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RESEARCH MEMORANDUM

CRYSTAL STRUCTURES AND ATOMIC VOLUMES

OF THE ELEMENTS

W. G. McMillan

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The following table is a compilation of the available data¹ on the crystal structures of the common modifications of the elements at zero pressure. From the lattice parameters the volume per atom (" $v_{x\text{-ray}}$ ") was calculated as the ratio of the volume of the unit cell to the number of atoms per unit cell, and compared with that (" v_{dens} ") calculated from the bulk density. Also given is the radius r_0 of the equivalent sphere, i.e., having the atomic volume. Where known, the experimental temperatures are given for the lattice parameter determinations; "RT" means room temperature. Temperatures of the experimental density measurements are $300 \pm 10^\circ\text{K}$, unless otherwise specified.

Although these calculations are exceedingly trivial, the frequent reference to the old manuscript copy appeared to indicate that a wider circulation might prove useful.

I have to thank Mr. D. C. MacNeillage for numerical assistance.

¹ The principal source of this data was the compilation by J. G. Albright in the Handbook of Physics and Chemistry, 35th ed. Where necessary this was supplemented with data from Wyckoff, The Structure of Crystals (looseleaf) and Barrett, Structure of Metals, 2nd ed., McGraw-Hill (1952). Data for plutonium ($Z=84$) were taken from E. R. Jette, "Some Physical Properties of Plutonium Metal," J. Chem. Phys., **23**, 365 (1955).

Z	A Mol. Wt.	Phase	Structure		Temp °K	Lattice Parameters			Atoms /Cell	v _{x-ray} Å ³	r _o Å	Expt'l Density g/cm ³	v _{density} Å ³
			Type	Sym		a	b/a	c					
						Å	Å/deg.	Å					
1 H	1.00813	(s) (t)	hex		2	3.75		6.11	4	18.60	1.644	0.070 (21°K)	23.9
n	2.01171												
T	3.01695												
2 He	4.003	(s) (t)	oph	A3	2	3.57		5.83	2	32.17	1.973	0.147 (2.4°K)	45.2
3 Li	6.940	cold worked	bcc fcc	A2 A1	RT 78	3.5093 4.41			2 4	21.6038 21.44	1.7279 1.723	0.534	21.58
4 Be	9.013	a	oph hex	A3	291	2.28105 5.12		3.5774 15.77	2 44 ?	8.05945 3.14 ?	1.2438 1.248 ?	1.84	8.13
5 B	10.82		hex tet monocl			11.98 8.57		9.54 8.13	180 78	6.587 7.655	1.163 1.223	3.33	5.39
6 C	12.010	diamond	cub	A1	291	3.56665- 3.56723			8	5.67141- 5.67119	1.1063 1.1065	3.52	5.66
		α-graphite	hex	A9	293	2.4611		6.7077	4	8.7964	1.2806		8.86
		β-graphite	rhbdr			3.635	39°30'		2 ?	8.746 ?	1.2781 ?		11.1-9.5
		"graphite"	cub									2.25	
		amorphous, blk										1.8-2.1	
7 N	14.008	a(s)	cub		21	5.66			4N ₂	22.67	1.756	1.026 (20.7°K)	22.67

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Z	A Mol.Wt.	Phase	Structure		Temp °K	Lattice Parameters			Atoms /Cell	V _{x-ray} Å ³	r ₀ Å	Expt'l Density gm/cm ³	V _{density} Å ³
			Type	Sym		a	b/c	c					
						Å	Å/dag.	Å					
8 O	16.000	α(s)	orthrb		21	5.50	b:3.82	3.44	4	18.07	1.628	1.426 (20.7°K)	18.63
		β(s)	rhhbr		35	6.19	c:99.1°		6	37.85 ⁺	2.083		
		γ(s)	cub		50	6.83			8	39.83	2.119		
		(s)	hex										
9 F	19.00	(t)									1.108 (86°K)	28.47	
10 He	20.183	(s)	f.c.c.	A1	20	4.52			4	23.09	1.766	1.204 (27.3°K)	27.83
		(t)											
11 Na	22.997		b.c.c.	A2	293	4.2820			2	39.2563	2.1083	0.9712	39.315 ⁺
12 Mg	24.32		c.p.h.	A3	298	3.20280		5.19983	2	23.0967	1.7667	1.741	23.19
13 Al	26.98		f.c.c.	A1	298	4.04145			4	16.5026	1.5794	2.699	16.597
14 Si	28.09		dia.cub.A4		298	5.43048			8	20.0182	1.6844	2.42	19.27
		stabilized by CaF ₂	hex.		high	6.86		10.29	20 †	20.97 †	1.711†		
15 P	30.975	met.	hex_rhhbr			5.14	c:34°07'		2	19.04	1.657	2.70	19.05
		"	rhhbr., f.c.			5.96	c:60°47'		8	19.04	1.657		
		blk	orthrb A16	R.T.		3.31	b:4.38	10050	8	19.03	1.656		
		white	cub.	238		7.17			8P ₄	23.04	1.765 ⁺		
		yellow	cub.										
red	cub.									1.82	28.3		
violet	monocl.									2.20	23.4		
										2.36	21.79		

