Preprocessing of Backprojection Images in the McClellan Nuclear Radiation Center Tomography System

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Abstract

Neutron tomography is being investigated as a nondestructive technique for quantitative assessment of low atomic mass impurity concentration in metals. Neutrons maximize the sensitivity given their higher cross sections for low Z isotopes while tomography provides the three dimensional density information. The specific application is the detection of Hydrogen down to 200 ppm weight in aircraft engine compressor blades. A number of preprocessing corrections have been implemented for the backprojection images in order to achieve the detection requirements for a testing rate of three blades per hour. Among the procedures are corrections for neutron scattering and beam hardening. With these procedures the artifacts in tomographic reconstructions are shown to be less than the signal for 100 ppm hydrogen in titanium alloy samples.
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1. INTRODUCTION

Neutron radiography has already proven itself as a reliable method for the detection of hydrogenous substances, such as moisture and corrosion, in aircraft components [fro90]. Internal properties of objects are distinguished by differences in the attenuation coefficients of different materials. The advantage with neutrons is that low atomic number nuclei such as hydrogen have higher interaction cross sections than the surrounding metal. At the McClellan Nuclear Radiation Center (MNRC) four radiography bays use both film and real-time imaging devices to inspect aircraft components [ric90] [alv90]. Radiographic images can be displayed in real-time at an operator's console as robots move parts across the neutron beam. Trained radiographers are able to rapidly identify regions of corrosion. Traditional radiography has limits since it only provides information on the total attenuation integrated over the path of the radiation through the material. The actual distribution of hydrogen across that path is not known precisely.

As an extension to radiographic methods the MNRC is investigating the use of neutron tomography to obtain quantitative hydrogen concentration data for aircraft engine compressor blades. The hydrogen concentration can be used as an indicator for the loss of mechanical properties, embrittlement, which can occur in metals after exposure to hydrogen [pat74] [nel83]. In this case the defect to be identified is low concentrations of hydrogen diffused into the metal not corrosion or cracks. The signals to be detected are too small to be recognized from a traditional radiograph by the human eye. The goal of the tomography system is to provide a nondestructive inspection technique giving accurate hydrogen concentration data from several thousand down to 200 parts per million (ppm) weight for a total engine fan blade at a rate of three blades per hour. The blades are composed of Ti6Al4V alloy with a height of 30 cm, an average width of 9 cm, and an average thickness of 0.64 cm. The blades twist from top to bottom and have a crescent cross section precluding the use of simple radiography which might be appropriate for a flat plate of metal.

The requirements for a system, that can achieve the above goal, result in
certain characteristics. The order of magnitude variation in spatial dimensions of the blades coupled with the rapid production rate favor a large neutron beam with a relatively high flux. The system must also be able to perform with a minimum number of tomographic projections to save time while maintaining a spatial resolution sufficient to resolve less than 0.5 cm. The requirement to detect the distribution of low hydrogen concentrations resulted, as mentioned previously, in the choice of tomography over radiography. In addition, errors and artifacts in the projections and reconstructions must be minimized to increase the signal to noise ratio for the calculated attenuation coefficients.

This paper describes the techniques used to preprocess the neutron radiographs so the resulting tomographic reconstructions meet the requirements for compressor blade evaluation. Preprocessing removes spurious signals caused by CCD camera dark charge, by beam intensity fluctuations, by background noise, by object neutron scattering, and by beam hardening. Reconstructions of various samples are shown to validate the techniques. The resulting neutron tomography system is applicable to a wide range of NDE tasks where rapid evaluation of low Z impurity concentrations is needed.

The tomography system consists of a neutron source, an object turntable, a scintillator screen, a mirror, a CCD camera, and computer support as shown in figure 1.1. The neutron source is a 2 MW TRIGA thermal reactor. The neutron beam in radiography bay 3 is approximately 50 cm in diameter at the scintillation screen, and the ratio of the collimator aperture to screen distance over the collimator diameter is 235 (653 cm/2.8 cm). The thermal neutron flux at 2 MW reactor power is $1.2 \times 10^7$ n/cm²s which is about 50% of the total flux in the beam. Four object turntables are fixed to a robot which can place them at different positions and orientations. Each turntable has fixtures that can accommodate up to three compressor blades. Normally one turntable is centered approximately 10 cm in front of the scintillator screen. A shutter blocks the beam port, when it is not in use, allowing access to the bay while the reactor is at power. With this bay configuration a dozen blades can be inspected, and then a new lot can be set in place without interrupting reactor operation.

The neutrons are detected with a scintillator screen which uses Li6 as the neutron absorber. Given the decrease in the Li6 absorption cross section with increasing energy, most of the neutrons detected are in the thermal region of the energy spectrum. The screen light output is $1.7 \times 10^5$ photons per neutron with an absolute scintillation efficiency of 9% and resolution limits of less than 100 µm[spo69] [net94].
Figure 1.1: The MNRC neutron tomography system
Photons generated in the screen are reflected from the mirror, pass through a lens and enter the CCD detector. Usually a 50 mm lens is used giving an image pixel size of 0.057 cm. The CCD detector has a rectangular array of 1024 x 1024 pixels (24 µm x 24 µm pixels). The photoelectrons generated at each CCD pixel comprise the electrical signal and are proportional to the number of neutrons detected. The CCD quantum efficiency is 80% in the 0.6-0.7 µm range where the scintillator emits its light [pim93]. The image data is collected in a 16 bit format.

Image acquisition and reconstruction is controlled with two workstations. One provides control to the CCD camera and sample turntable as well as image data capture and image analysis functions while the other provides tomographic reconstruction and image analysis functions.
2. Image Characteristics

The characteristics of the radiographic images, used as backprojections for the tomographic reconstruction, set the fundamental limits on the accuracy of the reconstruction. The noise and resolution characteristics of the images are described in this chapter.

2.1. Spatial Resolution and Focusing

The size of detectable defects in tomographic reconstructions is limited by the spatial resolution of the initial backprojection images. Focusing procedures and edge spread in the images are summarized in this section. We have not found it necessary to make corrections of the resolution in the backprojection images. This section provides the information necessary to perform such corrections should they become needed.

2.1.1. Camera Focusing

The camera is focused by imaging a sheet of paper with a set of five converging lines. The paper is placed on the back of the scintillation screen, and the camera lens is focused so that the lines can be distinguished as close as possible to the convergence point. The pixel size is found by counting the number of pixels required to extend a length of 10 inches as measured by an imaged ruler. The pixel size and lens configurations are listed in table 2.1. A focusing image with the 50 mm lens is shown in figure 2.1.

2.1.2. Spatial resolution in the beam image

After focusing is complete, the sharpness of an edge can be determined using neutron absorbing objects at various distances in front of the scintillation screen. Cadmium squares 4 cm across and 0.076 cm thick were placed at several distances in front of the screen. The intensity behind the Cd is approximately 10% of the
Figure 2.1: Focusing image generated with the 50 mm lens.
Table 2.1: Tomography system lens configurations

<table>
<thead>
<tr>
<th>Lens Configuration</th>
<th>Pixel size</th>
</tr>
</thead>
<tbody>
<tr>
<td>50 mm</td>
<td>0.0571 cm</td>
</tr>
<tr>
<td>50 mm and 2X teleconverter</td>
<td>0.0273 cm</td>
</tr>
<tr>
<td>135 mm and 2X teleconverter</td>
<td>0.0102 cm</td>
</tr>
</tbody>
</table>

unimpeded beam intensity. The resolution is calculated by fitting an edge spread function to an intensity curve which crosses each square. The intensities are normalized using an image of the unperturbed beam, a flat field image.

