ABSTRACT

The vapor pressure of 13 CHF $_3$ relative to the vapor pressure of 12 CHF₃ has been measured as a function of temperature between 161° K and 205° K through the use of a modified Bigeleisen distillation column. The transient build-up of the isotopic concentration gradient along the length of the packed column during the start-up period was monitored as a function of time by taking samples from the condenser section. The gaseous samples were completely oxidized to carbon dioxide in the presence of a platinum catalyst and a large excess of oxygen at temperatures between 1050° C and 1100° C. The combustion products were gas chromatographically purified and the purified carbon dioxide samples were analyzed in a Nier-type MASTER isotope-ratio mass spectrometer. The data of each distillation run were reduced in light of a modified Cohen's theory of the kinetics of a square cascade of close-separation stages.

The vapor pressure isotope effect for carbon substitution in CHF_3 in this temperature range has been found to be an inverse effect. A trend of increasing inverse effect with decreasing temperature has been observed. The relative vapor pressure may be expressed as

 $ln \frac{P'}{P} = \frac{(217 \pm 66)}{T} - \frac{(0.89 \pm 0.36)}{T}$ where P' and P are the vapor pressures of ¹²CHF₃ and ¹³CHF₃ respectively.

A cell model liquid force field for trifluoromethane has been derived. The accompanying table contains the <u>F</u> matrix elements fit to the observed vapor pressure isotope effect.

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	<u>F</u> Matrix 1	
Force Constants	Gas	<u>Liquid</u>
Internal		
Diagonal		
C-H stretch	5.000000	4.814698
C-F stretch	6.017878	6,206256
H-C-F bend	0.491320	0.489509
F-C-F bend	0.764617	0.765351
Interaction		
C-H str x C-F str	1.172021	0.859410
C-F str x C-F str	0.749878	0.474351
C-H str x H-C-F bend	-0.167382	-0.310438
C-H str x F-C-F bend	0.167382	0.310438
C-F str x adj H-C-F bend	0.194294	0.194294
C-F str x opp H-C-F bend	-0.265706	-0.265706
C-F str x adj F-C-F bend	0.256033	0.256033
C~F str x opp F-C-F bend	-0.180848	~0.180848
H-C-F bend x H-C-F bend	0.039340	0.041347
F-C-F bend x F-C-F bend	-0.097309	-0.096575
H-C-F bend x adj F-C-F bend	-0.151667	-0.125241
H-C-F bend x opp F-C-F bend	-0.266667	-0.240241
External		
Diagonal		
Translation		0.300000
Rotation		0.100000 ^{(b}
Internal-External Interaction		
C-H str x T_2		-0.840000
C-F str x T_z		0.840000
H-C-F bend \mathbf{x} T _z		0.300000
F-C-F bend x T_z^2		-0.300000

Liquid and Gaseous F Matrix for Trifluoromethane

(a) Unless otherwise noted, in units of mdyn/A.

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(b) In units of mdyn-Å.

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STUDIES OF

CARBON-13 VAPOR PRESSURE ISOTOPE EFFECT

IN CHF3

A Thesis

Presented to the Graduate Faculty of the Department of Chemistry Brooklyn College City University of New York

In Partial Fulfillment of the Requirement of the Degree of Master of Arts

by

Lester Borodinsky August 1976 I offer this unto That Truth which is Absolute.

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I. INTRODUCTION

The purpose of this study is twofold. The first is to experimentally determine the separation factor for carbon-13 as a function of temperature from its natural abundance by means of low temperature distillation of trifluoromethane, CHF_3 . Secondly, this study proposes to investigate theoretically the inverse vapor pressure isotope effect in $^{13}CHF_3/^{12}CHF_3$. This is to be done by a force field study utilizing Wilson's F and G matrix method.⁽²⁹⁾

Carbon-13 is a stable isotope that naturally occurs at an abundance of 1.11%. The fact that it is not radioactive has recently attracted the interest of biomedical scientists to its potential use as a tracer for carbon in medical and biological studies. Recent advances for detection and/or determination by 13 C NMR have made its use particularly attractive. In such tracer studies, this technique will not only trace the path of 13 C, but also determine its molecular environment.

 13 C is currently being enriched up to 95.5%⁽¹⁾ by means of cryogenic distillation of carbon monoxide. It has also been fractionated by the carbon dioxide-carbamate process⁽²⁾ and the thermal diffusion of methane.⁽³⁾

Other methods that have been investigated, but not adapted to production scale, include the following. In the process used by Urey et al, 13 C was enriched from its natural abundance by means of a carbon-isotope exchange between an aqueous solution of sodium cyanide and gaseous hydrogen

-1-

cyanide;⁽⁴⁾

 $H^{13}CN + {}^{12}CN^{-} = H^{12}CN + {}^{13}CN^{-}$.

The equilibrium constant was found to be 1.026 at room temperature, but in addition to the obvious toxicity of the substance, polymerization of HCN gradually sets in, leading to an equivalent loss of isotopes in a cascade operation.

A system that consists of a cuprous chloride-ammonium chloride solution and carbon monoxide (COCO system), developed at Oak Ridge National Laboratory, employs thermal reflux at both ends. The stage separation factor for this system is 1.015 at room temperature, and the isotope exchange is rapid enough to obtain a stage height of less than 1.5 times the column diameter.⁽⁵⁾

Another exchange system developed at Oak Ridge consists of a ketone cyanohydrin and aqueous cyanide solution. It has a very high separation factor of about 1.04 but requires a chemical reflux.⁽⁵⁾

The carbon dioxide-carbamate exchange was developed by T. I. Taylor and his students at Columbia University. It has since been scaled up by Mound Laboratory for enriching ¹³C from its natural abundance to about 93%. The effective stage separation factor depends on temperature, pressure, flow rate, solvent, and the choice of carbamate. The Mound process utilizes carbamate of n-dibutylamine dissolved in triethylamine and yields an effective single stage separation factor of 1.01.⁽⁶⁾ Because of the limited solubility of carbamate and the rather high vapor pressure

-2-

of the amine, the carbamate process is generally limited to operation at temperatures in the range of $25-40^{\circ}$ C.

Unlike processes such as distillation or isotope exchange reactions, thermal diffusion is a non-equilibrium process. Although thermodynamically unfavorable, the thermal diffusion process originally devised by Clausius and Dickel⁽⁷⁾ has been widely used for isotope separation purposes. This is due primarily to the simplicity of the aparatus and the relatively large separation factor yielded by the process. This process was used at Mound Laboratory in combination with the carbamate process.

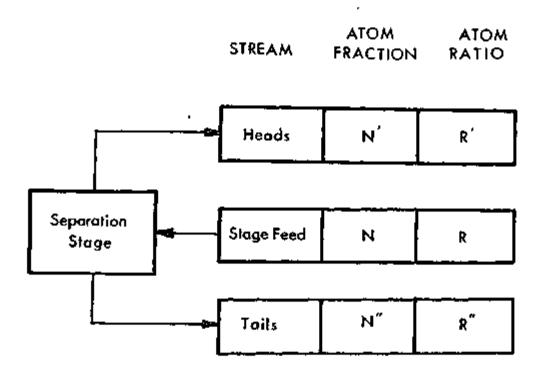
Before proceeding further, it seems appropriate to present the basic nomenclature used in the present study, and to discuss the relative advantages and disadvantages of the various processes. The basic unit of the separation process is the separating stage. Each stage is fed with material of the same composition and produces partially fractionated product streams. When the degree of separation effected by a single stage falls short of the desired separation between product and feed material, it is necessary to connect stages in series. A group of stages connected in series is referred to as a cascade. The degree of separation effected by a unit stage is expressed in terms of the separation factor. Referring to Figure 1, the stage separation factor, \mathbf{g} , is defined as

 $\alpha \equiv \frac{Abundance Ratio in Heads}{Abundance Ratio in Tails}$

-3-



•



$$= \frac{R'}{R''} = \frac{N}{N''} \frac{1-N''}{N'} .$$
 (1)

Since α for an isotoped exchange is generally close to unity (except for hydrogen isotopes), it is sometimes convenient to use ϵ , defined as

$$\epsilon \equiv \alpha - 1, \qquad (2)$$

For a distillation process, α is equal to the ratio of the vapor pressures of two isotopic molecules at a given temperature. As a rule of thumb, < for a distillation process for enrichment of isotopes of second period elements (Li-F) does not exceed 10^{-2} . At Mound Laboratory, CC1₃F (Halocarbon-11) was distilled at 24° C and the separation factor was found to be 1.0019 \pm 0.0003.⁽³⁾ For an exchange process, the separation factor is proportional to the equilibrium constant. These are not necessarily identical since an isotopic substitution at equivalent atomic positions in a given molecule does not lead to isotopic fractionation.⁽⁸⁾ Generally # for an exchange reaction often exceeds 2-3 x 10^{-2} which is attributable to a large change in bond order around the substituted atom as it is exchanged between two chemical species. The disadvantage of the exchange process is that it usually requires a chemical reflux at both ends of the cascade. Such a chemical reflux is necessary to achieve complete conversion of one chemical species into the other at the end of the cascade without any loss of isotopes from the system. This usually leads to costly chemical waste. The carbamate

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process achieves the reflux by thermal means, i.e., the carbamate is thermally decomposed at one end of the cascade while carbon dioxide and amine are thermally combined to form carbamate at the other end. Such an exchange process is called an exchange distillation, and has the advantages of both the exchange and distillation processes. The more important merits of a distillation lie in the absence of a chemical reflux and in a large material throughput, the latter being a very important consideration in an industrial size plant. Thus, a distillation plant which handles a substance with a molecular weight of 100 and a density of 2 grams/ml would be 20 times smaller in volume than an exchange plant handling 1 molar solutions.

The recently discovered method of laser-activated isotope separation has a special advantage of being capable of yielding a large separation factor, i.e., of the order of tens and hundreds for α .⁽⁹⁾ At this early stage of development, the material throughput is exceedingly limited due to the fact that the laser activation has to be achieved in the gaseous state of very low pressure, typically of the order of 1 torr. This dilute system is a necessary requirement for the achievement of the extremely high selectivity. The future of laser isotope separation seems to depend on ultra-powerful laser technology and a compromise between selectivity and throughput.

In Section I-1 that follows, the general theory of the vapor pressure isotope effect will be presented. Following

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it, in Section I-2, will be a discussion of preliminary investigations that lead to the choice of CHF_3 (Halocarbon-23) as the distillation material. The Introduction will be concluded with Section I-3, wherein the outline of the investigation will be presented.

I-1. Theory of Vapor Pressure Isotope Effect

The vapor pressure of a chemically and isotopically pure liquid is determined by the dynamic equilibrium between two species, i.e., the molecules in the gas phase and the molecules in the liquid phase. The vapor pressure of such a substance can be expressed in terms of the partition function of these two species. It follows then that the difference in the vapor pressures of a pair of isotopic liquids of the same substance is expressible in terms of four partition functions, the gas and liquid partion functions for each isotopic species.

Bigeleisen⁽¹⁰⁾ developed a fundamental theory of vapor pressure isotope effect based on the assumptions of the simple cell model of liquids, and the Born-Oppenheimer approximation. According to this theory, the ratio of the vapor pressures of the lighter isotopic species, P', to that of the heavier isotopic species, P, is given by

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$$ln\left(\frac{P'}{P}\right) = ln\frac{s}{s}, f_{c} - ln\frac{s}{s}, f_{g}$$
(3)

where s' and s are the symmetry numbers of the light and heavy isotopic species respectively, and f_c and f_g are the isotopic ratios of the reduced partition functions in the condensed phase and the gas phase respectively. They are "reduced" in the sense that they are the ratios of the partition functions to their classical limit, i.e.,

$$\frac{s}{s}, f = \frac{\left(\frac{Q}{Q}\right)_{gm}}{\left(\frac{Q}{Q}\right)_{c1}} = \frac{\left(\frac{Q}{qm}\right)_{Q_{c1}}}{\left(\frac{Q}{qm}\right)_{c1}}$$
(4)

where Q' and Q are the partition functions of the light and heavy species respectively, and the subscripts qm and c1 represent the quantum mechanical and classical respectively.

Within the framework of the Born-Oppenheimer approximation and under the assumption that the potential is harmonic and that the translational and rotational partition functions are classical, $\frac{S}{S}$, f can be expressed⁽⁷⁾ as

$$\frac{s}{s} \cdot f = \prod_{i=1}^{n} \frac{u_i}{u_i} \frac{e^{-u_i/2} \begin{pmatrix} -u_i \\ 1 - e \end{pmatrix}}{e^{-u_i'/2} \begin{pmatrix} -u_i \\ 1 - e \end{pmatrix}}$$
(5)

where ther product is taken over all degrees of vibrational freedom, and u is defined as

$$u \equiv \frac{hc\omega}{kT}$$
(6)

where h is Planck's constant, c the velocity of light, ω the normal frequency in units of wavenumbers (cm⁻¹), k the Boltzman constant and T the absolute temperature.

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When T is very large or when the ω 's are small, Equation 5 reduces to

$$\ln \frac{s}{s} = \frac{1}{24} \sum_{i} (u_{i}^{2} - u_{i}^{2})$$
 (7)

$$= -\frac{1}{T^{2}} \frac{1}{24} \left(\frac{hc}{\kappa}\right)^{2} \sum_{i} (\omega_{i}^{2} - \omega_{i}^{2})$$
(8)

When T is low or when the w's are large, Equation 5 approaches

$$\ln \frac{s}{s} = \sum_{i} \frac{u_{i} - u_{i}}{2}$$
(9)

$$= \frac{1}{T} \frac{hc}{2k} \sum_{i} \left(\omega_{i} - \omega_{i} \right)$$
(10)

In the simple cell model, $\ln \frac{s}{s}$, f_c in Equation 3 is evaluated by associating three translational degrees of freedom, three rotational degrees of freedom, and 3N-6 internal degrees of freedom, with each molecule. Furthermore, the translational and rotational motions are assumed to be oscillatory in nature, a consequence of the cell model assumption that a liquid can be represented by a representative molecule which oscillates independently in an isotropic liquid field. Due to the relatively weak external force (as compared to the forces within the molecule), the frequencies for external oscillation are small; $\omega_{ext} < 200$ cm^{-1} . Thus, $ln \frac{s}{s} f_c$ in Equation 3 can be thought of as consisting of two types of terms, one attributable to the weak external oscillations, which is proportional to $1/T^2$ in accordance with Equation 8, and the other to the internal vibrations in the condensed phase which is proportional to

1/T in agreement with Equation 10. The other term in Equation 3, $\ln \frac{S}{S} f_g$, of course contributes additional terms which are proportional to 1/T. Consequently, as a first approximation to Equation 3, Bigeleisen derived⁽¹⁰⁾ the following relationship

$$ln \frac{P^4}{P} = \frac{A}{r^2} - \frac{B}{T}$$
(11)

where

$$A = \frac{1}{24} \left(\frac{hc}{k}\right)^2 \sum_{k=1}^{6} \left(\omega'_{ext}^2 - \omega'_{ext}^2\right)$$
(12)

anđ

$$B = \left(\frac{hc}{2k}\right) \left\{ \begin{bmatrix} 3N-6 \\ \sum \omega_{g} \end{bmatrix}^{3N-6} - \begin{bmatrix} 3N-6 \\ \sum \omega_{c} \end{bmatrix}^{3N-6} - \begin{bmatrix} 3N-6 \\ \sum \omega_{g} \end{bmatrix}^{3N-6} - \begin{bmatrix} 3N-6 \\ \sum \omega_{c} \end{bmatrix}^{3N-6} + \begin{bmatrix} 3N-6 \\ 2 \end{bmatrix} \right\}$$
(13)

It is seen that A depends entirely on the external vibrations, while B represents the isotopic difference in the zero-point energy shift on condensation. It has been shown that A and B are always positive. According to Equation 11, the vapor pressure of the lighter isotope is greater than the heavier isotope at sufficiently low temperatures, while the effect could be reversed as the temperature increases above a certain point. If such a crossover temperature lies within the range of liquid temperature, i.e., at a temperature above the triple point and below the boiling point, then the inverse vapor pressure effect is expected to be advantageous in isotope production. The reason for this will be explained briefly in the following paragraph.

Since isotope separation is a close separation (small e), an isotope separation plant requires a large number of separation stages. At the initial startup of a plant, all stages are charged with material of natural enrichment, and the refluxers on both ends of the column are activated. During the initial transient period, an isotopic concentration gradient is gradually established along the length of the cascade. When the enrichment at the product end of the cascade reaches a steady level, slow product withdrawal is initiated and is accompanied by a corresponding material input at the feed point along the cascade. During the transient period, the cascade is operated at total reflux at both ends, i.e., material is neither withdrawn nor introduced into the system. This transient period increases the holdup (the amount of desired material held up in the system). According to the theory developed by Cohen, (11) the transient period is shorter when ϵ is negative. For a distillation fractionation of 13 C, the negative ϵ corresponds to the inverse vapor pressure isotope effect. A preliminary investigation, outlined in the following section, showed that the probability of finding such an inverse effect in the liquid temperature range would be sustantial for fluoromethanes.

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I-2. Investigation Leading to the Choice of Fluoromethanes

 13 CH $_A$ has a lower vapor pressure than 12 CH $_A$, at liquid methane temperature, (12) while 13 C substitution in $CC1_4$ leads to a slightly inverse isotope effect at 35° C.⁽¹³⁾ This is a consequence of the external (translational and rotational) modes approaching negligible levels, as a result of the symmetric substitution of the peripheral positions of heavy chlorine atoms, yielding a small A in Equation 11. The smallness of the inverse effect in CCl_A is attributable to the high temperature and the prohibited interaction between the rotation and internal motion of a tetrahedral molecule. A high molecular weight and a large magnitude of inertia reduce the magnitude of the $1/T^2$ term of Equation 11, thus favoring the inverse effect at low temperatures. The zero-point energy shift term is enhanced by strong interactions of liquid phase external modes with strongly infrared active internal mode actions, in which the center atom actively participates.⁽¹⁴⁾ Presence of fluorine atoms in a molecule brings the melting and boiling points down to regions that are much lower than those of the corresponding chloro-derivatives, thus raising the possibility of the occurence of the crossover temperature within the liquid range rather than in the solid. One of these compounds, trifluoromethane (Halocarbon-23) has C_{3v} symmetry, which is sufficiently non-symmetric to allow its carbon atom to participate in the normal vibrations that can interact with the external modes in the liquid. It has a melting

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point of -155.2° C and a normal boiling point of -82.03° C (see Table I), which can be conveniently handled by the cryogenic distillation column that was generously made available by Prof. Bigeleisen of the University of Rochester. Preliminary calculations⁽¹⁵⁾ on the zero-point energy shift on condensation, based on Wolfsberg's theory⁽¹⁴⁾ of London dispersion forces in liquids, showed that Halocarbon-23 had a good possibility of yielding the inverse isotope effect.

I-3. Outline of Investigation

The separation factor for 13 C fractionation in the cryogenic distillation of CHF₃ has been determined in the following manner. A portion of CHF₃ manufactured by Matheson Gas Products, which is 99.0% pure, was purified by repeated bulb-to-bulb distillation and distilled under total reflux in a cryogenic distillation column, which was designed and built by J. Bigeleisen⁽¹⁸⁾ and later modified.⁽¹⁹⁾ The build-up of the ¹³C enrichment gradient along the column was monitored as a function of time. This transient behavior under total reflux was analyzed according to the theory of K. Cohen, ⁽¹¹⁾ leading to the determination of the stage separation factor and the number of theoretical stages. The separation factor was then obtained as a function of temperature

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TABLE I, Physical Properties of Halocarbon-23(a)

Ł

Molecular Formula		CHF3
Molecular Weight		70.01
Normal Boiling Point		-82.03 ⁰ С(191.13 ⁰ К)
Normal Freezing Point		-155.2 ° C(118.0° K)
Critical Temperature		25.9 ⁰ C
Critical Pressure		47.7 atm
Critical Volume		133 cc/mol
cricical volume		
Critical Density		0.525 g/cm ³
Density of liquid	@ 298 ⁰ K	0.670 g/cm ³
	⊛ 200 ⁰ К	1.409 g/cm^{3} (b)
•	🕲 150 ⁰ К	1.555 g/cm^{3} (b)
Specific Heat of liquid	@ 285 ⁰ к	$0.252 \text{ cal/g}^{(b)}$
	@ 200 ⁰ К	0.168 cal/g (b)
	@ 180 ⁰ К	$0.162 \text{ cal/g}^{(b)}$
Heat of Vaporization	@ n.B.P.	57.23 cal/g
-	@ 200 ⁰ к	55.58 cal/g (b)
	е 150 ⁰ к	$64.47 \text{ cal/g}^{(b)}$
·		-

- (a) Unless otherwise noted, data taken from "Handbook of Chemistry and Physics", 53rd Edition, Chemical Rubber Co., (1972).
- (b) Taken from "Handbook of Fundamentals", American Society of Heating, Refrigerating, and Air-Conditioning Engineers, (1974)

The data was fit to Bigeleisen's formulae, Equations 3 and 11, and the result was compared with a theoretical calculation based on the theory of the simple cell model. In Chapter II (Experimental), the experimental procedures will be discussed in detail. The method of data reduction by modified Cohen's theory will be presented in Chapter III (Data Reduction). The derivation of the formula used in the data reduction will also be presented in that chapter. An extension of Cohen's theory to accomodate the need of the present investigation which deals primarily with the inverse isotope effect has been developed by Ishida and Wieck.⁽²⁶⁾ In Chapter IV, the presently obtained data on the 1^{12} CHF₃/ 1^{3} CHF₃ vapor pressure isotope effect will be compared with Bigeleisen's theory, and a cell model liquid force field for trifluoromethane will be derived accordingly.

II. EXPERIMENTAL

The low temperature distillation of Halocarbon-23 (CHF₃) necessitated the use of several pieces of apparatus. The two major pieces of apparatus, a low-temperature distillation column and a combustion train, are described in Section II-1, which follows. The acquisition of reliable vapor pressure data for Halocarbon-23 is described in Section II-2. Actual experimental procedures are presented in detail in Section II-3.

<u>II-1. Design and Construction</u>

Design and construction of the experimental apparatus used in this investigation has been fully described by Wieck and Ishida.⁽¹⁹⁾ The following is an exerpt from it, except for several modifications in the design and procedures as noted.

Preliminary purity analyses of Halocarbon-23 were performed on a Perkin-Elmer model 990 gas chromatograph. The resulting chromatograms indicated the presence of significant amounts of impurities. Air, the major impurity, was removed by repeated bulb-to-bulb distillation. The other impurities were shown to be CH_4 and SiF_4 . Low boiling impurities would lead to erroneous interpretations of the isotopic analyses of the distillate with respect to the distillation column characteristics. In order to bring the level of these impurities down to a more acceptable level, one part in 10⁵, further purification was necessary.

The distillation column of the Bigeleisen type was generously donated by its creator, Professor Jacob Bigeleisen of the University of Rochester. Since its movement from Rochester, the column has been cleaned, reassembled and modified.⁽¹⁹⁾

In order to perform isotope-ratio analyses of the Halocarbon-23 samples withdrawn from the column, the conversion of CHF_3 to carbon dioxide was found to be necessary. This conversion is accomplished by the use of a specially designed and constructed combustion system. Halocarbons, especially highly fluorinated ones, are chemically quite stable. A combustion train similar to that of McKenna, Priest, and Staple⁽²⁰⁾ with some modification was fabricated in quartz.

A) Distillation Column and Its Support System.

