

# DISTRIBUTION SHEET

<b>To</b> J. R. Bellomy	<b>From</b> B. F. Norman/Equipment Stress Analysis/8D430	<b>Page 1 of 1</b> <b>Date</b> October 4, 1994
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<b>Project Title/Work Order</b> Shot Loading Support Analysis/D2M9G	<b>EDT No.</b> 142181
	<b>ECN No.</b>

Name	MSIN	Text With All Attach.	Text Only	Attach./Appendix Only	EDT/ECN Only
L. W. Bartholf	H5-60			X	
J. R. Bellomy	S6-12	X			
J. P. Harris	S6-12			X	
R. L. Jorissen	H5-53			X	
T. C. Mackey	S2-03			X	
B. F. Norman	H5-53	X			
R. B. Pan	H5-53	X			
Central Files		X			
OSTI (2)	L8-07	X			

2. To: (Receiving Organization) Single-Shell Tank Retrieval/J. P. Harris	3. From: (Originating Organization) Equipment Stress Analysis	4. Related EDT No.: N/A
5. Proj./Prog./Dept./Div.: Shot Loading Platform Analysis/D2M9G	6. Cog. Engr.: J. R. Bellomy	7. Purchase Order No.: N/A
8. Originator Remarks:	9. Equip./Component No.: N/A	10. System/Bldg./Facility: N/A
	11. Receiver Remarks:	12. Major Assm. Dwg. No.: H-2-83738
		13. Permit/Permit Application No.: N/A
		14. Required Response Date:

15. DATA TRANSMITTED					(F)	(G)	(H)	(I)
(A) Item No.	(B) Document/Drawing No.	(C) Sheet No.	(D) Rev. No.	(E) Title or Description of Data Transmitted	Impact Level	Reason for Transmittal	Originator Disposition	Receiver Disposition
1	WHC-SD-W320-DA-005		0	Shot Loading Platform Analysis	SQ	1	1	

16. KEY		
Impact Level (F)	Reason for Transmittal (G)	Disposition (H) & (I)
1, 2, 3, or 4 (see MRP 5.43)	1. Approval 2. Release 3. Information Required	4. Review 5. Post-Review 6. Dist. (Receipt Acknow.)
		1. Approved 2. Approved w/comment 3. Disapproved w/comment
		4. Reviewed no/comment 5. Reviewed w/comment 6. Receipt acknowledged

(G)		(H)	17. SIGNATURE/DISTRIBUTION (See Impact Level for required signatures)						(G)	(H)
Reason	Disp.	(J) Name	(K) Signature (M) MSIN	(L) Date	(J) Name	(K) Signature (M) MSIN	(L) Date	Reason	Disp.	
1		Cog. Eng.	J. R. Bellomy	10/24/94	12	ESA Eng.	B. F. Norman	H5-53	1	
1		Cog. Mgr.	J. P. Harris	10/24/94	S6-12					
1		QA	J. Huston	10/24/94	S6-12					
1		Safety	G. E. McPherson	10/24/94	T4-10	52-41	10-10-94			
1		ESA Mgr.	R. B. Par	10/24/94	H5-53					

18. Signature of EDT Originator <i>B. F. Norman</i> B. F. Norman	10-7-94 Date	19. Authorized Representative for Receiving Organization <i>J. R. Bellomy</i> J. R. Bellomy	10/24/94 Date	20. Cognizant/Project Engineer's Manager <i>J. P. Harris</i> J. P. Harris	10/24/94 Date	21. DOE APPROVAL (if required) Ltr. No. <input type="checkbox"/> Approved <input type="checkbox"/> Approved w/comments <input type="checkbox"/> Disapproved w/comments
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**RELEASE AUTHORIZATION**

**Document Number:** WHC-SD-W320-DA-005, REV 0

**Document Title:** SHOT LOADING PLATFORM ANALYSIS

**Release Date:** 10/24/94

\* \* \* \* \*

**This document was reviewed following the  
procedures described in WHC-CM-3-4 and is:**

**APPROVED FOR PUBLIC RELEASE**

\* \* \* \* \*

**WHC Information Release Administration Specialist:**

  
Kara Broz

October 24, 1994

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(Signature)

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(Date)

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# SUPPORTING DOCUMENT

1. Total Pages **28**

2. Title

Shot Loading Platform Analysis

3. Number

WHC-SD-W320-DA-005

4. Rev No.

0

5. Key Words

Loading Platform  
Funnels  
Hopper

6. Author

Name: B. F. Norman

*B. F. Norman*  
Signature

Organization/Charge Code Equipment  
Stress Analysis/D2M9G

**APPROVED FOR  
PUBLIC RELEASE**

*KMC 10/24/94*

7. Abstract

This document provides the wind/seismic analysis and evaluation for the shot loading platform. Hand calculations were used for the analysis. AISC and UBC load factors were used in this evaluation. The results show that the actual loads are under the allowable loads and all requirements are met.

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10.

RELEASE STAMP

OFFICIAL RELEASE **58**  
BY WHC  
DATE **OCT 24 1994**  
*Sta. # 3*

9. Impact Level **SQ**

**MASTER**

**SPOOL ASSEMBLY SUPPORT ANALYSIS**

**OCTOBER 1994**

PREPARED BY: *B. F. Norman* DATE: 10-2-94  
B. F. Norman, Engineer  
Equipment Stress Analysis

REVIEWED BY: *Randy Jorissen* DATE: 10/2/94  
R. L. Jorissen, Principal Engineer  
Equipment Stress Analysis

APPROVED BY: *R. B. Pan* DATE: 10/8/94  
R. B. Pan, Manager  
Equipment Stress Analysis

**Westinghouse Hanford Company  
Hanford Operations and Engineering Contractor  
for the  
U.S. Department of Energy**

CHECKLIST FOR INDEPENDENT REVIEW

Document Reviewed WHC-SD-W320-DA-005, Rev. 0

Author B. F. Norman

Yes No NA

- [X] [ ] [ ] Problem completely defined.
- [X] [ ] [ ] Necessary assumptions explicitly stated and supported.
- [ ] [ ] [X] Computer codes and data files documented.
- [X] [ ] [ ] Data used in calculations explicitly stated in document.
- [X] [ ] [ ] Data checked for consistency with original source information as applicable.
- [X] [ ] [ ] Mathematical derivations checked including dimensional consistency of results.
- [ ] [ ] [X] Models appropriate and used within range of validity or use outside range of established validity justified.
- [X] [ ] [ ] Hand calculations checked for errors.
- [ ] [ ] [X] Code run streams correct and consistent with analysis documentation.
- [ ] [ ] [X] Code output consistent with input and with results reported in analysis documentation.
- [X] [ ] [ ] Acceptability limits on analytical results applicable and supported. Limits checked against sources.
- [X] [ ] [ ] Safety margins consistent with good engineering practices.
- [X] [ ] [ ] Conclusions consistent with analytical results and applicable limits.
- [X] [ ] [ ] Results and conclusions address all points required in the problem statement.

MANDATORY Software QA Log Number N/A

Randy Jorissen  
Reviewer/B. L. Jorissen

10/7/94  
Date

### DESIGN VERIFICATION METHOD

The need for design verification has been reviewed with the method selected as indicated below: (ESR/Work Plan # WP-23480-289).

<u>    X    </u>	Independent Review
<u>          </u>	Alternative Calculations
<u>          </u>	Qualification Testing
<u>          </u>	Formal Design Review

R. B. Pan   
Cognizant/Project/Design Manger

SD # WHC-SD-W320-DA-005

ECN #                                   

DWG(S) #



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## SHOT LOADING PLATFORM ANALYSIS

### 1.0 INTRODUCTION

Equipment Stress Analysis was asked to design a support system that would be able to transfer shot from a hopper into containers resting on the flatbeds of trucks. This support system also had to have shielding capability to protect workers from radiation exposure. A wind and seismic analysis was performed on the support system to determine member sizes. Hand calculations were used to determine stresses and overturning forces in the support structure.

The design is in accordance with SDC 4.1 (HPS) and is safety class 3SQ. The design and fabrication is in accordance with American Institute of Steel Construction, Manual of Steel Construction (AISC 1989). All welding and weld inspection is in accordance with AWS D1.1. The applied loads to the shot support system were in accordance with the UBC (ICBO 1991) and ASCE 7-88 (ASCE 1988).

Results of the analysis appear in Section 2.0. Loadings and configurations appear in Section 3.0. Section 4 discusses the stress analysis process, and the appendices contain the calculations.

### 2.0 RESULTS

The allowable loads and stresses for members were based on the *American Institute of Steel Construction* (AISC 1989). Overturning moments and restoring moments are based on the *Uniform Building Code* (UBC)(ICBO 1991).

The support structure was checked for overturning along its two main axes. Calculations indicate a safety factor greater than 1.5; therefore overturning will not occur.

The bending stresses in the shot support structure that result from lateral and gravity loads are acceptable. The bending stresses in the funnels are acceptable for the applied loads.

The hopper was provided by the GAR-BRO Company, Heber Springs, Arkansas. No structural analysis was performed on this piece of equipment by WHC engineering. Analysis was performed by GAR-BRO.

