 shows an example of the tomographs taken during the experiment for the region between boreholes Ne4 and Ne5 between 9.5 and 11.5 m depth. Unfortunately, the data used for these reconstructions was influenced by the proximity of this plane to the heater. However, we have determined that between 10.5 and 11.5 m the reconstructed $\varepsilon''$ is changed by less than 0.15 by the proximity of the heater. Shallower than 10.5 m the influence can be larger but varies a lot depending on the location within the image. Deeper than 10.5 m the reconstruction reflects more accurately, the heterogeneity in the rockmass permittivity before heating began. For this part of the image plane the variation in $\varepsilon''$ introduced by measurement imprecision is 0.04 (estimated by comparing two tomographs taken when no known changes were occurring in the rockmass).

Figure 5a is the tomograph between Ne4 and Ne5 before heating. The range of imaged relative permittivity deeper than 10.5 m is from about 6.2 to 16.0. The calibration data in Fig.
3 (extrapolated) suggests that this represents a fractional moisture content contrast of about 0.34. This is a fairly large range and is possible for only two regions, each represented by a single pixel. A more representative range of permittivity is 9.0 to 12.2 which implies a contrast of 0.11 in fractional water content.

In this same reconstruction, the region near Ne4, at about 960 cm depth, is imaged as a very low permittivity. Even though this data is contaminated by the presence of the heater, our tests indicate that this anomaly is indicative of a rockmass anomaly. This region is likely a highly fractured zone with apertures too large to retain a significant amount of water by capillarity. The preheating borehole logging identified a highly fractured zone exactly at this location in Ne4. Typically, fracture orientation was measured in these logs. At this location, however, orientation could not be determined because of the high fracture density. An interesting speculation is that a particularly high porosity was created during drilling as a washout in an intensely broken zone. For the image plane as a whole, however, there seems to be a poor correlation between logged fractures in either borehole and either high or low permittivity image anomalies.

Figure 5. Tomographs between Ne4 and Ne5 from 9.5 to 11.5 m depth.

(a) Baseline image of (εr)1½ taken before the heater was turned on, August 26, 1988. Fractures and approximate orientation are shown as logged in both boreholes before the test began. The approximate location of the heater and borehole are projected into the image plane.

(b) Alterant image of Δ(εr)1½ for January 9, 1989. The color scale represents the change in (εr)1½ calculated by subtracting the baseline tomograph from the January 9th image so that an increase in permittivity is positive in the alterant image. Each image area is 2 m by 1.5 m, contains 416 pixels (each about 9 cm by 8 cm) and is reconstructed from phase measurements along approximately 440 ray paths.

(b) Alterant image of Δ(εr)1½ for January 9, 1989. The color scale represents the change in (εr)1½ calculated by subtracting the baseline tomograph from the January 9th image so that an increase in permittivity is positive in the alterant image. Each image area is 2 m by 1.5 m, contains 416 pixels (each about 9 cm by 8 cm) and is reconstructed from phase measurements along approximately 440 ray paths.

Deeper than 10.5 m the image is more reliable. As in the baseline image, there is no strong correlation of image anomalies with borehole fractures. This means that these fractures are neither wetter (acting as a flow path for liquid water) or dryer than the surrounding rock and perhaps contribute little to the hydrology of the system.

One puzzling property of the alterant image of Fig. 5b is the high correlation between increases in permittivity during heating and regions of higher preheating rockmass permittivity. Conversely, regions of decreased permittivity correlate with regions of lower preheating permittivity. More specifically, while there is an overall decrease in permittivity during heating, the local regions that do indicate a small increase are those regions that have lower permittivity prior to heating. One possible explanation is that these are fractured zones: drained of water before the test, they contain condensate during heating.
Summary. HFEM data is useful for characterizing the water distribution in the near field of a simulated waste container. First, we used data from individual ray paths to determine quantitative estimates of how moisture content in the rockmass changes during heating. This interpretation is an average over the ray length between the boreholes so has little information on spatial variability. However, the results are semiquantitative; only with a valid calibration of the measurement system could the results be quantitatively reliable. With such a quantitative measurement, a determination of absolute water content of the rockmass may be possible. Second, we used the tomographs generated from the cross borehole data to infer properties of the spatial variability of water distribution. This interpretation lead to conclusions about the role of fractures in the system.

We have shown that the parallel scan data and the tomographs suggest that the rock immediately around the heater begins to dry as soon as the heater is turned on. Rock further from the heater shows an early wetting episode probably caused by condensation of steam in cooler portions of the rock. Following this wetting, the rock begins to dry as temperatures and evaporation rate increase. Some fractures and highly fractured zones may remain wetter than preheating conditions long after the surrounding rock matrix has begun dehydration. Our data does not directly indicate if this water is stationary or flowing. However, since other parts of the rockmass in these image planes are drying and these fractures are not, it is likely that these fractures are conduits for water movement during the heating process.

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