The low-temperature distillation column was originally designed by Bigeleisen and Ribnikar⁽²²⁾ at Brookhaven National Laboratory. It was applied in studies of the vapor pressure isotope effect in N₂O at 184^O K. Subsequently, it was used in the distillation studies of C_2H_3D and ${}^{12}CH_2 = {}^{13}CH_2$ by Bigeleisen, Cragg, and Jeevanandam⁽¹²⁾ for their study of isotopic methanes. This column was transported from the University of Rochester along with its brass housing and service vacuum line. The column has since been modified.^(12,19,20,23)

The reassembled column, in the same configuration as that most recently used, ⁽¹⁹⁾ had been cleaned, and was repacked with 76 grams of Podbelniak Nichrome Heli-pak No. 2916, which had been cleaned in a Soxhlet extractor with benzene for three days. The reassembled column is depicted in Figure 2 and an enlargement of the boiler is ' shown in Figure 3.

The entire column and service vacuum line were leaktested using a highly sensitive (minimum detectable leak is 5×10^{-11} ccNTP/sec) helium leak detector (Dupont Instruments model 25-120 B). It was found that the service line and column were able to attain a vacuum of 10^{-5} torr, a rather good vacuum considering the capillaries involved and the large surface area of the packing. The service Vacuum line is schematically represented in Figure 4.

The liquid nitrogen level in the dewar surrounding the column's helium jacket was maintained using a Veeco Instrument's model VLN 30 Liquid Nitrogen Level Controller. The controller, two sensor leads, and a three-way solenoid valve comprise a system (Figure 5) which can maintain a liquid nitrogen level between two predetermined points. The atmosphere above the liquid nitrogen in the liquid nitrogen tank is normally vented through the three-way

-18-

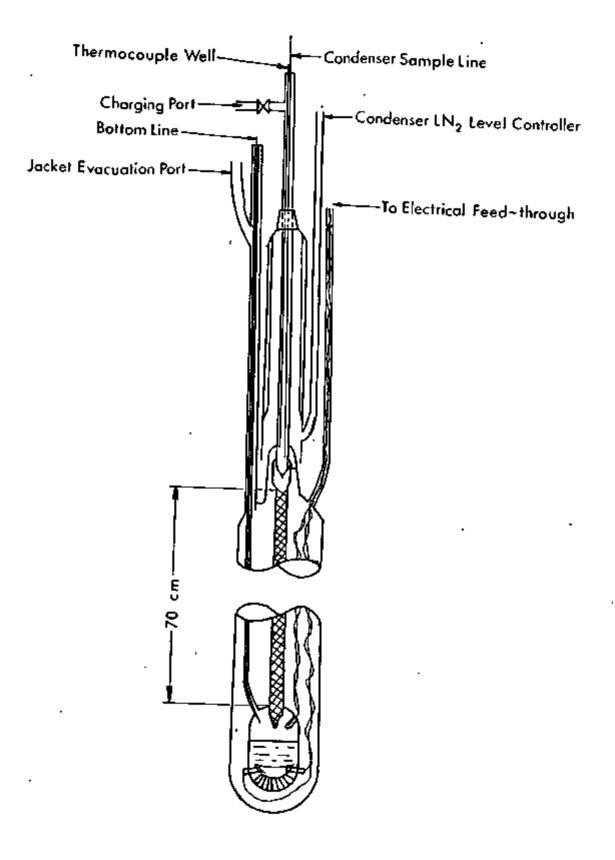
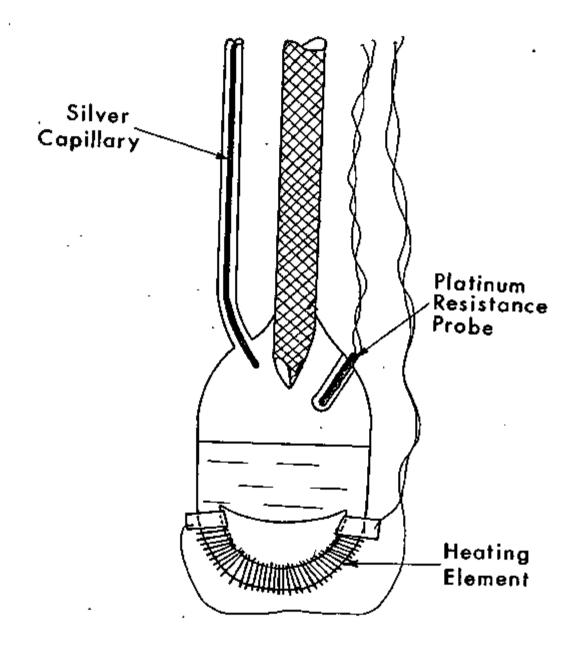


Figure 2. The Cryogenic Distillation Column



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Figure 3. Boiler

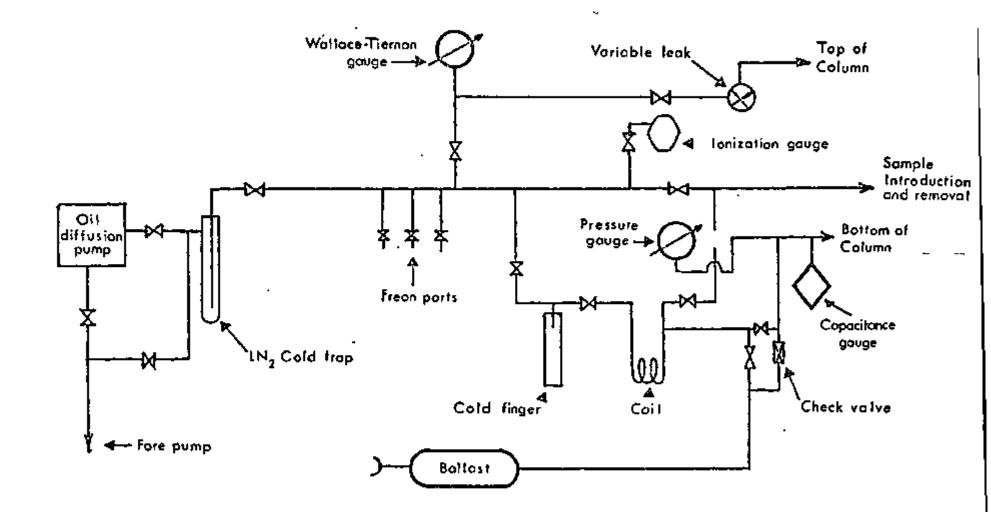
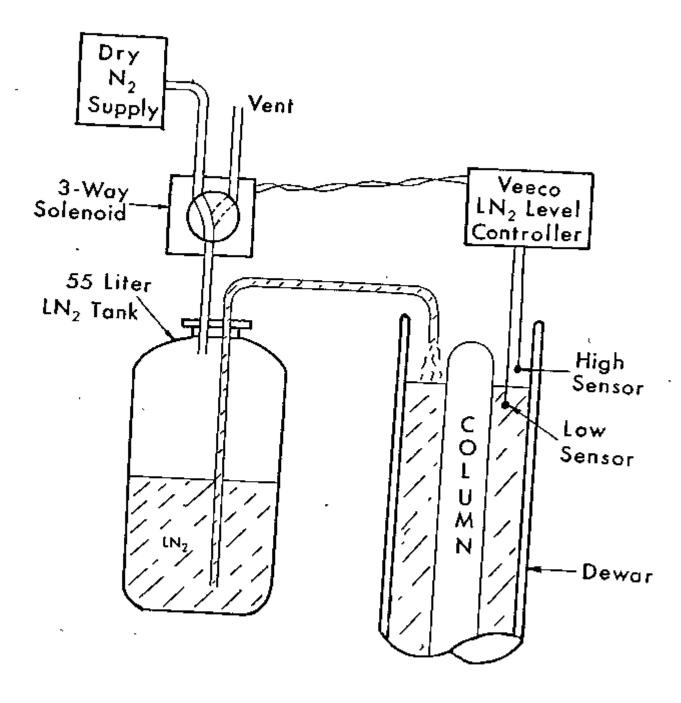
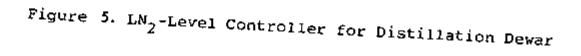


Figure 4. Service Vacuum Line





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solenoid valve. When the level of liquid nitrogen drops below the lower sensor, the three-way solenoid is activated, the vent closed, and a liquid nitrogen holding tank (Union Carbide's model UC-55) is pressurized with gaseous nitrogen. The dewar is filled until the level reaches the higher sensor. Upon achieving the required level, the holding tank is vented to the atmosphere. The close control of the liquid nitrogen level in the dewar is vitally important for the stable pressure maintenance within the column.

A vacuum system to maintain a high vacuum in the helium jacket of the column was fabricated primarily of stainless steel.⁽¹⁹⁾ The system, which is a one-inch vacuum pumping station, employs a Consolidated Vacuum Corporation type VMF 21 oil diffusion pump and a Vacuum Instrument Corporation's BT-20 liquid nitrogen bucket-type cold trap. The configuration of the system is schematically represented in Figure 6. The valves are Veeco Instrument's bellows sealed valves. Vacuum readings are obtained using a model TG-7 Thermocouple Gauge in conjunction with a model RG-81 Ionization Gauge Controller and model RG-75 Ionization Gauge Tube, all manufactured by Veeco Instruments, Inc.

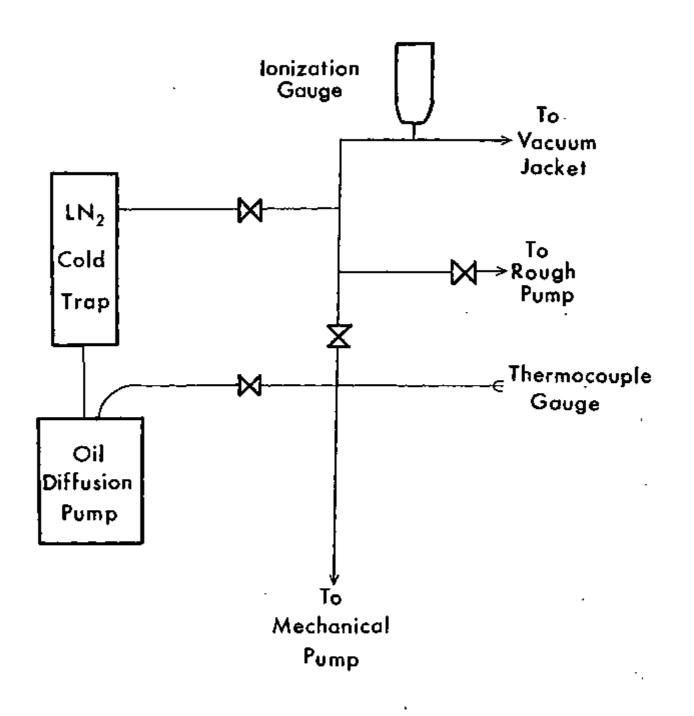


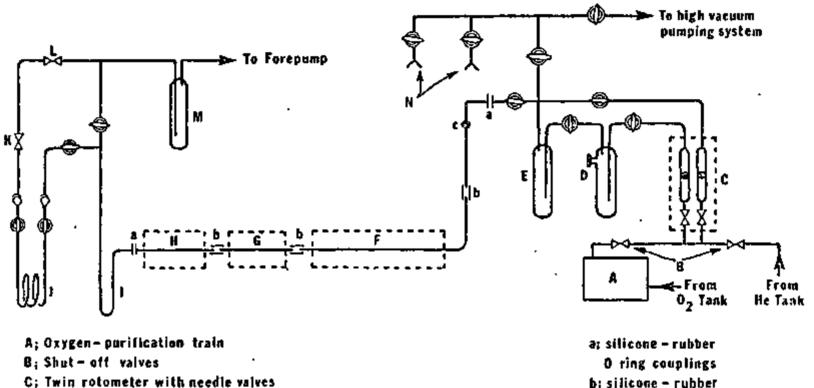
Figure 6. Vacuum System for Vacuum Jacket

B) Combustion Train

The isotopic analysis of the ${}^{13}\text{C}/{}^{12}\text{C}$ ratio is most easily performed on samples of carbon dioxide. A sample of CHF₃ introduced in a mass-spectrometer is hard to completely evacuate out of the system. This therefore necessitated a process for the oxidation of CHF₃ with sufficiently high yield so as to make any corrections for the ${}^{13}\text{C}/{}^{12}\text{C}$ isotope effect unnecessary. It was estimated that a 95% conversion of CHF₃ to CO₂ would limit the uncertainty on the isotopic ratio due to possible carbon isotope fractionation during the chemical conversion to an absolute maximum of ±0.0001, the limit which can be considered acceptable.

The combustion train consists of three sections (Figure 7). The first section is a quartz tube, 55 cm in length and 10 mm in outside diameter. The tube is packed alternately with platinum gauze and crushed quartz. It is heated by two Lindberg-Hevi Duty ovens, maintained at temperatures between 1000° C and 1050° C. In this temperature region, CHF_3 , in the presence of a large excess of oxygen, is decomposed to CO_2 , inorganic fluorine compounds (which are eventually converted to SiF_4), and $H_2^{\circ}O$. The second section of the train is a 10 mm outside diameter pyrex tube, which is packed alternately with pyrex wool and sodium fluoride. This 30 cm length of tubing is maintained at 250 $\pm 20^{\circ}$ C by an oven home-fabricated especially for this use.⁽³⁰⁾ The sodium fluoride section is employed to absorb SiF_4 . The final section is a pyrex U-tube at

-i



- D; injection port with silicone rubber
- E; Combustion sample trap
- F; Quartz tube with platinum gauze and crushed quartz
- G; Pyrex tube with silver wool packing
- H; Pyrex tube with NaF packing
- 1; U- Tube with silica gel packing
- J; Removable coiled CO2 trap
- K; Metering value
- L; Shut-off valve
- M;LN2-trap
- N, Combustion sample inlet ports

b; silicone - rubber tubing connections c; constriction

Figure 7. Combustion Train

room temperature filled with silica gel to remove H₂O.

Oxygen used in the train is obtained from a tank and purified by passing the stream through a concentrated H_2SO_4 bubble tower, a Drierite absorption tube, and finally an Ascarite absorption tube. After leaving the purifier, the stream is divided into two legs. One passes through the sample inlet area, thereby driving the sample into the oven and the other leg bypasses this area, flooding the oven with oxygen.

The combustion product, CO_2 , thus obtained was trapped in a liquid nitrogen trap. The product contained a small amount (less than one percent) of uncombusted sample plus traces (less than 0.05%) of yet undetermined impurities. The samples of CO_2 were then further purified by means of a home-fabricated gas-chromatograph⁽³⁰⁾ packed with alumina. After this final purification, the carbon dioxide samples were transferred to glass sample holders for analysis.

II-2. Precision Measurement of the Vapor Pressure of CHF_3

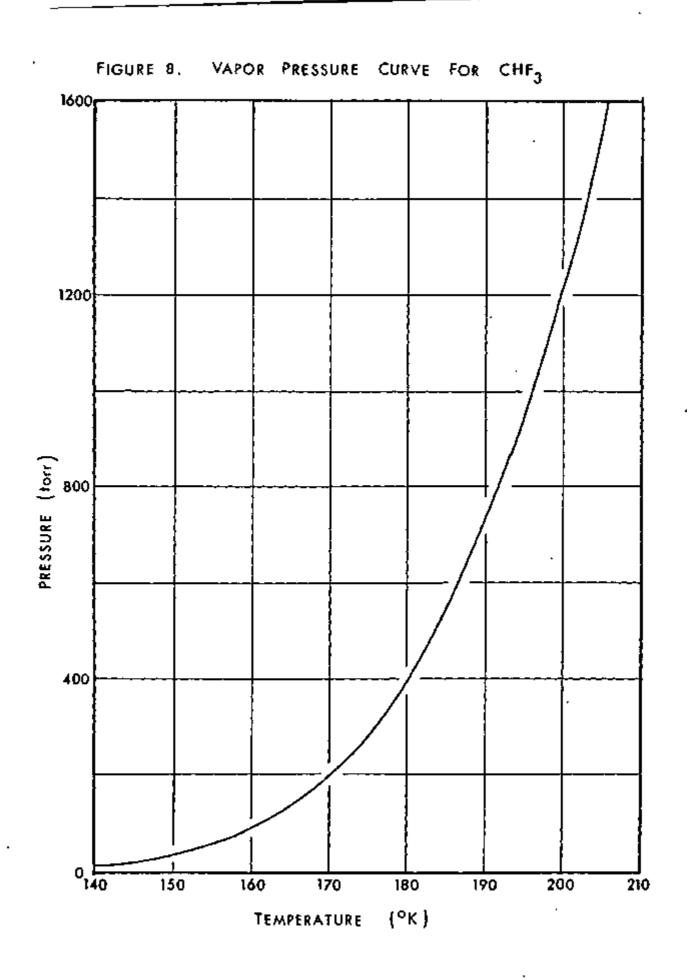
The only data available for the vapor pressure of $CHF_3^{(24)}$ is from an industrial source. In addition, there was no assurance of the accuracy of the temperatures reported by the investigator. Obtaining consistent vapor pressure data was therefore necessitated. For this purpose,

samples of CHF_3 were purified. All impurities in the samples were less than one part in 10^5 .

The manometry was performed in a cryostated differential manometer in Prof. J. Bigeleisen's laboratory at the University of Rochester. The cryostat⁽²⁵⁾ is capable of maintaining cryogenic temperatures to within $\pm 0.001^{\circ}$ C for several hours at a time. The differential manometry is accomplished through the use of differential capacitance gauges, which are capable of measuring pressure differences up to 50 torr ±0.1 millitorr. The vapor phase volume in the cryostated sample holder-manometer system is negligible compared to the amount of liquid in the sample holder. The absolute pressure of one of the liquid samples, which in this case was CHF_2 , is measured to within 11 millitorr by the use of a Texas Instruments' quartz spiral gauge. Vapor pressures of pur CHF_3 were measured in this apparatus at 29 temperatures between 139.3° K and 191.7° K. The results were least-squares fit to a four term equation:

$$\log_{10} P(\text{torr}) = \frac{-278.269}{T(0 \text{ K})} - 4.65910 + 0.0772937T - 0.000158127T^2$$
(14)

The single largest deviation of Equation 14 from an experimental point is 0.004 out of 1.183 in \log_{10} P. These results are plotted in Figure 8.



<u>II-3. Experimental Procedure</u>

A) Purification of CHF₃

After the removal of the major impurity, air, by repeated bulb-to-bulb distillation, gas chromatographic analyses, using the Perkin Elmer model 990 gas chromatograph, indicated the presence of 2.7×10^{-4} CH₄ and 1.2×10^{-4} SiF₄. A preliminary low-temperature distillation trial was performed and the resulting material was gas chromatographically analyzed. This procedure indicated that the level of the impurities was significantly reduced. Therefore, the entire supply of trifluoromethane was distilled at low temperature. Gas chromatographic analyses of the resulting material indicated that the CH₄ was reduced to a non-detectable level and that the SiF₄ was present to the extent of 1.7×10^{-5} . This material was then stored as that to be used in the distillation.

B) Distillation

The following paragraphs will outline the preparations for and the execution of a distillation run on the modified Bigeleisen column.

Approximately two days prior to a distillation run, the diffusion pumps on the service line and on the helium jacket line are started up and the liquid nitrogen holding tanks (used as a supply of liquid nitrogen for the cold traps) are filled. Until this point, these vacuum lines have been kept under rough vacuum. The night before the distillation run is performed, the UC-55 liquid nitrogen holding tank is filled to capacity. The "aging" of this liquid nitrogen was found to be essential, since the liquid nitrogen is shipped at a higher pressure than is maintained in the tanks. Therefore, time must be allowed for it to come to thermal equilibrium in its new environment.

On the morning of the distillation, various preparations are made, including preparation of the CHF_{γ} sample and cooling of the distillation column. The preparation of the CHF_3 sample involves condensing (using liquid nitrogen) into the cold finger, shown in Figure 4. When approximately $\frac{1}{2}$ mole (an amount in excess of that which will actually be needed for the distillation) of CHF₂ has been collected in the the cold finger, the liquid nitrogen is removed and replaced with a dry ice-acetone slurry. This maintains the pressure in the cold finger (which is isolated by the use of valves adjcent to each side) at approximately one atmosphere. It was observed that the nearer the temperature of the column was to the actual distillation temperature, the more smoothly the experiment proceeded. At this point, the liquid nitrogen level controller for the dewar surrounding the helium jacket was activated to automatic and the dewar was filled. The temperature within the boiler was monitored with the platinum resistance probe and, as it approached the target temperature for the distillation, the introduction of the CHF, into the column

was begun.

From its construction, it can be seen that, in the absence of a conducting gas within the vacuum jacket, the packed section of the column is cooled by the liquid nitrogen by conduction from near the condenser area. Therefore, it follows that a temperature gradient is established as the column temperature is lowered, with the boiler area the warmest and the condenser area the coldest. In order to properly charge and wet the column packing, this gradient was employed. It allowed the charge of CHF_3 to freeze and liquify on the packing rather than condense into the boiler immediately.

This charging procedure is as isothermal as can be hoped for. When the temperature probe in the boiler became near that temperature pre-selected for the run, the valve on the column side of the cold finger and the needle valve leading to the top of the column were slightly opened. As the CHF_3 entered the column, it condensed and warmed the area on which it was condensing, and this "wet" area can be thought of as having travelled along the column towards the boiler. The temperature profile along the column would become more uniform than it was before the charging started. During this time, the rate of addition of CHF_3 entering the column was adjusted using the needle valve in order to keep the temperature of the column as steady as possible by monitoring the pressure in the condenser and the platinum thermometer in the boiler. As the temperature gradient was

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removed by the entering CHF₃, the boiler started to fill with the charge and as soon as the level in the boiler was approximately ½" below the tip of the packed section, corresponding to approximately 20 ml of liquid in the boiler, the column was sealed and the boiler heater current activated. This was the start of the reflux and was time Zero for the experimental time measurement. This introduction practice helped minimize the uncertainties on time zero. At this point, the pressure is already stabilized and the column practically at equilibrium due to the "isothermal" charging procedure. Pressure throughout the charging was recorded using the output of the Setra Systems' model 236 differential capacitance gauge connected to the boiler section.

The column was then operated isothermally $(\pm 0.3^{\circ} \text{ C})$ under total reflux, and the buildup of the isotopeenrichment profile along the length of the column was monitored as a function of time by withdrawing gas samples from the condenser section of the column. The condenser samples (approximately 5 x 10^{-4} mole) were withdrawn through a variable leak into a small manifold of known volume (approximately 75 ml) and the sample pressure of approximately 100 torr was determined by use of a Wallace-Tiernan differential pressure gauge. A sample was usually withdrawn over a period of three to five minutes. Samples were generally taken every 15 minutes during the first hour, and then, succesively, two half-hour samples, two fourtyfive minute samples, and hourly samples, until approximately seven hours after time zero. Pressure and temperature measurements, as well as the current and voltage of the heater, were noted both before and after the extraction of each sample.

Samples of the boiler vapor were withdrawn as a control for the isotopic enrichment. A boiler sample was taken as close to time zero as possible and then at least once more during the course of the distillation. Boiler samples were removed by filling the service manifold, a volume of approximately 425 ml, with CHF_3 through the capillary leading to the boiler, the pressure monitored once again with the Wallace-Tiernan differential pressure gauge.

Samples were stored in 60 ml high vacuum glass gas sample holders.

All samples were now ready for combustion, which will be described in the following Subsection, II-3-C.

In order to apply the modified theory of K. Cohen to the kinetics of the distillation, it was necessary to determine the amount of CHF_3 held up in both the column and the condenser.