During operation, the maximum applied loads to the assembly are as follows: ten cubic feet of lead shot in the hopper, 2 personnel with associated equipment, and 1,000 lb of lead blankets spread over a minimum of 10 ft<sup>2</sup> area.

### 3.0 CONFIGURATIONS AND LOADINGS

#### 3.1 CONFIGURATIONS

The drawings listed below document the configurations for the shot loading platform assembly and the funnels:

- H-2-83738 Shot Loading Platform
- H-2-83745 Tank 241-C-106 Funnels  
& H-2-83756
- H-2-83751 Tank 241-SY-101 Funnels.

The configurations and dimensions of the components analyzed appear in Appendix A along with the calculations.

#### 3.2 LOADINGS

The loading criteria were based on the amount of shielding required to keep exposure limits to a minimum. Discussion of the weights and applied loads appears in Appendix A along with the calculations.

### 4.0 STRESS ANALYSIS

The applied loads to the shot support system were in accordance with the UBC (ICBO 1991) and ASCE 7-88 (ASCE 1988). Hand calculations were used to verify structural member sizes and weld sizes. Appendix A discusses the applied loads in depth, as well as the actual and allowable loads.

## 5.0 REFERENCES

- AISC, 1989, *Manual of Steel Construction, Allowable Strength Design*, Ninth edition, American Institute of Steel Construction, Chicago, Illinois.
- ASCE, 1988, *Minimum Design Loads for Buildings and Other Structures*, ASCE 7-88, American Society of Civil Engineers, New York, New York.
- ICBO, 1991, *Uniform Building Code*, International Conference of Building Officials, Whittier, California.

**APPENDIX A**  
**SHOT LOADING PLATFORM**

## ANALYTICAL CALCULATIONS

Page 1 of 14Subject LEAD SHOT SUPPORT ASSEMBLY (LSSA)Originator B. F. NORMAN Date 4-20-94Checker *Candy Jones* Date 9/28/94OBJECTIVE:

A DESIGN WAS REQUIRED TO LOAD LEAD OR STEEL SHOT INTO CONTAINERS LAYING ON FLATBED TRUCKS. THE SUPPORT HAD TO BE ABLE TO VARY IN HEIGHT, AND BE EASILY DISASSEMBLED TO BE MOVED FROM SITE TO SITE. ON THE FOLLOWING PAGES YOU WILL FIND THE ANALYSIS FOR A THREE PART SUPPORT SYSTEM WHICH HAS THE CAPABILITY TO MEET THE REQUIREMENTS. WE HAVE ONE PLATFORM ASSEMBLY AND TWO INDEPENDENT SIDE SUPPORTS. A STATIONARY HOPPER WAS ALSO ANALYSED TO PREVENT LEAD SHOT FROM BEING SPILLED DURING THE TRANSFER.

ANALYTICAL CALCULATIONS

Subject LEAD SHOT SUPPORT ASSEMBLY

Originator RF NORMAN Date 11-4-94

Checker Randy Joensen Date 9/28/94

WIND LOADS ASCE 7-88

SAFETY CLASS 3  
CLASSIFICATION

$$F = q_z G_h C_p A_f$$

$$q_z = 0.00256 K_z (IV)^2$$

$$K_z = \text{Exp. C } 20' \text{ HGT} = 0.87$$

$$V = 70 \text{ mph}$$

$$I = 1.07 \rightarrow \text{SOC 4.1 REV 12}$$

$$q_z = 0.00256 (0.87) (1.07 \cdot 70)^2$$

$$q_z = 12.49 = 12.5$$

$$G_h = 1.29 \text{ Exp C } H_g t = 20'$$

WIND DIRECTED @ SIDE  
WHERE VERTICAL LEAD  
SHIELDING IS  
SEE PG 6

$$C_f = H=12 \quad W=10 = 1.2 < 3$$

$$C_f = 1.2$$

$$F = 12.5 (1.29) (1.2) A_f$$

$$F = 19.35 A_f$$

USE 20 PSF WIND LOAD

SEISMIC LOADS UBC-1991

$$F_p = Z I C_p W_p \rightarrow \text{SOC 4.1 REV 12 } (Z = 0.2 \text{ CONSERVATIVE})$$

$$Z = 0.20 \text{ ZONE 2B (TABLE 23-I)}$$

$$I = 1.25 \text{ OCC. 4 CATEGORY (TABLE 23-L) VS SOC 4.1 REV 12}$$

$$C_p = 0.75 \text{ III EQUIPMENT (TABLE 23-P)}$$

→ COMPONENT WGT.

$$F_p = 0.19 W_p$$

THIS IS  
SINCE A TEMPORARY STRUCTURE SEISMIC WILL BE LOOKED  
@ FOR OVERTURNING ONLY. NO STRUCTURAL COMPONENTS  
WILL BE DESIGNED TO RESIST SEISMIC LATERAL LOADING.

ANALYTICAL CALCULATIONS

Subject LEAD SHOT SUPPORT ASSEMBLY  
 Originator BF NORMAN Date 4-7-94  
 Checker Randy Johnson Date 9/28/94

DESIGN WILL USE 2 1/8" PLATE BUT ACTUAL THICKNESS  
 WILL BE 2" (THIS WILL ALLOW FOR LEAD BLANKETS  
 TO BE ADDED IF RAD LIMITS ARE HIGHER THAN EXPECTED  
 = 536# USED FOR LEAD  
 BLANKETS.

TOP PLATFORM ANALYSIS

- SEE APPENDIX A FOR LEAD SHIELDING REQUIREMENTS
- WORKER DOSE RATE 10-15 mR/hr (VERIFIED)
- DOSE RATE OF 14 mR/hr = 3.5 CM OF LEAD

$3.5 \text{ CM} = 1.38'' \text{ OF LEAD}$

- GEOFFRY PETER (KEH ENGINEER) SAYS 1.0" LEAD = 1.5" STEEL  
 S.G. LEAD = 11.37 RATIO = 1.45 ≈ 1.50  
 S.G. STEEL = 7.85  $\frac{1.0}{1.15} = \frac{1.38}{?} \quad ? = 2.07'' \text{ STEEL}$

$2 \frac{1}{8}'' \text{ THK PL STEEL} = 86.79 \text{ PSF}$

PLATFORM = 10' x 10'-6" = 105 FT<sup>2</sup>

SNOW LOAD = 20 PSF  
 PER SAC 4.1 REV 12  
 NOT APPLIED SIMULTANEOUSLY W/ LIVE LOAD

LIVE LOAD/SNOW LOAD = 20 PSF

↓ (PEOPLE, RAILINGS, CONNECTIONS, MISC WGT)  
 TOTAL = 107 PSF  
 ↓ VERTICAL SHIELDING  
 CONSIDERING PLATFORM AS A ROOF STRUCTURE W/ NO ADDED EQUIPMENT BUT WHAT IS SHOWN

WGT. OF PLATFORM = 11,235 # + 2'(2) (3 SIDES) (86.79) - 2'(2) (86.79) HOLE IN FLOOR  
 WGT = 11,930 #

HOPPER WGT = 750 # FROM GAR-BRO COMPANY

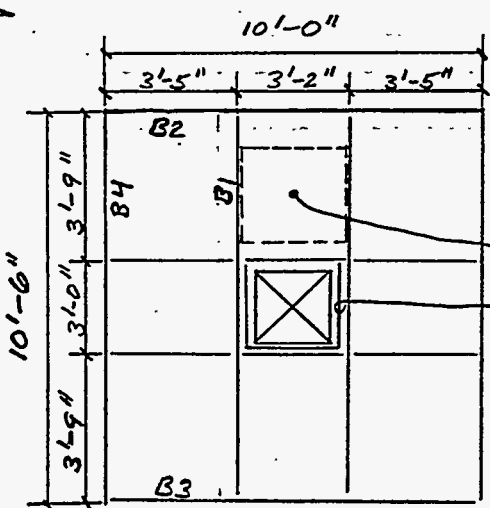
10 cuft of shot = 4,300 #

TOTAL = 3,050 #  
 #/LEG = 1,262 #

PLATFORM IS IN SYMMETRY  
 ANALYSE ONE SIDE & MIRROR TO OTHER.

- STRUCTURE OF PLATFORM CONSISTS OF 6X6X1/4 TS

HOPPER LOCATION  
 2' HIGH SHIELDING 3 SIDES



LL 2,000 POUNDS  
 TWO MEN & PERSONAL EQUIP  
 = 3,000 #

LEAD BLANKETS = 1,000 #  
 WHEN CONTAINERS ARE BEING LOADED.

USE 1000# OF LEAD BLANKETS SPREAD OVER 10 FT<sup>2</sup> AREA OR 100 PSF MAX.



