Study of Plasma Detachment in a Simplified 2D Geometry using UEDGE


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Study of Plasma Detachment in a Simplified 2D Geometry using UEDGE

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Abstract

The location of the ionisation front in a generic, detached plasma has been studied in a two-dimensional slab geometry by varying the core plasma density and input heating power. The ratio of the recombination to ionisation current and the momentum losses in the computational domain have been used to quantify the degree of detachment. Contours of constant ratio of these parameter in the core plasma density - heating power parameter space show that at high input power higher momentum losses can be achieved even at low density. High fraction of recombination, however, require high core densities to sufficiently separate the plasma from the target plate.

1 Introduction

The detachment of the scrape-off layer (SOL) plasma in tokamaks is one of the key provisions in the design of future fusion devices, providing the means to reduce the particle and heat loads onto the material surface to tolerable levels [1]. A detached plasma is characterised by two main features that co-exist synergetically: a radiation enhanced region and a recombination-dominated zone, where the gross of the plasma heat and momentum are dissipated, respectively. Radiation losses reduce the plasma temperature to drop to sufficiently low temperatures, that allowing ion-neutral friction to adequately occur; in return, ion-neutral collisions slow down the plasma flow, thus giving the plasma sufficient time require to recombine. These processes, which generally occur in different regions of the SOL, require plasma temperatures below 10eV. As a result, an ionisation front is formed which is well-separated from the target surfaces.

In a one-dimensional picture, the plasma temperature in the divertor SOL of tokamaks is determined by the influx of heat from the core plasma and the outflux of heat due to divertor plate heating and radiation. Neutral particles resulting from the recycling processes, whether volumetric or at the wall, provide the energy and momentum sink for the impinging plasma ions. In two dimensions, however, and depending on its rate, radial transport can be of great important, but is difficult to implement analytically. Numerical codes can aid our understanding of the interplay between the physics processes that are involved. Here, the numerical code package UEDGE [2] is used to simulate and examine plasma detachment of generic plasmas in a simplified two-dimensional (2D) geometry [3].
2 UEDGE in 2D slab geometry

The UEDGE code is a two-dimensional multi-fluid plasma code which can run with a variety of geometries [2]. Plasma transport along the magnetic field is assumed classical [4] with flux-limits imposed to simulate kinetic effects and prevent excessive parallel thermal transport in regions of steep temperature gradients. Perpendicular transport is assumed to be diffusive and anomalous, with spatially constant ion diffusion coefficient; here, $D_\perp = 0.5m^2/s$, and thermal diffusivity, $\chi_\perp = 0.7m^2/s$, for both electrons and ions. Neutrals arising from recycling at the target are treated as a fluid, with the neutral diffusivity determined by charge exchange (CX) and elastic scattering rates [3]. Volumetric momentum and energy losses are described by Braginskii's transport equation for the plasma momentum and energy [4], which are solved by UEDGE in poloidal, x-, and radial, y-direction of the 2D geometry [3] in this work. Thereby, a plasma is assumed that extends 1m in poloidal and 0.05m in radial direction. The toroidal field is taken to be constant at 5T, and the poloidal field is constant at 0.3T, giving a field pitch angle of 3.43°.

The particle and energy flow into the SOL is set in UEDGE by the core plasma density, $n_{core}$, and particle diffusivity, and the total heating power, $P_{tot}$, and the thermal diffusivity at the core boundary grid cells, respectively. Particles are removed from the system by means of ion pumping at the target plate (Recycling coefficient $R_P = 0.98$) and neutral pumping at the outer and private plasma walls (Albedo $\alpha_0 = 0.99$). Zero temperature and particle flux gradients are assumed at the outer and private plasma walls. The boundary condition at the target, $x = 1.0m$, follows the Bohm criterion [5], i.e. $M_{i,x=1} = 1$. The sheath heat transmission coefficients, $\gamma_i$ and $\gamma_e$, for the ions and electrons are 2.5 and 4.0, respectively.

3 Plasma detachment in UEDGE slab geometry: the base case solution

In the base case, the core plasma density is set to $n_{core} = 7.5 \cdot 10^{19}m^{-3}$. This gives, together with $D_\perp = 0.5m^2/s$, a particle in flux of $4.1 \cdot 10^{20}$ particles per second. In steady-state, particles are removed at a rate of $4.0 \cdot 10^{20}$ per second as neutrals at the outer wall, and the remaining $1 \cdot 10^{19}$ particles per second as ions at the target plate. The input power of $1 \cdot 10^4W$ is exhausted as hydrogenic radiation that is associated with ionisation of recycling neutrals, and also recombination, $9.5 \cdot 10^3W$, while the divertor plate heating is $5 \cdot 10^2W$. The divertor plasma is detached and the ionisation front is approximately 0.09m separated from the solid surface.

