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STRUCTURE AND PHASE TRANSFORMATIONS IN URANIUM METAL

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ABSTRACT

In common with other elemental actinides, metallic uranium exists in several allotropic forms, differing from one another by complex but subtle atomic rearrangements. This article reviews progress in understanding the successive phase transformations from the perspective of soft-mode instabilities.

I. Soft Mode Phenomena.

Certain structural phase transformations in solids result from a vibrational instability in the material. These are termed 'soft-mode' displacive transformations and the associated soft mode concept provides a unifying perspective.[1,2] This idea, combined with simple symmetry arguments and free energy considerations, provides a useful tool by which phase behavior of materials can be systematized and understood at the phenomenological level.

Any phase transformation can be characterized by an *order parameter*, a quantity which is non-zero in one of the phases but which vanishes in the other. Order parameters for displacive phase transformations are defined in terms of what may be called a phonon expansion,

$$u_{lk}(t) = \sum_{q,j} \xi_k(qj) Q_{qj}(t) e^{iq \cdot l}. \quad (1)$$

The displacement of the k'th atom in the l'th unit cell is decomposed into normal modes which are plane waves with a wave vector q and a branch label j. (There

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are three acoustic branches and $3N-3$ optic branches, if there are N atoms in the unit cell). Each mode has a polarization vector $\xi_k(qj)$ specifying the pattern of the displacements and an amplitude $Q_{qj}(t)$ which is called the normal coordinate. Any arbitrary set of displacements can be decomposed in this way. In a soft mode displacive transformation the resulting average static atomic displacements resemble the frozen-in pattern of vibrations from a single normal mode with wave vector q_s . In other words, the order parameter can be chosen as a static component, $\langle Q_{q,i} \rangle$, of a single normal mode. The displacements are always referred to the more symmetric of the two phases, and their appearance will generally produce a less symmetric phase.

Not all structural transformations can be described by a single normal mode, in fact most (including seemingly simple examples such as fcc $\rightarrow$ hcp) cannot. When such a description is possible, the natural presumption is to implicate the phonon in question in the mechanism of the transformation. The dynamics of a phase transformation concern the time-dependent fluctuations of the order parameter, i.e. the phonons. At a continuous, or second order, transformation, the amplitude of these fluctuations diverge and since phonon amplitudes are inversely proportional to the square of their vibrational frequency $\omega^2(q)$, one is led to the proposition that $\omega^2(q_s) \rightarrow 0$ along the phase boundary.

II. α -Uranium. The simple body centered cubic (bcc) structure, is the stable highest temperature solid modification of a majority of the simple metals. Bcc metals tend to have lower phonon energies, and thus higher vibrational entropy, than their fcc counterparts[3,4]. The high temperature phase diagram of uranium metal is shown in Figure 1. Not surprisingly γ -Uranium, which is the stable phase in equilibrium with the liquid, has bcc structure. It is thus natural to choose bcc as the parent structure in which to elaborate the remaining structures. (Th, Pa, Np, and Pu also have stable high temperature bcc phases, and it is the natural starting point for an inclusive structural 'theory' of all of the known actinide metals.)

The structural changes associated with the γ -U $\rightarrow$ β -U have been discussed recently[5], but are too complex to discuss here, and certainly do not represent a single phonon mode. By contrast the γ -U $\rightarrow$ α -U transformation lends itself naturally into 'soft-mode' description. Formally, the α -U structure results from

the freezing in of a transverse acoustic (TA) normal vibrational mode of the bcc structure with a wave-vector, $q=[1/2,1/2,0]$, i.e. with alternate [110] planes displaced in opposing [1-10] directions, as shown in Figure 2. The relative displacement of adjacent planes is quite large, but the pattern is precisely correct. In particular, the centered orthorhombic unit cell requires that all atoms within a given [110] plane be displaced identically. There are additional long wavelength elastic distortions that contract the unit cell in the bcc [001] direction (the a -direction in α -U) while expanding the lattice along the [1-10] direction, approximately preserving the crystal volume. But these secondary elastic distortions are required by basic symmetry arguments, and are thus 'built-in' to a soft-mode description in a satisfying way. On this basis, there is a strong presumption that transverse phonon anomalies exist in γ -U. Unfortunately corroborative neutron scattering experiments have not, to our knowledge, been attempted.

One odd thing about the γ -U- $\rightarrow$ α -U transformation (assuming this mechanism is the correct one) is that in the process of shifting, the [110] planes pass through and reject an hcp phase, which occurs for a relative displacement of $\sqrt{2}a/6=0.83\text{\AA}$, about half that required for α -U, as shown in Figure 2. Presumably the fact that most materials do not pass up an opportunity to form a close packed arrangement accounts for the unpopularity of the α -U structure in other regions of the periodic table, although it does occur for other actinides (Am-IV, Cm-III, Bk-III and Cf-III). This is made additionally plausible by the remarkable fact that the hcp structure is not found in among the actinides. The 'double hcp' structure (Am-I, Cm-I, Bk-I and Cf-I) derives from a freezing-in of a different TA phonon with wave-vector $[1/4,1/4,0]$. [5]

III. The Puzzle of Low Temperature α -Uranium. The α -U structure is as close as uranium comes to realizing a close-packed structure, and Figure 1 reveals no additional low temperature phases. Nevertheless, by 1980 a variety of measurements including anomalies in electron transport [6], elastic compliance [7] and thermal expansion [8] hinted at the existence of not one, but three additional low temperature phase transformations at 43K, 37K and 22K. Yet diffraction experiments designed to detect changes in crystal structure or onset of magnetic order had failed [9]. It has taken another decade to sort out the puzzle.