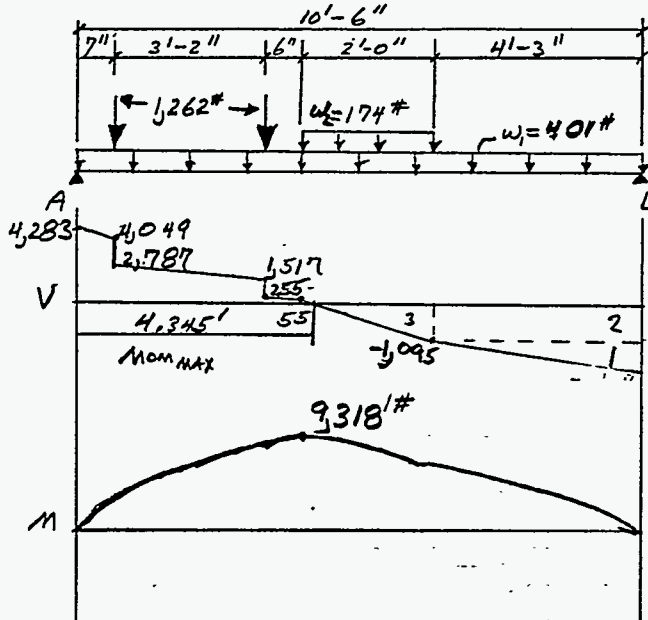
ANALYTICAL CALCULATIONS

Subject \_\_\_\_\_  
 Originator BF NORMAN Date 4-7-94  
 Checker Glenn Jansen Date 9/28/94

BEAM #1

\*\*\* ADD 25% IMPACT LOAD TO BEAM 1

USE BEAMS AS SIMPLY SUPPORTED



$321 \#(1.25) = 401$

$w_1 = 3' \text{ TRIB } (107) = 321 \#/\text{ft}$

$w_2 = 2' \text{ HEIGHT } (87) = 174 \#/\text{ft}$

$\Sigma M_A = 1,262(5.8) + 1,262(3.75)$

$+ 401(10.5)(5.25)$

$+ 174(2)(5.25)$

$= B(10.5)$

$B = 2,799 \#$

$\Sigma F_y A = 4,283 \#$

AREA 1 =  $1,704(4.25)(1/2)$

$= 3,621$

AREA 2 =  $1,095(4.25)$

$= 4,654$

AREA 3 =  $1,095(1.905)(1/2)$

$= 1,043$

SUM AREAS 1, 2, 3

SUM =  $9,318 \#$

TRY  $6 \times 6 \times 1/4$  TS  $S_x = 10.1 \text{ in}^2 I = 30.3 \text{ in}^4$

$f_b = M/S = 9,318(12) / 10.1$

$f_b = 11,071 \text{ psi}$

$F_b = .6(46) = 27.6 > 11.1 \therefore \text{OK}$

DEFLECTION CHECK - FIND MAX ALLOWABLE W FOR L/240 DEFLECTION (SEE NOTE)

NOTE: L/240 ALLOWABLE ROOF DEFLECTION UBC 1991

$L/240 = (10'-6'')(12) / 240 = 0.525''$

$.525 = \frac{5w(126)^4}{384(29e^6)(30.3)}$

$141 = w/12 \quad w = 1,687 \text{ PLF}$

DUE TO LARGE ALLOWABLE W & POSITIONING OF POINT LOADS, DEFLECTION IS OK FOR TUBE.

ANALYTICAL CALCULATIONS

Subject \_\_\_\_\_

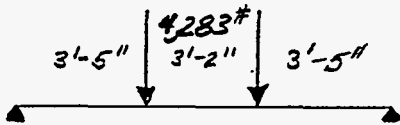
Originator BF NORMAN Date 4-7-94

Checker Randy Laurien Date 9/28/94

2

BEAM #2

$r = v = 4283\#$



$M_{MAX} = P_a = 4283 (3'5") = 14,633 \text{ l}\#$

$f_b = M/S = 14,633 (12) / 10.1 = 17,386 \text{ psi}$

$F_b = .6(46) = 27.6 > 17.4 \therefore \text{OK}$

$\Delta_{MAX} = \frac{P_a}{24EI} (3L^2 - 4a^2)$

$= \frac{4283(41)}{24(29000)(303)} (3(120)^2 - 4(41)^2) = 0.30 \text{ in}$

$\therefore \text{OK FOR DEFLECTION}$

$\therefore \text{BEAM IS OK}$

BEAM #3

SAME AS BEAM 2 BUT W/ 2,799 POUND POINT LOADS

$M = 2,799\# (3'5") = 9,563 \text{ l}\#$

$F_b = 9,563 (12) / 10.1 = 11,362 \text{ psi} < 27.6 \text{ ksi} \therefore \text{OK}$

DEFLECTION IS OK

$V = R = 2,799 \#$

BEAM 4

WILL BE ANALYSED AFTER A TOTAL FREEBODY DIAGRAM HAS BEEN DESIGNED AND THE REACTIONS ANALYSED

FORCES DUE TO WIND LOAD.

AREA FROM 2" PLATE = 10' x 10' = 100 ft<sup>2</sup>

AREA FROM EQUIPMENT & PLATFORM = 20 ft<sup>2</sup>

120 (20) = 2,400 #

120 ft<sup>2</sup>

- APPLY WIND LOAD AT TOP OF PLATFORM (CONS)  
SPLIT LOAD BETWEEN TWO COLUMNS ON SIDE SUPPORT.

$F = 1,200 \# / \text{SUPPORT}$

ANALYTICAL CALCULATIONS

Subject LEAD SHOT SUPPORT ASSEMBLY

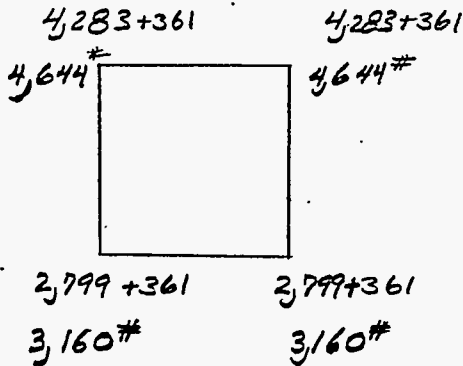
Originator BF NORMAN

Date 5-4-94

Checker Randy Jovisen

Date 9/28/94

VERT LOADS AT CORNERS DUE TO B1, B2, B3



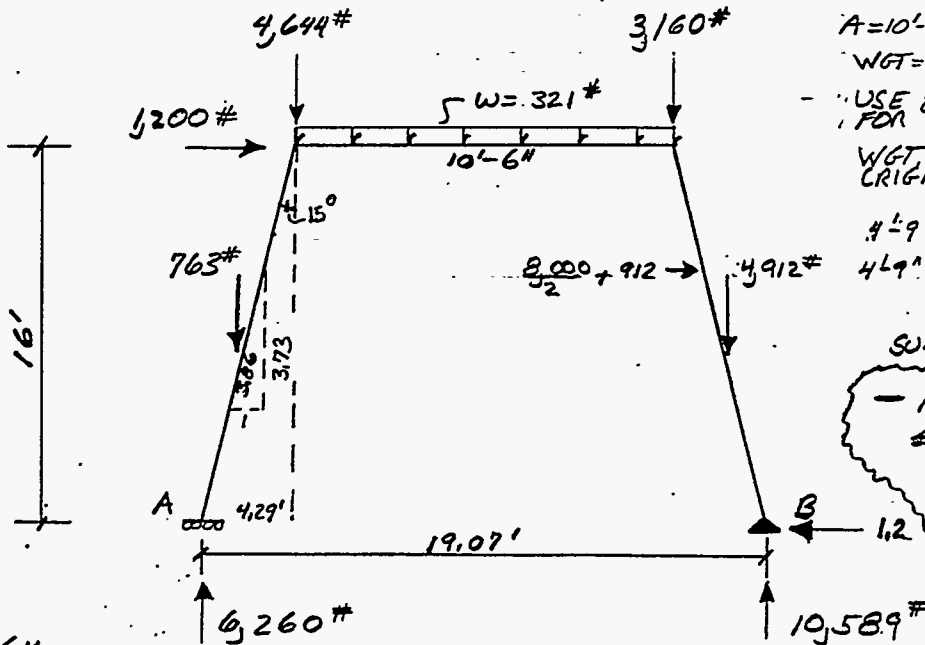
6x6x1/4 ST 76 LN FT  
WGT = 1,445 #

DISTRIBUTE TO 4 CORNERS  
361 #/CORNER

FREE BODY DIAGRAM

WGT. OF SIDE SUPPORT (LEFT)  
19'-6" 6x6x3/8 TS @ 27.48 #/ft = 536 #  
8' OF 5x5x1/2 TS @ 28.43 #/ft = 227  
SUM = 763 #

- 1) LOOK @ ONE SIDE OF SUPPORT & ANALYSE WORST CASE.
- 2) UNIFORM LOAD ON TOP BEAM IS FROM 3' TRIBUTARY AREA OF PLATFORM.



- WGT OF STEEL PLATE RIGHT SIDE

$A = 10'-4" \times 8'-9\frac{3}{4}" = 91 \text{ ft}^2$   
WGT =  $91 \cdot 87 = 7917 \#$

- USE 8000 # TO ACCT FOR MISC. WGT.