The SOL above the x-point is characterised by a radial inflow of particles and heat from the core plasma. The corresponding poloidal variation of the significant terms in the momentum and electron energy equation is shown for the separatrix flux tube in Fig.1. The ion parallel velocity, expressed as the fraction of the ion sound speed (Mach number) and the electron temperature are given by the right-hand scale of the plots, respectively. The inflow of particles and heat leads to a linearly rising parallel particle and heat flow. Across the x-point, momentum and heat is lost due to radial momentum diffusion and power flow into the private flux region (PFR). These processes occur as the shear in parallel velocity between the core and SOL plasma are large at, and the radial temperature and density gradients are reversed below the x-point. The plasma temperature and the poloidal momentum drop significantly around the x-point, which is a 2D effect that would not occur in a 1D treatment.
Fig. 1: Poloidal variation of the significant terms in the momentum (a) and energy equation (b) along the separatrix flux tube (base case). The ion speed (Mach number) and the electron temperature are given on the right-hand y-axis. The approximate location of the x-point and the ionisation front are indicated by the gray, vertical lines.

The outflow of heat into the PFR causes the plasma temperature to drop to a point where heat losses due to ionisation become significant, thus the plasma temperature is reduced even faster. In the UEDGE cases shown here, the temperature, at which radiation is the dominant term is of the order $5 - 10eV$, since only hydrogenic radiation losses are considered. This region is defined as the ionisation-dominated region (IDR). The radiated power is supported by a combination of parallel energy flow from the upstream SOL, and heating from the ions due to ion- electron temperature equipartition. As the radial temperature gradient relaxes within the IDR, the radial heat losses into the PFR are insignificant. In order to sustain heat conduction, the parallel temperature gradient steepens rapidly between 5 and 10eV, until, at 5eV, parallel heat convection becomes the major heat transport process.

The plasma that stretches from the IDR to the target is cold ($\sim 1eV$) and dense ($\sim 10^{20} m^{-3}$), and therefore dominated by recombination. We defined this region as the recombination-dominated region (RDR). The ion velocity is at its maximum at the entrance to the RDR, $M = 0.15$. Due to CX collisions occurring within the RDR, this velocity decreases significantly. As UEDGE has to converge with an ion speed equivalent to $M = 1$ at the target, the Mach number increases rapidly in the grid cells that are directly adjacent to the plate.

4 Effect of core density and input power on detached plasma

Experimentally, the core plasma density and heating power are the principal, external input parameter; their influence on the conditions of the detached plasma is therefore of great importance.

At fixed core plasma density, the total input power across the core boundary is varied, at fixed thermal diffusivity, from $5 \cdot 10^3 W - 2 \cdot 10^4 W$. Increasing the input power raises the radial heat flux into the SOL, heats the electrons and ions in the upstream SOL, and concomitantly generates a larger heat flux in the parallel field direction. Below the x-point, the temperature gradient between the SOL and the
Fig. 2: Poloidal variation of the ionisation and recombination sources along the separatrix flux tube: a) with increasing power, and b) increasing density. The changes in the poloidal temperature profile due to the increase in power and density are shown on the right-hand y-axis. The gray, vertical lines indicate the approximate position of the ionisation front.

PFR steepens, and more momentum and heat is transported into the PFR. Still, the parallel heat fluxes that enter the IDR are larger, while the neutral density adjacent to the target increases. Facing this larger influx of heat from the upstream SOL and an enhanced plasma cooling downstream, the plasma temperature gradient within the IDR steepens dramatically, subsequently narrowing this region. As shown in Fig.2a, the ionisation front is forced to move closer to the target, narrowing the RDR, and the fraction of plasma recombining to neutrals ionising decreases. The CX momentum losses, integrated over the SOL and PFR, are smaller at high input power, with similar Mach numbers at the RDR exit.

Increasing the core plasma density at fixed heating power moves the ionisation front further away from the target plate (Fig.2b). In this study, the core density is varied from $5 \times 10^{18} \text{m}^{-3}$ to $2.5 \times 10^{20} \text{m}^{-3}$, while keeping the diffusion coefficient fixed. Raising the core plasma density cools the SOL plasma and lowers the heat fluxes along the field lines. At the highest core plasma density, the SOL plasma becomes as cold as 10eV, so that heat convection becomes the dominant heat transport mechanism. The increased influx of particles into the divertor is followed by an increase in neutral density at the target plate; still, the temperature gradient within the IDR relaxes. The fraction of recombination to ionisation increases with increasing density. Increasing the neutral density at the target, by decreasing the neutral removal rate at the outer wall, moves the ionisation front further off the target and increases the ratio of recombination to ionisation. CX momentum losses are greater at high core plasma density. We conclude that the location of the ionisation front depends on both the upstream, core plasma conditions and re-ionisation processes that take place adjacent to the target plate.