The edge spread function is found from the point spread function, \( P(x, y) \), assumed for the beam. As in Harms and Wyman [har86], the general point spread function, which may be due to converter unsharpness, scattering, diverging beam, etc., is

\[
P(x, y) = \frac{\lambda^2}{2\pi \left[ 1 + \lambda^2 \left( (x-\eta)^2 + (y-\nu)^2 \right) \right]^{3/2}}
\]  

(2.1)

Here \( \lambda \) is the resolution parameter, \( x, y \) are the coordinates in the image plane, and \( \eta, \nu \) are the coordinates in the object plane.

The flux distribution at the screen, \( \Phi(x, y) \), is found from the convolution integral of the flux at the object, \( \Psi \), and the point spread function. The integral has the form

\[
\Phi(x, y) = \frac{\lambda^2}{2\pi} \int \int \frac{\Psi(x-u, y-v) \, du \, dv}{(1 + \lambda^2 (u^2 + v^2))^{3/2}}
\]  

(2.2)

where \( u = x - \eta \) and \( v = y - \nu \). Assuming a constant flux, \( I_o \), and integrating over \( du \), we find

\[
\Phi(x, y) = \frac{\lambda^2}{2\pi} \int \frac{I_o \, du \, dv}{(1 + \lambda^2 v^2) \left( 1 + \lambda^2 (u^2 + v^2) \right)^{1/2}}
\]  

(2.3)

The final result is

\[
\Phi(x, y) = \frac{I_o}{2\pi} \arctan \left( \frac{\lambda^2 uv}{\left( 1 + \lambda^2 (u^2 + v^2) \right)^{1/2}} \right)
\]  

(2.4)

Consider a rectangle of material which attenuates the normalized signal to the level \( \alpha \) and has spatial extent from \( x_m \) to \( x_p \) and \( y_m \) to \( y_p \). The function of eq. (2.4)
must be integrated over five regions. The result along \( y = 0 \) for a rectangle of material extending from \(-b\) to \(b\) in \(y\) is

\[
\Phi(x, 0) = 1 + \frac{1}{\pi} (1 - \alpha) \left[ \arctan \left( \frac{\lambda^2(x-x_p)b}{(1+\lambda^2((x-x_p)^2+b^2))^{1/2}} \right) \right. \\
- \arctan \left( \frac{\lambda^2(x-x_m)b}{(1+\lambda^2((x-x_m)^2+b^2))^{1/2}} \right) \right] \\
(2.5)
\]

The spatial resolution, defined as the distance over which the intensity decreases from \(.75(1 - \alpha) + \alpha\) to \(.25(1 - \alpha) + \alpha\), is approximately \(2/\lambda\). Note that the result in the limit of \(b \to \infty\) is

\[
\Phi(x, 0) = 1 + \frac{1}{\pi} (1 - \alpha) \left[ \arctan (\lambda(x-x_p)) - \arctan (\lambda(x-x_m)) \right] \\
(2.6)
\]

A Levenberg-Marquardt [pre88] algorithm was used to find a best \(\chi^2\) fit to the data with \(\alpha, \lambda, x_m, x_p\) as parameters for the nonlinear edge spread equation. The limiting equation, (2.6), was found to be sufficient since the vertical extent of the object would have to be less than 0.5 cm before the results are significantly affected.

A significant portion of the edge spread is due to the divergence of the neutron beam. The flux profile due to diverging beam edge spread is flatter behind the absorbing object than that resulting from the general edge spread function. Since this project requires the accurate determination of small changes in attenuation, it is important to consider the edge spread function specific to a diverging beam. For this work consider a strip beam of half width \(a\).

\[
\Phi(x) = \frac{\lambda I_o}{\pi} \int_{-a}^{a} \frac{\Psi(x + \eta l/L) d\eta}{1 + \lambda^2 (x - \eta)^2} \\
(2.7)
\]

Here \(L\) is the beam collimator plane to object plane separation, \(l\) is the object plane to image plane separation, and \(\lambda = 1/(L + l)\).

If there is no object in the beam the flux is

\[
\Phi(x) = -\frac{I_o}{\pi} \left[ \arctan \left( \frac{x - a}{L + l} \right) - \arctan \left( \frac{x + a}{L + l} \right) \right] \\
(2.8)
\]

At \(x = 0\) this becomes

\[
\Phi(0) = \frac{2I_o}{\pi} \arctan \left( \frac{a}{L + l} \right) \\
(2.9)
\]
Now consider an absorbing object with attenuation $\alpha$ positioned from $x = -\infty$ to $x = 0$. The image flux becomes

$$\Phi(x) = \frac{M_\lambda}{\pi} \int_{-\infty}^{a} \frac{1}{1 + \lambda^2 (x - \eta)^2} \left[ \alpha H(-x - \eta l/L) + x + \eta l/L \right] d\eta \quad (2.10)$$

where $H(x)$ is the Heaviside function. The solution is

$$\Phi(x) = \begin{cases} 
\frac{-\alpha}{\pi} [\arctan(\lambda (x - a)) - \arctan(\lambda (x + a))] & xL/l \leq -a \\
\frac{-1}{\pi} [\arctan(\lambda (x - a)) - \arctan(\lambda x (1 + L/l))] & a \geq xL/l > -a \\
\frac{-\alpha}{\pi} [\arctan(\lambda x (1 + L/l)) - \arctan(\lambda (x + a))] & xL/l > a 
\end{cases}$$

The total width of the intensity transition region from 0 to 1.0 is approximately $2\alpha l/L$ for divergences small compared to $\alpha$. The spatial resolution is given by $\alpha l/L$. For the MNRC reactor $\alpha = 1.41$ cm (before the 1996 upgrade to 2 MW $\alpha = 2.81$ cm) and $L = 653$ cm. This function, unlike the general point spread function, results in a penumbra which does not extend beyond the spatial resolution distance.

The edge spread results for several Cd positions are shown in table 2.2. Column three of the table lists the results from fits of the general edge spread function to the experimental data, and column four lists the expected result for beam divergence. The resolution is worse than what is predicted from beam divergence alone. Results before and after the reactor upgrade from 1MW to 2 MW are listed. With the upgrade the collimator diameter was decreased to maintain the same flux at the end of the beam tube. The resolution has become finer but not by a factor of two. This result is consistent with edge spreads having sources other than beam divergence. The important result for the tomography project is that objects centered at 10 cm from the screen have resolutions of approximately 0.5 mm.