WGT. OF SIDE SUPPORT (RIGHT) 763 #

4'-9" TS 6x6x3/8 = 130 #  
4'-9" L 2 1/2 x 2 1/2 x 1/4 @ 4.1  
19 #

SUM RIGHT = 912 #

- FOR NO WIND  
 $\sum M_A = 0$  = SAME EQ MINUS WIND FACTOR

$R_B = 9,582 \#$   
 $R_A = 7,266 \#$

$\sum M_A = 0$

$1,200(16) + 763(2) + 4,644(4.29) + 321(10.5) + 3,160(14.78) + 4,912(16.78) = R_B(19.07)$   
 $R_B = 10,589$   
 $R_A = 6,260$

ANALYTICAL CALCULATIONS

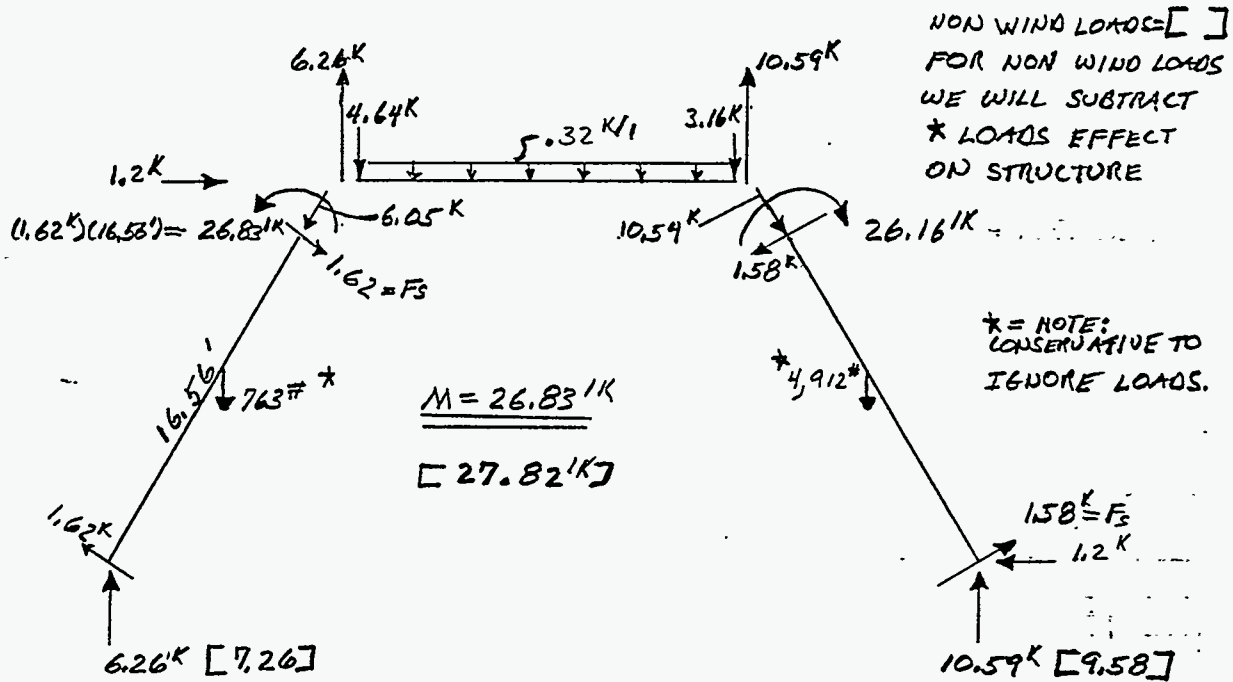
Subject LEAD SHOT SUPPORT ASSEMBLY

Originator RF NORMAN

Date 5-5-94

Checker Gregory Johnson / TW Fisher

Date 9/28/94



$$F_A = \frac{3.73}{3.86} (6.26) = 6.05 \text{ K} \quad [7.01 \text{ K}]$$

$$F_S = \frac{1}{3.86} (6.26) = 1.62 \text{ K} \quad [1.68 \text{ K}]$$

$$F_A = \frac{1}{3.86} (1.2) + \frac{3.73}{3.86} (10.59)$$

$$F_A = 10.54 \text{ K} \quad [9.25 \text{ K}]$$

$$F_S = \frac{1}{3.86} (10.59) - \frac{3.73}{3.86} (1.2)$$

$$F_S = 1.58 \text{ K} \quad [1.47 \text{ K}]$$

CHECK LOADS SEEN BY 6X6X3/8 TS      $A = 8.08 \text{ in}^2$       $S = 13.9 \text{ in}^3$       $r = 2.27 \text{ in}$

COMBINED WORSE CASE LOADS FROM EACH LEG. (CONS)

$$P_b = M/S = 26.83(12) / 13.9 = 23.16 \text{ Ksi} \quad [24.01]$$

$$F_b = .6(CF_y) = .6(46) = 27.6 > 23.16 \text{ } \therefore \text{OK}$$

$$F_a = 10.54 \text{ K} / 8.08 = 1.31 \text{ Ksi} \quad [1.18 \text{ Ksi}]$$

$$F_a = K/r = (1.2)(10)(12) / 2.27 = 63.45$$

COMPARE W/ A-36 STEEL - AISC 9th edition (PG 3-16)

$$F_a = 17.04 \text{ Ksi}$$

COMBINED LOADS

WIND -  $23.16 / 27.6 + 1.3 / 17.04 = 0.92 < 1.33$  (INCLUDES 1/3 INCREASE FOR LATERAL LOADS)

NO WIND -  $24.01 / 27.6 + 1.18 / 17.04 = 0.94 < 1.0$

USE 6X6X3/8 TS FOR SIDE SUPPORTS

**ANALYTICAL CALCULATIONS**

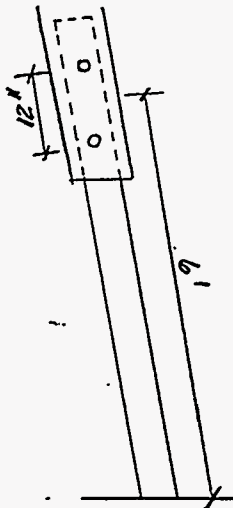
Page 8 of 14

Subject LEAD SHOT SUPPORT ASSEMBLY

Originator B F NORMAN Date 5-6-94

Checker (w) Fickel Date 9-28-94

CHECK 5X5X1/2 TS (TELESCOPING INSIDE 6X6X3/4)



↓ PG# 7  
MOM ON BOLTS  $M = 6'(1.68) = 10.08 \text{ K}'$   
2 BOLTS = FORCE COUPLE =  $10.08 \text{ K}' / 1' = 10.08 \text{ K}$   
← 10.08 COUPLE

→ 10.08  
Force axial = 10.54 K  
ASSUME ONE BOLT TAKES ALL AXIAL LOAD

$f_r = [(10.54)^2 + (10.08)^2]^{1/2} = 14.58 \text{ K}$

TRY 3/4" Ø A325 BOLTS (AISC 9th ed pg 4-5)

BOLTS ARE IN DOUBLE SHEAR

$F_{\text{SHEAR}} = 18.6 \text{ K}$  PER BOLT → (CONS USE N TYPE BEARING CONNECTION)

$F_{\text{TEN}} = 19.4 \text{ K}$  (NOMINAL DIAMETER) — (NO TENSION PRESENT)

$F_{\text{SHEAR}} = 14.58 \text{ K} < 18.6 \text{ K}$  OK USE 3/4" Ø A325 BOLTS

CHECK 5X5X1/2 ST

- TAKE REACTION FROM TOP OF 6X6 TS & TRANSFER TO 5X5

↓ PG. 7  
 $M(1.68)(10') = 16.8 \text{ K}$

$F_b = M/S = 16.8(12) / 108 = 18.66 \text{ KSI}$

$F_b = 1.6(46) = 27.6$  (NO LATERAL LOAD ADDITIVES) CONS.