The procedure developed to determine the column holdup was essentially a two-stage shut-down of the column. After the last samples were removed from the column during the distillation operation, the line connecting the boiler to the service vacuum line was opened in order to drain the CHF_3 remaining in the boiler. The heater current was

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increased to compensate for the additional heat required for the increased rate of vaporization, thereby maintaining pressure in the column at the same constant level as that in the normal distillation operation of the column. When the boiler was emptied, which was checked visually by watching the boiler through an opening in the silvermirroring on the dewar, the column was sealed and the heater current was deactivated. The liquid nitrogen level controller maintaining the level in the dewar surrounding the column assembly was shut off and the liquid nitrogen allowed to boil off. The liquid nitrogen level in the dewar was allowed to come down to a level below the boiler. This made the boiler the coldest spot of the distillation column, and the CHF_3 originally held in the column packing condensed down into the boiler. The column heater was turned on again and all the material "held up" in the column was collected through the boiler sample line into a high vacuum stainless steel weighing vessel. The vessel was then weighed, its empty weight of 126.02 grams subtracted and thereby the amount of CHF_3 held up in the column was precisely determined.

The holdup in the condenser, another quantity needed for the column kinetics calculations, was determined in a separate series of experiments. The manifold of known volume leading to the column was filled with a known pressure (approximately 500 torr) of CHF_3 . The charge was slowly allowed to enter the column until the first drop appeared at the condenser tip. The remaining pressure in the manifold was the observed. The amount of CHF₃ that entered the condenser before the first drop was determined by applying the ideal gas laws, and this amount was considered to be equal to the condenser holdup.

C) Combustion and Purification

In order to facilitate the isotopic analysis of the CHF_3 samples taken from the column, They were combusted to carbon dioxide, using the apparatus shown in Figure 7 and described in Subsection II-1-B.

Each sample was transferred from its holder into a manifold of known volume, and its pressure was measured using a Wallace-Tiernan differential pressure gauge. The sample was then transferred to the combustion sample trap by condensing the sample into the trap at liquid nitrogen temperature. Oxygen was allowed to flow through the oven for five minutes using the bypass stopcock. At this point, the liquid nitrogen was removed from around the combustion sample trap and oxygen was allowed to flow both through the bypass and to sweep through the sample trap for ten minutes. At the end of this ten minute period, the oxygen flow was halted and five minutes of pump-down time was allowed, followed by two minutes of helium flow to remove any traces of sample from the system. Another ten minute pump-down period was allowed at this point. In all cases, the flow rate of the gases entering the ovens was 0.05 liters/min. The combustion product, CO₂, was clearly visible at this time in the collector coils. The sample was then transferred to the inlet side of the purification gas chromarograph. Using a flow rate of 20 ml/min at 300° C and an alumina-packed column, the carbon dioxide was purified and collected. The sample pressure was measured in a known volume with a Wallace-Tiernan differential pressure gauge.

D) Mass Spectrometry

An isotopic analysis was performed on each sample using a Consolidated Engineering Corporation's model 21-201 Isotope Ratio Mass Spectrometer. This model is of the Nier type construction. The feature which makes this particular model very attractive for isotopic analysis is its dual collector instrumentation (see Figure 9). In this mass spectrometer, gas molecules enter at low pressure(approximately 10⁻⁶ torr), are ionized, and accelerated into a magnetic field. In this magnetic field, all particles follow paths which are arcs of circles, with the heavier particles travelling paths of larger radius than the lighter particles. After passing through the magnetic field, each mass (or more correctly, mass-to-charge ratio) is focussed at a different point. The model 21-201's dual collector allows the beam impinging on one of its collectors to be compared with the beam falling on its other collector

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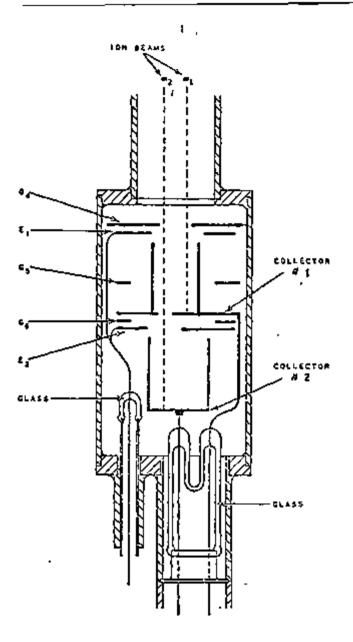


Figure 9. Dual Collector used in the Model 21-201 Mass Spectrometer.

Ion beams enter from top. The higher mass m_1 reaches Collector #2. The lower mass impinges on Collector #1. (Each collector has a box-like shield.) G₅ and G₆ are grounded shields to prevent electrical leakage between E₁ or E₂ and Collector #1. E₁ and E₂ operate at -45 volts with respect to ground and act as suppressors of secondary electrons released by ion bombardment from the collectors. Their slits are large enough so that they intercept no ions. concurrently. This allows simultaneous recording of the number of ions hitting each collector.

A model 21-201 was generously made available at Brookhaven National Laboratory in the laboratory of Dr. L. Friedman.

Prior to each isotopic analysis, a standard carbon dioxide sample was introduced into the inlet system. With the ion accelerating voltage set at approximately 1175 volts, the magnetic field was scanned and recorded using the number two collecter (narrow slit). Upon detecting the mass 44 and 45 peaks (${}^{12}CO_7$ and ${}^{13}CO_7$ respectively), the field was varied to place the 45 peak on the number two collector. The peak was placed directly on the collector by using the ion accelerating voltage as a fine adjustment. With mass 45 on the number two collector, the number one collector collected masses 42.6 to 46.5. In order to get more accurate data, all samples were analyzed at uniform pressure. Amplifiers were zeroed and checked periodically throughout each analysis session. Adequate time was allowed for pump-out in order to avoid any "memory" from previous samples.

III. DATA REDUCTION

Cohen's theory⁽¹¹⁾ of the transient kinetics of a square cascade was applied to the data obtained from the mass-spectrometric analyses of the samples from the condenser and boiler in order to determine the relative vapor pressures of the isotopic species. A modification of the theory of long-time kinetics (LTK) was developed, ⁽²⁶⁾ and was used to map the kinetics parameters, A and B, in the ranges of the overall separation and relative (condenser to column) holdups needed for the reduction of the present data. The following Section, III-1, contains an outline of the modified Cohen's theory of long-time kinetics. Section III-2 will outline the method of application of Cohen's theory to the present problem, and Section III-3 will contain a complete set of sample calculations pertaining to the experimental runs.

<u>III~1. Modified Cohen's Theory</u>

The transient behavior of a square, counter-current cascade of close separation stages during the start-up period was theoretically analyzed by K. Cohen⁽¹¹⁾ in relation to the fractionation of uranium-235. A consideration of the material balance of the desired substance

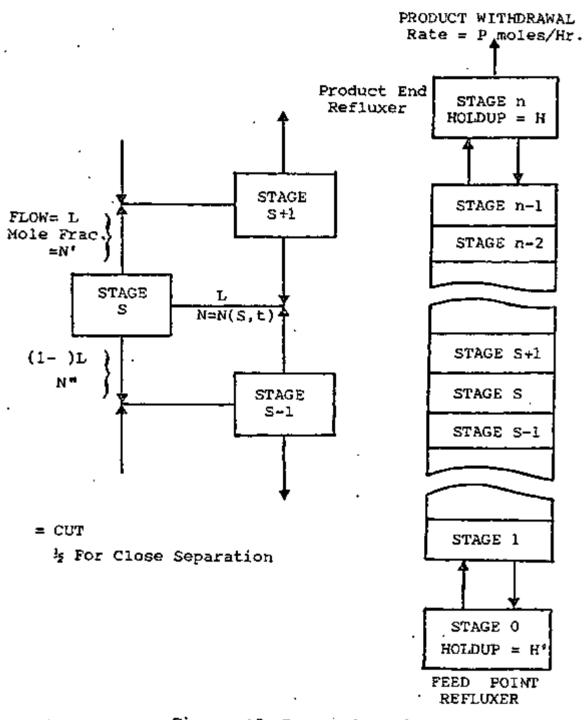
between the product stage and the s-th stage under conditions of constant flows leads (11) to a partial differential equation:

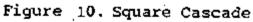
$$\lambda \frac{\partial N}{\partial t} = \frac{\partial^2 N}{\partial s^2} - \epsilon \frac{\partial}{\partial s} \left[\psi N + N(1-N) \right]$$
(15)

where N = N(s,t) is the average mole fraction of the desired substance in the input streams for the s-th stage (cf: Figure 10), counted toward the product end starting from the feed point in the cascade, at time t from the start-up of the cascade. Other quantities used in Equation 15, all dimensionless, are:

- $\epsilon = \alpha 1$, where α is the "head-to-tail" separation factor. This use of α is different from Cohen's, in that the latter α is the "head" or "tail" separation factor. The α used in the present study is twice Cohen's $\alpha_1(12,22,23,27)$
- $\lambda = 2h$, where h is the holdup per stage per unit flow, on the average process time per stage.
- $\psi = \frac{2P}{EL}$, where P is the production rate, or the rate of withdrawal of the product at the productend of the column, and L is the total interstage flow rate at stage s. In a square distillation cascade under total reflux, L is also equal to twice the boilup rate.

When the mole fraction of the desired substance is negligibly small compared to unity Equation 15 becomes





linear:

$$\lambda \frac{\partial N}{\partial t} = \frac{\partial^2 N}{\partial s^2} - \epsilon (1 + \psi) \frac{\partial N}{\partial s}$$
(16)

This would be the case in preliminary fractionation processes of isotopes, such as 235 U, D, 13 C, and 15 N. Cohen solved the equation under the following initial and boundary conditions:

at	t	-	0	;	$N(s,t=0) = N_0$	at all s
at	s	=	0	(feed point);	$N(0,t) = N_0$	at all t
at	\$	=	'n	(product end);	P = 0 Holdup in ref)	at <mark>all t</mark> tuxer = H

Such a solution is of general interest for two reasons. First, in large-scale production one seeks to minimize the initial start-up period during which the system is operating under total reflux. Second, observation of the transient behavior can be used for evaluating such separation system constants as the number of the theoretical plates and the separation factor.⁽¹¹⁾

Cohen's first-order solution of Equation 16 can be expressed in the form

$$\frac{N_{\infty} - N}{N_{\infty} - N_{O}} = Ae^{-B\tau}$$
(17)

where τ is the reduced time and is equal to $t/\lambda n^2$, and N_{∞} is the mole fraction of the desired substance at $t \rightarrow \infty$. A and B are Cohen's kinetics parameters, which were tabulated,⁽¹¹⁾ both dependent on two factors, En and $k/\lambda n$; n is the number of theoretical plates, and k is the ratio of the holdup in the condenser to the boil-up rate. Thus,

$$\frac{N_{\infty}}{N_{O}} = e^{\in n}$$
 (18)

and

$$\frac{k}{\lambda n} = \frac{\text{Holdup in the condenser (= H_{cond})}}{\text{Total holdup in the column (= H_{col})}}$$
(19)
Cohen's solution, Equation 17, was estimated⁽¹¹⁾ to be

valid at large t, satisfying the condition $t > n^2/10$.

The modification (26) of Cohen's LTK theory takes into account the second-order term for the solution of Equation 16 and can be represented as

$$\frac{N_{\infty} - N}{N_{\infty} - N_{0}} = A_{1} e^{-B_{1}\tau} + A_{2} e^{-B_{2}\tau}$$
(20)

where A_1 and B_1 are Cohen's first-order parameters, A and B respectively, and A_2 and B_2 are the second-order parameters calculated and tabulated by Ishida and Wieck. ⁽²⁶⁾ A_2 and B_2 depend on the same two factors, \in n and $k/\lambda n$, as do Cohen's parameters. Table XV contains the first-order parameters A_1 and B_1 in the ranges of \in n and $k/\lambda n$ observed in this study, Table XVI contains the second-order parameters A_2 and B_2 in the same ranges of \in n and $k/\lambda n$.

The first-order solution, Equation 17, has the advantage of a straight-line least-squares fit: from Equation 17,

$$Y_{L}(\tau) \equiv ln \left[\frac{q_{\infty} - q}{q_{\infty} - 1} \right] = ln A - Br \qquad (21)$$

where

$$q \equiv \frac{N}{N_0}$$
 (22)

and

$$N = \frac{R}{R+1}$$
(23)

In this study, in order to take advantage of the linear least-squares fit (LSF) while applying the second-order Equation 20, the second-order term of Equation 20 was used as a correction for the left-hand side of the equation. Thus,

$$y_{L}(\tau)_{corr} = ln \left[\frac{q_{ro} - q}{q_{ro} - 1} - \lambda_{2} e^{-B_{2}\tau} \right] = ln \lambda_{1} - B_{1}\tau$$
 (24)

and the left-hand side of Equation 24 was plotted against time t. A_2 and B_2 were obtained from a knowledge of $\in n$, obtained as $ln q_{\infty}$, and $k/\lambda n$, obtained from the holdup measurements. A straight line is obtained from the above plot with

$$Intercept = ln A_1$$
 (25)

and

Slope =
$$\frac{B_1}{\lambda n^2}$$

= $\frac{B_1(L/2)}{n H_{col}}$ (26)

Then,

$$n = \frac{(Boil-up rate)(B_1)}{(Column holdup)|Slope|}$$
(27)

By knowing B_1 from Cohen's table, one obtains n and subsequently 4.

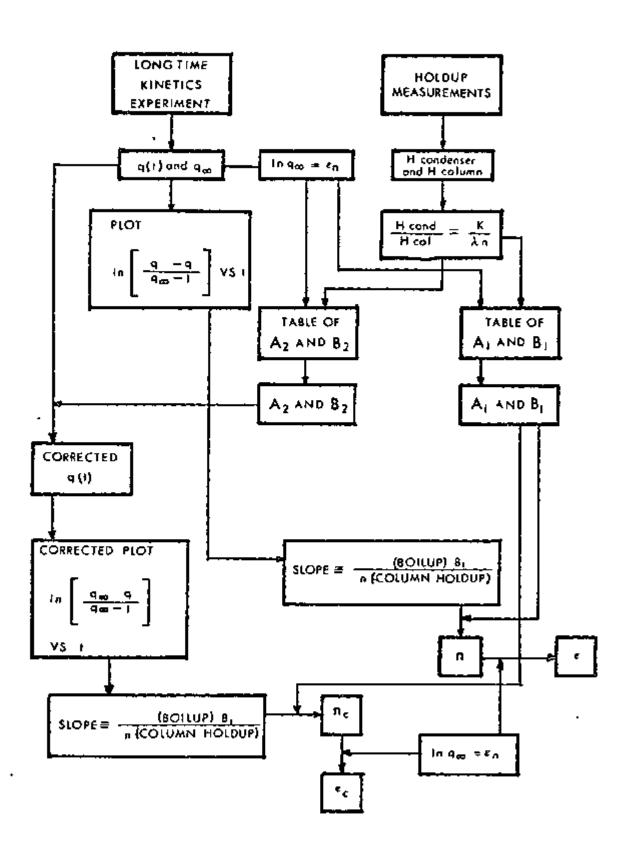
III-2. Outline of Method of Data Reduction

For each run, the mass-spectrometric data was processed according to the following procedure, outlined schematically in Figure 11.

The raw mass-spectrometric data of the 45/44 relative peak ratio represents the atom ratio, R, of 13 C to 12 C contained in the CO₂ samples. The overall separation, g, between the top and bottom of the column at time t is given by Equation 22.

Thus, from the isotopic ratio of $^{13}C/^{12}C$, R, of a condenser sample, and the isotopic ratio of $^{13}C/^{12}C$, R_o, of a boiler sample, N was calculated by Equation 23. Then, q was calculated from Equation 22, and both $ln (q_{\infty} - q)/$ $(q_{\infty} - 1)$ and $\ln \left[(q_{\infty} - q)/(q_{\infty} - 1) - A_2 e^{-B_2 t} \right]$ were plotted as a function of time t. The plots were fit to a linear function of t, using equal weights for all points: the possible error in the plotted quantity due to uncertainties of $\pm 2.2 \times 10^{-5}$ in the isotopic ratio measurements are of the order of 0.014 and do not vary significantly from point to point, so that their effect on the slope of the leastsquares fit line going through these points is insignificant. The errors on the LSF parameters, the slope and the intercept, were estimated based on the root-mean-square error (RSME) of the actual scatter of the experimental points around the best-fit line.⁽²⁸⁾ The points with the largest deviations were eliminated until the estimate of error on the slope became no more than 10% of the absolute

FIGURE 11. FLOW CHART OF DATA REDUCTION



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 magnitude of the slope. It was found that the values of the slope are rather insensitive to decisions to retain or discard points, while the intercept is very sensitive to such decisions. Therefore, the slope would lend to relatively objective evaluations of n and ϵ , despite the rather arbitrary decisions made on the experimental points. It was also found that the intercept of the LTK plot, which is equal to $ln A_1$, is too sensitive to relatively small uncertainties in time zero. Thus, for example, referring to Table XIV(C), the intercept for Run LD-10 is -0.554, whereas the value determined from ϵn and $k/\lambda n$ (i.e., $ln A_1$) is -0.173. The latter value of the intercept could have been obtained if time zero were set approximately 15 minutes earlier than time zero actually used.

<u>III-3. Sample Calculations</u>

As an illustrative example, run LD-10 will be used. The average R of the boiler samples is equal to 0.011759.

 $N_{\text{Boiler}} = N_{\text{o}} = \frac{0.011759}{1+0.011759} = 0.011622$

The equilibrium value of separation (or the overall separation value) is equal to 0.012189.

 $\therefore N_{\infty} = \frac{0.012189}{1+0.012189} = 0.012042$

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For condenser sample #1:

$$N = \frac{0.011879}{1 + 0.011879} = 0.011740$$

$$q = \frac{N}{N_0} = \frac{0.011740}{0.011622} = 1.0101$$

$$q_{\infty} = \frac{N_{\infty}}{N_{0}} = \frac{0.012042}{0.011622} = 1.0361$$

$$\therefore y_{L}(\tau) = \ln \left[\frac{q_{\infty} - q}{q_{\infty} - 1} \right] = -0.3279$$

Since $k/\lambda n$ is equal to 0.0374 and $\in n$ has a value of 0.03551, the following values of the "correctional" LTK parameters, A_2 and B_2 are obtained from Table XVI as:

$$A_{2} = 0.0879$$

$$B_{2} = 20.5846$$

$$\therefore y_{L}(\tau) = \ln \left[\frac{q_{\infty} - q}{q_{\infty} - 1} - A_{2} e^{-B_{2}\tau} \right] = -0.2940$$

These corrected $\textbf{y}_{L}(\tau)$ were then least-squares fit (LSF), yielding

 $slope = -0.00772 \pm 0.00080$

Intercept = -0.580 ± 0.297

The values of $y_{L}(\tau)$ calcaluated from this LSF are compared to their corresponding experimental values under the column "First LSF" in Table II. Since the RMSE of the above slope is more than 10% of the absolute magnitude of the slope, the experimental points No. 7, 10, and 12 were removed. Another linear LSF was then performed on the remaining eleven points. The Second LSF yielded

 $slope = -0.00787 \pm 0.00075$

Intercept = -0.554 ± 0.220

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TABLE	11.

SAMPLE CALCULATION OF RUN LD-10

		FIRST	LSF	SECON	D LSF
	EXP	CALC	EXP-CALC	CALC	EXP-CALC
SAMPL	$E Y_{L}(\tau)$	<u>y_L(7)</u>	$y_{L}(\tau)$	$y_{L}(\tau)$	$Y_{L}(\tau)$
1	-0.294039	-0.663129	0.369	-0.688027	0.394
2	-0.917590	-0.790411	-0.127	-0,806163	-0.111
3	-0.963767	-0.931827	-0.032	-0.932176	-0.032
4	-1.169525	-1.051503	-0.118	-1.050313	-0.119
5	-1.357729	-1.308424	-0.049	-1.302338	-0.055
6	-1.609364	-1.516499	-0,093	-1.514984	-0.094
, 7	-0.600317	-1.981516	1.381		
8	-2.862201	-2.587957	-0.274	-2.578214	-0.284
9	-3.207041	-2.902441	-0.305	-2.877494	-0.330
10	-4.728409	-3.419253	-1.309		
11	-3.332205	-3.721396	0.389	-3.696575	0.364
12 ·	-2.666173	-4.187942	1,522	_ 	
13	-3.401197	-4.436931	1.036	-4.413271	1.012
14	-6.040255	-5.243201	-0.797	-5.295358	-0.745

and the values of $y_{L}(\tau)$ calculated thusly are arrayed in Table II under the column headed "Second LSF". The experimental values of $y_{L}(\tau)$ are plotted versus time in Figure 12, and the line drawn is according to the calculation of the Second LSF.

Since $\in n$ and $k/\lambda n$ are equal to 0.03551 and 0.0374 respectively, A_1 and B_1 are obtained from Table XV as 0.8411 and $\overline{2}.2589$ respectively.

$$\therefore n = \frac{(1.2922)(2.2589)}{(6.762)[-0.00787]} = 54.8$$

The error on n is assumed to be due to that on the slope of the linear LSF only. Therefore,

$$\sigma_n = 54.8 \frac{(0.00075)}{(0.00787)} \approx 5.2$$

Knowing the value of \in n and n, \in can subsequently be ascertained:

$$\epsilon = \frac{\epsilon n}{n} = \frac{0.03551}{54.8} = 0.000647$$

and

$$\sigma_{\epsilon} = 0.000647 \frac{(0.00075)}{(0.00787)} = 0.000061$$

Thus

$$\alpha = \frac{1}{1+\epsilon} = \frac{1}{1+0.000647} = 0.999352$$

In order to observe the effect of the second-order correction term of $y_L(\tau)$ in Equation 24, run LD-02 will be used as an example.

Since \in n and k/ λ n have values of 0.03565 and 0.0400 respectively, values of A₁ and B₁ (from Table XV) as well as A₂ and B₂ (from Table XVI) are as follows:

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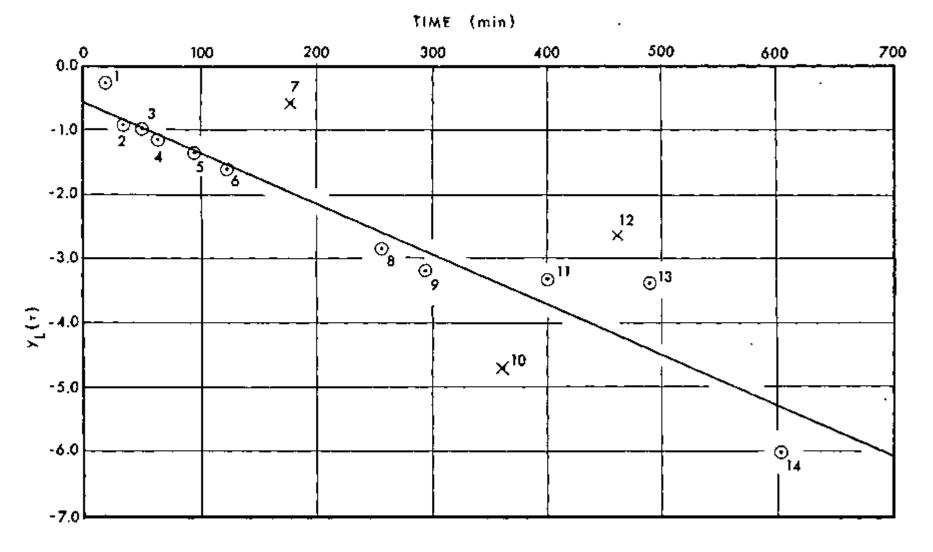


FIGURE 12, LONG TIME KINETICS PLOT OF RUN LD-10

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 $A_1 = 0.8428$ $B_1 = 2.2475$ $A_2 = 0.0877$ $B_2 = 20.4830$

Both Equation 21 and Equation 24 are least-squares fit using the above information.

For the uncorrected fit (Equation 21), the LSF yields Slope = -0.01335Intercept = -0.629For the corrected fit (Equation 24), the LSF yields Slope = -0.01456Intercept = -0.538

Both the LSF of Equation 21 (dashed line) and the LSF of Equation 24 (solid line) are plotted in Figure 24. It can be seen that the effect of the second-order term in Equation 24 is that of an improvement of the fit to the experimental points.