Progress began with the measurement of the room temperature lattice dynamics by inelastic neutron scattering.[10] Figure 3 shows the phonon

energies plotted against their wave-vector along the principle symmetry directions for the α -U structure. The deep minimum in the Σ_4 branch at $q=[1/2,0,0]$, indicative of a tendency of adjacent [100]-planes to dimerize, is quite unusual. Furthermore, the minimum phonon frequency shows classical 'soft-mode' behavior, moving to lower frequency upon lowering the temperature, reaching a minimum at about 70K, and stiffening somewhat thereafter. And at low temperatures weak elastic (Bragg) scattering was observed to persist at (or at least very near) the positions in reciprocal space where the inelastic scattering occurred.[11] While these peaks, known as the 'Smith peaks', were the first solid diffraction manifestations of the structural modifications taking place, they only raised two further difficulties--

- 1) They occurred at an onset temperature (about 60K) considerably higher than those suggested by the anomalies in the bulk properties discussed above.
- 2) More fundamentally, they made no 'sense' as modulations of the α -U structure.

This last point requires further discussion. Conventional soft-mode phonon condensation modulates the parent structure in such a way as to leave the parent Bragg peak positions unaffected but causes each of them to be decorated new Bragg 'satellites'. The Smith peaks could be classified according to this scheme, but only as satellites of unobserved 'ghost' parent Bragg peaks with a lattice constant differing by about 10^{-3} from the one actually observed. The discrepancy was small, but impossible to dismiss. The understanding of this 'ghost' lattice was the last piece of the puzzle to fall into place.

IV. Incommensurate Modulation. In the course of attempting to sort out the Smith-peaks, a new set of diffraction satellites were discovered[12], which further detailed investigations [13] showed to suffer from none of the difficulties discussed above. Although weak (about 1% of the parent α -U Bragg peaks), they were nevertheless about 100 times stronger than the original Smith-peaks. The onset temperature ($T_0=43$ K) agreed with the highest suggested transition temperature from the bulk measurements, and the peak positions indexed properly as modulations of the established α -U structure. The reason that they had been missed in earlier investigations is that the modulation wave-vector is incommensurate with that of the parent structure, so that the peaks could not be detected in Bragg-peak scans along directions of high symmetry.

When the wave-vector, q_s , of the modulation cannot be related to the periodicity of the underlying lattice by multiplication by a rational number, the structure is said to be incommensurate. Other examples of incommensurate structures occur in surface reconstruction, quasi-crystals and in some antiferromagnets. In metals incommensurate displacive transformations may result from a charge density wave (CDW) in the conduction electrons near the Fermi Surface.[14] The atomic cores displace in response to the electric fields set up by the CDW. CDW instabilities are favored when two large portions of the Fermi surface differ by the wave-vector q_s (Fermi surface nesting), which is most common for quasi-one-[15] or quasi-two-dimensional[16] metals, as the Fermi energy is then independent of some component(s) of the electron momenta. The phonon mode softening in CDW transformations are brought about by conduction electron screening effects (giant Kohn anomalies)[17], but classical examples of incommensurate soft-mode transformations occur in insulators as well as metals.[18]

As discussed above, the diffraction from a modulated lattice causes each of the parent Bragg peaks [HKL] to be decorated with Bragg satellites, which appear at the positions $(hkl)=(H\pm q_x, K\pm q_y, L\pm q_z)$, where $q_s=(q_x, q_y, q_z)$ is the soft mode wave-vector. The measured values for q_s at temperatures near T_0 are approximately (0.49, 0.13, 0.22), and since all components of q_s are non-zero, there are eight satellites about each parent Bragg reflection. The nature of the modulation displacement pattern has been deduced from a study of the intensity of the satellite peaks [12]. The intensities are well reproduced by a sinusoidal displacement pattern with the largest displacement amplitude (0.027Å) along the [100] direction. The displacement pattern is consistent with that required by symmetry for a Σ_4 phonon mode, confirming the soft-mode nature of the instability.

V. Lock-in Transformations. The discovery of the incommensurate soft mode instability resolved the nature of the 43K transformation, but left unanswered the lower temperature anomalies at 37K and 22K. The key to the further understanding of these effects came from careful synchrotron x-ray (and later neutron) diffraction experiments, which determined the exact wave-vector, q_s , and its variation with temperature [19]. A summary of these results is shown in Figure 4. Between 43K and 37K all components of q_s change smoothly, but

below 37K q_x is frozen at $1/2$. Similarly, q_y and q_z vary freely until 22K, where they become frozen at rational values.