$> 17.66 \therefore \text{OK}$

$f_a = 10.54 / 8.36 = 1.26 \text{ KSI}$

$F_a = K L / r = 2.0(6)(12) / 1180 = 80$

COMPARE W/ A-36 STEEL ALLOWABLES

$K L / r = 80 \quad F_a = 15.36$  (AISC 9th ed)

COMBINED LOADS

$18.66 / 27.6 + 1.26 / 15.36 = 0.76 < 1.0 \therefore \text{OK}$  (NO LATERAL LOAD ADDITIVES) (CONS)

USE 5X5X1/2 TS FOR TELESCOPING SUPPORTS

**ANALYTICAL CALCULATIONS**

Subject LEAD SHOT SUPPORT ASSEMBLY

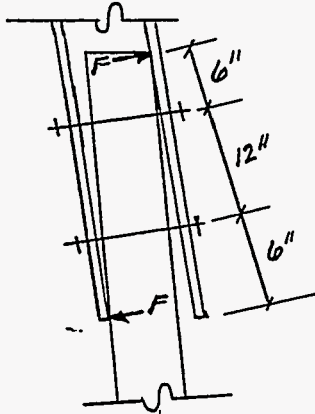
Originator BF NORMAN

Date 5-7-94

Checker TU Fife

Date 9-28-94

CHECK INTERNAL BENDING DUE TO TELESOPING MEMBERS



- WORST CASE ANALYSIS

- CHECK PUNCHING SHEAR  $F = 10.08^k$  FROM PG 8

AREA OF CONTACT = 5" x 1" OF TUBE FACE

$$f_v = P/A = 10.08 / 5 (3/8" \text{ TUBE WALL}) = 5.38$$

$$F_v = .4(CF_y) = 18.4^k$$

$$18.4^k > 5.38^k$$

∴ OK IN SHEAR

CHECK HORIZONTAL TS WITH R RESTING ON IT

$$\text{SIDE R} \rightarrow 104" \times 8'-9\frac{3}{4}" = 9152 \cdot 87 = 7,917 \#$$

$$\text{WGT PER LNIFT} = 766 \#/\text{LNIFT}$$

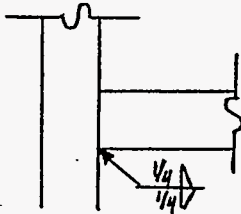
- MEMBER'S FIXED @ EACH END  $M = wL^2/12$

$$= 766 (9.5)^2 / 12 = 5,761 \#$$

$$P_b = M/s = 5,761 (12) / 139 = 4,973 \text{ psi}$$

$$F_b = .6(CF_y) = 27.6 \rightarrow 4.97 \text{ ∴ OK FOR BENDING}$$

- CAPACITY OF WELD JOINT



5"  
6"

$$s_w = b d = 30$$

$$A_w = 10"$$

$$P_b = M/s = 4,973 (12) / 30 = 1,989 \text{ psi}$$

$$f_y = 3,958 / 10 = 395.8 \text{ lbs/inch}$$

$$f_r = [(1,989)^2 + (395.8)^2]^{1/2}$$

$$f_r = 2,028 \#/\text{in}$$

TRY 1/4" FILLET  $(.3670,000)$  E70 ELECTRODES

$$1707 (21,000 \times .25) = 3,712$$

$$3,712 > 2,028$$

USE 1/4" FILLET TOP & BOTTOM

ANALYTICAL CALCULATIONS

Subject LEAD SHOT SUPPORT ASSEMBLY

Originator BF NORMAN

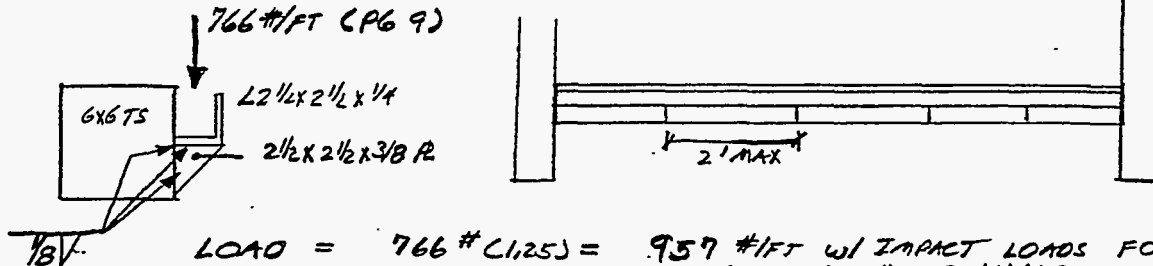
Date 5-7-94

Checker Y W Feltz

Date 9-28-94

CHECK 2 1/2" ANGLE USED AS SHELF SUPPORT FOR PLATE

- ANGLE WILL BE TOTALLY WELDED ALONG BOTTOM EDGE
- GUSSET PLATES 2 1/2 x 2 1/2 x 3/8 R



LOAD = 766 # (1.25) = 957 #/FT W/ IMPACT LOADS FOR ENTIRE LENGTH OF ANGLE

- USE 2' SPACING FOR GUSSETS

$A = 1.19 \text{ in}^2$   
 $S = 1.394 \text{ in}^3$

$M = wL^2/8 = 47.9 \text{ l}\#$

$f_b = M/S = 47.9 \text{ l}\# (12) / 1.394 \text{ in}^3 = 14,599 \text{ psi}$

$(6)(36) = F_b = 216 \text{ Ksi} > 14.6 \text{ Ksi} \therefore \text{OK}$

- TRY 1/8" FILLET WELD ALL ALONG BOTTOM

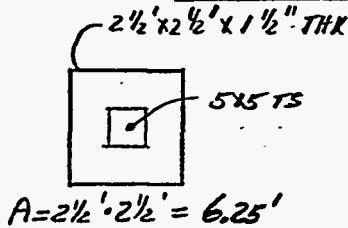
- LOAD =  $957/12 = 80 \text{ \#/in}$

$1/8" = .707 (21,000) (1/8) = 1,856 \text{ \#/in}$

GUSSET R  
LOAD = 2W  
= 1,914 #  
- USE 1/8" WELDS  
MIN 2" LENGTH  
GUSSET R IS  
OK BY ENGINEERING  
JUDGEMENT

USE 1/8" WELD ALONG BOTTOM AROUND GUSSET R

CHECK BOTTOM PLATE



CHECK SHEAR 10.54 K (PG #7)

$A = 1.5 (20) = 30 \text{ in}^2$  PUNCTURE SHEAR AREA

$F_u = 351 \text{ psi}$

$f_v \ll F_v$  For  $F_y = 36 \text{ Ksi}$

- CHECK BENDING

- SUPPOSEDLY NO MOMENT SINCE MOMENT IS BEING RESISTED BY TOP CONNECTION

- (CONS) USE FULL MOMENT ON R

$M = 27.82 \text{ l}\#$       $S = 1/6 (2'-6") (1.5)^2 = 11.25 \text{ in}^3$

$F_b = .75 (36) = 27 \text{ Ksi}$

$f_b = 27.82 \text{ l}\# (12) / 11.25 \text{ in}^3 = 29.67 \text{ Ksi} > 27$

NEW  $F_b$

$(27)(1.33) = 36 \text{ Ksi} > 29.67 \therefore \text{OK}$  PLATE IS OK FOR APPLIED MOMENT

- CHECK SOIL PRESSURE

$10.54 \text{ Ksi} / 6.25 \text{ ft}^2 = 1,686 \text{ PSF} < 2,000 \text{ PSF}$

SOIL BEARING PRESSURE IS OK.

ANALYTICAL CALCULATIONS

Subject LEAD SHOT SUPPORT ASSEMBLY  
 Originator BF NORMAN Date 5-17-94  
 Checker [Signature] Date 9-28-94

PLATE CONNECTIONS BETWEEN PLATFORMS & POSTS

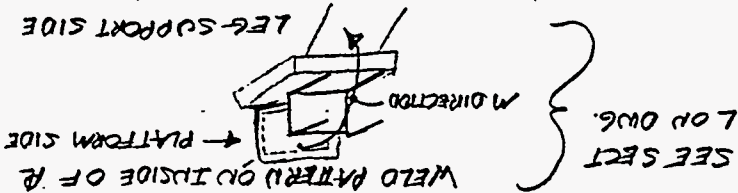
(OUT H-2-B3738 SH #2) SECTION K L & DETAIL 1  
 - USE 1" PLATE FOR CONNECTIONS  
 $M = 27.821K$  (PG. #7)

5 PL VERTICALS  $S = 1/6 C^3 = 1/6 (1")^3 = 1/6 C^3 = 5 = 4.166$  PLATE  
 5 PL HORIZONTAL TOP  $1/6 (6) C^3 = 1.0$   
 5 PL HORIZONTAL BOTTOM  $1/6 (7) C^3 = 1.166$   
 5 PL VERTICAL BACK  $1/6 C^3 (6)^2 = 6.0$   
 $S_{TOTAL} = 2C(4.166) + 1.0 + 1.166 + 6.0$   
 $S = 16.49$

- S AS SUM OF THE INDIVIDUAL PIECES. (MOST CONSERV)
- IF STRENGTH OF WELDS ARE ADEQUATE THEN
- ANALYZE END CONFIGURATION AS A HOLLOW RECTANGLE

$- S = b d^3 - b' d'^3 = 6 (7)^3 - 4 (5)^3 = 3709$   
 $\frac{6d}{6 (7)} = 1$

$f_b = M/S = (27.82) (12) / 37.09 = 9.000$  psi  
 $f_b = .75 (F_y) = 27.6$  ksi > 9.0 ksi ∴ OK



CHECK WELDS

TWO SEPARATE WELDS [ + ] TO GET TOTAL REQUIRED STRENGTH

$S_w = b d + d^2/6 = 6 (5) + 25/6 = 34.16$   
 $S_{TOT} = 2 (34.16) = 68.33$

$f_b = M/S = 27.82 (12) / 68.33 = 4.885$  psi  
 $weld r = 4.885 / 1.07 (2) = 0.329$   
 $3/8" = 0.375 > 0.329$

USE 3/8" WELD FOR PL.