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IV. RESULTS AND DISCUSSION

This chapter is comprised of two parts. Section IV-1, which follows, will contain the results of the experimental aspect of this study and a discussion thereof. In the second part of this chapter, Section IV-2, the cell-model force field calculations will be developed.

<u>IV-1. Experimental Results of the Separation Factor as a</u> Function of Temperature

Results of the mass-spectrometric analyses of the samples for all eleven runs are presented in Tables III to XIII, one table for each distillation run. Tables XIV(A) through XIV(D) summarize the calculations of the number of theoretical stages, n, and the separation factor, \in (= α -1).

The headings in Tables III to XIII are self-explanatory. In Table XIV(A), the heading "T (O K) from P" was obtained using Equation 14 and the pressure, tabulated under "P (torr) from W-T gauge", read from the Wallace-Tiernan differential pressure gauge. Using the Platinum Resistance Thermometer (PRT) readings, the temperature is additionally obtained through a calibration traceable to the National Bureau of Standards. The least-squares fit formula for the calibration is:

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TABLE III. Data for Run LD-02

N _{Boiler} ≈ 0.011610	Epsilon x n = 0.03565
N _{Infinity} = 0.012031	Q _{Infinity} = 1.0363
Column Holdup = 6.320 grams	Boilup Rate = 0.7049 grams/min.

N Reading	Q _{Reading}	y _L (r) <u>uncorr.</u>	y _L (,) _corr	Time <u>(min)</u>
0.011784	1.0150	-0.5340	-0.5145	17
0.011837	1.0196	-0.7743	-0.7713	33
0.011871	1.0225	-0.9677	-0.9668	48
0.011923	1.0270	-1.3581	-1.3603	62
0.011960	1.0302	-1.7771	-1.7799	82
0.011995	1.0332	-2.4570	-2.4591	102
0.012002	1.0338	-2.6664	-2.6753	122
0.012004	1.0339	-2.7356	-2.7468	152
0.012016	1.0349	-3.2962	-3.3346	182
0.012023	1.0355	-3.8710	-3.9632	242
0.012030	1.0361	-5.3763	-6.0426	302
0.012027	1.0359	-4.4600	-4.6563	358

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TABLE IV. Data for Run LD-03

N _{Boiler} = 0.011635	Epsilon x n = 0.05377
N _{Infinity} = 0.012277	$Q_{\text{Infinity}} = 1.0552$
Column Holdup = 6.421 grams	Boilup Rate = 0.7538 grams/min.

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N. Reading	Q _{Reading}	y _L (†) <u>uncorr,</u>	Y _L (*) <u>corr.</u>	Time <u>(min.).</u>
0.011815	1.0155	-0.3287	-0.3017	17
0.011971	1.0289	-0.7406	-0.7371	47
0.012076	1.0380	-1.1623	-1.1595	62
0.012104	1.0403	-1.3084	-1.3109	82
0.012139	1.0433	-1.5344	-1.5372	102
0.012169	1.0459	-1.7807	-1.7824	122
0.012179	1.0468	-1.8752	- 1,8796	153
0.012218	1.0501 .	-2.3794	-2.3871	183
0.012227	1.0509	-2.5389	-2.5526	2 42
0.012263	1.0540	- 3.7815	-3.8255	302
0.012272	1.0547	-4.6978	-4.8552	367

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TABLE V. Data for Run LD-04

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N _{Boiler} = 0.011855	Epsilon x n = 0.02731
N _{Infinity} = 0.012183	Q _{Infinity} = 1.0277
Column Holdup = 6.234 grams	Boilup Rate = 0.6313 grams/min.

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N Reading	Q _{Reading}	Υ _L (τ) uncorr.	y _L (7) _corr,	Time <u>(min.)</u>
0.011878	1.0020	-0.0749	-0.0502	17
0.011932	1.0065	-0.2689	-0.2604	33
0.011985	1.0110	-0.5048	-0.5020	47
0.012085	1.0195	-1.2129	-1.2079	92
0.012125	1.0228	-1.7405	-1.7326	122
0.012113	1.0218	-1,5555	-1.5445	155
0.012135	1.0237	-1.9264	-1.9218	182
0.012145	1.0245	-2.1546	-2.1554	243
0.012152	1.0251	-2.3528	-2.3590	302
0.012180	1.0274	-4.7232	-4.6944	405

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TABLE VI. Data for Run LD-05

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N _{Boiler} = 0.011506	Epsilon $x n = 0.05039$
N _{Infinity} = 0.012101	Q _{Infinity} = 1.0517
Column Holdup = 6.309 grams	Boilup Rate = 0.8838 grams/min.

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N. Reading	Q _{Reading}	y _L (7) <u>uncorr.</u>	y _L (†) corr.	Time <u>(min.)</u>
0.011710	1.0177	-0.4155	-0.3894	18
0.011787	1.0245	-0.6319	-0.6268	32
0.011844	1.0294	-0.8272	-0.8349	47
0.011917	1.0357	-1.1543	-1.1717	62
0.011959	1.0393	-1.3982	-1.4255	92
0.012032	1.0457	-2.0915	-2.1545	152
0.012072	1.0491	-2.8389	-3.0213	183
0.012085	1.0503	-3.3310	-3.6160	242
0.012096	1.0513	-4.0247	-4.7791	302
0.012095	1.0512	-3.9376	-4.5968	417
0.012100	1.0516	-4.4788	-6.3886	738

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TABLE VII. Data for Run LD-06

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$N_{Boiler} = 0.011495$	Epsilon x n = 0.04899
N _{Infinity} = 0.012072	Q _{Infinity} = 1.0502
Column Holdup = 6.884 grams	Boilup Rate = 0.9861 grams/min.

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N Reading	Q _{Reading}	y _L () <u>uncorr.</u>	y _L (+) 	Time <u>(min.)</u>
0.011658	1.0141	-0.3299	- 0.2867	17
0.011752	1.0223	- 0.58 90	-0.5642	32
0.011857	1.0314	-0.9840	-0.9727	49
0.011860	1.0317	-0.9976	-0.9942	62
0.011945	1.0391	-1.5071	-1.5108	87
0.011930	1.0378	-1.3986	-1.4019	142
0.012020	1.0456	-2.3933	- 2,4066	272
0.012030	1.0455	-2.5983	~ 2.6202	302
0.012032	1.0467	-2.6689	-2.6690	362
0.012060	1.0491	-3.8178	-3.8729	422

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TABLE VIII. Data for Run LD-07

$N_{Boiler} \approx 0.011440$	Epsilon $x = 0.04894$
N _{Infinity} = 0.012014	Q _{Infinity} = 1.0502
Column Holdup = 6.473 grams	Boilup Rate = 1.0547 grams/min.

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N _{Reading}	Q _{Reading}	y _L (+) uncorr.	Y _L (*) COTT.	Time <u>(min.)</u>
0.011573	1.0117	~0.2645	-0.2217	17
0.011733	1.0256	-0.7132	-0.6844	- 31
0.011788	1.0304	-0.9388	-0,9171	47
0.011824	1.0335	-1.1032	-1.0980	62
0.011889	1.0392	-1.5242	-1.5224	94
0.011944	1.0440	-2.0996	-2.1035	122
0.011943	1.0439	-2.0859	-2.0899	182
0.011948	1.0444	-2.1568	-2.1630	212
0.011970	1.0463	-2.5696	-2.5684	287
0.011976	1.0468	-2.7130	-2.7150	317
0.012011	1.0499	-5.2756	-5.2540	437
0.012008	1.0496	-4.5843	-4.5609	629

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TABLE IX. Data for Run LD-08

$N_{Boiler} = 0.011567$	Epsilon x n = 0.05427
N _{Infinity} = 0.012212	Q _{Infinity} = 1.0558
Column Holdup = 5.765 grams -	Boilup Rate = 0.5051 grams/min.

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N. Reading	Q _{Reading}	$y_{L}(\tau)$ uncorr.	$\gamma_{L}(\tau)$	Time <u>(min.)</u>
0.011715	1.0128	-0.2609	-0.2187	20
0.011821	1.0219	-0.4995	-0.4743	35
0.011985	1.0361	-1.0426	-1.0318	62
0.012032	1.0402	~1.2788	-1.2725	92
0.012059	1.0425	-1.4375	-1.4378	122
0.012091	1.0453	-1.6734	-1.6731	152
0.012101	1.0461	-1.7576	-1.7596	182
0.012125	1.0483	-2.0052	-2.0033	212
0.012154	1.0508	-2.4163	-2.4088	244
0.012165	1.0517	-2.6226	-2.6191	302
0.012197	1.0545	-3.7864	-3.7612	350
0.012203	1.0550	-4.2968	-4.2720	390
0.012210	1.0556	-5.8002	-5.7761	752

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TABLE X. Data for Run LD-09

N _{Boiler} = 0.011456	Epsilon x n = 0.04490
N _{Infinity} = 0.011982	Q _{Infinity} = 1.0459
Column Holdup = 7.282 grams	Boilup Rate = 1.4197 grams/min.

N Reading	Q. Reading	y _L (7) <u>uncorr.</u>	y _L (7) _corr.	Time <u>(min.)</u> ·
0.011473	1.0015	-0.0334	-0.0224	18
0.011616	1.0140	- 0.3650	-0.3599	32
0.011710	1.0222	-0.6618	-0.6590	49
0.011906	1.0393	-1.9327	-1.9342	62
0.011917	1.0403	-2.1000	-2.0909	94
0.011943	1.0425	-2.6005	-2.6017	122
0.011959	1.0440	-3.1542	-3.1298	188
0.011960	1.0441	-3.1985	-3.1743	226
0.011970	1.0449	-3.8050	-3.7804	252
0.011977	1.0455	-4.6819	-4.6559	304
0.011980	1.0458	-5.6005	-5.5722	364
0.011981	1.0458	-6.2824	-6.2653	422

TABLE XI. Data for Run LD-10

$N_{Boiler} = 0.011622$	Epsilon x n = 0.03551
N _{Infinity} = 0.012042	Q _{Infinity} = 1.0361
Column Holdup = 6.762 grams	Boilup rate = 1.2922 grams/min.

N <u>Reading</u>	<u>Q</u> Reading	y _L (+) uncorr.	y _L (†) _corr.	Time <u>(min.)</u>
0.011740	1.0101	-0.3279	-0.2940	17
0.011878	1.0220	-0.9407	-0.9176	32
0.011883	1.0225	-0.9709	-0.9638	48
0.011912	1.0250	- 1.1743	- 1.1695	63
0.011934	1.0268	-1.3552	-1.3577	95
0.011958	1.0289	-1.6104	-1.6094	122
0.012018	1.0340	~2.8 466	~2.8622 .	257
0.012025	1.0346	-3.1744	-3.2070	295
0.012027	1.0348	-3.2929	-3.3322	399
0.012028	1.0349	-3,3574	-3.4012	490
0.012041	1.0361 ·	-6.0654	-6.0403	602

TABLE XII. Data for Run LD-11

N _{Boiler} = 0.011726	Epsilon x $n = 0.04456$
$N_{Infinity} = 0.012260$	Q _{Infinity} = 1.0456
Column Holdup = 7.289 grams	Boilup Rate = 0.3927 grams/min.

N. <u>Reading</u>	Q. Reading	y _L (†) uncorr.	y _L (*) 	Time <u>(min.)</u>
0.011906	1.0154	-0.4108	-0.3808	18
0.011980	1.0217	-0.6459	-0.6331	32
0.012078	1.0301	⊷1.0797	-1.0715	49
0.012177	1.0385	-1.8628	-1.8612	93
0.012218	1.0420	-2.5443	- 2.5427	167
0.012220	1.0422	- 2.5921	-2,5915	208
0.012243	1.0442	-3.4719	-3.4472	243
0.012252	1.0449	-4.2261	-4.2010	303
0.012255	1.0452	-4.6944	-4.6710	373
0.012253	1.0450	-4.3593	-4.3345	413
0.012255	1.0452	~ 4.6944	-4.6710	517
0.012259	1.0455	-6.3085	-6.2804	654

TABLE XIII. Data for Run LD-12

$N_{Boiler} = 0.011701$	Epsilon x n = 0.04276
$N_{\text{Infinity}} = 0.012212$	Q _{Infinity} = 1.0437
Column Holdup = 7.219 grams	Boilup Rate = 1.1930 grams/min.

N _{Readinq}	Q _{Reading}	y _L (τ) uncorr.	γ _L (•) _corr	Time <u>(min.)</u>
0.011776	1.0064	-0,1582	-0.1314	17
0.011934	1.0199	-0.6084	-0.6050	49
0.012026	1.0278	-1.0087	~1.0086	62
0.012035	1.0286	-1.0625	-1.0600	92
0.012080	1.0324	-1.3558	-1.3535	122
0.012131	1.0368	-1.8423	-1.8419	193
0.012159	1.0392	-2.2722	-2.2661	222
0.012167	1.0399	-2.4324	-2.4297	274
0.012190	1.0418	-3.1253	-3.1453	302
0.012187	1.0415	-3.0029	-3.0175	362
0.012192	1.0419	-3.2163	-3.2406	435
0.012201	1.0428	-3.8621	-3.8385	487
0.012211	1.0436	-6.2548	-6.2364	632

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Run No.	P (torr) from W-T _qauge	T (^O K) from P	PRT (ohms)	т (^о к) from PRT	Column Holdup (g)	Boilup Rate <u>(g/min)</u>
LD-11	93 [±] 11	161.2±0.9	55.4±0.5	161.1±0.9	7.287	0.3927
LD-08	153±11	167.3±0.9	57.9±0.4	167.2±0.8	5.765	0.5051
LD-04	265±13	174.7±0.8	61.0±0.3	174.9±0.6	6.234	0,6313
LD-02	366±11	179.3±0.4	62.8±0.3	179.3±0.6	6.320	0.7049
LD-03	428 <u>+</u> 12	181.7±0.7	63.8±0.2	181.8 <u>+</u> 0.4	6.421	0.7538
LD-05	592±16	186.8±0.5	65 .9± 0.2	187.0±0.5	6.309	0.8938
LD-06	730±14	190.4±0.5	67.3±0.3	190.5±0.6	6.884	0.9861
LD-07	846±29	193.0±0.7	68.1±0.3	192.5 <u>†</u> 0.5	6.473	1.0547
LD-12	1015±24	196.520.5	· 70.0±0.2	197.2±0.3	, 7.219	1.1930
LD-10	1225±33	200.2±0.5	71.4±0.3	200.6±0.5	6.762	1.2922

204.0±0.3

7.282

1.4197

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204.6±0.5 72.7±0.2

TABLE XIV(A). Summary of Distillation Data for Halocarbon 23

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LD-09

1497±38

Run No.	k/λn	Epsilon x n	A	B_1	A	2
LD-11	0.0347	0.04456	0,8400	2,2621	0.0872	20.6734
LD-08	0.0439	0.05427	0.8466	2.2132	0.0859	20.3046
LD-04	0.0406	0.02731	0.8425	2.2528	0.0884	20,4757
LD-02	0.0400	0.03565	0.8428	2.2475	0.0877	20,4830
LD-03	0.0394	0.05377	0.8438	2,2330	0.0862	20,4741
LD-05	0.0401	0.05039	0.8440	2.2331	0.0865	20.4531
LD-06	0.0368	0.04899	0.8417	2.2489	0.0868	20.5898
LD-07	0.0391	0.04894	0.8432	2.2389	0.0866	20.4764
LD-12	0.0350	0.04276	0.8400	2.2625	0.0874	20.6650
LD-10	0.0374	0.03551	0.8411	2.2589	0.0879	20.5846
LD-09	0.0347	0.04490	0.8400	2.2618	0.0872	20.6547

TABLE XIV(B). Summary of Distillation Data for Halocarbon-23

TABLE XIV(C). Summary of Distillation Data for Halocarbon-23

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Run No.	Negative of Slope of LTK (uncorr) (min ⁻¹)	Negative of Intercept of LTK (uncorr)	Negative of Slope of LTK (corr) (min ⁻¹)	Negative of Intercept of LTK (corr.)
LD-11	0.00883 20.00072	0.813 ±0.232	0.00880 10.00072	0.803 ±0.233
LD-08	0.00781 ±0.00054	0.470 ±0.160	0.00780 ±0.00054	0.459 ±0.160.
LD-04	0.01019 20.00108	0.022 ±0.214	0.01019 10.00202	0.014 ±0.144
LD-02	0.01335 ±0.00128	0.629 ±0.225	0.01456 ±0.00135	0.538 ±0.214
LD-03	0.01151 20.00161	0.254 ±0.114	0.01188 20.00116	0.216 ±0.100
LD-05	0.00870 ±0.00089	0.839 ±0.289	0.00814 20.00080	0.820 ±0.271
LD-06	0.00713 ±0.00058	0.482 ±0.131	0.00727 ±0.00061	0.459 ±0.138
LD-07	0.00749 10.00091	0.645 ±0.247	0.00750 ±0.00072	0.634 20.228
LD-12	0.00842 ±0.00057	0.218 ±0.176	0.00842 ±0.00056	0.215 ±0.175
LD-10	0.00781 ±0.00077	0.564 ±0.225	0.00787 ±0.00075	0.554 ±0.220
LD-09	0.01438 ±0.00092	0.311/ ±0.204	0.01432 ±0.00094	0.308 ±0.206

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TABLE XIV(D). Summary of Distillation Data for Halocarbon-23

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Run No.	h (uncorr)	e (u	ncorr)	n (corr)	<u>.</u> (corr)	Holdup per Stage (q)
LD-11	13.7 ±1.1	0.00323	±0.00026	13.8 ±1.1	0.00322	±0.00026	0.527
LD-08	24.8 ±1.7	0.00218.	±0.00015	24.8 ±1.7	0,00218	±0.00015	0,231
LD-04	22,3 ±2.3	0.00122	±0.00012	22.3 ±2.2	0.00122	±0.00012	0.278
LD-02	18.7 ±1.8	0.00189	±0.00018	17.2 ±1.5	0.00207	10.00019.	0.367
LD-03	22.7 ±12.1	0.00236	±0,00125	22.0 ±2.1	0.00243	±0.00023	0.290
LD-05	35.5 1 3.6	0.00141	±0.00014	35.7 ±3.5.	0.00140	±0.00014(0.176
LD-06	46,1 ±3.7 ·	0.00108	±0.00008	44.2 ±3.7	0.00110	±0.00009	0.155
LD-07	48.6 ±5.9	0.00100	±0.00012.	48.6 ±4.6.	0.00100	±0.00009	0.133
LD-12	44.4 ±3.0	0.00096	±0.00006.	44.3 ±2.9	0.00096	±0.00006	0.162
LD-10	55.2 ±5.4	0.00064	±0.00006.	54.8 ±5.2,	0.00064	±0.00006	0.123
LD-09	30.6 ±1.9	0.00146	±0.00009	30.7 ±2.0,	0.00145	±0.00009	0.236.

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<u>κ/λn</u>												
•n		0.035	0.036	0.037	0.038	0.039	0.040	0.041	0.042	0.043	0.044	
0.027	А=	0.8387	0.8394	0.8401	0.8407	0.8414	0.8421	0.8427	0.8434	0.8440	0.8447	
	В=	2.2776	2.2732	2.2688	2.2644	2.2601	2.2557	2.2514	2.2470	2.2427	2.2384	
0.028	A=	0.8388	0.8395	0.8402	0.8408	0.8415	0.8421	0.8428	0.8435	0.8441	0.8447	
	B=	2.2766	2.2722	2,2678	2.2635	2.2591	2.2548	2.2504	2.2461	2.2418	2.2375	
0.029	A=	0.8389	0.8396	0.8402	0.8409	0.8416	0.8422	0,8429	0.8435	0.8442	0.8448	
	B=	2.2757	2.2713	2.2669	2.2625	2.2581	2.2538	2,2495	2.2451	2.2408	2.2365	
0.030	A≃	0.8390	0.8396	0.8403	0.8410	0.8416	0.8423	0.8430	0.8436	0.8443	0.8449	
	B≠	2.2747	2.2703	2.2659	2.2616	2.2572	2.2529	2.2485	2.2442	2.2399	2.2356	
0.031	A=	0.8391	0.8397	0.8404	0.8411	0.8417	0.8424	0.8430	0.8437	0.8443	0.8450	
	B=	2.2738	2.2694	2.2650	2.2606	2.2562	2.2519	2.2476	2,2433	2.2389	2.2347	
0,032	A≕	0.8391	0.8398	0.8405	0.8411	0.8418	0.8425	0.8431	0.8438	0.8444	0.8451	
	B≕	2.2728	2.2684	2.2640	2.2597	2.2553	2.2510	2.2466	2.2423	2.2380	2.2337	
0,033	A=	0.8392	0.8399	0.8406	0.8412	0.8419	0.8425	0.8432	0.8438	0.8445	0.9451	
	B=	2.2719	2.2675	2.2631	2.2587	2.2543	2.2500	2.2457	2.2414	2.2371	2.2328	
0.034	A=	0.8393	0.8400	0.8406	0.8413	0.8420	0.8426	0.8433	0.8439	0.8446	0.8452	
	B=	2.2709	2.2665	2.2621	2.2578	2.2534	2.2491	2.2447	2.2404	2.2361	2.2318	
0.035	A=	0.8394	0.8400	0.8407	0.8414	0.8420	0.8427	0.8433	0.8440	0.8446	0.8453	
	B=	2.2699	2.2656	2.2612	2.2568	2.2524	2.2481	2.2438	2.2395	2.2352	2.2309	
0.036	A⇒	0.8394	0.8401	0.8408	0,8415	0.8421	0.8428	0.8434	0.8441	0.8447	0.8454	
	B=	2.2690	2.2646	2.2602	2,2559	2.2515	2.2472	2.2428	2.2385	2.2342	2.2299	

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TABLE XV. First Order Term Kinetics Parameters A and B

TABLE XV. (Continued)

		<u> </u>				<u>\n</u>					
<u></u>		0.035	0.036	0.037	0.038	0.039	0.040	0.041	0.042	0.043	0.044
0.037	A=	0.8395	0.9402	0.8409	0.8415	0.8422	0.8428	0.8435	0.8441	0.8448	0.8454
	B≈	2.2680	2.2636	2.2593	2.2549	2.2506	2.2462	2.2419	2.2376	2.2333	2.2290
0.038	A=	0.8396	0.8403	0.8409	0.8416	0.8423	0.8429	0.8436	0.8442	0.8449	0.8455
	B=	2.2671	2.2627	2.2583	2.2540	2.2496	2.2453	2.2409	2.2366	2,2323	2.2280
0.039	A=	0.8397	0.8404	0.8410	0.8417	0.8423	0.8430	0.8437	0.8443	0.8449	0.8456
	B=	2.2661	2.2617	2.2574	2.2530	2.2487	2.2443	2.2400	2.2357	2.2314	2.2271
0.040	A=	0.8398	0.8404	0.8411	0.8418	0.8424	0.8431	0.8437	0.8444	0.8450	0.8457
	B=	2.2652	2.2608	2.2564	2.2521	2.2477	2.2434	2.2391	2.2347	2.2304	2.2262
0.041	A=	0.8398	0.8405	0.8412	0.8418	0.8425	0.8432	0.8438	0.8445	0.8451	0.8457
	B=	2.2642	2.2598	2.2555	2.2511	2.2468	2.2424	2.2381	2.2336	2.2295	2.2252
0.042	A=	0.839 9	0.8406	0.8413	0.8419	0.8426	0.8432	0.8439	0.84 45	0.8452	0.8458
	B=	2.2633	2.2589	2.2545	2.2502	2.2458	2.2415	2.2372	2.2329	2.2286	2.2243
0.043	A=	0.8400	0.8407	0.8413	0.8420	0.8427	0.8433	0,8440	0.8446	0.8453	0.8459
	B=	2.2623	2.2579	2.2536	2.2492	2.2449	2.2405	2,2362	2.2319	2.2276	2.2233
0.044	A=	0.8401	0.8407	0.8414	0.8421	0.8427	0.8434	0.8440	0.8447	0.8453	0.8460
	B≈	2.261 4	2.2570	2.2526	2.2483	2.2439	2.2396	2.2353	2.2310	2.2267	2.2224
0.045	A≃	0.8402	0.8408	0.8415	0.8422	0.8428	0.8435	0.8441	0.8448	0.8454	0.8461
	B⇔	2.2604	2.2560	2.2517	2.2473	2.2430	2.2386	2.2343	2.2300	2.2257	2.2215
0.046	A=	0.8402	0.8409	0.8416	0.8422	0.8429	0.8435	0.8442	0.8448	0.8455	0.8461
	B=	2.2595	2.2551	2.2507	2.2464	2.2420	2.2377	2.2334	2.2291	2.2248	2.2205