Z	A Mol.Wt.	Phase	Structure		Temp °K	Lattice Parameters			Atoms /Cell	$v_{x\text{-ray}}$ Å ³	r_o Å	X-ray Density g/cm ³	v_{density} Å ³	
			Type	Sym		a	b/a	c						
						Å	Å/deg.	Å						
16 S	±0.003 32.066	α	orthrb	A17	293	10.48	b:12.92	24.55	128	25.97	1.837	2.07	25.7	
			monocl		376	10.90	b:11.02	10.96	48	27.24	1.866	1.96	27.2	
			plastic, str.?			26.4	m:83°16'			112	?			
			rhombic pseudocell?			8.90	m:9°26'	12.32		32	?			
		γ-amorphous									1.92	27.7		
17 Cl	35.457	(s) (t)	tetr		88	3.56		6.12	8	56.05	2.374	1.507 (239.6°K)	39.06	
18 A	39.944	(s)	fcc	A1	20	5.43			4	40.03	2.122	1.65 (40°K)	40.2	
19 K	39.100		bcc	A2	123	5.20			2	70.3	2.560	0.87	74.6	
20 Ca	40.08	α	fcc	A1	193	5.565			4	43.086	2.1748	1.54	43.2	
			γ	A3	723	3.98		6.52	2	44.7	2.202			
21 Sc	44.96	α	fcc	A1	293	4.532			4	23.271	1.7711			
			β	A3	RT	3.302		5.245	2	24.763	1.8082	2.5	30.	
22 Tl	47.90	α	cph	A3	298	2.92		4.67	2	17.24	1.603	4.5	17.7	
			β	A2	>1173	3.32			2	18.30	1.635			
23 V	50.95		bcc	A2	293	3.0338			2	13.9615	1.4938	5.96	14.19	

Z	A Mol. Wt.	Phase	Structure		Temp °K	Lattice Parameters			Atoms /Cell	$v_{x\text{-ray}}$ Å ³	r_0 Å	Expt'l Density gm/cm ³	v_{density} Å ³		
			Type	Sym		a	b/c	c							
						Å	Å/deg.	Å							
24 Cr	52.01	α	b.c.c.	A2	291	2.8796			2	11.9390	1.4178	7.20	11.99		
			β	e.p.h.		A3	2.717			4.418	2			14.122	1.4995
			γ	b.c.c.		A2	8.717				58			11.420	1.3970
25 Mn	54.93	α	cub	A12	293	8.894			58	12.130	1.4254	7.20	12.29		
			β	cub		A13	R.T.	6.300			20			12.502	1.4398
			γ	tetr., f.c.		A6	R.T.	3.774			4			12.555 ⁺	1.4418
26 Fe	55.85	α	b.c.c.	A2	293	2.86635			2	11.7749	1.4113	7.86	11.80		
			β	b.c.c.		A2	1073	2.90			2			12.19	1.428
			γ	f.c.c.		A1	1373	3.63			4			11.96	1.419
			δ	b.c.c.		A2	1698	2.93			2			12.58	1.443
				gray cast white cast											
27 Co	58.94	α	e.p.h.	A3	293	2.5017		4.0629	2	11.0105	1.3801	8.9	11.0		
			β	f.c.c.		A1	R.T.	3.554			4			11.223	1.3889
28 Ni	58.69	α	e.p.h.	A3	443	2.65		4.32	2	13.14	1.464	8.90	10.95		
			β	f.c.c.		A1	298	3.51684			4			10.8742	2.3744
29 Cu	63.54	compressed	f.c.c.	A1	291	3.6073			4	11.7351	1.4097	8.9376	11.804		
30 Zn	65.38	wrought	e.p.h.	A3	298	2.65949		4.93685	2	15.1198	1.5340	7.19	15.10		