A comparison between the data and the fit for the 10.0 cm position, 2 MW case is shown in figure 2.2. The data intensity is essentially flat behind the cadmium. This behaviour is best fit by the edge spread function specific to beam divergence; however, the collimator diameter used to achieve this fit was significantly larger (13.4 cm) than the actual collimator. The edge spread appears to have contributions from other sources which worsen the resolution, but keep the intensity behind the object relatively flat. The general edge spread function tends to cause a small dip in intensity of about 1% behind the object. This could
Table 2.2: Tomography system resolution

<table>
<thead>
<tr>
<th>Cd Position (cm)</th>
<th>λ (cm⁻¹) resolution (cm)</th>
<th>resolution (cm)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>general</td>
<td>general</td>
</tr>
<tr>
<td>1 MW on screen</td>
<td>44.83 0.0446 0.0</td>
<td></td>
</tr>
<tr>
<td>4.0</td>
<td>30.17 0.0663 0.0172</td>
<td></td>
</tr>
<tr>
<td>11.5</td>
<td>27.97 0.0715 0.0495</td>
<td></td>
</tr>
<tr>
<td>31.5</td>
<td>20.45 0.0978 0.136</td>
<td></td>
</tr>
<tr>
<td>2 MW on screen</td>
<td>49.63 0.0403 0.0</td>
<td></td>
</tr>
<tr>
<td>10.0</td>
<td>33.11 0.0604 0.0215</td>
<td></td>
</tr>
<tr>
<td>30.0</td>
<td>24.21 0.0826 0.0645</td>
<td></td>
</tr>
</tbody>
</table>

be a matter of concern since the signals to be detected with the system require the intensity to be accurate to less than 1%. As shall be shown in chapter 3, the intensity information in images will be related to object thickness through a table of attenuation vs thickness. Images which have been corrected for edge spread must use material thickness data from a table generated using calibration images which were corrected for edge spread in the same manner.

Correction of images can be accomplished by considering the convolution integral resulting in the image flux

\[ \Phi(x,y) = \Psi(x,y) * P(x,y). \] (2.12)

The Fourier transform of the convolution is

\[ \mathcal{F} \{ \Phi(k_x, k_y) \} = \mathcal{F} \{ \Psi(k_x, k_y) \} * \mathcal{F} \{ P(k_x, k_y) \}. \] (2.13)

So the actual object intensity distribution is found from the inverse Fourier transform, IFT,

\[ \Psi(x,y) = \mathcal{F}^{-1} \{ \mathcal{F} \{ \Phi(k_x, k_y) \} / \mathcal{F} \{ P(k_x, k_y) \} \}. \] (2.14)

The Fourier transform of the point spread function is called the modulation transfer function, MTF. A filter function may be necessary to limit anomalously large signals at high frequency due to noise in the image signal. The only quantity needed for these corrections is the resolution parameter given in table 2.2. Since the resolution is about the same as the pixel size, edge spread corrections have not been incorporated into the image preprocessing at the present time.
2.2. Noise in images

Noise will exist in any image taken using the system. This section identifies the sources of noise, its magnitude, and possible improvements. We shall note the contribution of the noise sources to either random or systematic errors. Random error measurements will be used to determine the limit on the minimum signal magnitude while systematic error measurements will provide the parameters necessary for image correction.

2.2.1. Random errors

The pixels in a CCD experience a thermally induced buildup of charge as a function of time. Each pixel will tend to build up charge at a slightly different rate as
Table 2.3: CCD camera dark charge

<table>
<thead>
<tr>
<th>Exposure (sec)</th>
<th>Intensity mean</th>
<th>Intensity standard deviation</th>
</tr>
</thead>
<tbody>
<tr>
<td>5</td>
<td>247.</td>
<td>48.2</td>
</tr>
<tr>
<td>10</td>
<td>339.</td>
<td>86.4</td>
</tr>
<tr>
<td>20</td>
<td>527.</td>
<td>175.</td>
</tr>
<tr>
<td>40</td>
<td>935.</td>
<td>365.</td>
</tr>
</tbody>
</table>

well as suffer from statistical noise within each pixel. The manufacturer quotes a rate of 3-6 electrons/pixel/sec when this camera is operated at -50 °C which corresponds to 0.5 counts /pixel/sec[93]. This gives 6 to 12 electrons for each intensity value. Thus a signal of 50,000 represents 300,000 to 600,000 electrons. There is an increase of the dark charge rate by a factor of approximately two for every 7 °C[93]. Our operating temperature of -27 °C should give a dark charge signal of approximately 5 counts/pixel/sec.

Assuming a Gaussian distribution for the variation of dark charge between the pixels with mean, \( \mu \), and standard deviation, \( \sigma \), the distribution will remain the same as long as the ratio, \( \mu/\sigma \), is constant for various sample times. In addition a dark charge rate of electrons/pixel/sec implies \( \mu \) has a linear dependence on time. The dark charge was measured by acquiring images over several time intervals with the camera shutter closed and the radiation bay shutter closed. The measured intensities are listed in table 2.3. A linear fit to the data gives the magnitude of the dark charge as a function of time, \( t \), in seconds

\[
I_\mu = 19.71t + 142. \\
I_\sigma = 9.12t - 2.38
\]  

(2.15)

The offset from zero is probably due to electronic noise in the system. The rate of 20 counts/pixel/sec is a factor of four larger than the manufacturer estimate.

With the bay shutter open, scattered radiation from the neutron beam can interact with the CCD camera even with the camera shutter closed. This will add another noise component to the images. Table 2.4 lists the image characteristics with the camera shutter closed and the bay shutter open. A linear fit to this data results in

\[
I_\mu = 25.09t + 183. \\
I_\sigma = 9.12t - 2.38
\]  

(2.16)

16
Table 2.4: CCD camera dark charge with bay shutter open

<table>
<thead>
<tr>
<th>Exposure (sec)</th>
<th>Intensity mean</th>
<th>Intensity standard deviation</th>
</tr>
</thead>
<tbody>
<tr>
<td>5</td>
<td>310.</td>
<td>157.</td>
</tr>
<tr>
<td>10</td>
<td>433.</td>
<td>201.</td>
</tr>
<tr>
<td>20</td>
<td>684.</td>
<td>305.</td>
</tr>
<tr>
<td>40</td>
<td>1190.</td>
<td>506.</td>
</tr>
</tbody>
</table>

$I_\sigma = 10.1t + 104$.

With the bay shutter open the rate of dark charge buildup is approximately the same, but the scattered radiation causes an additional signal offset of 40. The rate of dark charge accumulation appears to be consistent so a dark charge image can be subtracted from neutron beam images to remove this unwanted signal. The uncertainty is quantified by the standard deviation, $\sigma$, in the dark charge signal. It must be remembered that the standard deviation is the variation in dark charge from pixel to pixel not the variation for different exposures in the same pixel. However, requiring signals to be larger than $\sigma$ for a given exposure time serves as a standard guaranteeing a signal larger than the noise. Thus eq. (2.16) indicates the magnitude required for the signal to be above the noise. As an example, a two byte signal should be accumulated in less than 22 seconds to keep the noise fraction under 0.005.

