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**Chemical-Equilibrium Calculations for
Aqueous Geothermal Brines**

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University of California

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Jerry F. Kerrisk

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CHEMICAL EQUILIBRIUM CALCULATIONS FOR AQUEOUS GEOTHERMAL BRINES

by

Jerry F. Kerrisk

ABSTRACT

Results from four chemical-equilibrium computer programs, REDEQL.EPAK, GEOCHEM, WATEQF, and SENECA2, have been compared with experimental solubility data for some simple systems of interest with geothermal brines. Seven test cases involving solubilities of CaCO_3 , amorphous SiO_2 , CaSO_4 , and BaSO_4 at various temperatures from 25 to 300°C and in NaCl or HCl solutions of 0-4 molal have been examined. Significant differences between calculated results and experimental data occurred in some cases. These differences were traced to inaccuracies in free-energy or equilibrium-constant data and in activity coefficients used by the programs. Although currently available chemical-equilibrium programs can give reasonable results for these calculations, considerable care must be taken in the selection of free-energy data and methods of calculating activity coefficients.

I. INTRODUCTION

Many of the recent attempts to develop geothermal technology by using geothermal brines have encountered severe problems.¹ Much of the difficulty can be traced to the chemistry of brines and involves precipitation and deposition of scale in production wells, in plant equipment or in reinjection wells, and corrosion of equipment. A complicating feature of these problems is that the chemistry of geothermal brines is highly dependent on the source of the brine, differing from field to field and even among wells in a given field. Thus, problems with one brine (along with solutions to these problems) may not be relevant to other brines.

A fundamental understanding of the chemistry of geothermal brines will be necessary to economically use these energy sources. A worthwhile goal would be the capability of modeling precipitation and corrosion reactions under conditions of varying temperature and pressure. Modeling of these processes must start with an understanding of equilibrium chemical behavior of brines (for example, with a knowledge of what species are

actually present in brine and under what conditions precipitation or corrosion reactions can occur). Following this, kinetics of precipitation or corrosion reactions, diffusion of the species concerned, and physical or chemical processes involved in the deposition of scale must also be understood and modeled.

Modeling equilibrium chemical behavior of geothermal brines is conceptually a simple problem, given the thermodynamic basis of chemical-equilibrium calculations and the wide range of applications.² In practice, however, a number of difficulties complicate the calculations. One of the most important difficulties involves availability of free-energy or equilibrium-constant data for the chemical reactions involved. Often only room-temperature data are known, and only rarely are high-pressure data available. Methods of estimating this information can be used, but they generally lack the accuracy needed. A second and equally important difficulty is the need for a method of calculating activity coefficients of species in brine at the high ionic strengths encountered. Conventional methods of calculating

activity coefficients are limited to ionic strengths of 0-1 molal, giving only rough estimates above that range.³ Effects of temperature and pressure on activity coefficients are also important. A third difficulty involves the method employed to calculate the equilibrium composition of a brine. A method is needed that is efficient, insensitive to the initial estimate of composition, and capable of selecting which solids will precipitate from a multitude of potential precipitates. No single method available seems to possess all these attributes.²

In the face of these difficulties, it is uncertain how well currently available chemical-equilibrium computer programs can model geothermal brines. To help answer this question, this report describes a comparison of results from four chemical-equilibrium computer programs with experimental solubility data for some simple systems of interest with geothermal brines. The four programs tested were REDEQL.EPAK,⁴ GEOCHEM,⁵ WATEQF,⁶ and SENECA2.^{1,7} The systems employed involve the solubility of CaCO_3 , amorphous silica, CaSO_4 , and BaSO_4 at various temperatures in NaCl or HCl solutions of 0-4 molal. These comparisons test the free-energy or equilibrium-constant data available with each program and the methods employed for activity-coefficient calculations. The sources of differences between calculated results and experimental data are discussed. Finally, some more complex problems were employed to obtain timing data for three of the codes.

Calculations in high ionic strength solutions (> 1 molal) are certainly outside the range of applicability of these programs. This work was undertaken, however, to test the utility of various programs. Calculations outside the accepted range of applicability are a necessary part of the test.

II. CHEMICAL-EQUILIBRIUM COMPUTER PROGRAMS

Four chemical-equilibrium computer programs were employed in this test. They are REDEQL.EPAK, GEOCHEM, WATEQF, and SENECA2. These programs were chosen because they all contain thermodynamic data bases (free-energy or equilibrium-constant data) and they all calculate activity coefficients for species involved. The following sections briefly describe some features of each program, such as

the method of calculating equilibrium compositions, the range of applicability (temperature, species, etc.), and the activity-coefficient calculations.