Z	A Mol.Wt.	Phase	Structure		Temp	Lattice Parameters			Atoms /Cell	$v_{x\text{-ray}}$	r_o	Expt'l Density	v_{density}	
			Type	Sym		a	b/a	c						
					$^{\circ}\text{K}$	\AA	$\text{\AA}/\text{deg.}$	\AA			g/cm^3	\AA^3		
31	Ge	69.72	tetr (simple) orthrb rhombic			4.51 4.5107	b:4.5167	7.51 7.6448	8 8 7	19.09 19.4689 7	1.658 1.6689 7	5.903	19.610	
32	Ge	72.60	dis cub	A4	293	5.62			8	22.19	1.743	5.46	22.08	
33	As	74.91	met amorphous, brwn-blk yellow	rhbdr rhbdr, fc hex cub	A7	293	4.123 5.599	$\alpha:54^{\circ}10'$ $\alpha:34^{\circ}18'$	2 8	21.405* 21.635	1.7224 1.7286	5.727 3.70 2.0	21.718 33.62 62.	
34	Se	78.96	α -red metastable	monocl.I	RT	8.992	b:8.973 $\alpha:91^{\circ}34'$	11.52	20.04	29.04	1.907	4.46	29.39	
			β -red metastable	monocl.II	RT	12.74	b:8.04 $\alpha:93^{\circ}04'$	9.25	32	29.57	1.918			
			stable gray- met.	hex	A8	293	4.337		4.944	3	26.845*	1.8575		
			amorphous red-powder vitreous, dark brwn-blk gray met.	trig									4.82 4.14 4.79	27.20 31.67 27.37
35	Br	79.916	(s) (l)	orthrb	123	4.48	b:6.67	8.72	8	32.57	1.981	3.12	42.5	

Z	A Mol. Wt.	Phase	Structure		Temp °K	Lattice Parameters			Atoms /Cell	$v_{x\text{-ray}}$ Å ³	r_0 Å	Expt'l Density gm/cm ³	v_{density} Å ³
			Type	Sym		a Å	b/c Å/deg.	c Å					
36	Kr	83.8	(s) (f)	f.c.c.	A1	89	5.694		4	46.152	2.2252	2.155 (120.3K)	64.56
37	Rb	85.48		b.c.c.	A2	292	5.709		2	93.04	2.8110	1.532	92.64
38	Br	87.63		f.c.c.	A1	293	6.049		4	55.334	2.3639	2.50-58	58.2-56A
39	Y	88.92		c.p.h.	A3		3.629	5.750	2	32.790	1.9856	5.51	26.79
40	Zr	91.22	α β	c.p.h. b.c.c.	A3 A2	1123	3.23 3.61	5.14	2 2	23.22 23.52	1.770 1.777	6.44	23.52
41	Nb	92.91		b.c.c. rhombic	A2		3.2941		2	17.8723	1.6219	8.55	18.04
42	Mo	95.95		b.c.c.	A2	298	3.14103		2	15.4948	1.5466	10.2	15.6
43	Te	(99)*		c.p.h.	A3		2.735	4.388	2	14.213	1.5027		
44	Ru	101.7	α gray white br-met. blk porous	c.p.h. hex.	A3	293	2.69844	4.27305	2	13.4730	1.4761	12.063 12.6	14.00 13.4
45	Rh	102.91	β	f.c.c.	A1	291	3.79559		4	13.6703	1.4833	12.44	13.74
46	Pd	106.7		f.c.c.	A1	291	3.88238		4	14.6297	1.5172	11.40	15.54