It is possible that sources of light within the bay can cause a noise signal in images. A 10 second exposure was taken with the camera shutter open and the bay shutter closed. The average intensity and standard deviation were 435. and 96.1 respectively. Since there is a negligible difference from the case with the camera shutter closed, the bay appears to be sufficiently light tight.

The neutron flux reaching the screen also suffers from statistical fluctuations. These fluctuations can be estimated from the number of electrons, $N_e$, produced in the CCD pixels by the beam. $N_e$ is given by

$$N_e = L \varepsilon_L \varepsilon_Q (N_p \varepsilon_s \Phi A l) = \alpha (N_p N_n). \quad (2.17)$$

Here $L$ is the fraction of light captured by the lens system. $\varepsilon_L$ is the lens transmission coefficient (0.85). $\varepsilon_Q$ is the CCD quantum efficiency (0.8)[pim93].
Table 2.5: Lens configuration parameters

<table>
<thead>
<tr>
<th>Configuration</th>
<th>f number</th>
<th>minification</th>
<th>L</th>
</tr>
</thead>
<tbody>
<tr>
<td>I</td>
<td>1.2</td>
<td>23.75</td>
<td>$2.83 \times 10^{-4}$</td>
</tr>
<tr>
<td>II</td>
<td>2.1</td>
<td>11.38</td>
<td>$3.71 \times 10^{-4}$</td>
</tr>
<tr>
<td>III</td>
<td>2.0</td>
<td>4.25</td>
<td>$2.27 \times 10^{-3}$</td>
</tr>
</tbody>
</table>

$N_p$ is the number of photons generated per neutron ($1.7 \times 10^5$)[spo69]. $c_s$ is the scintillation screen efficiency (0.09)[spo69]. $\Phi$ is the neutron flux ($1.2 \times 10^7$ n/cm²/s). $A$ is the pixel area (0.0032 cm²). $t$ is the exposure time.

For a Lambertian radiator[nus68]

$$L = \frac{1}{(2F(m + 1))^2}. \quad (2.18)$$

Here $F$ is the lens f number, and $m$ is the minification or the ratio of the pixel size on the screen to the CCD pixel size (0.0024 cm). Table 2.5 lists the parameters for our lens system.

The standard deviation, $\sigma_e$, for the electron number is found from standard error analysis to be

$$\sigma_e^2 = \alpha^2 \left[ N_n \sigma_p^2 + N_p \sigma_n^2 \right]. \quad (2.19)$$

Assuming a normal distribution for $N_n$ and $N_p$, the fractional standard deviation becomes

$$\frac{\sigma_e}{N_e} = \left[ \frac{1}{N_p} + \frac{1}{N_n} \right]^{1/2}. \quad (2.20)$$

Table 2.6 has the image intensity and fractional standard deviation for the various lens configurations. The calculated intensity is found from the electron number by assuming 12 electrons per intensity value. The calculated intensities agree sufficiently with the measured intensities to give us confidence in the beam noise estimates. The calculated beam noise will be combined with the calculated dark charge noise to estimate the total random noise in image intensities.

The random errors of the dark charge and high frequency beam noise can be added in quadrature and compared to measured values. The dark charge noise is calculated using eq. (2.16) and the exposure times required to get the 55000 average beam intensity. The beam noise is taken from table 2.6. The measured
### Table 2.6: Beam random image noise

<table>
<thead>
<tr>
<th>Configuration</th>
<th>$\alpha$</th>
<th>$N_n$</th>
<th>$N_e$</th>
<th>Calculated Intensity</th>
<th>Measured Intensity</th>
<th>Acquisition Time (sec)</th>
<th>$\sigma_e/N_e$</th>
</tr>
</thead>
<tbody>
<tr>
<td>I</td>
<td>$1.92 \cdot 10^{-4}$</td>
<td>$3.4 \cdot 10^4$</td>
<td>$1.1 \cdot 10^6$</td>
<td>92000.</td>
<td>55000.</td>
<td>8.2</td>
<td>0.0060</td>
</tr>
<tr>
<td>II</td>
<td>$1.26 \cdot 10^{-4}$</td>
<td>$6.0 \cdot 10^4$</td>
<td>$1.3 \cdot 10^6$</td>
<td>$1.1 \cdot 10^6$</td>
<td>55000.</td>
<td>64.</td>
<td>0.0047</td>
</tr>
</tbody>
</table>

### Table 2.7: Total random image noise

<table>
<thead>
<tr>
<th>Configuration</th>
<th>Exposure Time (sec)</th>
<th>Random Error (calculated)</th>
<th>Random Error (measured)</th>
</tr>
</thead>
<tbody>
<tr>
<td>I</td>
<td>8.2</td>
<td>0.0069</td>
<td>0.0062</td>
</tr>
<tr>
<td>II</td>
<td>64.</td>
<td>0.014</td>
<td>0.015</td>
</tr>
</tbody>
</table>

Noise values are found by dividing two images taken with the same exposure time and normalized to an average intensity of one. The error, $\sigma_e/N_e$, is assumed to be the standard deviation of the pixel intensities from the average of one. The results are shown in table 2.7. The beam noise is not much different than the dark charge noise, and both are usually only a few tenths of one percent. This bodes well for small signal detection, but leaves no clear avenue for random noise reduction. Longer exposures will decrease the beam noise, but this is offset by an increase in the dark charge noise. The optimum choice for random noise reduction would be an increase in beam flux.

#### 2.2.2. Systematic errors

Light caused by the beam on the scintillation screen may scatter off of surfaces and reach the camera. To quantify this noise a ruler was placed on the back of the scintillation screen and imaged for 6.5 seconds. The result for lens configuration I is shown in figure 2.3. After the dark charge was subtracted a signal of up to 800 exists behind this opaque object. With a maximum beam intensity of 50,000 this represents a noise signal on the order of 1.5% or 0.0022$t$ with $t$ in seconds. Reflection of light off of the screen frame and other surfaces may be the cause of this noise.
Figure 2.3: Image of a ruler behind the scintillation screen.
Table 2.8: Neutron backscatter intensity

<table>
<thead>
<tr>
<th>Lens Configuration</th>
<th>Exposure Time (sec)</th>
<th>Normalized Intensity</th>
<th>Scattered Light Intensity</th>
</tr>
</thead>
<tbody>
<tr>
<td>I</td>
<td>8.2</td>
<td>0.05347</td>
<td>0.018</td>
</tr>
<tr>
<td>II</td>
<td>64.0</td>
<td>0.06273</td>
<td>0.026</td>
</tr>
</tbody>
</table>

As a further check an image using lens configuration II was taken with a 55 second exposure in order to obtain the 50,000 intensity level in each pixel. Again a substantial intensity exists behind the ruler (a fraction of 0.022 or 0.00044).

Another noise signal can be found by placing a 1” thick strip of 30% borated polyethylene on the beam side of the scintillation screen. The borated polyethylene absorbs all of the neutrons incident on it. Any intensity measured behind the strip is noise. The normalized intensities behind the strip are shown in table 2.8. The last column in the table is the expected intensity due to the scattered light of the previous section. These background noise measurements are taken without an object in the beam. The borated polyethylene strip will also provide information on the object neutron scattering, but we separate the signals during preprocessing of images. The treatment of both signals will be discussed in the section on image preprocessing. This method is similar to Ikeda, et. al. [ike96]; however, they did not separate the background and object scatter signals.