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					k/	٦n					
€n		0.035	0.036	0.037	0.038	0.039	0.040	0.041	0.042	0.043	0.044
0.047	A=	0.8403	0.8410	0.8416	0.8423	0.8430	0.8436	0.8443	0.8449	0.8456	0.8462
	B=	2.2858	2.2541	2.2498	2.2454	2.2411	2.2368	2.2324	2.2281	2.2239	2.2196
0.048	A=	0.8404	0.8411	0.8417	0.8424	0.8430	0.8437	0.8443	0.8450	0.8456	0.8463
	B≠	2.2576	2.2532	2.2488	2.2445	2.2401	2.2358	2.2315	2,2272	2.2229	2.2186
0.049	А=	0.8405	0.8411	0.8418	0.8425	0.8431	0.8438	0.8444	0.8451	0.8457	0.8464
	В=	2.2566	2.2523	2.2479	2.2435	2.2392	2.2349	2.2306	2.2263	2.2220	2.2177
0.050	А=	0.8405	0.8412	0.8419	0.8425	0.8432	0.8439	0.84 45	0.8451	0.8458	0.8464
	В=	2. 255 7	2.2513	2.2469	2.2426	2.2382	2.2339	2.2296	2.2253	2.2210	2.2168
0.051	A=	0.8406	0.8413	0.8420	0.8426	0.8433	0.8439	0.8446	0.8452	0.8459	0.8465
	B≃	2.2547	2.2504	2.2460	2.2416	2.2373	2.2330	2.2287	2.2244	2.2201	2.2158
0.052	A=	0.8407	0.8414	0.8420	0.8427	0.8434	0.8 440	0.8447	0.8453	0.8459	0.8466
	B=	2.2538	2.2494	2.2450	2.2407	2.2364	2.2 320	2.2277	2.2234	2.2191	2.2149
0.053	A=	0,8408	0.8414	0.8421	0.8428	0.8434	0.8441	0.8447	0.8454	0.8460	0.8467
	B=	2,2528	2.2485	2.2441	2.2398	2.2354	2.2311	2.2268	2.2225	2.2182	2.2139
0.054	À= B=	0.8409 2.2519	0.8415 2.2475	0.8422	0.8428 2.2388	0.8435 2.2345	0.8442 2.2302	0.8448 2.2258	0.8455 2.2216	0.8461 2.2173	0.8467 2.2130
0.055	A=	0.8409	0.8416	0.8423	0.8429	0.8436	0.8442	0.8449	0.8455	0.8462	0.8468
	B=	2.2509	2.2466	2.2422	2.2379	2.2335	2.2292	2.2249	2.2206	2.2163	2.2121
0.056	A=	0.8410	0.8417	0.8423	0.8430	0.8437	0.8443	0.84 50	0.8456	0.8463	0.8469
	B=	2.2500	2.2456	2.2413	2.2369	2.2326	2.2283	2.22 40	2.2197	2.2154	2.2111

TABLE XV. (Continued)

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TABLE XVI. Second Order Terr	Kinetics Parameters	A ₂ and	^B 2
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		k/λn										
_€ <u>n</u>		0.035	0.036	0.037	0.038	0.039	0.040	0.041	0.042	0.043	0.044	
0.027	A= B=	0.0885 20.6977				0.0884 20.5374					0.0883 20.3560	
0.028	A= B≂					0.0883 20.5366						
0.029	A= B=					0.0882 20.5348						
0.030	A≔ B≃					0.0882 20.5330						
0.031	A= B=					0.0881 20.5312						
0.032	A= B≈					0.0880 20.5294						
0.033	A= B=					0.0880 20.5276						
0.034	A= B=					0.0879 20. 52 58						
0.035	A= B=					0.0878 20.5240					0.0877 20.3417	
0.036		0.0878 20.6813										

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TABLE XVI. (Continued)

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				<u>_</u>	k/	<u>/λn</u>					
<u> en</u>		0.035	0.036	0.037	0.038	0.039	0.040	0.041	0.042	0.043	0.044
0.037	A⇒ B =	0.0877 20.6795	0.0877 20.6397					0.0876 20.4450		0.0875 20.3737	
0.038	A= B=		0.0877 20.3678								
0.039	A≃ B=		0.0876 20.6360								
0.040	A= B=		0.0875 20.6342		+						
0.041	A= B≂		0.0874 20.6324								
0.042	A= B=		0.0873 20.6306								
0.043	A= B≈		0.0872 20.6288								
0.044	A= B=		0.0871 20.6270								
0.045	A= B=	0.0871 20.6650	0.0871 20.6252								
0.046	A≃ B=		0.0870 20.6235								

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TABLE XVI. (Continued)

					k/	<u>/λn</u>					
<u>••n</u>		0.035	0.036	0.037	0.038	0.039	0.040	0.041	0.042	0.043	0.044
0.047	A= B≃	0.0869 20.6614		0.0869 20.5820				-			
0.048	A= B=			0.0868 20.5802							
0,049	А= В=			0.0867 20.5784							
0.050	А= В=			0.0866 20.5766							
0.051	A= B=			0.0865 20.5748							
0.052	A= B≈			0.0864 20.5730					-		
0.053	A= B=			0.0864 20.5712							
0.054	A≃ B≂			0.0863 20.5695							
0.055	A= B≂			0.0862 20.5677							
0.056	A≃ B=			0.0861 20.5659							

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$$T (^{\circ} K) = \frac{-0.59608}{R (ohm)} + 31.028 + 2.279R + 2.432 \times 10^{-1}R^2 - 4.9494 \times 10^{-4}R^3 (28)$$

The discrepancy between the two temperature readings is an indication of the reliability of the Wallace-Tiernan gauge, which is excellent. In Table XIV(D), the last column, entitled "Holdup per Stage (g)" is an indication of the degree of wetness of the column packing.

The data of Tables III to XIII have been plotted in Figures 13 to 23, one figure for each distillation run. These figures are the plots of the overall separation, q, as a function of time, t, and the solid lines through the figures correspond to the second-order corrected long-time kinetics, Equation 24.

The data from runs LD-02, LD-03, LD-06, and LD-10 have been plotted in Figures 24 to 27 respectively in order to demonstrate the effect of the second-order correction term of Equation 24. In each of these figures, the solid line represents the solution of the second-order corrected Equation 24, while the dashed line represents the firstorder solution, Equation 21. The effect is observable only within approximately the first 100 minutes of each distillation run, since the second term in the left-hand side of Equation 24 becomes insignificant for large values of r, which is equal to $t/\lambda n^2$.

The mass spectrometric analyses of these distillation experiments indicates that all the data attests to the inverse vapor pressure isotope effect.

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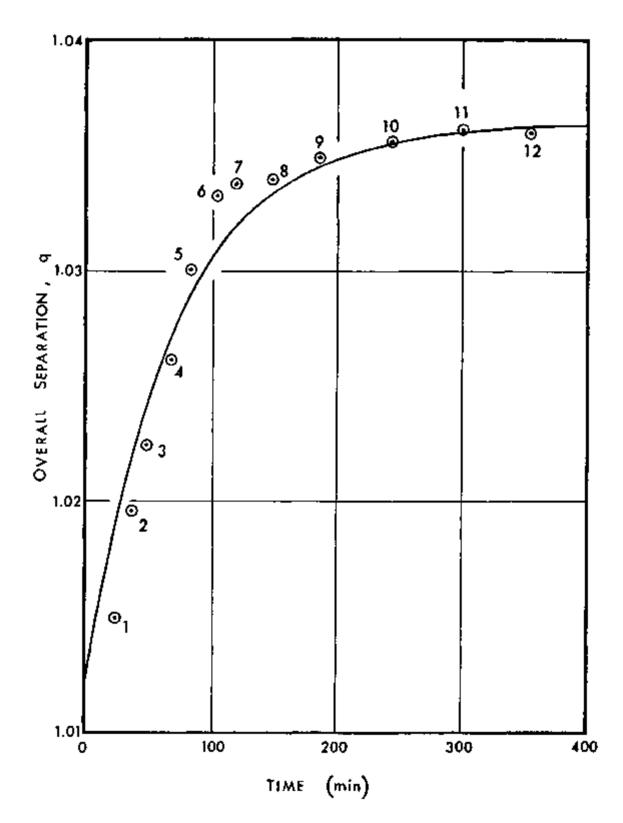


FIGURE 13. SEPARATION AS A FUNCTION OF TIME, RUN-02

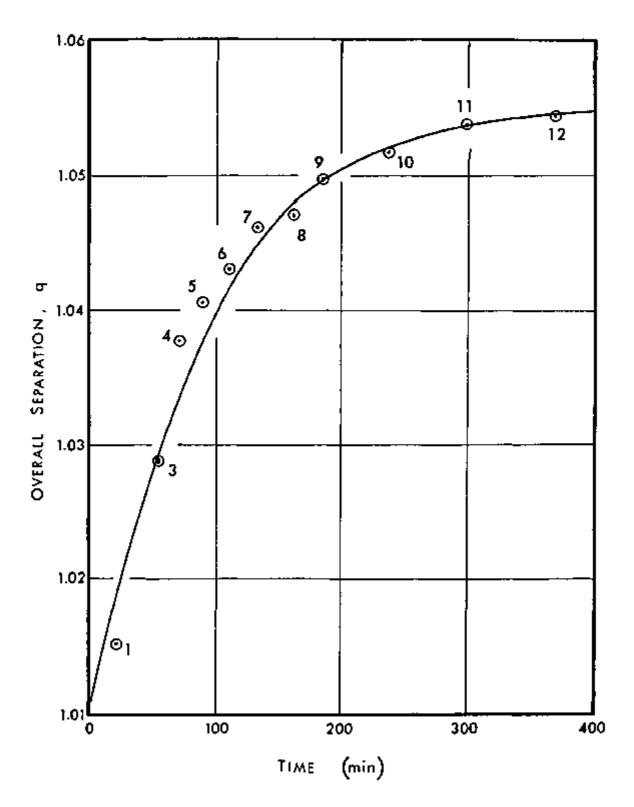


FIGURE 14. SEPARATION AS A FUNCTION OF TIME, RUN LD-03

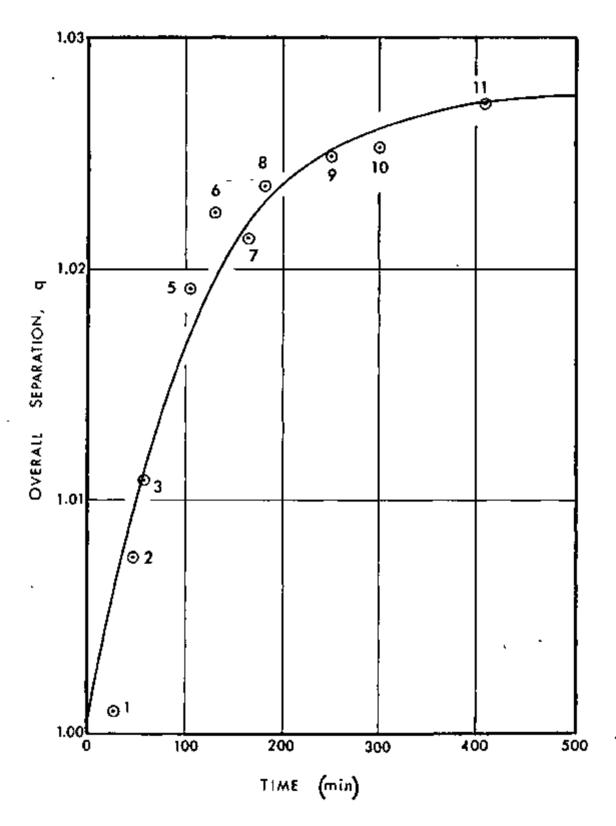
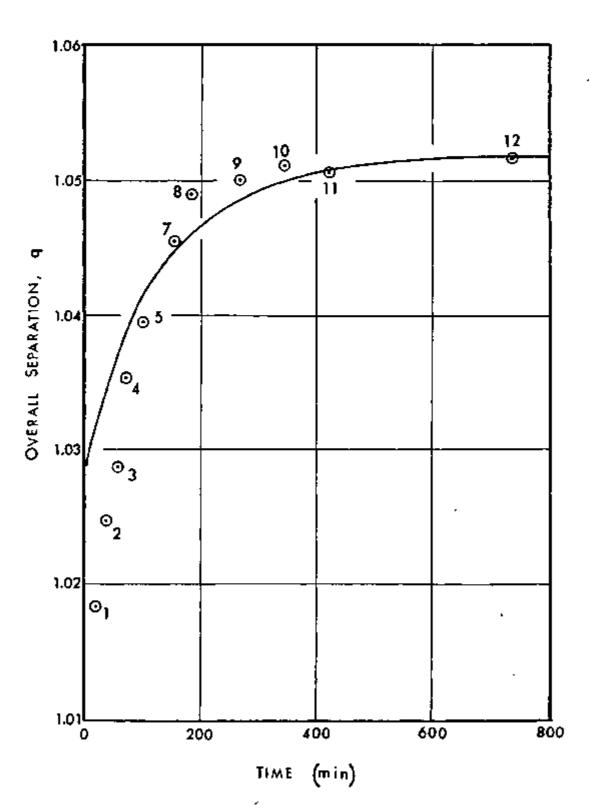
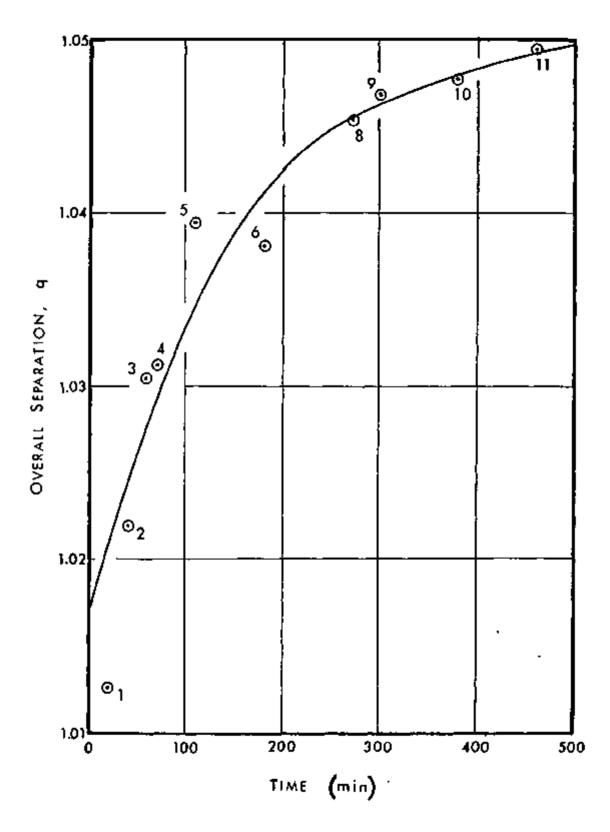