* Most stable isotopes

Z	A Mol. Wt.	Phase	Structure Type	Sys	Temp °K	Lattice Parameters			Atoms /Cell	$v_{x\text{-ray}}$ Å ³	r_0 Å	Expt'l Density gm/cm ³	v_{density} Å ³	
						a	b/m	c						
47	Ag	107.880	compressed	fcc cub	A1	298	4.07787		4	16.9527	1.5936	10.503	17.054	
48	Cd	112.41	vacuo-distilled	cpb hex	A3	298	2.97311		5.60694	2	21.4610	1.7239	8.648	21.582
49	In	114.76		tetr, fc	A6	293	4.583		4.963	4	26.060	1.8392	7.28	26.17
50	Sn	118.70	α-gray β-white γ-br-white	fla, cub	A4	291	6.46		8	33.70	2.004	5.75	34.28	
				tetr rhombic	A5	293	5.818		4	26.859	1.8578	7.28	27.07	
51	Sb	121.76		rhbdr	A7	298	4.49762	a: 57° 06'	2	30.0242	1.9281			
				rhbdr, fc hex			6.226	a: 87° 24'	8	30.077	1.9292	6.684	30.246	
52	Te	127.61	sil-wh-cst crystal	hex rhbdr	A8	293	4.495		5.912	3	34.483	2.0192	6.25	33.90
			br-blk amorphous									6.00	35.31	
53	I	126.91		orthrb rhombic		291	4.7761	b: 7.2501	9.7711	8	42.2932	2.1614	4.94	42.65*
54	Xe	131.3	(s) (t)	fcc	A1	88	6.24			4	60.74	2.439	3.52 (164°K)	61.9

Z	A Mol. Wt.	Phase	Structure		Temp	Lattice Parameters			Atoms /Cell	$v_{x\text{-ray}}$	r_o	Ext'd Density	v_{density}	
			Type	Sym		a	b/c	c						
					$^{\circ}\text{K}$	\AA	$\text{\AA}/\text{deg.}$	\AA		\AA	gm/cm^3	\AA^3		
55	Ce	132.91	bcc hex	A2	88	6.05			2	110.7	2.979	1.873	117.82	
56	Ba	137.36	bcc	A2	293	5.009			2	62.84	2.4663	3.78	60.3	
57	La	138.92	α	cph	A3	293	3.75		6.06	2	36.90	2.065*	6.15	37.50
			β	fcc	A1	RT	5.294			4	37.093	2.0689		
58	Ce	140.13	α	cph	A3		3.65		5.96	2	34.38	2.017	6.7	34.7
			β	fcc	A1	RT	5.140			4	33.949	2.0087	6.90	33.72
			at ca 12450 atmos.		fcc	A1	RT	4.84			4	28.34	1.891	
59	Pr	140.92	α	cph	A3	293	3.662		5.908	2	34.307	2.0157	6.475	36.135*
			β	fcc	A1	RT	5.151			4	34.168	2.0130		
60	Nd	144.27	cph	A3	293	3.650		5.890	2	33.978	2.0093	6.96	34.42	
61	Pm	(145)												
62	Sm	150.43	hex									7.7-8	32.4-0	
63	Eu	152.0	bcc	A2	293	4.573			2	47.82	2.2516			
64	Gd	156.9	cph	A3	293	3.622		5.748	2	32.652	1.9828			
65	Tb	159.2	cph	A3	293	3.585		5.662	2	31.510	1.9594			