The majority of the signal behind the borated polyethylene is not due to scattered light. The cause may be backscattered neutrons from the beam stop, mirror, and other structures which intersect the beam. The flux of scattered neutrons at the screen will result in an added signal from the screen independent of objects in the beam. Measurements of the neutron flux were taken outside of the beam path. These measurements were taken before and after installation of shielding for the CCD camera, and they are an indicator of the backscatter. For a point 348 cm from the beam exit and 48 cm from the beam center, the flux was $3.3 \cdot 10^6$ n/cm$^2$s. As a point of reference, the scintillation screen is 330 cm from the beam exit and at the beam center. The beam stop is 446. cm from the beam exit or 116. cm from the screen. The location of the screen versus the location of the flux measurement point will alter the flux at the screen compared to the flux measurement point. With this in mind the measurement will be used as an approximation of the backscatter flux at the screen. This
measurement was taken outside of the camera shielding before a reentrant beam stop was installed. Inside the shield the flux was found to be $10^5 \text{n/cm}^2\text{s}$. After installation of the reentrant beam stop, the flux inside the shield became $2.5 \cdot 10^4 \text{n/cm}^2\text{s}$. Assuming the same decrease in the flux outside of the shielding, the approximate backscatter flux at the screen becomes $8.3 \cdot 10^3 \text{n/cm}^2\text{s}$. Comparing to the beam flux of $1.2 \cdot 10^7 \text{n/cm}^2\text{s}$, the calculated fractional backscatter signal is 0.068. This calculated signal is quite close to the part of the signal behind the borated polyethylene not taken into account by the scattered light signal. The problem with this approximately constant background is the net decrease in attenuation detected for an object placed in the neutron beam. This is equivalent to part of the beam never being attenuated by objects which could lead to beam hardening artifacts in reconstructed tomographic images [kak88]. The large size of the neutron backscatter and scattered light signals is a result of the large area of the beam. A small area beam would have much smaller scatter noise due to the isotropic scattering of the neutrons and light. The advantage, that size gives for fast processing of large objects, adds an extra noise signal which must be removed.

The analysis of the random error section assumed a constant flux for the beam on the time scale of image acquisition. It also indicates the fluctuations between pixels for images exposed to the same fluence eventhough the fluxes and acquisition times might be different. In the actual system the acquisition times are constant, but the average flux from the MNRC reactor oscillates over time. This is indicated by variations of up to ±5% in the average intensity of flat field images. These variations are much larger than the fluctuations indicated in the previous section. The variation manifests itself as an average variation of the pixel intensities between images not as a larger fluctuation between pixels in the same image. These variations must be taken into account when images are normalized by the flat field.
3. PREPROCESSING OF IMAGES

3.1. Correction of scattering and fluctuation errors

As a first step toward tomographic reconstruction, an accurate measure of the beam attenuation caused by an object is required. The objective is to find the intensity behind the object, \( I_o \), normalized by the beam intensity, \( I_b \), despite corruptions due to system noise, image spreading, object scattering, and beam energy spread. An initial estimate can be found by only considering the dark charge intensity, \( I_d \), the background noise, \( I_n \), the object scattered beam intensity, \( I_s \), and the fluctuation of the beam magnitude, \( f \). The dark charge is subtracted during image acquisition. The portion of the dark charge signal affected by beam fluctuations is small so those fluctuations are neglected. We shall consider the rest of the quantities to be spatially independent.

The intensity actually measured in the flat field image, \( I_{bf} \), becomes

\[
I_{bf} = I_b + I_n. \tag{3.1}
\]

As mentioned above a borated polyethylene strip blocks part of the beam. This portion of the image acts as a scattering detector. Without an object in the beam there is no object scattering so the intensity behind the strip, \( I_{sf} \), is just the background intensity

\[
I_{sf} = I_n. \tag{3.2}
\]

Next the intensities in the object image are considered. A typical image with the borated polyethylene strip and an engine compressor blade is shown in figure 3.1. The intensity in an unobstructed portion of an object image, \( I_{bo} \), is

\[
I_{bo} = (1 + f) (I_b + I_n + I_s). \tag{3.3}
\]

The intensity behind the object in an object image, \( I_{oo} \), is

\[
I_{oo} = (1 + f) (I_o + I_n + I_s). \tag{3.4}
\]
The scattering detector has an intensity in an object image, $I_{so}$, of

$$I_{so} = (1 + f) (I_n + I_s). \quad (3.5)$$

Now define $\delta_{bof}$ as $I_{bo}/I_{bf}$, $\delta_{oof}$ as $I_{oo}/I_{of}$, and $\delta_{sof}$ as $I_{so}/I_{sf}$. These quantities are found from the quotient of the object image and the flat field image. Also define $\delta_o$ as $I_o/I_b$, $\delta_n$ as $I_n/I_b$, and $\delta_s$ as $I_s/I_b$. Note that $\delta_n$ was measured earlier in the section on background noise. Dividing the object image by the flat field image, equations (3.3), (3.4), and (3.5) become

$$\delta_{bof} = (1 + f) (1 + \delta_n + \delta_o) / (1 + \delta_n) \quad (3.6)$$

$$\delta_{oof} = (1 + f) (\delta_o + \delta_n + \delta_s) \quad (3.7)$$

and

$$\delta_{sof} = (1 + f) (1 + \delta_s/\delta_n) \quad (3.8)$$

The drop in beam intensity at the edge of the image, as shown in figure 3.1, is the most compelling reason for normalization of the object images by the flat field image. We can solve for $\delta_s$ using eq. (3.6)

$$\delta_s = (1 + \delta_n) \delta_{bof} / (1 + f) - 1 - \delta_n. \quad (3.9)$$

Placing this into eq. (3.8) results in a solution for $(1 + f)$ in terms of $\delta_{bof}$ and $\delta_{sof}$

$$(1 + f) = (1 + \delta_n) \delta_{bof} - \delta_n \delta_{sof} \quad (3.10)$$

Given $(1 + f)$ and $\delta_s$, the object intensity normalized by the beam intensity, $\delta_o$, becomes

$$\delta_o = (1 + \delta_n) \delta_{oof} / (1 + f) - \delta_n - \delta_s. \quad (3.11)$$

The procedure for determining $\delta_o$ is

1) Divide the object image by the flat field image.

2) Find $\delta_{bof}$ by averaging the intensity for a region of pixels that are not blocked by the scattering detector or by the object to be reconstructed.

3) Find $\delta_{oof}$ by averaging the intensity for a region of pixels that are located behind the scattering detector.

4) Calculate $(1 + f)$ and $\delta_s$.

5) Calculate $\delta_o$ for each pixel in the object image.

This procedure is repeated for each backprojection image since $(1 + f)$ and $\delta_s$ will change from image to image.
Figure 3.1: Typical image of a compressor blade before noise correction and normalization. The drop in beam intensity can be seen at the edges of the image. The borated polyethylene can be seen as the dark stripe across the image. The rod to the left of the blade is a centering rod. The rod is removed during backprojection image acquisition.