Instead of attempting to approximate the momentum and energy equation in the RDR to derive an analytic expression for the location of the ionisation front, the approach taken here is to describe divertor detachment in the parameter space of core density and input power. For that purpose, the recombination to ionisation current
ratio, $I_{rec}/I_{ion}$, and the CX momentum losses, $S_{mom}$, are calculated to measure the degree of detachment. The former quantity is obtained by integrating over the PFR and divertor SOL domain,

$$\frac{I_{rec}}{I_{ion}} \propto \frac{n_i^2 \langle \sigma v \rangle_{rec}^{RDR}}{\langle n_0 n_i \langle \sigma v \rangle_{ion}^{IDR}}$$

where $n_i$ and $n_0$ denote the ion and neutral density, and $\langle \sigma v \rangle_{rec}$ and $\langle \sigma v \rangle_{ion}$ the recombination and ionisation rates in the RDR and IDR, respectively. CX momentum losses are determined by the drop in (static, $p$, and dynamic, $m_i n_i u_i^2$) pressure in parallel field direction,

$$S_{mom} \propto 1 - \frac{mom_{RDR}}{mom_{up}} \equiv 1 - \frac{(p_i + p_e + m_i n_i u_i^2)^{RDR}}{(p_i + p_e)^{up}}$$

where $m_i$ is the ion mass. Momentum balance for attached cases can only be achieved when integrating radially over the PFR and the SOL domain due to the radial outflow of momentum around the x-point. Upstream from the x-point, the pressure is integrated over the SOL domain only. The core plasma density input to UEDGE is normalised to the upstream density, $n_{up}$, as given by the 2-Point Model [7],

$$n_{up-2PM} = \sqrt{\frac{2 m_i}{e} \frac{\gamma q_i L}{2 \kappa_{0e}}}^{4/7} \frac{\gamma^2 e^2 T_i}{\gamma^2 e^2 T_i}$$

where $e$ is the electron charge, $L$ is the length of the field line, $\gamma = 6.5$, is the total sheath heat transmission coefficient, and, $\kappa_{0e} \approx 2000$, is the Spitzer conductivity for single ion species of charge $Z_i$. A target plasma temperature, $T_i$, of 1eV is assumed, a temperature at which the divertor plasma is still in the attached, high recycling regime. The parallel heat flux density, $q_{||}$, as in Eq.3, assumes that heat is transported by conduction only. This term is approximated by the input power, $P_{in}$, and the radial power scale length, $\lambda_{q||}$, obtained by UEDGE,

$$q_{||} = \frac{P_{in}}{\lambda_{q||}} = \frac{B_T}{B_p}$$

Typically, $\lambda_{q||}$ varies between 5–10mm, giving a parallel heat flux density of $10^7 W/m^2$.

Resulting contours of constant $I_{rec}/I_{ion}$ and $p_{RDR}/p_{up}$ ratio in the core density-heating power parameter space are shown Fig.3a and 3b. At low density, the divertor plasma is dominated by ionisation, with negligible recombination; the ratio of $I_{rec}/I_{ion}$ is therefore low. To achieve significant recombination, the core plasma density must exceed about 3 at low input power, and about 2 at high power. The ratio of recombination to ionisation depends on the divertor plasma and neutral density, but also whether the plasma flow is sufficiently low to permit significant recombination [8]. The competition between the time required for sufficient recombination and the ion transit time across the RDR is proportional to the inversed product of $n_{RDR} \Delta x$, $\Delta x$ being the width of the RDR. Increasing the core plasma density lowers the divertor density, but widens the width of the RDR. The opposite effect occurs when increasing the heating power.
Fig. 3: Contours of constant recombination to ionisation (a) and momentum loss (b) in (normalised) core density - heating power space.

The CX momentum losses depend mainly on plasma and neutral density in the divertor, but also over which distance the ion-neutral friction acts, $S_{\text{mom}} \propto n_p n_d \Delta x$. Under detached conditions, increasing the core plasma density reduces the divertor plasma density, but raises neutral density and expands the RDR. When increasing the power both the plasma and neutral density is raised, but the width of the RDR becomes significantly shorter.

There is a trade-off between these processes, and depending on which process exerts the stronger influence, the recombination-to-ionisation ratio and the momentum losses increase or decrease. Operation at high density and high power seems to increase both the recombination-to-ionisation ratio and the CX momentum losses.

5 Conclusions

The location of the ionisation front in a generic plasma has been studied in a 2D geometry using UEDGE. On the high-temperature side, the location of the ionisation front is very sensitive to the particle and heat influx from the core into the divertor, but also the radial losses into the PFR. On the low temperature side, the critical parameters are radiation losses due to ionisation, CX momentum losses and the level of neutral density adjacent to the target. The location of the ionisation front has been examined as a function of the core plasma density and heating power. Increasing the core plasma density or decreasing the input power moves the ionisation front away from the target. Concomitantly, the region that is dominated by recombination expands, allowing more CX momentum loss collision to occur. Higher influxes of heat and larger neutral densities at high power lead to steep temperature gradients the region of high ionisation.

The dependence of the degree of detachment on core density and input power has been discussed in their parameter space. Based on the ratio of recombination to ionisation and downstream to upstream momentum, it has been shown that a higher degree of detachment can be achieved at the highest core density and heating input power.
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References


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