\* WE ALSO HAVE EXTERNAL WELDS WHICH WILL HELP TO MOMENT & SHEAR CAPACITIES.  
 ∴ OK



ANALYTICAL CALCULATIONS

Subject LEAD SHOT SUPPORT ASSEMBLY  
 Originator BF NORMAN Date 5-17-94  
 Checker TW Felt Date 9-28-94

LIFTING LUG ANALYSIS

WGT OF PLATFORM

78' OF 6X6X 1/4" @ 19.02	=	1,484
87' OF 6X6X 3/8" @ 27.48	=	2,391
32' OF 5X5X 1/2" @ 28.43	=	910
25' OF 1 1/2" R @ 61.26	=	1,532
7' OF 1" R @ 40.84	=	286

LIFTING LUGS ARE  
@ 4 CORNERS OF

SUM = 6,603

PLATFORM (SEE DWG H-2-83738 FOR LOCATION)

2 LIFTING LUGS TO SUPPORT LOAD = 3,302 #/LUG

CHECK PLATE

$f_b = m/s$

$M = PL/4 = 3,302(6)/4$   
 $M = 4,953 \text{ "#}$

$f_b = 4,953 \text{ psi}$

$S = 1/6 (6)(1)^2 = 1.0$

$f_b \ll F_b \therefore$  PLATE IS OK

USE 5,000# LOAD RATED HOIST RING

MIN. RATING  
REQUIRED FROM  
CERTIFIED LIFTING  
LUG VENDOR.

TOP PLATFORM (H-2-83738 SH3)

$10'-5" \times 10'-5" = 110.25 \text{ - 4 (HOLE OPENING)}$

$WGT = 81.68(106.25) = 8,679 \text{ #}$

TOTAL WGT = 8,679 #

LOAD ACTS OVER TWO LUGS

$\#/LUG = 4,339 \text{ #}$

USE 10,000# LOAD RATED HOIST RING

\* SAME FOR SIDE 2" STEEL PANEL \*

USE 10,000# LOAD RATED HOIST RINGS FOR SIDE PLATE

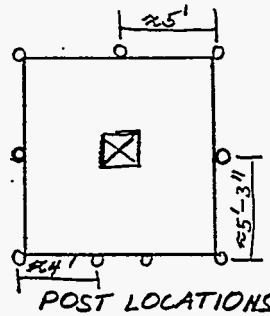
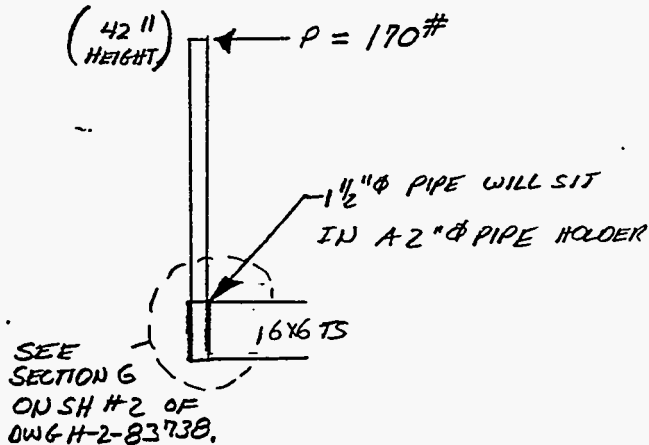
ANALYTICAL CALCULATIONS

Subject SHOT PLATFORM ASSEMBLY  
 Originator B F NORMAN Date 4-13-94  
 Checker J W [Signature] Date 9-28-94

HR 1

HARD RAIL POST SUPPORTS [SEE H-2-83738 SH #2, 4]

- USE VERTICAL SUPPORTS 6' SPACING MAX
- HORIZONTAL BARS
- WITHSTAND 200 # LATERAL FORCE @ TOP RAILING
- TOP OF GUARDRAIL MIN 42" ABOVE FLR.
- DESIGN SO SPHERE 12" CANNOT PASS THROUGH



- DESIGN SIDE POST RAILINGS FOR TWO SPAN SITUATION
- END POST OF 2 SPAN = 85% OF APPLIED LOAD (SEE ATT #.B)

$$P = 200 \cdot 85 = 170 \#$$

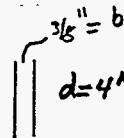
- USE A 500 B. SCHED 40 PIPE  $\rightarrow$  USE SCHED 80 FOR HANDRAILS, HAVE MATERIAL AVAILABLE
- TRY 1 1/2" PIPE  $S = .326$   $A = 2.72$   $I = .310$  (CONS. #5)

$$F_b = M/S = 170(42) / .326 = 21,902 \text{ psi}$$

$$F_b = .6(46) = 27.6 \quad 27.6 > 21.9 \therefore \text{OK}$$

USE 1 1/2" SCHED 40 PIPE

- CHECK WELDS
- WELD ALONG BOTH SIDES OF PIPE



$$S_w = d^3/3$$

$$S_w = 16/3 = 5.33$$

$$F_b = M/S = 170(42) / 5.33 = 1,340 \text{ psi}$$

$$\text{WELD REQUIRED } 1,340 / (2)(.707) = 0.09"$$

USE 3/16" FLAME BEVEL WELD MIN BOTH SIDES OF TUBE

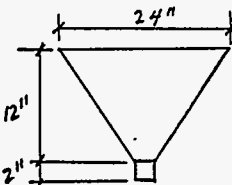
ANALYTICAL CALCULATIONS

Page 14 of 14

Subject LEAD SHOT SUPPORT ASSEMBLY  
 Originator BF NORMAN Date 5-20-94  
 Checker [Signature] Date 9-28-94

FUNNEL ANALYSIS

- FUNNELS WILL BE MADE OUT OF STAINLESS STEEL . 16
- DIMENSIONS WILL BE 12" HIGH AND 24"  $\phi$  OPENING ON TOP TO A TWO INCH OPENING ON BOTTOM - MAX SIZE, SOME FUNNELS WILL BE SMALLER. (BY ENGINEERING JUDGEMENT)
- $F_y = 30,000 \text{ psi}$   $F_u = 80,000 \text{ psi}$
- LEAD SHOT = 450 #/cu FT (CONS -  $\approx 430 \text{ #/cu FT}$ )
- STAINLESS ST = 304 #/cu FT



$$\begin{aligned} \text{VOLUME OF FUNNEL} &= \pi/12 h (R^2 + Dd + d^2) \\ &= \pi/12 (12) (24^2 + 2(24) + 2^2) \\ &= 1,973 \text{ in}^3 \rightarrow 1.14 \text{ ft}^3 \end{aligned}$$

$$\text{WGT} = 1.14 (450) = 513 \#$$

IMPACT LOAD 25% - APPLY LOAD FOR DROP INTO FUNNEL  
 LOAD = 642 #

FUNNEL CAN ALSO ATTACH TO A 4" COUPLING. LOADS CHANGE SLIGHTLY BUT CLASSIFY OR BY ENGINEERING JUDGEMENT

LOAD ACTS OVER AN AREA OF 10 in<sup>2</sup> @ BOTTOM OF FUNNEL, APPLY THAT LOAD TO TOP OF FUNNEL FOR ANALYSIS (CONS)

$$P = 642 / 10 = 64.2 \text{ lbs/in}^2$$

hoop stress =  $P r / t$  USE MINIMAL  $F_b$  AFTER WELDED

$$\sigma = .6 (30) = 18,000 \text{ psi}$$

$$t = 64.2 (12) / 18,000 = 0.0428 \text{ " } \Rightarrow \text{USE MIN. 18 GAUGE MATERIAL}$$

AREA OF FUNNEL SHELL

$$\pi/2 (17)(24+2) = 694 \text{ in}^2 = 4.82 \text{ ft}^2$$

WGT OF FUNNEL W/ 18 GAUGE WALLS

$$4.82 \cdot 0.0428 / 12 = 0.0172 \text{ ft}^3$$

$$\text{WGT} = 8.66 \# \text{ MINIMAL WGT}$$

- CSP WELDS FOR TWO SIDE PIECES & WELD TO 2" STAINLESS STEEL PIPE 2" LONG.
- PLATE MATERIAL WILL THEN GOVERN FOR BENDING.
- ASSUME 6" OFFSET FOR LOAD  $M = 642 (6) = 3,852 \text{ " #}$   
 $S = 3.14 \text{ in}^3$   $F_b = 3,852 / 3.14 = 1,226 \text{ psi} < 18,000 \text{ psi}$

D. B. Calmus  
Page 3  
September 7, 1993

22570-HJG-019

The problem was run utilizing the program ISOSHL on a Cray mainframe computer. The hardware was modeled as a cylinder of waste of density  $\rho=1.2 \text{ g/cm}^3$ , surrounded by a cylinder of air, two shielding cylinders, and a steel cylinder whose thickness equaled the sum of the two packages. The shielding cylinders were run as an inner cylinder of lead and an outer cylinder of air. The thicknesses of these two cylinders were varied from all air to almost all lead. In all cases, the thickness of these two cylinders combined remained the same. The exposure rate was taken at the center of the length of these cylinders at the outer surface.