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Z	A Mol. Wt.	Phase	Structure		Temp °K	Lattice Parameters			Atoms /Cell	$v_{x\text{-ray}}$ Å ³	r_0 Å	Expt'l Density gm/cm ³	v_{density} Å ³
			Type	Sym		a	b/c	c					
						Å	Å/deg.	Å					
66 Dy	162.146		cph	A3	293	3.578		5.648	2	31.310	1.9552		
67 Ho	164.94		cph	A3	293	3.557		5.620	2	30.790	1.9443		
68 Er	167.2		cph	A3	293	3.532		5.539	2	30.191	1.9317	14.77 ?	58.2 ?
69 Tm	169.4		cph	A3	293	3.523		5.564	2	29.903	1.9255		
70 Yb	173.04		fcc	A1		5.468			4	40.872	2.1369		
71 Lu	174.99		cph	A3	293	3.509		5.559 ?	2	29.639 ?	1.9198?		
72 Hf	178.6	gray	cph	A3	293	3.32		5.46	2	26.06	1.839	13.3	22.3
73 Ta	180.88	gray-blk metal blk powder	bcc cub	A2	293	3.2959			2	17.9017	1.6228	16.6 14.491	18.1 20.725
74 W	183.92	α β -unstable	bcc cub	A2 A15	298 293	3.15837 5.04			2 8	15.7528 16.00	1.5551 1.563	19.3	15.82
75 Re	186.31		cph	A3	293	2.7553		4.4493	2	14.6262	1.5171	20.53	15.068
76 Os	190.2		cph	A3	293	2.72980		4.3104	2	13.9085	1.4919	22.48	14.048
77 Ir	193.1		fcc	A1	291	3.3312			4	14.0587	1.4972	22.421	14.300
78 Pt	195.23		fcc	A1	291	3.91580			4	15.0107	1.5303	21.45	15.112

E	A Mol. Wt.	Phase	Structure		Temp °K	Lattice Parameters			Atoms /Cell	V _{x-ray} Å ³	r ₀ Å	Expt'l Density gm/cm ³	V _{density} Å ³
			Type	Sym		a Å	b/c Å/deg.	c Å					
79 Au	197.2	cold rolled	f.c.c.	A1	298	4.07042			4	16.8600	1.5907	19.296	16.968
80 Hg	200.61	(a)	rhbdr		227	2.997	a: 70° 30'		1	23.170	1.7685 ⁺	14.383 (85°K)	23.158
		(a)	rhbdr.f.c.		227	4.578	a: 98° 13'		4	23.168	1.7685 ⁻		
81 Tl	204.39	α	e.p.h.	A3	R.T.	3.4496		5.5137	2	28.4106	1.8929	11.86	28.61
		β	f.c.c.	A1	>303	4.841			4	28.362	1.8918		
			b.c.c.	A2		3.874			2	29.070	1.9074		
82 Pb	207.21		f.c.c.	A1	298	4.9408			4	30.1530	1.9308	11.3437	30.329
83 Bi	209.00	vacuo-distilled hex.	rhbdr.	A7	298	4.7364	a: 57° 14.5'		2	35.1800	2.0327	9.781	35.478
			rhbdr.f.c.				6.578	a: 87° 34'		8	35.486		
84 Po	210	α	cub(simple)		263	3.34			1	37.3	2.072		
			monocl.				7.42	b: 4.29 a: 92° 1'	14.10	12 1	37.4 1		
85 At	(210)												
86 Rn	222	(f)										4.4 (211°K)	84.
87 Fr	(223)												
88 Ra	226.05											5. 1	80. 1

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Z	A Mol. Wt.	Phase	Structure		Temp K°	Lattice Parameters			Atoms /Cell	v _{x-ray} Å ³	r ₀ Å ³	Expt'l Density gm/cm ³	v _{density} Å ³		
			Type	Sym		a Å	b/a Å/deg.	c Å							
89	Ac	227													
90	Th	232.12	f.c.c.	A1	293	5.04			4	32.01	1.970	11.3-7	34.1-32.9		
91	Pa	231													
92	U	238.07	α	orthrb. A20	293	2.852	b: 5.865	4.945	4	20.679	1.7027	18.7	21.1		
					1073	3.474	b: 4.887	3.308	2	20.963	1.7105				
				monocl.		2.829	a: 1		2						
93	U ₂₃₇	(237)													
94	Pu	239	α									19.737 (298°K)	20.11		
														17.65 (423°K)	22.48
						orthrb., f.c.	483	3.1603	b: 5.7624	10.141	8	23.085	1.7664	17.19 (483°K)	23.08
						f.c.c.	593	4.6370			4	24.9259	1.8121	15.92 (593°K)	24.9
						tetr., f.c.	738	4.701		4.489	4	24.801	1.8091	15.99 (738°K)	24.8
				b.c.c.	773	3.638			2	24.075	1.7912	16.48 (773°K)	24.1		
95	Am	(243)													
96	Cm	(243)													
97	Bk	(245)													
98	Cf	(246)													

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