FIGURE 15. SEPARATION AS A FUNCTION OF TIME, RUN LD-04

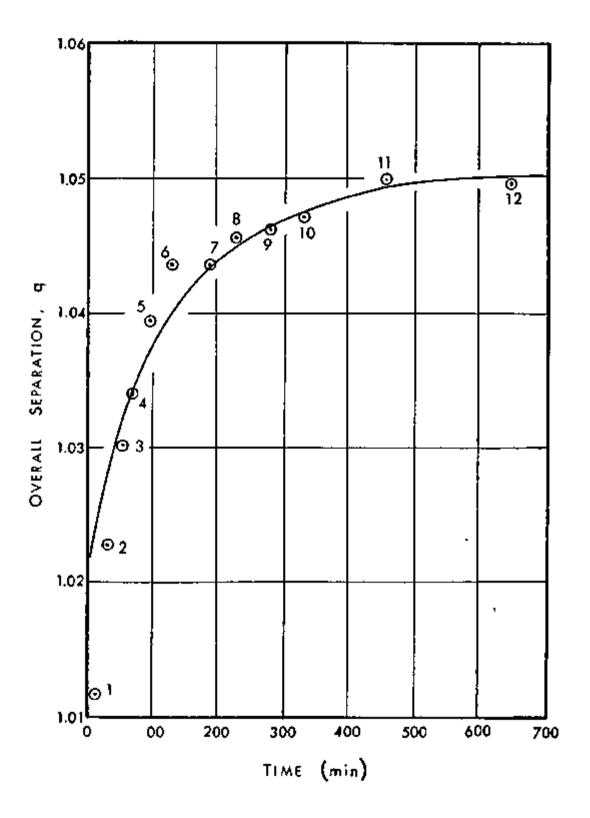


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FIGURE 16. SEPARATION AS A FUNCTION OF TIME, RUN LD-05







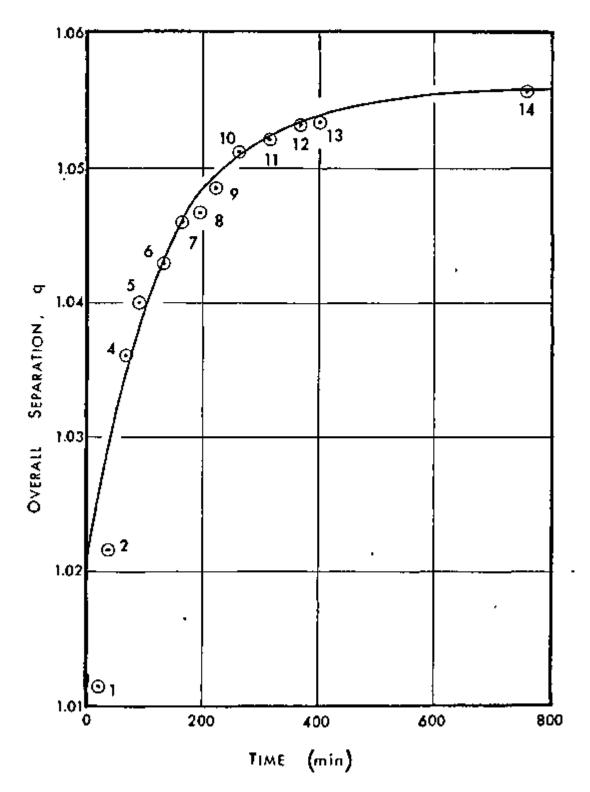


FIGURE 19. SEPARATION AS A FUNCTION OF TIME, RUN LD-08

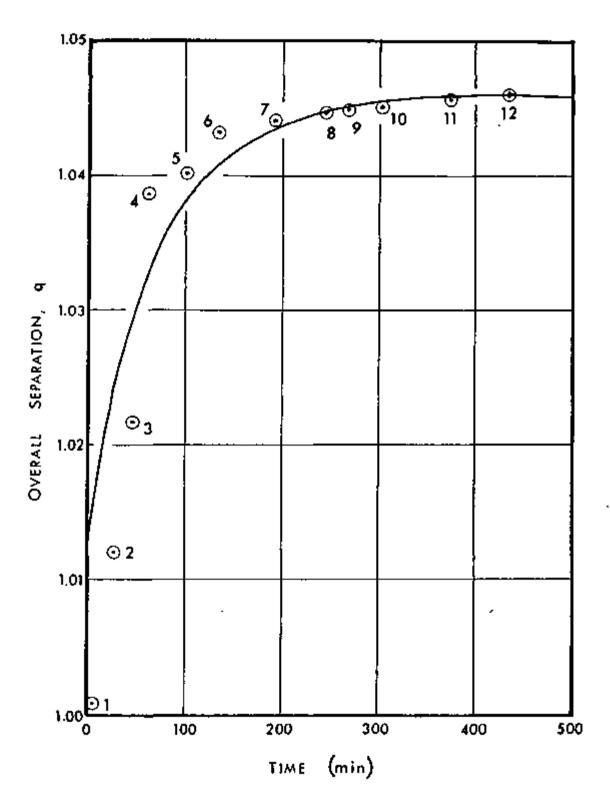


FIGURE 20. SEPARATION AS A FUNCTION OF TIME, RUN LD-09

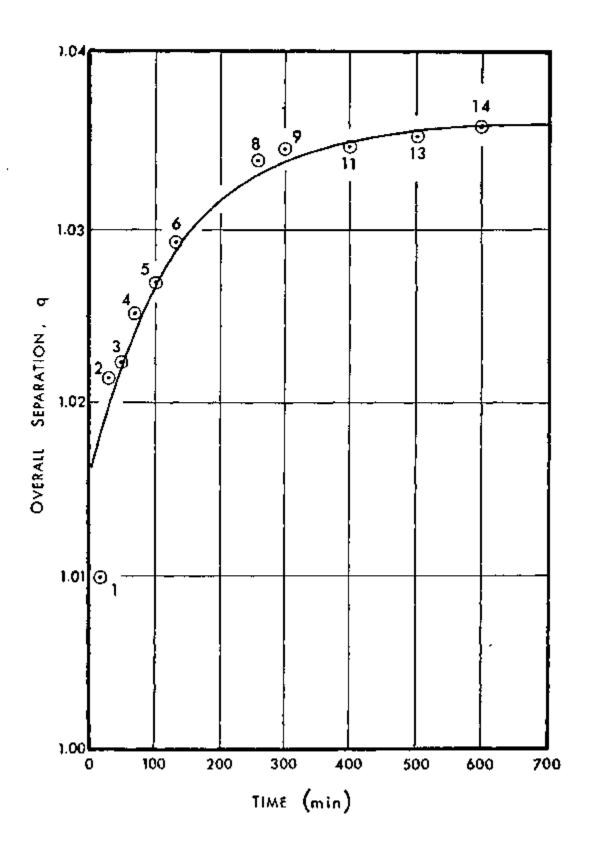


FIGURE 21. SEPARATION AS A FUNCTION OF TIME, RUN LD-10

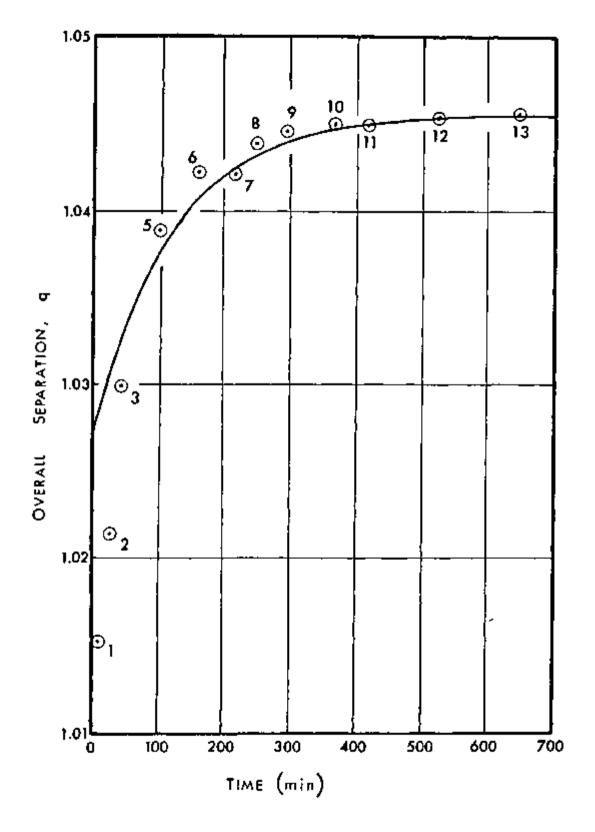


FIGURE 22. SEPARATION AS A FUNCTION OF TIME, RUN LD-11

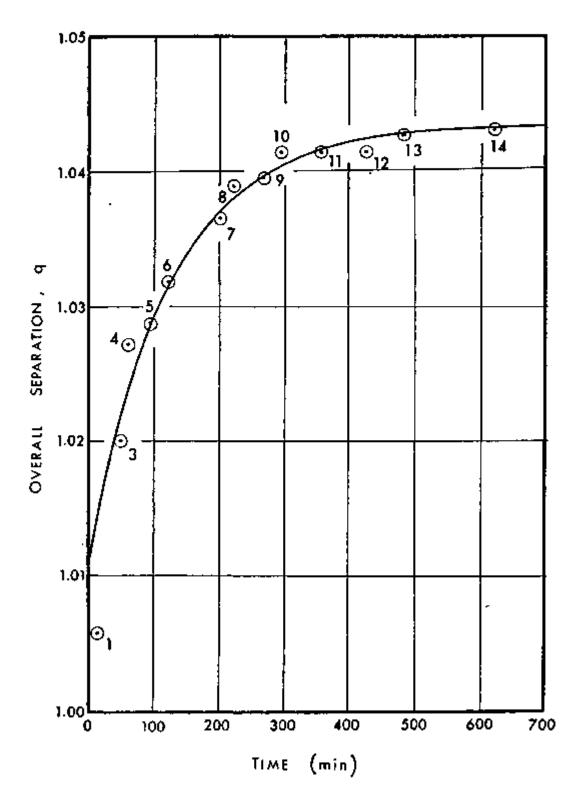
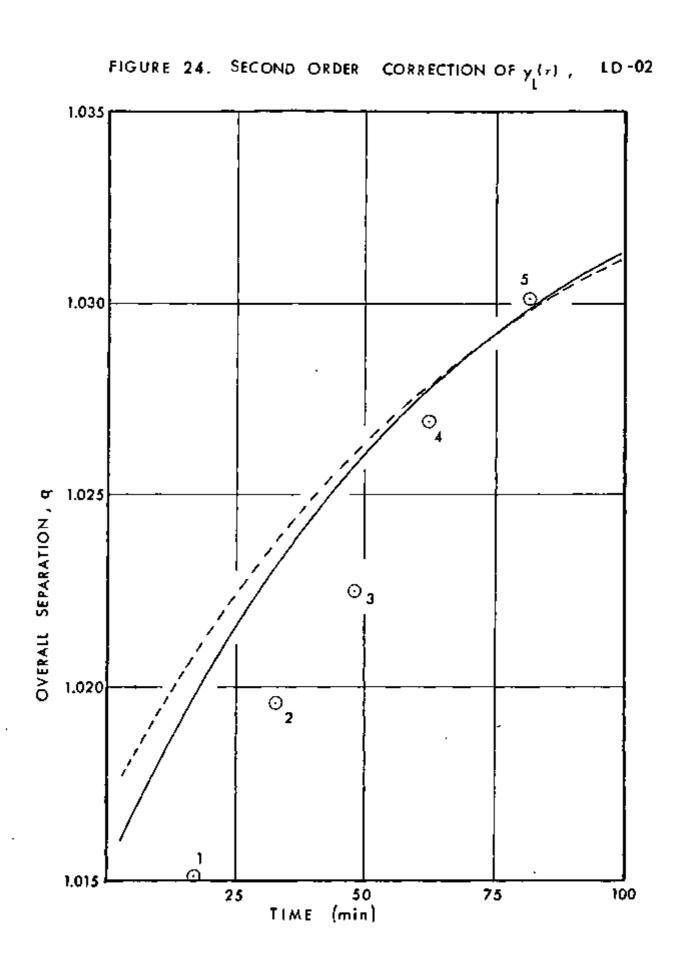


FIGURE 23. SEPARATION AS A FUNCTION OF TIME, RUN LD-12



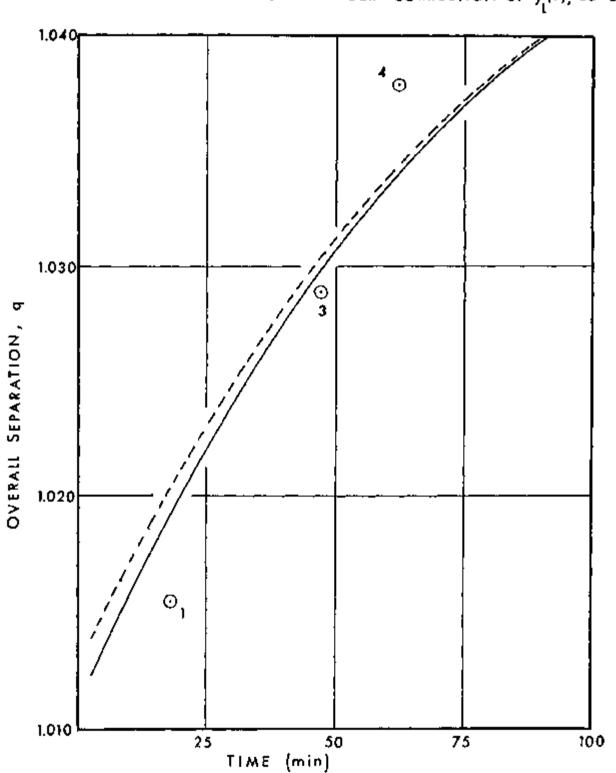
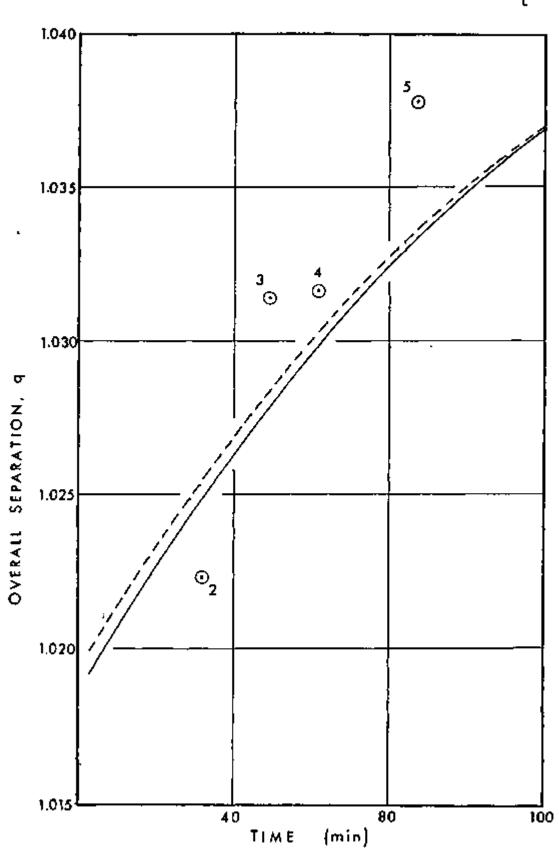


FIGURE 25. SECOND ORDER CORRECTION OF Y (+), 10-03





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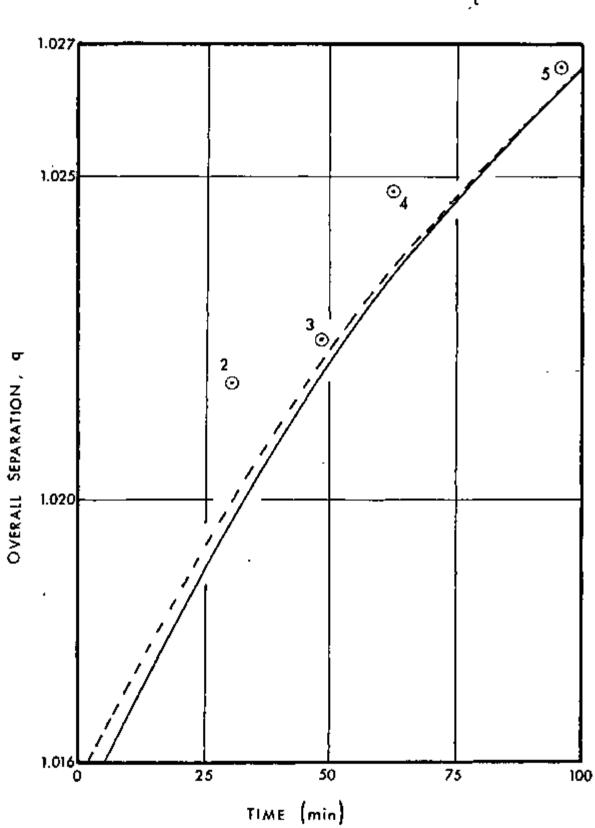


FIGURE 27. SECOND ORDER CORRECTION OF $y_{L}(r)$, LD-10

The results on \in summarized in Table XIV(D) were least-squares fit to two functional forms:

$$\ell n \left(\frac{P^*}{P} \right) = \frac{A}{T^2} - \frac{B}{T}$$
(11)

$$\ln\left(\frac{\mathbf{P}'}{\mathbf{P}}\right) = \frac{\mathbf{A}'}{\mathbf{T}} - \mathbf{B}' \tag{29}$$

where P' and P are the vapor pressures of the 12 CHF₃ and 13 CHF₃ molecules respectively, so that

$$ln\left(\frac{P^{*}}{P}\right) \approx ln \alpha = ln (1 + \epsilon) \approx \epsilon$$
 (30)

Equation 11 is Bigeleisen's first-order approximation⁽¹⁰⁾ for the relative vapor pressures of the isotopic molecules under the assumptions of the Born-Oppenheimer approximation, harmonic potentials, and the liquid cell model. According to this theory, A represents the isotopic difference in the first quantum correction for the loose external oscillations of liquid molecules, and B represents the isotope effect in the shift of the Zero-point energy upon condensation. Both A and B are positive according to this approximation.⁽³⁸⁾

For 13 CHF₃/ 12 CHF₃, it has been found that

$$A = 217 \pm 66$$

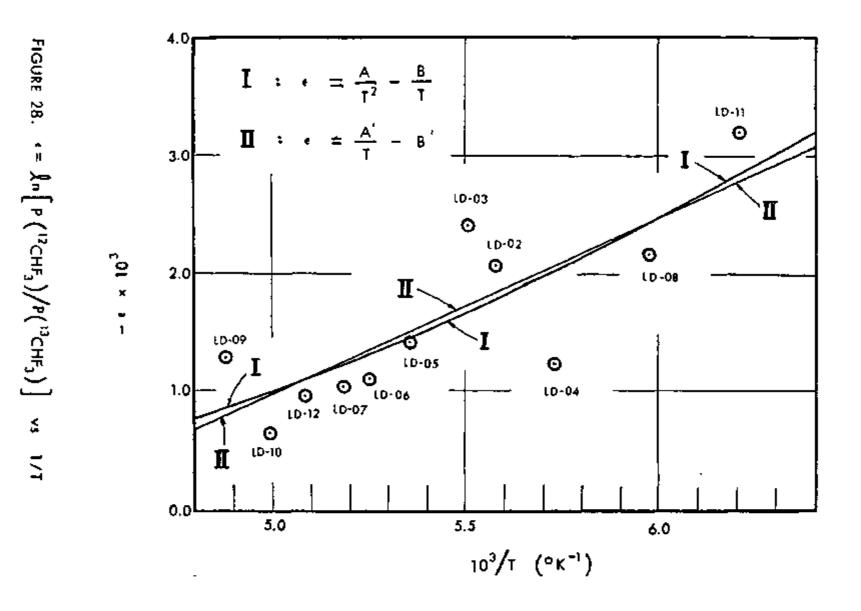
B = 0.89 \pm 0.36 (31a,b)

and

$$\begin{array}{l} A' = 1.49 \pm 0.38 \\ B' = (6.49 \pm 2.06) \times 10^{-3} \end{array}$$
 (32a,b)

The errors guoted in Equations 31 and 32 are the root-meansquares deviation of the experimental points around the least- squares fit curve. Figure 28 depicts the comparison

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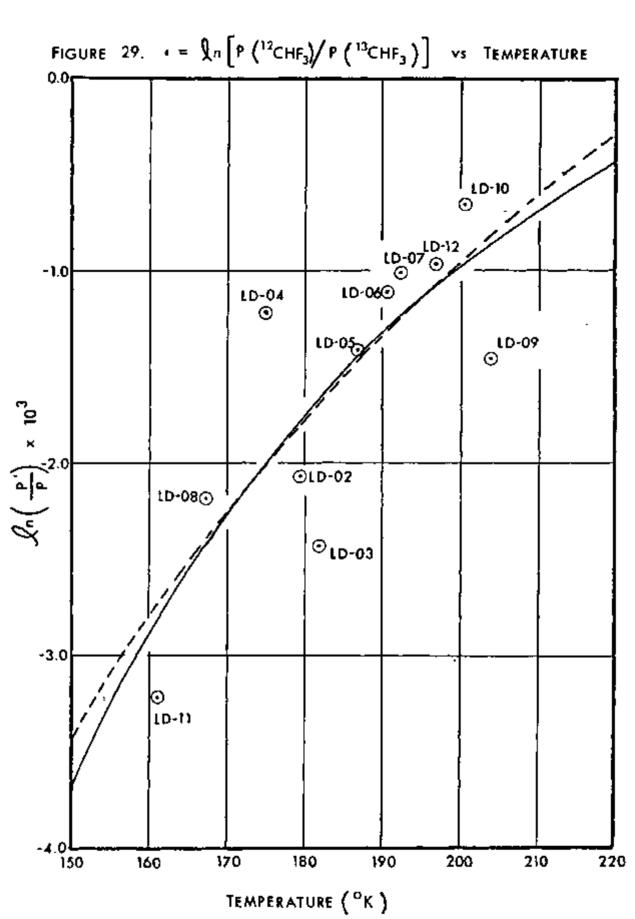
of these least-squares fits obtainable by the two functional forms, Equation 11 (curve I) and Equation 29 (curve II) as a function of 1/T, and Figure 29 represents Equation 11 (solid line) and Equation 29 (dashed line) plotted as a function of T. Aside from the physical meaning that may be attached to the constants A and B, Equation 11 is able to account for the existence of curvature in the plot of ln (P'/P) vs 1/T, Figure 28.

The ratio of A to A' is 145, while the ratio of B to B' is 137. Therefore, the functional form of Equation 29 can be thought of as a variation of Equation 11 in which A/T_{av} is set equal to a constant A' and B/T_{av} is set equal to B'. However, there is little difference between the line given by Equations 11 and 31 and the one represented by Equations 29 and 32, as seen in Figure 28.

Bigeleisen, Cragg, and Jeevanandam⁽¹²⁾ reported that, for the ¹³C/¹²C sffect in liquid methane, A = 93.8 \pm 6.1 and B = 0.535 \pm 0.06, according to Equation 11. The value of A = 217 \pm 66 for ¹³CHF₃/¹²CHF₃ is considerably greater than A = 93.8 \pm 6.1 for ¹³CH₄/¹²CH₄. This must be due to the larger intermolecular forces in the polar CHF₃ liquid.

In order to further investigate the intermolecular forces in the liquid CHF_3 , a cell-model calculation has been performed to reproduce the observed vapor pressure isotope effect in ${}^{13}CHF_3/{}^{12}CHF_3$ within the framework of the Bigeleisen-Stern-Van Hook-Wolfsberg theory. The result is presented in the next section, Section IV-2.

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IV-2. Cell Model Calculations

The utility of the cell model lies in the fact that, under the harmonic force field assumptions, all degrees of freedom of a liquid molecule can be treated by the standard method of normal coordinate analysis. Wilson's \mathcal{E} G matrix method⁽²⁹⁾ provides a mathematical procedure necessary for such molecular vibration problems. In this section, this \mathcal{F} G matrix method and its application to high speed computer programming originally developed by Schachtschneider and Snyder⁽³¹⁾ will first be described. The application of the method to the present problem of gaseous and liquid trifluoromethane for the purpose of fitting the \mathcal{E} matrices to observed vapor pressure isotope effect as well as the internal frequencies will be presented in the latter subsections.

A) Wilson's £ & Matrix Method

Wilson's \underline{F} <u>G</u> matrix method is based on classical mechanics. If $(q_1, q_2, ..., q_f)$ is a complete set of f coordinates, where f is the degree of freedom of a molecular system (f may be 3N, 3N-5, or 3N-6), the potential energy V can be expressed in the form of an f-dimensional Taylor expansion:

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$$V = V_{o} + \sum_{i=1}^{f} \left(\frac{\partial V}{\partial q_{i}}\right)_{c} q_{i} + \frac{1}{2} \sum_{i=1}^{f} \sum_{j=1}^{f} \left(\frac{\partial^{2} V}{\partial q_{i} \partial q_{j}}\right)_{o} q_{i} q_{j}$$

+ (higher terms), (33)

where the subscript "o" refers to the value of the appropriate function at the origin. In isotope effect studies, the origin is chosen to be at the minimum of the potential function. Then, $V_0 = 0$ and $\left(\frac{\partial V}{\partial q_1}\right)_0 = 0$ for all i. In the harmonic approximation, the "(higher terms)" of Equation 33 vanish. Thus

$$2V = \sum_{i=1}^{f} \sum_{j=1}^{f} \left(\frac{\partial^2 V}{\partial q_i \partial q_j} \right)_0 q_i q_j$$
(34)

or

$$2V = \sum_{i=1}^{f} \sum_{j=1}^{f} f_{i,j} q_{i} q_{j}$$
(35)

where

$$f_{ij} \equiv \left(\frac{\partial^2 v}{\partial q_i \partial q_j}\right)_0 \qquad (36)$$

The kinetic energy T in cartesian coordinates is

$$2T = \sum_{i=1}^{3N} m_i q_i c^2$$
 (37)

where m_i is the atomic mass associated with the i-th cartesian coordinate $q_i^{\ C}$. If the coordinate transformation between this coordinate and a system of internal coordinates q_i is given by

$$q_{i}^{C} = \sum_{j=1}^{a} a_{ij}q_{j},$$
 (38)

then the expression for the kinetic energy in the new coordinate system will become

$$2T = \sum_{i=1}^{3N} m_i \left(\sum_{j=1}^{n_i j} a_{ij} \dot{q}_{j} \right)^2$$
$$= \sum_{i=1}^{3N} \sum_{j=1}^{N} \sum_{k=1}^{m_i j} m_i a_{ij} a_{ik} \dot{q}_j \dot{q}_k$$
$$= \sum_{i=1}^{N} \sum_{k=1}^{N} \left(\sum_{i=1}^{m_i j} a_{ij} a_{ik} \right) \dot{q}_j \dot{q}_k$$
$$= \sum_{i=1}^{N} \sum_{k=1}^{N} g_{jk} a_{ij} \dot{q}_k,$$

 \mathbf{or}

$$2T \approx \sum_{i=1}^{f} \sum_{j=1}^{f} g_{ij}^{-1} \dot{q}_{i} \dot{q}_{j}$$
, (39)

where

$$g_{ij}^{-1} = \sum_{i=1}^{3N} m_i a_{ij} a_{ik}$$
, (40)
and g_{ij}^{-1} is the (ij) element of Wilson's kinetic energy

matrix, g^{-1} .

Application of the Lagrangian equation of motion,

$$\frac{d}{dt} \left(\frac{\partial T}{\partial \dot{q}_i} \right) + \left(\frac{\partial V}{\partial q_i} \right) = 0 , \qquad (41)$$

to the present problem leads to

$$\sum_{i=1}^{f} g_{ij}^{-1} \ddot{q}_{j} + \sum_{i=1}^{f} f_{ij} q_{j} = 0 .$$
(42)

Since of interest is a set of solutions of q_i of Equation 42 in a particular form in which every part of the molecule oscillates in unison, the following is substituted:

$$q_j = A_j \sin 2\pi r t, [j = 1, 2, ..., f]$$
 (43)

into Equation 42, which then becomes

$$\sum_{j=i}^{l} (f_{ij} - \lambda g_{ij}^{-1}) A_{j} = 0 \quad [i = 1, 2, ..., f] (44)$$

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where

$$\lambda = 4\pi^2 r^2 = 4\pi^2 c^2 \omega^2$$
 (45)

The non-trivial solution of the simultaneous linear Equations 44 exist if and only if the following secular equation is satisfied:

$$\left| \mathbf{E} - \lambda \mathbf{G}^{-1} \right| = 0 , \qquad (46)$$

where

$$\mathbf{E} \equiv \begin{bmatrix} \mathbf{f}_{11} & \mathbf{f}_{12} & \cdots & \mathbf{f}_{1\mathbf{f}} \\ \mathbf{f}_{21} & \mathbf{f}_{22} & \cdots & \mathbf{f}_{2\mathbf{f}} \\ \vdots & \vdots & \ddots & \vdots & \vdots \\ \vdots & \vdots & \ddots & \vdots & \vdots \\ \vdots & \vdots & \vdots & \vdots & \vdots \\ \mathbf{f}_{f1} & \mathbf{f}_{f2} & \vdots & \vdots & \mathbf{f}_{ff} \end{bmatrix}$$
(47)

and

$$\mathbf{g}^{-1} \equiv \begin{pmatrix} g_{11}^{-1} & g_{12}^{-1} & \cdots & g_{1f}^{-1} \\ g_{21}^{-1} & g_{22}^{-1} & \cdots & g_{2f}^{-1} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ \vdots & \vdots & \vdots & \vdots & \vdots \\ g_{f1}^{-1} & g_{f2}^{-1} & \vdots & \vdots & g_{ff}^{-1} \\ \end{pmatrix}$$
(48)

The force constant matrix E can be defined for a gas molecule with f = 3N-6 or 3N-5 and for a liquid molecule with f = 3N. The present purpose is to find such E matrices which best reproduce the observed vapor pressure isotope effect as well as the spectroscopically observed internal

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frequencies. The kinetic energy matrix \underline{G}^{-1} is fixed as soon as the molecular geometry and the atomic masses are known. The secular Equation 46 can be alternately solved by solving either

$$E = 0, \qquad (49)$$

or

$$\left| \begin{array}{ccc} \underline{G} \ \underline{F} \ - \ \lambda \underline{I} \end{array} \right| = 0 \ . \tag{50}$$

B) The Schachtschneider and Snyder Program

The Schachtschneider and Snyder program consists of two parts. The first part calculates the <u>G</u> matrix for every isotopic molecule, given the molecular geometry and the atomic masses. The second part solves the secular equation after reading in the <u>G</u> matrix calculated in the first part, as well as an <u>F</u> matrix. The Ishida-Bigeleisen modification of the second part also calculates the vapor pressure isotope effects and several contributions to it at various temperatures.⁽³²⁾ All calculations were performed through the use of an IBM 370/168 computer at the City University of New York/University Computer Center. Communication with the CUNY/UCC was effected through the use of CRT terminals, and the printouts were produced at the Brooklyn College School of Science Data Acquisition Facility.