### The Results

ISOSHL Results			
Results are in rem/hr rather than the Sv/hr required by WHC.			
Lead Thickness (cm)	106-C	106-C	102-AY
	Heel Pump	Transfer Pump	Agitator Pump
No Lead	1.130	0.1458	0.07419
0.5	0.5840	0.0741	0.03631
1.0	0.3036	0.03800	0.02129
1.5	0.15907	0.01969	0.01326
2.0	0.08437	0.01036	0.008543
2.5	0.04552	0.005556	0.005634
3.0	0.02511	0.003053	0.003780
3.5	0.01422	0.001724	0.002568
4.0	0.008291	0.001003	0.001763
4.5	0.004983	0.0006026	0.001292
5.0	0.003088	0.0003731	0.0008491
5.5	0.001969	0.0002377	0.0005946
6.0	0.001287	0.0001552	0.0004185
6.5	0.0008597	0.0001036	0.0002958
7.0	0.0005844	0.00007034	0.0002098
7.5	0.0004028	0.00004843	0.0001494
8.0	0.0002808	0.00003372	0.0001067

APP A.

# Designing Metal Guard and Hand Rails

by William Thurnauer  
Julius Blum & Company

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## Design Considerations:

There are five major considerations in the structural design of railings:

- Structural loading and dimensional criteria as established by local building codes, regulatory agencies or special design requirements.
- Mechanical properties of handrail materials and their allowable design stresses.
- Elements of sections of railing components.
- Load stress and deflection relationships as expressed in formulae for engineering design.
- Proper attachment and sound supporting structure.

## Code Requirements

Local building code requirements for dimensions and loading of railings can vary greatly. For most applications (except low rise residential buildings) OSHA requirements must be complied with. They state that railings "shall be capable of withstanding a load of at least 200 lbs. applied in any direction at any point of the top rail." Local building codes take precedence when established structural loading criteria exceed OSHA requirements.

The absence of uniform loading criteria among building codes is partly due to the wide range of applications and traffic exposures and partly due to the absence of objective data from which reliable or generally acceptable live loading factors can be determined.

An ambiguity also arises from the OSHA phrase "withstanding a load." This phrase may be interpreted conservatively as the design limit based on allowable stress of the material. However, most railings built to conventional standards and demonstrated to

be safe in many years of use do not conform under that interpretation.

Often, the OSHA standard is interpreted to mean that a railing must not fail totally under the specified loading but that a permanent deformation may be tolerated. The theory is that a railing, even though somewhat deformed, still provides safety and can be repaired if need be.

The more conservative interpretation may well result in overdesign and higher cost, but the more liberal interpretation, in case of a failure involving injury to persons, might lead to serious problems of liability. Thus, until the expression "to withstand a load" is either changed or officially defined, the more conservative interpretation should be applied.

## Mechanical Properties of Materials and Allowable Stresses:

To provide proper safety factors, the engineering profession assigns to each metal an allowable design stress which is defined as the minimum yield strength divided by 1.65. "Minimum strength" is defined as the test value exceeded by 99% of a large number of specimens. The "yield point" for

metals other than carbon steel is indeterminate and therefore, according to ASTM, it is arbitrarily defined as the point of stress at which permanent set is 0.2% of gauge length of the test piece (see Figure A).

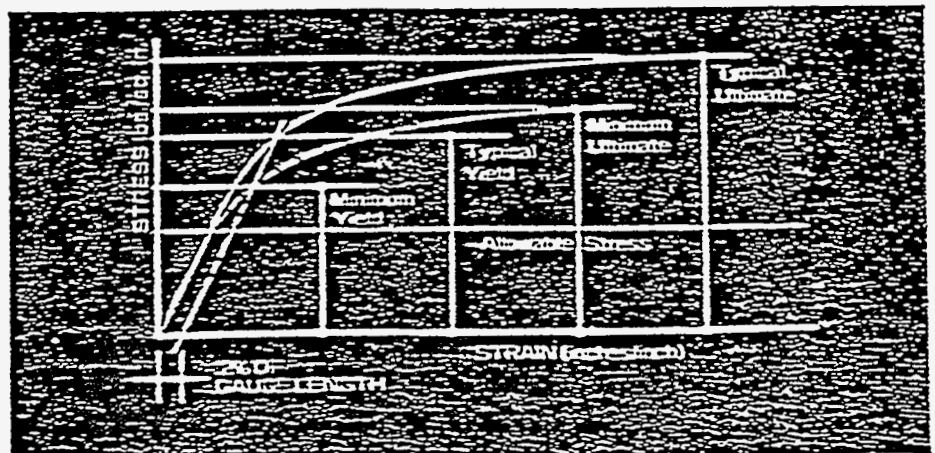
This rule applies to metals such as aluminum, bronze and stainless steel which are commonly used in railings. Mechanical properties of materials used in metal guard rails and handrails are shown in Figure B.

## Elements of Sections

Properties of many sizes of bars, shapes, pipe and tubing used in railing construction can be found in tables issued by industry associations and by some of the suppliers of these products. For proprietary sections such as handrail mouldings and ornamental railing posts check manufacturers' catalogs. Figure C lists the engineering properties of a few sizes of pipe commonly used for railings in steel, aluminum, bronze or stainless steel.

## Railing Formulae

The loading characteristics of any specific railing design can be computed, given the mechanical properties



of the material, the engineering properties of the structural components and the dimensions, including post height and post spacing (rail spans) of the completed structure. The formulae follow conventional engineering design procedures. Stresses are calculated from bending moments and section properties, using the flexure formula (explanation of symbols shown in Figure D):

$$f = \frac{M \times c}{I} \text{ or } \frac{M}{S}$$

**Posts**

Posts act as vertical cantilever beams in resisting horizontal thrust applied at the top rail. Bending moments produced by horizontal thrust normally controls design, and stresses may be calculated by the formula:

$$f = \frac{w/12 \times L \times h}{S} \text{ for uniform loading}$$

or

$$f = \frac{F_H \times h}{S} \text{ for concentrated loading}$$

**Rails**

Distribution of loads through multiple spans decreases maximum bending moment in horizontal members. Calculation of stresses for different numbers of spans is accomplished by varying the bending moment constant. The following formulae apply:

For uniform vertical or horizontal loads:

$$f = \frac{w/12 \times L^2}{S \times K}$$

K = 8 for one or two spans

K = 9.5 for three or more spans

For concentrated loads, applied at mid-span:

$$f = \frac{F \times L}{S \times K}$$

K = 4 for one span

K = 5 for two or more spans

Any of these equations can be solved for allowable load, post spacing or rail span, or for the required metal properties or section modulus. (For the purpose of these calculations it is assumed that connections between posts and rails are free of pivot and that railings run in a straight line.)

**Load Distribution**

In most railing installations, the load applied to the rail at any one post is distributed in part to other posts on either side of the post under loading. Therefore, in many instances, railing posts may be designed for an allowable load (F<sub>a</sub>) which is less than the total required loading of the railing.

Load distribution is dependent on the stiffness of the rail relative to the stiffness of the posts and on the total number of spans in the run. For a straight run of railing, the load proportion factor may be determined from the graph in Figure E, once the stiffness ratio has been calculated.

The formula used in determining this graph assumes that all posts are of identical material and section. If one or both ends of the railing are free standing, the "end loaded" condition must be assumed. If both ends of the run are laterally braced by a change in direction or attachment to a firm structure, the "center loaded" load proportion factor may be used.

In pipe railings, where posts and rails are of identical material and section

(continues on next page)

Material	Allowable Stress (psi)	Minimum Yield (psi)	Modulus of Elasticity (psi x 10 <sup>6</sup> )
Aluminum 6061-T6	21,000	35,000	10.0
Aluminum 6061-T6 (pipe)	24,000*	35,000	10.0
Aluminum 6053-T52	9,500	16,000	10.0
Aluminum 6053-T52 (pipe)	11,500*	16,000	10.0
Aluminum 6053-T6	15,000	25,000	10.0
Aluminum 6053-T632 (pipe)	24,000*	35,000	10.0
Bronze alloy 385;	11,500	19,000	14.0
Red Brass alloy 230 (annealed pipe)	7,200	12,000	17.0
Red brass alloy 230 (drawn square and rectangular tubing)	11,000	18,000	17.0
Type 304 Stainless Steel (annealed)	18,000	30,000	28.0
Type 304 Stainless Steel Tubing (as welded)	30,000	50,000**	28.0
Carbon Steel Structural Tubing ASTM A500 Grade B	25,500	42,000	29.0
Carbon Steel C1010	17,000	28,000	29.0
Elyria Steel Structural Tubing ASTM A370	30,000	50,000	29.0
Acrylic Wood	3,750	4,975	1.8

\* Allowable = min. yield x 1.17 = 1.55 (Ref. ASCE and Alum. Assn.)  
\*\* Guaranteed by producing manufacturers of Stainless Tubing.