3.2. Beam attenuation and hardening

The tomographic reconstruction algorithm calculates the spatially dependent attenuation coefficient, $\mu(x, y, s)$, from the line integrals, $p(\theta, x, y)$, in the backprojection images [kak88].

$$p(\theta, x, y) = \int_{-\infty}^{\infty} \mu(x, y, s) \, ds$$  \hspace{1cm} (3.12)

The coordinates $x$ and $y$ designate the position on the scintillator screen, $s$ is the path along the beam and perpendicular to the screen, and $\theta$ is the angular rotation of the object. The line integrals are found from the attenuation of the
beam intensity as it passes through an object which for a monoenergetic beam is

\[ I_0(\theta, x, y) = I_0(\theta, x, y) \exp (-\rho(\theta, x, y)) \]  

(3.13)

The density of the attenuating material can then be found from

\[ n(x, s) = \mu(x, s) / \sigma(E_0) \]  

(3.14)

where \( \sigma(E_0) \) is the neutron cross section at energy \( E_0 \).

Unfortunately, the neutron beam provided by the MNRC reactor is not monoenergetic. The spectrum has a distribution similar to a Maxwellian in the thermal region, a distribution proportional to \( 1/E \) above 0.5 eV, and a bump in the fast region around 2 MeV. Above 10 MeV the distribution drops to zero rapidly. The spectrum, as determined through foil measurements\[\text{[boo79][gib95]}\] and calculation with the code SANDII\[\text{[mce67][kel87]}\], is shown in figure 3.2. Because of the beam energy distribution, the energy dependence of the neutron cross...
sections for the sample and the scintillator screen becomes important. The general trend is for cross sections to decrease as the energy increases. This is useful in the detector since higher energy parts of the spectrum will not be absorbed. In the sample materials this trend leads to beam hardening. As the sample becomes thicker, the lower energy parts of the spectrum are depleted at a faster rate than the higher energy parts because of the larger cross section at low energy.

The effect of the hardening is shown in figure 3.3 for samples of titanium alloy Ti6Al4V and polyethylene. Disks of titanium alloy were obtained from the National Institute of Standards and Technology (NIST). The 3.5 cm diameter disks were stacked end to end to provide different thicknesses for attenuation. A step wedge of polyethylene with a hydrogen density of \( 7.8 \times 10^{22}/\text{cm}^3 \) was also imaged. The percent of each element by weight in the polyethylene is 60.02% C, 31.95% O, 8.00% H, and 0.014% N with a density of 1.19 g/cm\(^3\)[1]. While the molecular structure in this material is not the same as hydrogen in titanium, the data does give an estimate for hydrogen attenuation equivalent to 29000 ppm weight in titanium. The wedge is 2.54 cm thick, and the distance from step to step is 0.3175 cm. The images were preprocessed using the procedures to correct for noise. The intensity was averaged over a number of pixels behind each object, and the objects were large enough to minimize effects from edge unsharpness. The attenuation coefficients were calculated from the measured intensities, the thickness of the samples, and eq. (3.13). As can be seen in the figure the exponential attenuation assumption causes a change in the effective attenuation coefficient for the titanium alloy of 12% for a 3 cm change in thickness. The effect in the polyethylene is even greater.

The attenuated intensity for a beam with energy distribution \( f(E) \) is

\[
\frac{I_0(\theta, x, y)}{I_0(\theta, x, y)} = \frac{\int f(E) \exp(-p_n(\theta, x, y) \sigma(E)) (1 - \exp(-p_d(E))) dE}{\int f(E) (1 - \exp(-p_d(E))) dE}
\]  

(3.15)

Here \( p_n \) is the line integral of the sample density, and \( p_d \) is the line integral of the detector attenuation coefficient. Given a function for the beam energy spectrum, eq. (3.15) can be solved for \( p_n \). Note that \( \sigma(E) \) was removed from the line integral. This is possible if all constituents of the sample have the same energy dependence for their cross sections. This is not the case for titanium and hydrogen; however, we are using this formulation in investigations of the beam hardening correction. For many structural materials (Ti, V, W, Fe) the low energy cross section is proportional to \( 1/\sqrt{E} \) [sch59] while hydrogen has a low energy cross section proportional to \( 1/E \) [sac41][mel49][mes51]. The cross section for Al has no
particular trend but several resonances at low energy[bro58]. The general trend of increasing cross section with decreasing energy combined with low hydrogen concentrations should result in adequate correction of the beam hardening.

The correction for beam hardening in images is accomplished with a table of intensity versus titanium thickness. The table is plotted in figure 3.4 along with the exponential attenuation result, assuming an attenuation coefficient independent of energy. The difference between the two curves is not large for small thicknesses; however, the signals to be detected can cause changes in intensity as small as 0.005. The table was generated by using eq. (3.15) to interpolate between the data points measured with the NIST titanium standards. Eq. (3.15) was fit to the data by changing the detector attenuation coefficient and the ratio between the thermal and epithermal parts of the assumed beam energy spectrum. A precise match to the data from first principles was not attempted. Eq. (3.15) was simply used as an interpolating function which was more physically consistent than a linear, spline, or other interpolating function.

The preprocessing procedure for backprojection images is now complete. First
Figure 3.4: Dependence of intensity on Ti6Al4V thickness. The solid curve is the fit to the data points represented by squares. The dashed curve is the result assuming exponential attenuation and a constant attenuation coefficient.

A flat field image and a dark charge image are taken. The object to be reconstructed is then placed on the turntable, and the backprojection images are collected. The dark charge image is subtracted automatically during image acquisition. The images are preprocessed with the code PREPROC to correct for noise errors. Each image is divided by the flat field image. The code requires the user to supply the coordinates of square regions to be used for the beam intensity check and the scatter check. The background noise magnitude must also be provided. Smoothing of the image data can be applied according to the binomial 9-point filter (4,2,1)[bir85]. The resulting images have intensities normalized to a maximum value of 1.0. The code then uses the attenuation table to convert the intensities in each pixel into equivalent thicknesses of the titanium alloy. The resulting pixel values are multiplied by 1000 to provide convenient values to be
copied to binary image files of 16 bits per pixel. These files are processed by the tomographic reconstruction program resulting in a plot of the material attenuation coefficient relative to Ti6Al4V without error due to beam hardening. Since we know the density of Ti6Al4V, the ratio of the alloy cross section to a sample material cross section gives the density of the sample material. The effective cross sections of materials must be found for our system by initially reconstructing samples of known material and density. The cross sections can then be used to determine samples of unknown density such as unknown concentrations of hydrogen in known metal components. For highly accurate measurements standard samples without hydrogen must be reconstructed first for comparison.