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C) F Matrix for Gaseous Trifluoromethane

Previously published results on the observed and calculated frequencies for gaseous trifluoromethane are outlined in Table XVII. For the present study, the F matrix of Long, Gravenor, and Jones⁽³³⁾ was chosen as the basis of the normal coordinate analysis for the gaseous molecule. Tables XVIII, XIX, and XX summarize the definition of the internal coordinates, the definition of the symmetry coordinates, and the gaseous E matrix obtained by Long et al respectively. Figure 30 schematically represents the definition of the internal coordinates. In this figure, atom 4 is in the yz-plane. The frequencies calculated in the present study by using these coordinate definitions and this F matrix along with the international mass scale based on 12 C (i.e., C = 12.000000 amu, H = 1.007825 amu, D = 2.014000 amu, F = 18.998400 amu, and ${}^{13}C = 13.003335$ amu) are tabulated in Table XXI. There is a noticeable disagreement between the frequencies calculated in this study and those of Long et al. A modification of the F matrix of Long et al was performed by first calculating the differential effects on frequencies of each symmetry F matrix element. These effects, $\partial_{\mathbf{k}}/\partial F_{ij}$, are summarized in Table XXII. The final F matrix and the corresponding gaseous frequencies are tabulated in Tables XXIII and XXIV respectively. Table XXIV shows a significant improvement in the agreement between the calculated and observed gaseous frequencies.

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Molecule	Frequency number	Long <u>obs.</u>	(33) <u>calc.</u>	Gala. <u>obş.</u>	550 (34) <u>calç.</u>	D'Cu obs.	nha (35) <u>calc.</u>
CHF ₃	ຶ່າ	3035	3036 [′]	3031	3030.5	3031	3034.4
	~ 2	1137	1138	1140	1146.4	1140	1141.3
	" 3	700	702	700	700.8	700	700.7
	" 4	1376	1379	1372	1379.3	1372	1375.5
	"5	1152	1156	11 52	1158.3	1152	1155.2
	°6	50 8	508	507	505.4	507	508.4
CDF3	۲.	2257	2256	2273	2274.0	2257	2254.5
	ັ2	1110	1110	1109	1103.0	1109	1107.7
	" 3	693	691	693	691.7	693	692.3
	^w 4	1210	1207	1207	1200.1	1207	1203.2
	* 5	977	971	974	968.8	974	971.8
:	" 6	502	502	504	505.4	504	502.6

1

		_1				
<u>TABLE XVII, Gaseous</u>	<u>Freqencies</u>	(in cm ⁻¹)	Observed	and Calculated	for	Trifluoromethane

.

<u>Coordinate number</u>	Definition
1	C-H stretch
2	C-F stretch
3	C-F stretch
4	C-F stretch
5	H-C-F bend (b)
б	H-C-F bend ^(b)
7	H-C-F bend ^(b)
8	F-C-F bend ^(b)
9	F-C-F bend ^(b)

Atom	<u>X Coordinate</u>	<u>Y Coordinate</u>	<u>Z_Coordinate</u>
с	0.00000	0.00000	0.000000
н	0.000000	0.00000	1.098000
F ₂	1.083050	0.625299	-0.458505
F ₃	-1.083050	0.625299	-0.458505
F4	0.000000	-1,250599	-0.458505

F-C-F bend^(b)

- (a) Refer to Figure 30 for the schematic diagram of internal coordinates.
- (b) Weighted by the C-F bond length, 1.322 \AA .

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TABLE XVIII. Definition of Internal Coordinates (a)

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TABLE XIX. Definition of Symmetry Coordinates (a)

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$$S_{1} = D$$

$$S_{2} = \frac{1}{\sqrt{3}} \cdot (d_{2} + d_{3} + d_{4})$$

$$S_{3} = \frac{1}{\sqrt{6}} \cdot (\beta_{23} + \beta_{34} + \beta_{24} - a_{12} - a_{13} - a_{14})$$

$$S_{4} = \frac{1}{\sqrt{6}} \cdot (2d_{2} - d_{3} - d_{4})$$

$$S_{5} = \frac{1}{\sqrt{6}} \cdot (2a_{12} - a_{13} - a_{14})$$

$$S_{6} = \frac{1}{\sqrt{6}} \cdot (2\beta_{34} - \beta_{23} - \beta_{24})$$

$$S_{7} = \frac{1}{\sqrt{2}} \cdot (d_{3} - d_{4})$$

$$S_{8} = \frac{1}{\sqrt{2}} \cdot (a_{13} - a_{14})$$

$$S_{9} = \frac{1}{\sqrt{2}} \cdot (\beta_{24} - \beta_{23})$$

(a) Refer to Figure 30 for schematic diagram of internal coordinates.

<u>Coordinate</u>	<u>F Matrix Element (mdyne/A)</u>
F ₁₁	5.00
F ₁₂	2.03
F ₁₃	0.41
^F 22	7.70
F ₂₃	0.44
F ₃₃	1.14
F ₄₄	5.29
F ₄₅	0.43
F ₄₆	-0.43
^F 55	0.46
F56	-0.09
F ₆₆	0.82

TABLE XX. F Matrix for Gaseous Trifluoromethane by Long (33)

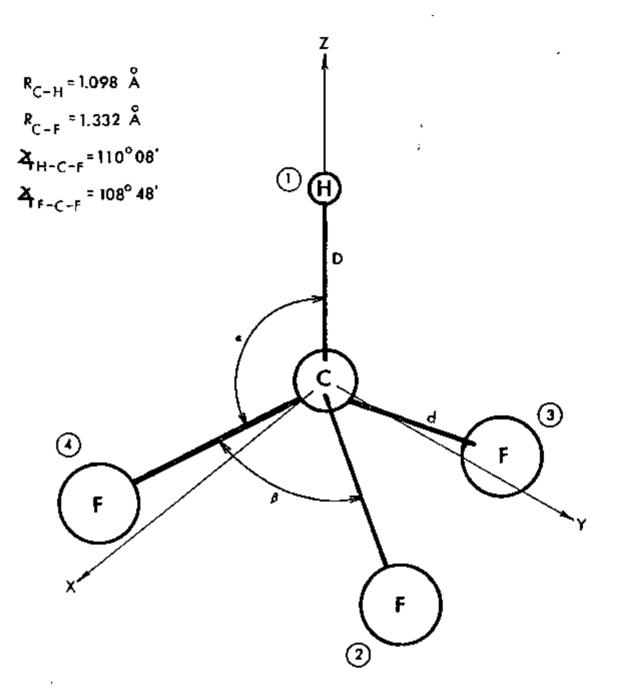


FIGURE 30. INTERNAL COORDINATES FOR TRIFLUOROMETHANE

.

TABLE XXI. Calculated Frequencies f	From F Matrix of Long (33)
-------------------------------------	----------------------------

Frequency number	<pre>Frequency(cm⁻¹)</pre>
" 1	3036.4
2	1154.7
" 3	702.1
" 4	1390.3
" 5	1150.9
[~] 6	503.1
"1	2257.1
[∞] 2	1124.8
" 3	690.8
°4	1207.4
^{°°} 5	974 . 9
" 6	497.7
	"1 "2 "3 "4 "5 "6 "1 "2 "3 "4 "4 "5

					-	ð″ <u>k</u> ðF _{i í}	(cm ⁻¹	•mdyn ⁻¹	L.A.)				
Molecule	Frequency <u>number</u>	<u>F</u> <u>11</u>	F ₁₂	F <u>13</u>	F <u>22</u>	F_23	F ₃₃	F ₄₄	F45	F ₄₆	F ₅₅	F ₅₆	F66
CHF3	۳ı	298	-19	122	0	-4	12	0	0	0	0	0	0
	~ 2	0	-5	12	45	-233	294	0	0	0	0	Q	0
	"3	11	-33	-78	24	115	135	0	0	0	0	0	0
	۳4	o	0	0	0	0	0	12	-268	37	1524	-403	28
	"5	0	0	0	0	0	0	104	63	208	11	64	105
	6″	0	0	0	٥	0	0	3	÷22	~59	37	194	266
CDF3	" 1	214	- 30	180	1	-13	38	0	0	0	0	0	0
	·ª2	1	7	-15	47	-221	257	0	0	0	0	0	0
	۳з	14	-33	-87	22	112	145	0	. 0	0	0	0	0
	" 4	0	٥	0	0	0	0	100	-418	230	448	-479	139
	"5	0	0	0	0	0	0	17	211	11	678	73	2
	[∞] 6	0	0	0	0	0	0	3	-26	-56	55	236	263

TABLE XXII. Differential Effects of Symmetry Coordinate F Matrix Elements

Simmotre	y Coordinates	Tat or	nal Coordinates
Coord.	F Matrix Element (mdyne/A)		F Matrix Element (mdyne/A)
F ₁₁	5.000000	۲ _D	5.000000
F ₁₂	2.030000	fd	6.017878
P 13	0.410000	f _{dD}	1.172021
F22	7.517634	fdd	0.749878
F23	0.476755	f _{Da}	-0.167382
ғ ₃₃	1.140000	f _{D<i>B</i>}	0.167382
F ₄₄	5.268000	fa	0.491320
ŕ ₄₅	0.460000	faa	0.039340
F46	-0.430983	fø	0.764617
F ₅₅	0.455380	f _{øø}	-0.097309
F ₅₆	-0.115000	f _{da} (b)	0.194294
F66	0.861926	f_{da} , (c)	-0.265706
		$f_{d\beta}$	0.256033
		$f_{d\beta}$	-0.180848
		$f_{\alpha\beta}^{(d)}$	-0.151667
		f _{aß} .(e)	-0.266667

TABLE XXIII. F Matrix of Gaseous Trifluoromethane in

Symmetry and Internal Coordinates

(a) Refer to Figure 30

(b) Non-prime refers to the bond length adjacent to bond angle(c) Prime refers to the bond length opposite to the bond angle(d) Non-prime refers to the bond angle adjacent to bond angle(e) Prime refers to the bond angle opposite to bond angle

<u>Molecule</u>	Frequency number	<pre>Frequency(cm⁻¹)</pre>
CHF ₃	ωı	3036.2
	<mark>2</mark>	1138.9
	۳3	701.4
	^ب 4	1381.0
	~ 5	1151.8
	" 6	507.7
CDF3	" 1	2256.5
	°2	1109.2
	" 3	690.4
	" 4	1205.4
	" 5	973.7
	" 6	500.7

TABLE XXIV, Final Calculated Gaseous Frequencies

D) F Matrix for Liquid Trifluoromethane

As mentioned previously, the external vibrations of a liquid molecule are treated by the cell model as weak harmonic oscillations. They consist of three translational and three rotational motions. The Schachtschneider and Snyder <u>G</u> matrix program, after calculations of the internal G matrix, computes the center of mass and the three principal axes of the molecule. Furthermore, it calculates the <u>G</u> matrix elements involving the external motions and the g_{ij} 's representing the interactions between the external and internal motions. Based on the experimental data on the interatomic distances and the atomic bond angles, as shown in Figure 30, the principal moments of inertia, in the units of mdyne per Angstrom per atom mass unit, for ${}^{12}_{\text{CHF}_3}$ are

 $I_{a} = 89.140306$

and

 $I_{\rm B} = I_{\rm C} = 48.820360$

The fundamental frequencies of liquid trifluoromethane have been observed, as summarized in Table XXV, but there has been no published liquid <u>F</u> matrix.

Towards the determination of the liquid F matrix, the gaseous F matrix was first modified to roughly reproduce the observed liquid frequencies. After a series of calculations of the effects of the diagonal elements for the translational and rotational motions, several sets of

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Frequency number	Glockler (36) Frequency(cm ⁻¹)	Rank (37) Frequency(cm ⁻¹)
μ	3062	3062
<mark>2</mark>	1117	1117
ω ₃	697	697
^ω 4	1376	1376
ω ₅		1160
6	50 8	508

TABLE XXV.	Liquid	Frequencies	Observed	for	<u>Trifluoromethane</u>

these diagonal external force constants, f_{tr} and f_{rot} , were chosen, and the effects of the various internalexternal interaction force constants for each set of f_{tr} and f_{rot} selected were studied. This determined the set of external diagonals and internal-external interaction elements of the liquid <u>F</u> matrix that best reproduced the vapor pressure isotope effect observed in the experimental part of the present study. A final adjustment to the internal part, E_{ii} , was then made to finally adjust the liquid internal frequencies to the observed frequencies.

As a first step, the gaseous \underline{F} matrix was modified to roughly reproduce the observed liquid frequencies tabulated in Table XXV. For this purpose, certain values for the diagonal elements for the translational and rotational motions had to be chosen, but the effects of any reasonable changes in these external force constants on the internal frequencies were found to be negligible. The tentative \underline{F}_{ii} matrix obtained by using $f_{tr} = 0.300000$ mdyn/Å and $f_{rot} = 0.050000$ mdyn-Å is tabulated in Table XXVI. This is the \underline{F}_{ii} used in the subsequent \underline{F}_{liq} adjustment procedures, until the last step mentioned in above outline.

The next step was a study of the effects of f_{tr} and f_{rot} on the ${}^{13}C/{}^{12}C$ isotope effect in trifluoromethane. During this stage of the study, that part of of the E_{1iq}

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	for Trifluoromethane
<u>Coordinate(a)</u>	<u>f</u> Matrix Element (mdyn/Å)
f _D	4.820698
fd	6.247256
f dD	0.900410
f _{dd}	0.498351
f Da	-0,310438
f _{Dβ}	0.310438
fα	0.489509
f _{aa}	0.041347
f _β	0.765351
f _{ßß}	-0.096575
f _{da} (b)	0.194294
$f_{d\alpha}$ (c)	-0.265706
f _d β ^(b)	0.256033
f _{dβ} ,(c)	-0.180848
$f_{\alpha\beta}^{(d)}$	-0.125241
f _{αβ} , (e)	-0.240241

TABLE XXVI. Internal Part of the Tentative Liquid F Matrix

(a) Refer to Figure 30

(b) Non-prime refers to the bond length adjacent to bond angle(c) Prime refers to the bond length opposite to bond angle(d) Non-prime refers to the bond angle adjacent to bond angle(e) Prime refers to the bond angle opposite to bond angle

matrix representing the internal-external interaction, ${f E}_{ic}$, was set to be a null matrix. The diagonal translational element was varied between 0.01000 and 3.000000 mdyn/R, and the three equal rotational elements were varied between 0.001000 and 3.000000 mdyn- $\frac{9}{4}$, representing unrealistically high and low values for external forces. Table XXVII summarizes the results of these studies. Table XXVII shows the magnitude and slope of ln (P'/P) based on these F_{lig} matrices and the F_{gas} matrix of Table XXIII. It is obvious that the \mathcal{E}_{lig} matrix in the absence of force constant elements representing interactions between internal and external motions cannot predict the observed inverse vapor pressure isotope effect and the observed positive slope of the plot of *in* (P'/P) versus temperature. As will become obvious in the latterpart of this subsection when possible effects of some significant changes in $\mathbf{F}_{i,i}$ will be discussed, this conclusion on the importance of f_{ie} remains unalterable.

In the next series of studies, the internal-external interaction force constants were included. A symmetry consideration indicated that the translational motion in the direction of the C-H axis, T_z , interacts significantly with the C-H stretch, C-F stretches, H-C-F bends, and F-C-F bends. Accordingly, the differential effects of variations in the \underline{F} matrix elements representing these internal-external interactions on ln (P'/P) were calculated. The results obtained, using $f_{tr} \approx 0.300000$ mdyn/ $\overset{0}{A}$ and

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<u>in Trifluoromethane</u>							
F	e	£	n (P'/P) ^(a)				
f _{tr} (mdyn/A)	frot (mdyn-A)	@ T ₁	<u>. @ т</u> 2	Δ			
0.01	0.001	0.011807	0.009386	-0.002421			
0.01	0.01	0.011812	0.009389	-0.002423			
0.01	0.1	0.011864	0.009421	-0.002443			
0.01	1.0	0.012360	0.009733	-0.002627			
0.01	3.0	0.013340	0.010374	-0.002966			
0.1	0.001	0.012103	0.009569	-0.002534			
0.1	0.01	0.012108	0.009572	-0.002536			
0.1	0.1	0.012160	0.009604	-0.002556			
0.1	1.0	0.012657	0.009916	-0.002741			
0.1	3.0	0.013637	0,010557	-0,003080			
1.0	0.001	0.014979	0.011365	-0.003614			
1.0	0.01	0.014984	0.011369	-0.003615			
1.0	0.1	0.015036	0.011401	-0.003635			
1.0	1.0	0.015533	0.011712	-0.003823			
1.0	3.0	0.016514	0.012354	-0.004160			
3.0	0.001	0.020851	0.015146	-0.005705			
3.0 '	0.01	0.020856	0.015150	-0.005706			
3.0	0.1	0.020908	0.015181	-0.005717			
3.0	1.0	0.021405	0.015493	-0.006012			
3.0	3.0	0.022386	0.016135	-0.006251			

TABLE XXVII. Effects of the Translational and Rotational Force Constants on the 13 C/12 C Vapor Pressure Isotope Effect

(a) $T_1 = 161.1^\circ$ K and $T_2 = 204.6^\circ$ K, corresponding to the lowest and highest temperatures respectively at which the distillation study was performed. Δ is the difference of in (P'/P) minus in (P'/P) T.

 $f_{rot} = 0.100000 \text{ mdyn-} \text{Å}$, are tabulated in Table XXVIII. Ohter choices of F_{tr} and f_{rot} yielded almost identical differential effects as those summarized in Table XXVIII, although the general magnitude of ln (P'/P), in the absence of \mathcal{F}_{ie} , was strongly dependent on the choice of these external diagonal elements. In all cases, an increase in the slope of the plot of ln (P'/P) versus temperature is accompanied by a shift toward a larger inverse vapor pressure isotope effect. Using these differential parameters, The following, which best fit the experimantal vapor pressure isotope effect data, were obtained:

> $f(T_{z}, C-H) = -0.840000 \text{ mdyn/}^{A}$ $f(T_{z}, C-F) = 0.840000 \text{ mdyn/}^{A}$ $f(T_{z}, H-C-F) = 0.300000 \text{ mdyn/}^{A}$ $F(T_{z}, F-C-F) = -0.300000 \text{ mdyn/}^{A}$

The introduction of these non-vanishing internalexternal interaction force constants, however, shifted the internal frequencies to a slight degree. Therefore, a slight modification in the \underline{F}_{11} was necessitated. The final \underline{F} matrix thus obtained is presented in Table XXIX. The liquid internal frequencies that the \underline{F}_{11q} matrix predicts are tabulated in Table XXX. These frequencies should be compared with the experimental values listed in Table XXV. In Figure 31, the vapor pressure isotope effect calculated (solid line) by using this \underline{F}_{11q} matrix and the \underline{F}_{qas} matrix of Table XXIII in conjunction with the exact

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	In	volving T _z	: f _{tr} = 0	.3 mdyn/8,	$f_{rot} = 0.$	1 mdyn-A(a)		
<u>Eie</u> Elements (d)				ℓn (P'/P)				
f(T ₂ ,CH)	$f(T_z, CF)$	$f(T_z, HCF)$	$f(T_z, FCF)$	@ T ₁ (b) _{@ T2} (b)		(c)	Δ ₂ (c)
0	0	0	0	0.012813	0.010009	-0.002804		
0.01	0	0	0	0.012824	0.010018	-0.002806	0.000011	0.000009
0	0.01	o	0	0.012760	0.009969	~0.002791	-0.000053	-0.000040
0	0	0.01	0	0.012640	0.009883	-0.002757	-0.000173	-0.000126
0	0	0	0.01	0.012991	0.010137	-0.002854	0.000178	0.000128

TABLE XXVIII. Differential Effects of Internal-External Interaction Force Constants

(a) For \underline{F}_{ij} , see Table XXVI

(b) T₁ = 161.1° K and T₂ = 204.6° K, corresponding to the lowest and highest temperatures respectively at which the distillation study was performed. A is the difference of ln (P'/P)_{T2} minus ln (P'/P)_{T1}.
(c) Δ₁ = [ln (P'/P)_{T1} with f_{ie} = 0.01] - [ln (P'/P)_{T1} with f_{ie} = 0] Δ₂ = [ln (P'/P)_{T2} with f_{ie} = 0.01] - [ln (P'/P)_{T2} with f_{ie} = 0]
(d) In units of mdyn/Å.

Force Constants		<u>Elements</u> (a)
	<u> </u>	<u>Liquid</u>
Internal		
Diagonal		
C-H stretch	5,000000	4,814698
C-F stretch	6.017878	6.206256
H-C-F bend	0.491320	0.489509
F-C-F bend	0.764617	0.765351
Interaction		
C-H str x C-F str	1.172021	0.859410
C-F str x C-F str	0.749878	0.474351
C-H str x H-C-F bend	-0.167382	-0.310438
C-H str x F-C-F bend	0.167382	0.310438
C-F str x adj H-C-F bend	0.194294	0.194294
C-F str x opp H-C-F bend	-0.265706	-0.265706
C-F str x adj F-C-F bend	0.256033	0.256033
C-F str x opp F-C-F bend	-0.180848	-0.180848
H-C-F bend x $H-C-F$ bend	0.039340	0.041347
F-C-F bend x F-C-F bend	-0.097309	-0.096575
H-C-F bend x adj F-C-F bend	-0.151667	-0.125241
H-C-F bend x opp F-C-F bend	-0.266667	-0.240241
External		
Diagonal		
Translation	₩ ₩₩₩₩₩₩ ₩₩₩₩₩₩₩₩₩₩₩₩₩₩₩₩₩₩₩₩₩₩₩₩₩₩₩₩₩	0.300000
Rotation		0.100000 ^(b)
Internal-External Interaction		
C-H str x T_{z}		-0.840000
C-F str x T		0.840000
H-C-F bend x T		0.300000
F-C-F bend x T		-0.300000

TABLE XXIX. Liquid and Gaseous E Matrix for Trifluoromethane

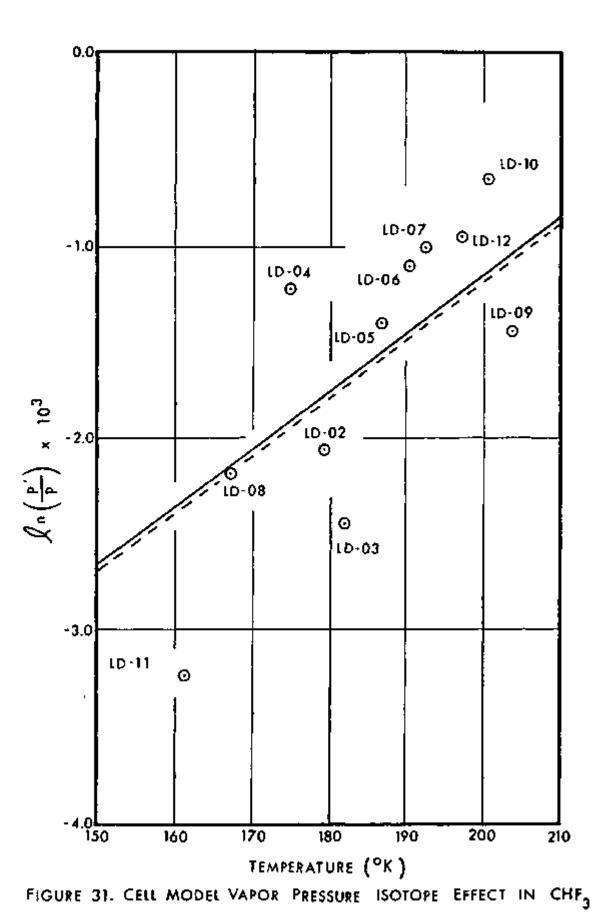
(a) Unless otherwise noted, in units of mdyn/A.

(b) In units of mdyn-A.