Figure B

Nominal Pipe Size	OD	ID	Thickness	Area	I	S
SCHEDULE 5						
1 1/4"	1.660	1.530	.055	.326	.104	.125
1 1/2"	1.900	1.770	.055	.375	.158	.165
SCHEDULE 10						
1 1/4"	1.660	1.442	.109	.531	.161	.193
1 1/2"	1.900	1.552	.109	.614	.247	.250
SCHEDULE 40						
1"	1.315	1.049	.133	.494	.057	.133
1 1/4"	1.660	1.350	.149	.659	.195	.235
1 1/2"	1.900	1.510	.145	.800	.210	.225
2"	2.375	2.057	.154	1.075	.655	.551

Figure C

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and where post spacing usually varies between 3 feet and 6 feet, load distribution is fairly uniform and the greatest proportion of a concentrated load carried by any one post can be estimated as follows:

- End posts:
  - of a 2 span railing — 85%
  - of 3 or more spans — 82%

- Intermediate posts:
  - of a 2 span railing — 65%
  - of 3 or more spans — 60%

Thus, if a 200 lb. concentrated load is specified, actual design load to be applied at the top of the end post is 82% of 200 lbs. or 164 lbs; design load to be applied to intermediate posts is 60% of 200 lbs. or 120 lbs.

*Note: If end posts differ from intermediate posts in strength, the load distribution pattern becomes indeterminate and end posts should then be designed to carry 100% of the concentrated load. Intermediate posts may then be designed to the "center loaded" condition.*

In single span railings, each post must be designed to carry the full concentrated load.

The stiffness of a rail or post is:

$$k = \frac{E \times I}{L} \text{ for the rail}$$

$$k = \frac{E \times I}{h} \text{ for the post}$$

Stiffness ratio is determined as:

$$R = \frac{k_{\text{rail}}}{k_{\text{post}}} = \frac{\frac{E \times I}{L}}{\frac{E \times I}{h}}$$

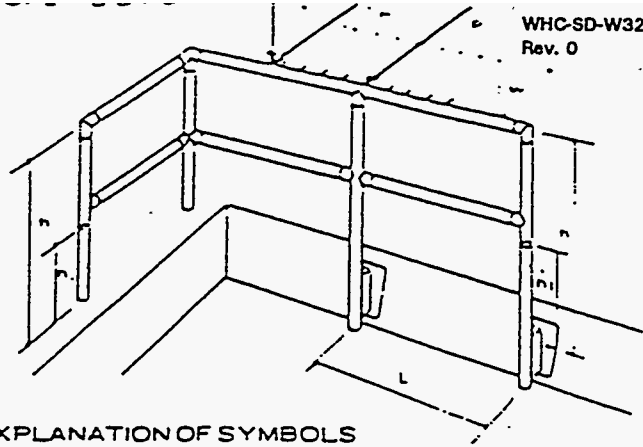
The stiffness ratio (R) is then plotted on a graph to obtain Load Proportion Factor (P<sub>f</sub>). (See Figure E). When the load proportion factor has been determined, it is multiplied by the total load to determine the load one post must sustain.

*(The Figure E graph has been determined by computer analysis and confirmed by laboratory test.)*

### Load Tests

In a typical test of a railing designed by the above method, permanent deformation will occur at about twice the design load, and failure will usually occur at about 2½ times the design load.

*(continued on next page)*

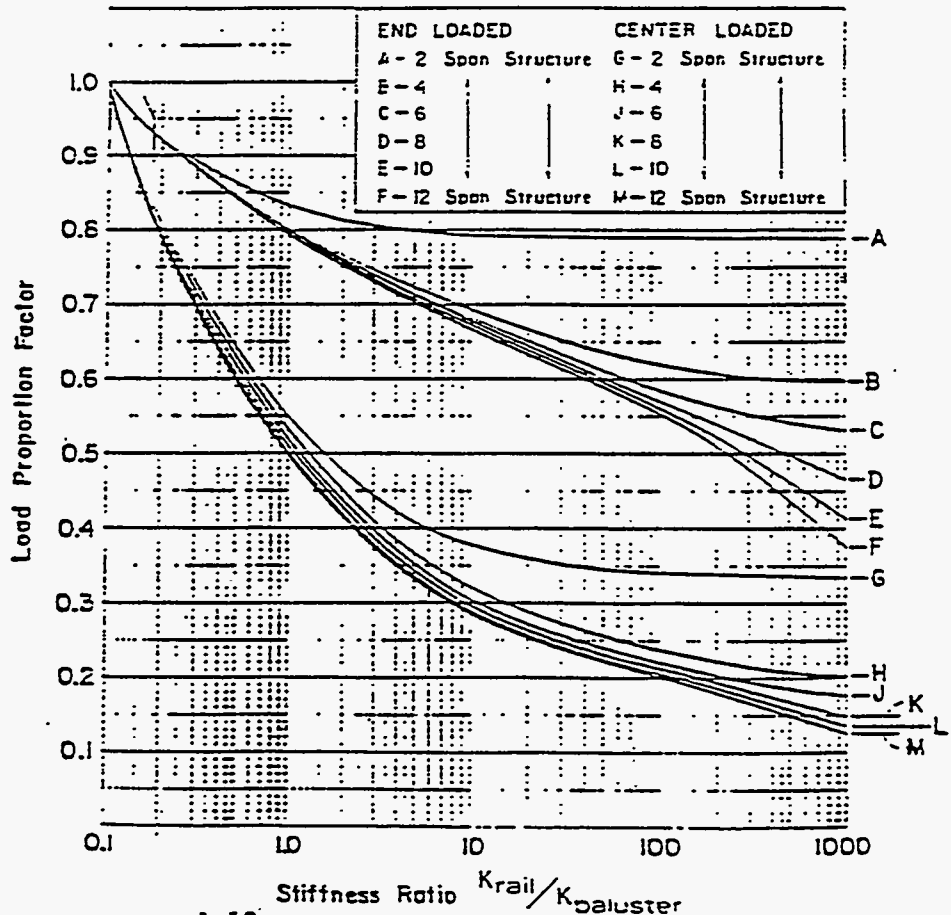


### EXPLANATION OF SYMBOLS

- w = Uniform horizontal loading, lbs/ft (perpendicular to the rail).
- L = Span between centerlines of posts, or brackets (inches).
- F = Horizontal force, perpendicular to rail applied at top of post (lbs).
- F<sub>H</sub> = Horizontal force, perpendicular to rail at any point along the railing (lbs).
- F<sub>V</sub> = Vertical force, perpendicular to rail at any point between posts (lbs).
- h = Height of post. Distance from point of load application above top of attachment (in).
- M = Bending moment (in. lbs.)
- f = Unit stress (psi.)
- f = Allowable fiber stress for design (psi.)
- S<sub>x</sub> = Section modulus (in.<sup>3</sup>)
- I = Moment of inertia (in.<sup>4</sup>)
- k = Stiffness of member
- K = Bending moment constant
- c = Distance from the neutral axis to the extreme fiber of any section (in.)
- E = Modulus of elasticity (psi.)
- Δ = Deflection (in.)

NOTE: Values for "w" (uniform load in lbs./ft.) are converted to lbs./in. by dividing by 12.

Figure D





## Deflection Considerations

Despite an absence of deflection criteria for railings, elastic deflection under load should be considered by the designer. Even though installations meet strength requirements, excessive deflection under load can produce a psychological feeling of structural inadequacy. On the other hand, a certain ductility in the rail helps to absorb the shock of an impact. Where there is no ductility, as in a concrete railing, the shock of an impact is much greater and there is increased risk of a person being injured by a fall against the rail.

In a recent government research project which attempted to determine the impact of a falling human body on a guard rail, ductility of the rail was not considered and the test set-up was of a completely rigid design. Accordingly, the test results showed unreasonably high impact loads and the loading criteria recommended by that agency were far beyond accepted practice and reasonable economics.

The decision of how much elastic deflection is reasonable is left with the designer. Lateral deflection of posts and horizontal or vertical deflection of rails are computed as follows:

For posts:

$$\Delta = \frac{w/12 \times L \times b^3}{3 \times E \times I} \text{ or } \frac{P \times b^3}{3 \times E \times I}$$

For rails:

Concentrated load at center of span:

$$\Delta = \frac{F \times L^3}{48 \times E \times I}$$

Uniform loading:

$$\Delta = \frac{5 \times w/1q \times L^4}{384 \times E \times I}$$

## Conclusion

It is important to keep in mind that the engineering calculations apply only to the structural members of the railing itself and that a number of other factors are essential to a safe railing which complies with codes and regulations:

- Connections within the railing, whether welded or mechanical, must be properly designed and executed.
- Ends and changes of direction must be properly supported, avoiding excessive overhang and unsupported turns.

- Mounting hardware, such as brackets, floor flanges and fascia flanges must be so designed as to sustain whatever load they may normally be subjected to. Test reports should be available from the manufacturers of these parts.

- Fasteners, used for anchoring must be of the proper size and type for the required loading and must be corrosion resistant if exposed to the elements or to corrosive conditions. The manufacturer of proprietary anchoring devices usually publishes tables of allowable loads and applicable factors of safety.

- The supporting structure must be sound so as to provide proper anchorage for the railing and give it adequate support.

Engineering design is only one phase in the construction of a safe railing. Good workmanship, suitable accessories and proper installation on a sound supporting structure are all essential. Failure in any one of these areas may cause serious problems.