3.3. The hydrogen signal

Estimates are now needed for the hydrogen signal relative to the titanium alloy signal. The attenuation caused by a number of test objects is listed in table 3.1 under the intensity column. The first four objects are Ti6Al4V plates (20 x 10 x 0.343 cm³) loaded with hydrogen at Pratt and Whitney [pri94]. Plugs from each plate were tested with an inert gas fusion analyzer. In addition NIST performed Cold Neutron Prompt Gamma Activation Analysis (CNPGAA) on several spots of each plate [pau96]. The rest of the entries are from the polyethylene step wedge. The values, $T_e$, in the effective thickness column result from the conversion of the measured intensities using the table of figure 3.4. The actual thicknesses, $T$, were measured with a micrometer. The Ti6Al4V thickness is the thickness of each sample due to the titanium alloy. It is assumed that the hydrogen has not changed the thickness of the alloy plates. The effective thickness of the object due only to hydrogen, $d_H$, is found by subtracting $T$ from $T_e$.

The change in normalized density due to 100 ppm hydrogen can be determined by

$$\frac{n_{100 ppm H}}{n_T} = \frac{d_H 100 ppm}{n_H}$$

Dividing by the actual hydrogen concentration in ppm, $n_H$, gives the normalized density per ppm. Multiplying by 100 ppm scales the density conveniently to the range of interest for the embrittlement application. The normalized density, calculated for each sample, is in the last column of the table. According to the table, hydrogen at 100 ppm will cause an increase in the normalized density of approximately 0.018 ± 0.002. Subtracting the density in a standard without hydrogen from the density in a test sample and dividing by 0.018 will result in the
hydrogen concentration in units of 100 ppm. The variation of 36% in the table 3.1 results indicates the need for further investigation to refine the magnitude of the hydrogen signal.
Table 3.1: Hydrogen normalized density

<table>
<thead>
<tr>
<th>Sample</th>
<th>Intensity</th>
<th>Effective Thickness (cm)</th>
<th>Actual Thickness (cm)</th>
<th>Ti6Al4V Thickness (cm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Plate 115</td>
<td>0.8557</td>
<td>0.3284</td>
<td>0.3276</td>
<td>0.3276</td>
</tr>
<tr>
<td>Plate 175</td>
<td>0.8476</td>
<td>0.3486</td>
<td>0.3404</td>
<td>0.3404</td>
</tr>
<tr>
<td>Plate 4400</td>
<td>0.5769</td>
<td>1.180</td>
<td>0.3353</td>
<td>0.3353</td>
</tr>
<tr>
<td>Plate 1735</td>
<td>0.4583</td>
<td>1.689</td>
<td>0.3442</td>
<td>0.3442</td>
</tr>
<tr>
<td>Polyethylene</td>
<td>0.5785</td>
<td>1.174</td>
<td>0.2032</td>
<td>0.0</td>
</tr>
<tr>
<td>Polyethylene</td>
<td>0.3615</td>
<td>2.223</td>
<td>0.4064</td>
<td>0.0</td>
</tr>
<tr>
<td>Polyethylene</td>
<td>0.2438</td>
<td>3.130</td>
<td>0.6096</td>
<td>0.0</td>
</tr>
<tr>
<td>Polyethylene</td>
<td>0.1762</td>
<td>4.160</td>
<td>0.8103</td>
<td>0.0</td>
</tr>
<tr>
<td>Polyethylene</td>
<td>0.1407</td>
<td>4.920</td>
<td>1.011</td>
<td>0.0</td>
</tr>
<tr>
<td>Polyethylene</td>
<td>0.1187</td>
<td>5.510</td>
<td>1.189</td>
<td>0.0</td>
</tr>
<tr>
<td>Polyethylene</td>
<td>0.1122</td>
<td>5.710</td>
<td>1.277</td>
<td>0.0</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Sample</th>
<th>Hydrogen concentration (ppm)</th>
<th>$d_H$</th>
<th>Normalized density</th>
</tr>
</thead>
<tbody>
<tr>
<td>Plate 115</td>
<td>115 ± 30</td>
<td>0.0008</td>
<td>0.00212</td>
</tr>
<tr>
<td>Plate 175</td>
<td>170 ± 20</td>
<td>0.0082</td>
<td>0.0142</td>
</tr>
<tr>
<td>Plate 4400</td>
<td>12900 ± 900</td>
<td>0.8442</td>
<td>0.0195</td>
</tr>
<tr>
<td>Plate 1735</td>
<td>17900 ± 700</td>
<td>1.345</td>
<td>0.0218</td>
</tr>
<tr>
<td>Polyethylene</td>
<td>29000</td>
<td>1.174</td>
<td>0.0199</td>
</tr>
<tr>
<td>Polyethylene</td>
<td>29000</td>
<td>2.223</td>
<td>0.0189</td>
</tr>
<tr>
<td>Polyethylene</td>
<td>29000</td>
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</tr>
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<td>Polyethylene</td>
<td>29000</td>
<td>4.160</td>
<td>0.0177</td>
</tr>
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<td>Polyethylene</td>
<td>29000</td>
<td>4.920</td>
<td>0.0168</td>
</tr>
<tr>
<td>Polyethylene</td>
<td>29000</td>
<td>5.510</td>
<td>0.0160</td>
</tr>
<tr>
<td>Polyethylene</td>
<td>29000</td>
<td>5.710</td>
<td>0.0154</td>
</tr>
</tbody>
</table>
4. Tomographic Reconstruction Results

Reconstruction was accomplished with the filtered backprojection routine from the Donner algorithms library [hue77]. The exposure time for each backprojection image was 6.2 seconds. Another 13 seconds was required for downloading and dark charge subtraction by the PC. The reconstructions shown below were calculated from sets of 180 backprojections (1° increments) resulting in an image acquisition time of 60 minutes. As mentioned above the code PREPROC performs the preprocessing procedures on the images. The code IMGPROC does the 2-D reconstruction from desired slices of the original images. This section contains results from the reconstructions of a NIST titanium standard, a phantom with various metals, and an engine compressor blade. The reconstructions quantify the reported magnitude of the titanium alloy density as well as fluctuations due to noise. The response to metals with different attenuation coefficients indicates the ability to evaluate components made of various materials. The blade reconstruction shows the result for thin objects.

4.1. NIST titanium alloy standard

One of the titanium alloy standards, previously used in the measurements of attenuation coefficient, was reconstructed as shown in figure 4.1a and b. The standard is a circular disk 3.5 cm in diameter and 1.97 cm thick. The axis of the disk was placed perpendicular to the rotation axis resulting in a rectangular cross section in the reconstruction. The color scale was set in the figure to only include densities from the maximum to 15% below the maximum which heightens the contrast for the features inside the standard. Figure 4.1a is the result without image corrections and attenuation calculated using the exponential approximation. Figure 4.1b is the result with all of the corrections. The first reconstruction has attenuation coefficient in units of cm⁻¹ while the second reconstruction has...
attenuation coefficient normalized to the titanium alloy.