The behavior of q_x observed at 37K had been previously predicted on theoretical grounds.[20] It is an example of incommensurate lock-in, a phenomenon common in the study of incommensurate structures.[16] An incommensurate sinusoidal modulation of the form of Eq. 1, is continuously going in and out of phase with the underlying periodic lattice, and extracts no net interaction energy. (In fact the phase of the modulation with respect to the lattice is freely variable, giving rise to a 'phason' degree of freedom.) However, by adding multiple harmonics to the spatial modulation with appropriate phasing, the regions with favorable (unfavorable) interaction can be expanded (contracted), thereby gaining further overall stabilization of the modulation. Careful consideration reveals that this process also drives the fundamental wave-vector, q_s , toward a sub-multiple of the periodicity of the underlying lattice [21], leading to the lock-in behavior observed.

The q_x lock-in is driven by terms fourth-order in the amplitude of the primary harmonic displacement amplitude. Grübel, et. al. [19] extended the work of Walker [20] to show how terms sixth order in the amplitude would cause both q_y and q_z to lock-in simultaneously to the value $1/6$. Figure 4 shows that the observed value of $q_y=1/6$, whereas q_z takes a slightly different value of $2/11$ or $5/27$, close to but not equal to $1/6$. This can be explained by introducing into the $q_z=1/6$ structure occasional phase slips, where the modulation changes not by the prescribed value $\phi=2\pi/6$ between adjacent unit cells along the c-axis, but by twice that amount. If, on average, there is one phase slip for every n unit cells and they repel one another, they can form a regular array with an average wave-vector $q_z=(1+1/n)/6$. Thus the $q_z=2/11$ and $5/27$ structures are easily recognized as the $n=11$ and $n=9$ phase-slip defects in the basic $q_z=1/6$ structure. The diffraction signature of such a phase-slip structure consists of another hierarchy of diffraction peaks that decorate the primary satellite peaks, in much the same way that the primary satellites decorate the main Bragg peaks. The correctness of the above explanation was confirmed with the observation of these phase-slip satellites as shown in Figure 5.[19]

A Ghost Story. The remaining puzzle of α -U are the anomalous Smith peaks that seem to arise from diffraction from a 'ghost' lattice with different lattice spacing. A way to understand this phenomenon has recently been proposed by

Yamada[22]. In reality there are four distinct but equivalent α -U structures below 37K corresponding to modulation wave-vectors $q_s = (1/2, \pm q_y, \pm q_z)$. They differ only in the phase relationship of the various sinusoidal components of the displacements. In general, a given specimen will be divided roughly equally into domains of each type. In the region that separates two domains, the modulation wave-vector changes smoothly as shown schematically in Figure 6. Yamada shows by symmetry that in the interior of each domain there is a uniaxial strain along the x-axis, e_{11} , that is proportional to $[q_y^2 + q_z^2]$, producing an identical transformation induced strain within all of the domains. But this strain vanishes within the domain boundary region where $q_y = q_z = 0$, leaving the region with a slightly different lattice spacing. Since within the boundary region the modulation wave-vector points along the [100] direction, diffraction from the domain boundary regions can satisfactorily explain the existence of the Smith peaks.

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Figure Captions.

Figure 1. High temperature phase diagram for uranium.

Figure 2. Transformations induced by [110] TA displacements on a bcc lattice. a) [110] planes of the bcc structure. The open circles represent atoms in the plane above those represented by shaded circles. b) Shifting alternate layers along [1-10] (and stretching the long- to short-axis ratio from $\sqrt{2}$ to $\sqrt{3}$) produces a hcp-like structure. c) further shifting of alternate layers produces the α -U structure.

Figure 3. Phonon energy vs. wave-vector along symmetry directions in α -U. Anomalous dispersion indicative of soft mode behavior is seen in the TA branch labelled Σ_4 . (After Ref. 11)

Figure 4. Temperature dependence of the modulation wave-vector in α -U at low temperature, showing lock-in transformations at $T=37K$ and $22K$. Crosses (circles) refer to x-ray (neutron) data. (After Ref. 19)

Figure 5. X-ray diffraction scan at 22K, showing primary modulation satellites at values of $l=1\pm 2/11$, each surrounded by a pair of weaker secondary satellites displaced by $\Delta l=\pm 1/11$. This pattern confirms the existence of phase-slip defects in the low temperature phase of α -U. (After Ref. 19)

Figure 6. A schematic representation of the domain-boundary region in low temperature α -U. The lines represent the nodal planes of the sinusoidal modulation. Notice that the wave-vector is along the symmetric [100] direction within the boundary region. (After Ref. 22)

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bcc(Im3m)

pseudo-hcp (P63/mmc)

α -Uranium(Cmcm)

Fig. 3

Fig. 4

Fig. 5

Fig. 6

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