Frequency number	¹² CHF ₃ Frequency (cm ⁻¹)	¹³ CHF ₃ Frequency (cm ⁻¹)
" 1	3062.4	3046.3
" 2	1116.7	1097.0
" 3	697.0	692.9
° 4	1376.1	1366.6
5	1159.9	1133.6
° 6	507.8	506.8
"tr	125.8	124.4
"tr	85.3	84.7
"tr	85.3	84.7
"rot	59.0	58.9
۳rot	59.0	58.9
"rot	43.6	43.6

TABLE XXX. Liquid Frequencies Calculated from E Matrix of Table XXIX

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Bigeleisen formulae, Equations 3 and 5 is compared with the experimental values of ln (P'/P). According to Equations 12 and 13, the l_{1ig} matrix of Table XXIX yields the following values of A and B, the coefficients appearing in Bigeleisen's two term approximation for ln (P'/P), Equation 11: A = 19.25, B = 1.31. Agreement btween these calculated values fo A and B and those obtained by the least-squares fit of the experimental vapor pressure data to the two term equation is apparently poor. This point will be discussed again at the end of this subsection. The effect of a 10% decrease in l_{tr} has also been plotted (dashed line) in Figure 31. A 10% change in l_{rot} is too insignificant to appear in the plot at that same scale.

Differential effects of other force constant elements in \underline{F}_{ie} are similar to those interactions involving the \underline{T}_z coordinate. Some examples in support of this observation are presented in Tables XXXI, XXXII, and XXXIII. The final \underline{F}_{liq} matrix was chosen not to include these other internal-external interaction force constant elements. The interactions between any two external motions, i.e., translation-translation, rotation-rotation, or translationrotation, have been found to have differential effect values an order of magnitude smaller than those of the internalexternal interactions. Therefore, the external-external interactions have not been included in the final result.

It is noted in Table XXIX for the final \mathcal{F}_{lig} , that

Involving T_x , R_x and R_y : f_{tr}	$= 0.3, f_{\underline{r}}$	ot = 0.1	·)		_
Elements ^(b,c)			n (P'/P)		
~	@ T ₁ (d)	@т ₂ ^(d)	۵ ^(d)	∆ ₁ (e)	∆2 ^(e)
$f_{13,5} = 0.1; f_{13,6} = 0.1; f_{13,7} = 0.2$	0.012040	0.009431	-0.002804	-0,000773	-0.000578

TABLE XXXI.	Differential	Effects of	f Internal-External	Interaction	Force Constants
111000 1001					. dice conquig

13,5 - 0.1, 13,6 - 0.1, 13,7 - 0.2	0.012040	0.009431	-0.002004	-0.000773	-0.000110
$f_{13,8} = 0.2; f_{13,9} = 0.1; f_{13,10} = 0.1$	0.013620	0.010597	-0.003023	0.000807	0.000588
$f_{13.5} = 0.1; f_{14.6} = 0.1; f_{14.7} = 0.2$	0.013151	0.010271	-0.002880	0.000338	0.000262
$f_{16,5} = 0.1; f_{16,6} = 0.1$	0.012801	0.010001	-0.002800	-0.000012	-0.000008
All $f_{ie} = 0$	0.012813	0.010009	-0.002804	- , , · <u></u>	<u> </u>

(a) For F_{ii} , see Table XXVI.

- (c) For coordinate definitions, see Table XVIII.
- (d) $T_1 = 161.1^{\circ}$ K and $T_2 = 204.6^{\circ}$ K, corresponding to the lowest and highest temperatures respectively at which the distillation study was performed. A is the difference of $\ln (P^*/P)_{T_2}$ minus $\ln (P^*/P)_{T_1}$.

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(e)
$$\Delta_1 = [ln (P'/P)_T]$$
 with $f_{ie} = 0.1$] - $[ln (P'/P)_T]$ with $f_{ie} = 0$
 $\Delta_2 = [ln (P'/P)_T]$ with $f_{ie} = 0.1$] - $[ln (P'/P)_T]$ with $f_{ie} = 0$]

<u>TABLE XXXII. Differential Effects of Internal-External Interaction Force Constants</u> Unvolving T _x , R _x , and R _y : $f_{tr} = 0.3$, $f_{rot} = 0.05^{(a)}$						
@ T ₁ (d)	@ T ₂ ^(d)	_ ^(d)	(e)	(e)		
0.012011	0.009413	-0.002598	-0.000773	-0.000578		
			0.000807	0.000588		
0.013123	0.010253	-0.002870	0.000338	0.000262		
			-0.000013	-0.00008		
0.012785	0.009991	-0.002794	<u>_</u>			
((((d) • T ₁ 0.012011 0.013592 0.013123 0.012772	$\begin{array}{c} \begin{array}{c} \begin{array}{c} \begin{array}{c} \begin{array}{c} \\ \\ \end{array} \end{array} \end{array} \\ \begin{array}{c} \begin{array}{c} \end{array} \end{array} \\ \end{array} \\ \begin{array}{c} \end{array} \end{array} \\ \begin{array}{c} \end{array} \end{array} \\ \begin{array}{c} \end{array} \end{array} \\ \end{array} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \end{array} \end{array} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \end{array} \end{array} \\ \end{array} \\ \end{array} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \end{array} \end{array} \\ \end{array} \\ \end{array} \\ \end{array} \\ \end{array} \\ \end{array} \end{array} \\ \end{array} \\ \end{array} \\ \end{array} $	$\frac{\ln (P'/P)}{\underbrace{@ T_1}(d)} \underbrace{@ T_2}(d) \underbrace{(d)}_{0.012011} \underbrace{(0.009413)}_{0.010579} -0.002598}_{0.013592} \underbrace{(0.010579)}_{0.010253} -0.002870}_{0.013123} \underbrace{(0.010253)}_{0.002789} -0.002789}$	$\frac{\ln (P'/P)}{\underbrace{@ T_1}^{(d)} \underbrace{@ T_2}^{(d)} \underbrace{a^{(d)}}_{-0.002598} \underbrace{a_1^{(e)}}_{-0.000773} \\ 0.012011 \\ 0.009413 \\ -0.002598 \\ -0.000773 \\ 0.013592 \\ 0.010253 \\ -0.002870 \\ 0.000338 \\ 0.012772 \\ 0.009983 \\ -0.002789 \\ -0.000013 \\ -0.000013 \\ -0.000013 \\ -0.000013 \\ -0.000013 \\ -0.000013 \\ -0.000013 \\ -0.000013 \\ -0.000013 \\ -0.000013 \\ -0.000013 \\ -0.000013 \\ -0.000013 \\ -0.000013 \\ -0.000013 \\ -0.000013 \\ -0.000013 \\ -0.000013 \\ -0.0000013 \\ -0.0000013 \\ -0.0000013 \\ -0.0000013 \\ -0.0000013 \\ -0.0000013 \\ -0.0000000000000 \\ -0.000000000000000$		

- (b) In units of mdyn/A.
- (c) For coordinate definitions, see Table XVIII.
- (d) $T_1 = 161.1^{\circ}$ K and $T_2 = 204.6^{\circ}$ K, corresponding to the lowest and highest temperatures respectively at which the distillation study was performed. A is the difference of $\ln (P'/P)_{T_2}$ minus $\ln (P'/P)_{T_1}$.

(e)
$$\Delta_1 \approx [\ln (P'/P)_T]$$
 with $f_{ie} \approx 0.1] - [\ln (P'/P)_T]$ with $f_{ie} = 0$]
 $\Delta_2 = [\ln (P'/P)_T]$ with $f_{ie} = 0.1] - [\ln (P'/P)_T]$ with $f_{ie} = 0$]

Elements ^(b,c)	£n (P*/P)					
	@ т ₁ (d)	@ T ₂ (d)	۵ ^(ط)	(e) ▲1	∆2 ^(e)	
$f_{13.5} = 0.1; f_{13.6} = 0.1; f_{13.7} = 0.2$	0.011355	0.009007	-0.002348	-0.000777	-0.000577	
$13,3 = 0.2; f_{13,9} = 0.1; f_{13,10} = 0.1$	0.012942	0.010176	-0.002766	0.000810	0.000590	
$14.5 = 0.1; f_{14.6} \simeq 0.1; f_{14.7} = 0.2$	0.012470	0.009849	-0.002621	0.000338	0.000263	
$16.5 = 0.1; f_{16.6} = 0.1$	0.012119	0.009579	~0.002540	-0.000013	-0.000007	
$11 f_{ie} = 0$	0.012132	0.009586	-0.002546			
(a) For F _{ii} , see Table XXVI.				- <u>-</u>		

TABLE XXXIII. Differential Effects of Internal-External Interaction Force Constants

- (d) $T_1 = 161.1^\circ$ K and $T_2 = 204.6^\circ$ K, corresponding to the lowest and highest temperatures respectively at which the distillation study was performed. A is the difference of $\ln (P'/P)_{T_2}$ minus $\ln (P'/P)_{T_1}$.
- (e) $\Delta_1 = [\ln (P'/P)_T]$ with $f_{ie} = 0.1] [\ln (P'/P)_T]$ with $F_{ie} = 0]$ $\Delta_2 = [\ln (P'/P)_T]$ with $f_{ie} = 0.1] - [\ln (P'/P)_T]$ with $F_{ie} = 0]$

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the C-H and the C-F stretching force constants for the liquid are 4.814698 mdyn/ \hat{A} and 6.206256 mdyn/ \hat{A} respectively, in contrast to the corresponding values for gaseous trifluoromethane of 5.000000 mdyn/Å and 6.017878 mdyn/Å respectively. While f_{C-H} decreased upon condensation, f_{C-F} increased. On the other hand, it can be noted that in Tables XVII and XXV the frequency for the C-H stretching mode (w_1) increases from 3035 cm⁻¹ to 3062 cm⁻¹ upon condensation, while the frequencies involving the C-F stretching motions decrease upon condensation. The natural choice for f_{C-H} and f_{C-F} , therefore would involve an increase in the former and a decrease in the latter upon condensation. The F_{lig} fitting process, similar to those to that described above, using an increased C-H stretching force constant, lead to another $\mathbf{F}_{11\sigma}$ matrix, tabulated as " $f_{1i\sigma}(I)$ " in Table XXXIV. The vapor pressure isotope effect that this \mathbf{F}_{lig} yields (dashed line) is compared to the results obtained from the F_{1ig} of Table XXIX (solid line) in Figure 32. The increase in f_{C-H} upon condensation leads either to a) a too shallow slope when the magnitude of ln (P'/P) is comparable to those in the experimental data, or b) too large an inverse effect when the slope is comparable to that of the experimental data.

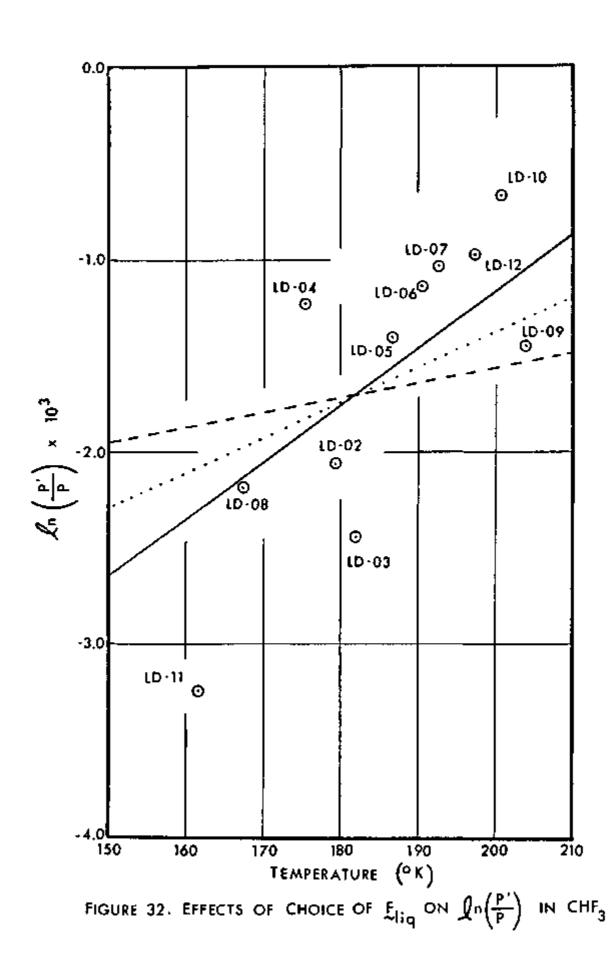
As a further alternative, the effects of an increase, in both f_{C-H} and f_{C-F} have been investigated. Table XXXV summarizes the effects of f_{tr} and f_{rot} when F_{ii} constructed from the internal elements listed uder " $E_{lig}(II)$ " in Table

	£ Matrix	Elements (a)
Force Constants	$E_{1ig}(\mathbf{I})$	Elig(II)
Internal	~	
Diagonal		
C-H str	5.069799	5.079799
C-F str	6.000442	6.070442
H-C-F bend	0.475929	0.475929
F-C-F bend	0.751771	0.751771
Interaction		
C-H str x C-F str	0.982035	1.070196
C-F str x C-F str	0.653696	0.723596
C-H str x H-C-F bend	-0.167382	-0.167382
C-H str x F-C-F bend	0.167382	0.167382
C-F str x adj H-C-F bend	0.194294	0.194294
C-F str x opp H-C-F bend	-0.265706	-0.265706
C-F str x adj F-C-F bend	0.256033	0.256033
C-F str x opp F-C-F bend	-0.180848	-0.180848
H-C-F bend x H-C-F bend	0.027767	0.027767
F-C-F bend x F-C-F bend	-0.110155	-0.110155
H-C-F bend x adj F-C-F bend	-0.138821	-0.138821
H-C-F bend x opp F-C-F bend	-0.253821	-0.253821
External		
Diagonal		
Translation	0.300000	0.300000
Rotation	0.050000 ^(b)	0.050000 ^(b)
Internal-External Interaction		
C-H str x T _z	-0.080000	-0.030000
C-F str x T_{7}	0.080000	0.030000
H-C-F bend $x T_{2}$	0.040000	0.010000
$F-C-F$ bend x T_2	-0.040000	-0.010000

TABLE XXXIV. Trial Liquid F Matrices for Trifluoromethane

(a) Unless otherwise noted, in units of mdyn/A.

(b) In units of mdyn-A.



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ftr o	frot					
(mdyn/A)	(mdyn-A)		@т ₂	Δ		
0.01	0.001	-0.001208	-0.000925	0.000283		
0.01	0.01	-0.001203	-0.000922	0.000281		
0.01	0.1	-0.001151	-0.000890	0.000261		
0.01	1.0	-0.000655	-0.000578	0.000077		
0.01	3.0	0.000326	0.000063	-0.000263		
0.1	0.001	-0.000911	-0.000742	0.000169		
0.1	0.01	-0.000906	-0.000739	0.000167		
0.1	0.1	-0.000854	-0.000707	0.000147		
0.1	1.0	-0.000358	-0.000395	-0.000037		
0.1	3.0	0.000623	0.000246	-0.000377		
1.0	0.001	0.001965	0.001054	-0.000911		
1.0	0.01	0.001970	0.001057	-0.000933		
1.0	0.1	0.002022	0.001090	-0.000932		
1.0	1.0	0.002518	0.001401	~0.001117		
1.0	3.0	0.003499	0.002043	-0.001456		
3.0	0.001	0.007836	0.004834	-0.003002		
3.0	0.01	0.007841	0.004837	-0.003004		
3.0	0.1	0.007893	0.004869	~ 0.003024		
3.0	1.0	0.008390	0.005181	-0.003209		
3.0	3.0	0.009371	0.005823	-0.003548		

TABLE XXXV. Effects of the Translational and Rotational

Force Constants on &n (P*/P) for Trial Liquid E Matrix

(a) $T_1 = 161.1^{\circ}$ K and $T_2 = 204.6^{\circ}$ K, corresponding to the lowest and highest temperatures respectively at which the distillation study was performed. Δ is the difference of $\ln (P'/P)_{T_2}$ minus $\ln (P'/P)_{T_1}$.

XXXIV is used. None of the internal-external interaction constants were included. Tables XXXVI and XXXVII are summaries of the differential effects of the interaction force constants involving T_{π} and the internal coordinates. These illustrate the general observation that the differential effects of the internal-external interaction force constants are similar for different choices of F_{ij} and f_{ee} . However, these different choices significantly effect the magnitude of *ln* (P'/P). Thus, the choice of E_{ii} and E_{ee} of Table XXIX sets the level of ln (P'/P) at a sufficiently positive (normal) level with $\underline{F}_{ie} = 0$, so that sufficiently large F_{ie} elements could be included in order to achieve a reasonably large slope without going too far into the inverse region. The choice of $\mathbf{F}_{i\,i}$ and F_{ee} of $F_{liq}(II)$ in Table XXXIV leads to an agreement with the experiment which is intermediate in slope between F_{lig} of Table XXIX and $F_{1ig}(I)$ of Table XXXIV, as shown by the dotted line in Figure 32.

The importance of the effect of the non-classical rotation of gaseous molecules towards $\ln \frac{S}{s}$, f_g was pointed out by Bigeleisen, Cragg, and Jeevanandam⁽¹²⁾ in relation to the vapor pressure isotope effect in methane. When this effect is explicitly included, Equation 3 becomes

$$\ln \frac{\mathbf{P}'}{\mathbf{P}} = \ln \frac{\mathbf{s}}{\mathbf{s}} \cdot \mathbf{f}_{\mathbf{C}} - \ln \frac{\mathbf{s}}{\mathbf{s}} \cdot \mathbf{f}_{\mathbf{g}}^{\mathbf{O}} - \ln \mathbf{f}_{\mathbf{R}}$$
(51)

where $\frac{s}{s}$, f_{g}^{o} is the reduced partition function of the

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TABLE XXXVI. Differential Effects of Internal External Interaction Force Constants

for Trial Liquid F Matrix :	$f_{tr} = 0.3 \text{ mdyn/}^2$,	$f_{rot} = 0.05 \text{ mdyn-A}^{(a)}$
-----------------------------	----------------------------------	---------------------------------------

Eiements(b)				£	n (P'/P)	_		
f(Tz,CH)	f(T _z ,CF)	f(T ₂ ,HCF)	$f(T_z, FCF)$	@ T ₁ (c)	● T ₂ (c)	(c)	(d)	(d)
0	0	0	0	-0.000230	-0.000320	-0.000090	<u> </u>	
0.01	0	0	O	-0.000209	-0.000303	-0.000094	0.000021	0.000017
0	0.01	0	0	-0.000285	-0.000361	-0.000076	-0.000055	~0.000041
0	0	0.01	0	-0.000403	-0.000446	-0.000043	-0.000173	-0.000126
0	0	0	0.01	-0.000053	-0.000191	-0.000138	0.000177	0.000129

(a) For
$$\mathcal{E}_{ii}$$
, see Table XXXIV (" $\mathcal{E}_{liq}(II)$ ").

(b) In units of mdyn/A.

TABLE XXXVII. Differential Effects of Internal-External Interaction Force Constants

for Trial Liquid E Matrix : $f_{tr} = 0.1 \text{ mdyn/A}, f_{rot} = 0.05 \text{ mdyn-A}^{(a)}$

Fie Elements(b)			<i>l</i> n (P'∕P)					
f(T ₂ ,CH)	f(T _z ,CF)	$f(T_z, HCF)$	$f(T_z, FCF)$	@ T ₁ (c)	(c)	(c)	(d)	2 ^(d)
0	o	0	0	-0.000883	-0.000725	0.000158		
0.01	0	0	0	-0,000862	-0.000708	0.000154	0.000021	0.000017
0	0.01	0	0	-0.000938	-0.000766	0.000172	-0.000055	-0.000041
0	0	0.01	0	-0.001057	-0.000851	0.000206	-0.000174	-0.000126
0	0	0	0.01	-0.000705	-0.000595	0.000110	0.000178	0.000130

(a) For E_{ii}, see Table XXXIV ("E_{lig}(II)").

(b) In units of mdyn/A.

(c) T₁ = 161.1° K and T₂ = 204.6° K, corresponding to the lowest and highest temperatures respectively at which the distillation study was performed. A is the difference of ln (P'/P)_{T2} minus ln (P'/P)_{T1}.
(d) A₁ = [ln (P'/P)_{T1} with f_{ie} = 0.01] - [ln (P'/P)_{T1} with E_{ie} = 0]
A₂ = [ln (P'/P)_{T2} with f_{ie} = 0.01] - [ln (P'/P)_{T2} with E_{ie} = 0]

internal vibrations of the gaseous molecule and

$$f_{R} = \frac{\left(\frac{Q_{qm}}{Q_{qm}} \right)_{R}}{\left(\frac{Q_{qm}}{Q_{e1}} \right)_{R}}$$
(52)

For a symmetric top molecule, the reduced partition function of the non-classical rotor, $\left(Q_{qm}/Q_{cl}\right)_R$, is given by ⁽³⁹⁾

$$\frac{Q_{cm}}{Q_{cl}} = e^{\sigma_{B}/4} \left\{ 1 + \frac{1}{12} \left[1 - \frac{B}{A} \right] \sigma_{B} + \frac{7}{480} \left[1 - \frac{B}{A} \right] \sigma_{B}^{2} + \dots \right\} + \dots \right\}$$
(53)

where

$$r_{\rm B} = \frac{\rm hcB}{\rm kT}$$
(54)

$$A = \frac{h}{8\pi^2 c I_A}$$
(55)

$$B = \frac{h}{8\pi^2 c I_{A}}$$
(56)

Use of $I_A = 1.48019 \times 10^{-38} \text{ erg-sec}^2$ and $I_B = 8.10673 \times 10^{-39} \text{ erg-sec}^2$ for ¹²CHF₃, and $I_A = 1.48019 \times 10^{-38} \text{ erg-sec}^2$ and $I_B = 8.12771 \times 10^{-39} \text{ erg-sec}^2$ for CHF₃ in Equation 52 leads to

$$ln f_{R} = \frac{3.08 \times 10^{-3}}{T} - \frac{3.423 \times 10^{-5}}{T^{2}}$$
(57)

It is apparent that the non-classical rotational correction for ${}^{13}C/{}^{12}C$ substitution in CHF₃ is insignificant primarily due to its large molecular weight and moments of inertia.

The disagreement between the calculated and the

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least-squares fit values of A and B of Bigeleisen's two term approximation, Equation 11, as pointed earlier, is not significant per se. First. Bigeleisen's two term expression for ln (P'/P) is an approximation to the exact expression, Equation 3. Second, the large degree of scatter of the experimental points led to large uncertainties in the least-squares fit values of A and B. The true test for an agreement between experiment and theory lies in a comparison of the calculated ln (P'/P), according to Equation 3, and the experimental values. Even the solid line in Figures 31 and 32, however, does not quite follow the trend of the experimental points. This discrepancy is probably a consequence of the simplifying assumptions implied in the simple cell model of the liquid. In this model, a single liquid molecule represents the entire liquid and this molecule interacts with the remainder of the phase which is structureless. The present liquid force field calculation has strongly indicated the existence of an unusually higher degree of interaction between the representative molecule and the remainder of the phase as exemplified by the large shifts in the diagonal F matrix elements upon condensation and the existence of large internal-external interaction force constants. This would suggest a significant degree of molecular association, perhaps through hydrogen bonding of molecules. Such a liquid system cannot be well represented by the simple cell model. The disagreement is probably due to this

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inadequacy of the model used.

V. CONCLUSION

The vapor pressure difference between the vapor pressure of 12 CHF₃, P', and the vapor pressure of 13 CHF₃, P, between the temperatures of 161° K and 205° K, may be expressed as

$$ln \frac{P'}{P} = \frac{(217 \pm 66)}{T^2} - \frac{(0.89 \pm 0.36)}{T}$$
(58)

according to Bigeleisen's two term equation, Equation 11.

The inclusion of the second-order term in Cohen's Long Time Kinetics Theory, Equation 20, affords a closer least-squares fit of the experimental isotopic ratios of samples within approximately the first 100 minutes of time zero of the distillation. After this initial period, the effect of this modification is insignificant.

According to the cell model, the experimentally obtained data of ln (P'/P) is not reproduced in the absence of internal-external interaction force constants, within reasonable limits of the external force constants. The experimental data can be adequately reproduced with the gaseous and liquid \underline{F} matrices summarized in Table XXIX through the use of Wilson's \underline{F} \underline{G} matrix method.

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