The main feature of the uncorrected reconstruction is the larger attenuation coefficient around the edges versus the center. This result is typical in cases where beam hardening is significant [kak88] [mcd77]. The backprojection images show a relatively higher attenuation coefficient for those line integrals which pass through less material. The tomography algorithm responds to this by partially "hollowing out" what should be a uniform density object. Both the actual beam hardening and the background signals contribute to this effect. Figure 4.2a is a curve of the density across the center of the disk showing the magnitude of the effect. The edges of the disk have an attenuation coefficient approximately 10\% larger than the center, a change from 0.37 cm\(^{-1}\) to 0.41 cm\(^{-1}\). If we did not know that this NIST standard has less than 50 ppm hydrogen in it, we might conclude that up to 500 ppm hydrogen had diffused into the surface layers of the disk. The elimination of the beam hardening artifacts is obvious in the corrected image reconstruction. The normalized density curve in figure 4.2b shows a flat profile across the standard. The average density is 1.008, and the noise has a standard deviation of ±0.008 or ±50 ppm.

4.2. Cylindrical phantom

The next set of experiments involved a phantom constructed from an aluminum cylinder 4 cm in diameter and 10 cm long. It is similar to experiments reported
Figure 4.2: Attenuation coefficient across the center of the disk for the a) uncorrected and b) corrected backprojection images.
by Zanarini, et. al. [zan95]; however, the differences in configurations highlight some of the features of the MNRC tomography system. Their experiments used a cold neutron beam which eliminates the energy corrections necessary in the MNRC system. This also results in a smaller, 4 cm diameter, and lower flux, $8 \cdot 10^5 \text{n/cm}^2\text{s}$, beam. This beam would not be sufficient to acquire images for the compressor blades in a production mode. The large MNRC beam has deficiencies, background noise and hardening, which can be corrected to provide a production capable system.

Figure 4.3: Reconstruction of aluminum cylinder with Ti90Al6V4, Ti, Cu, W, and Ni rods. A backprojection image is also shown.

The aluminum phantom had five holes with diameters of 1 cm. The first
Table 4.1: Relative attenuation coefficients for different metals

<table>
<thead>
<tr>
<th>Sample</th>
<th>Measured Coefficient</th>
<th>Calculated Coefficient (cm$^{-1}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ti90Al6V4</td>
<td>1.022 ± 0.018</td>
<td>0.544</td>
</tr>
<tr>
<td>Ti</td>
<td>1.089 ± 0.013</td>
<td>0.573</td>
</tr>
<tr>
<td>Cu</td>
<td>1.883 ± 0.017</td>
<td>0.993</td>
</tr>
<tr>
<td>W</td>
<td>2.486 ± 0.062</td>
<td>1.163</td>
</tr>
<tr>
<td>Ni</td>
<td>4.270 ± 0.064</td>
<td>1.984</td>
</tr>
</tbody>
</table>

phantom reconstruction in figure 4.3 has rods of Ti6Al4V, Ti, Ni, W, and Cu in the holes. This serves as a check of the preprocessing algorithm for materials with attenuation coefficients different than titanium. The transition in color from blue-green to pink represents a change in effective attenuation coefficient by a factor of four. Even with this large change in attenuation coefficient the reconstruction results in a fairly uniform density across each rod. The variation is less than 2% of the average density for each rod. Since the absolute magnitude of the noise increases for the higher attenuation coefficient materials, the minimum detectable hydrogen concentration will also increase for these materials.

As a check for consistency, the attenuation coefficients (cm$^{-1}$), based on the thermal neutron cross sections and material densities, are compared to the measured attenuation coefficients. The data is listed in table 4.1 and plotted in figure 4.4. The close fit to a linear relationship indicates that the attenuation coefficients are being reconstructed correctly even for materials causing significant attenuation of the beam. The beam intensity is 0.63 after attenuation by 1.0 cm of Ti and 0.17 after attenuation by 1.0 cm of Ni. These results are similar to Ikeda, et. al.[ike90]. Again the measured attenuation coefficients and calculated cross sections are not the same since the measured values are normalized to the titanium alloy during image preprocessing. The most important result is the uniformity of the reconstructed density across each of the rods. A wide range of components can be evaluated with the system in its present configuration.

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Figure 4.4: The measured attenuation coefficient, normalized to the titanium alloy during image preprocessing, plotted versus the thermal neutron attenuation coefficient for several metals.
4.3. Compressor blade reconstruction

The result of the reconstruction for a new engine compressor blade is shown in figure 4.5. In this picture the color scale includes all attenuation coefficient values so the reconstruction artifacts can be seen. Notice that the radial variations in the blade correspond to the radial artifacts in the reconstruction. These radial artifacts are due to the finite number of backprojection images. The interior region of the blade does not suffer too badly from these artifacts. The density is $1.009 \pm 0.008$ which represents a variation of only $\pm 50$ ppm hydrogen. This signal is so low that we cannot be certain if it is due solely to noise or if there is some hydrogen signal present. Since the requirement is to detect levels only down to 100 to 200 ppm, the level of noise appears tolerable. At least as far as the interior of the blade is concerned, the shape of the blade has not adversely impacted the hydrogen detection capability. This was not the case for reconstructions generated from 60 backprojection images. In the 60 image case the radial artifacts caused variations equivalent to a signal due to 400 ppm hydrogen. Because of these artifacts the choice was made to use 180 images at the cost of a longer acquisition time.

Cross sections of the blade reconstruction are in figure 4.6a and b. Again in the interior of the blade, the effective density is near 1.0 as required for the titanium alloy. These curves illustrate the limits of spatial resolution in the reconstructions. Curve a) passes across the thin dimension of the blade while curve b) passes along the width of the blade. In curve a) the blade is only 10 to 12 pixels thick and the edges are seen to spread over 4 pixels. The dashed line represents a hypothetical reconstruction with no edge spread. The result is the degradation of the density signal for two pixels or $\sim 1$ mm inward from the edge of the object. Since the blade
Figure 4.6: Cross section of engine compressor blade reconstruction a) across the thickness of the blade and b) across the width of the blade.

has a crescent shape, the width of the edges are exaggerated in curve b). The spatial resolution limits could be a problem if hydrogen diffuses only into a thin layer on the surface of parts. If the hydrogen mobility is sufficient to diffuse more evenly through a part, the spatial resolution should be adequate.
5. CONCLUSION

The MNRC neutron tomography system has demonstrated the capability to detect hydrogen in titanium components to levels of 100 ppm weight with an acquisition time of 60 minutes. Since the turntable fixtures accommodate three engine compressor blades, nondestructive testing can be accomplished at a rate of three blades per hour. These testing characteristics were achieved by using a large, thermal beam with preprocessing of backprojection images to correct for image errors. The preprocessing included correction for CCD camera dark charge, correction for background, correction for reactor fluctuations, correction for scattering, and correction for beam hardening.

Further work has been completed to address the remaining artifacts in reconstruction images. Comparison of standards without hydrogen to objects with unknown hydrogen will be used to detect hydrogen signals even in parts of the reconstruction which have artifacts. The standard and test objects will have the same physical dimensions and metal matrix. The difference between the two reconstruction images should reveal the hydrogen signal assuming the artifacts remain the same. The artifacts should remain essentially unchanged given small hydrogen signals. Large hydrogen signals may have a significant impact on the artifacts, but the large signals will be easy to detect above the noise. The techniques for reconstruction image comparison will be addressed in a future report. Standards with various levels of hydrogen are also being developed so the magnitude of the hydrogen signal can be quantified more precisely.
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