A. REDEQL.EPAK

REDEQL.EPAK is a modification of REDEQL2 made at the Corvallis Environmental Research Laboratory of the US Environmental Protection Agency.⁴ The program computes equilibrium compositions in aqueous systems; complex formation, precipitation of solids, oxidation-reduction reactions, and the presence of a gas phase are all considered. The set of mass-balance and mass-action equations is solved by iteration using the Newton-Raphson technique for a given group of possible solid phases in equilibrium with the aqueous phase.² This operation is repeated with different groups of solid phases until the correct solid phases are found. The correct set is defined as a set for which no solubility products are exceeded and the mass-balance conditions are satisfied. Thermodynamic data for complexes and solids of 35 metals and 59 ligands are available for 25°C with the version employed for these tests. Although the program can adjust equilibrium constants for temperatures other than 25°C, data needed for this adjustment (enthalpy change of the formation reaction at 25°C) are available for only a small percentage of complexes or solids. Activity coefficients for charged species are calculated with the Davies equation⁸

$$-\log_{10}\gamma(Z) = AZ^2 \left[\frac{(I)^{1/2}}{1+(I)^{1/2}} - 0.2I \right], \quad (1)$$

where γ is the activity coefficient of a species with charge Z in a solution of ionic strength I molar. The parameter A is calculated as a function of temperature.⁴ Activity coefficients for H^+ are taken as $1/2 \log_{10}\gamma(Z=1)$. Uncharged species are assumed to have unit activity coefficients. Composition data can be input in units of molarity, or mg/L; output is in molar units. Calculated results were converted to molality units for comparison with experimental data. Corrections were less than 8 per cent at 25°C, but were 20-30 per cent at 300°C. Along with total concentrations of the species, estimates of the ionic strength and pH of the aqueous phase must be input.

The ionic strength and pH can be held fixed or allowed to vary during the calculation. The partial pressure of CO₂ or N₂ gas can be fixed for a given calculation. No other gases are considered. The electron activity or pE must be fixed if oxidation-reduction reactions are included.

B. GEOCHEM

GEOCHEM is also a modification of REDEQL2, made at the Department of Soil and Environmental Sciences of the University of California at Riverside.⁵ The general features and method of calculation of GEOCHEM are similar to those of REDEQL.EPAK. The basic differences between the two programs, as far as calculations reported here are concerned, are in the thermodynamic data base, the activity-coefficient calculation, and the limitation of GEOCHEM to 25°C. Thermodynamic data for 36 metals and 69 ligands are available in the version employed for these tests. Although most of the metals and ligands are the same as those covered in REDEQL.EPAK, the thermodynamic data are generally different. Activity coefficients are calculated using the equation

$$-\log_{10}\gamma(Z) = \frac{AZ^2(I)^{1/2}}{1+aB(I)^{1/2}} + B^*I, \quad (2)$$

where $A = 0.5116$, $B = 0.3292 \times 10^8$, and a and B^* are specified as noted below.⁵ For $I \leq 0.5$ molar, $a = 1/B$ and $B^* = 0.3AZ^2$; this reduces to a variant of the Davies equation. For $I > 0.5$ molar, $B^* = 0.41$ and $a = 4 \times 10^{-8}$, 5×10^{-8} and 6×10^{-8} for monovalent, divalent, and trivalent ions, respectively. Activity coefficients for H⁺ are taken as $1/2 \log_{10}\gamma(Z=1)$. The two equations do not give the same activity coefficient at $I = 0.5$. For neutral ions, $B^* = 0.1$ for all values of I ; only the linear term in I contributes to γ for neutral species. Data are input and output in molar units. As with REDEQL.EPAK, calculated results from GEOCHEM were converted to molality units for comparison with experimental data. In addition to ionic strength and pH estimates, a measure of the total H⁺ (free and combined) must be input.⁵ The partial pressure of CO₂ and N₂ can be fixed; no other gases are considered. The electron activity or pE must be fixed if oxidation-reduction reactions are included.

C. WATEQF

WATEQF is a FORTRAN version of the WATEQ program prepared at the US Geological Survey in Reston, Virginia.⁶ The program calculates the equilibrium distribution of species in an aqueous system. It differs from the other three programs involved in this test in that it does not determine the actual amount of particular solid phases that are formed; it calculates the distribution of species as if no solid phases were formed and indicates the state of saturation of the solution for possible solid phases contained in the data base. Complex formation, oxidation-reduction reactions, and the presence of a gas phase are considered. The set of mass-balance and mass-action equations is solved by iteration.⁹ These equations have been rearranged to express each free-ion concentration in terms of other ion concentrations, activity coefficients, and equilibrium constants. With this method, the internal construction of the program is intimately connected to the chemistry of the species considered. Total concentrations of the various species are employed as initial estimates. Thermodynamic data for almost 200 complexes, solids, and gases are available with the version used for these tests. Most of these species have the data needed to estimate equilibrium constants as a function of temperature. Activity coefficients are determined in a number of ways.^{6,9} Eight species employ Eq. (2), where a and B^* have been estimated from experimental data. The parameters A and B are calculated as a function of temperature. Activity coefficients for these eight species are always calculated in this manner. The remainder of the charged species uses Eq. (2) with $B^* = 0$ and a ranging from $2.5-9 \times 10^{-8}$, depending on the species.⁹ These are called Debye-Huckel activity coefficients. A variant of the Davies equation,

$$-\log_{10}\gamma(Z) = AZ^2 \left[\frac{(I)^{1/2}}{1+(I)^{1/2}} - 0.3 I \right],$$

can also be employed for these species. For neutral species, the activity coefficient is calculated as $\log_{10}\gamma = 0.1 I$.

Composition data can be input in units of meq/L, mg/L, ppm, or molality; output is in ppm and molality. Results in units of molality were used directly for WATEQF. Along with total concentrations of species, the pH of the solution must be input. The calculation is performed at constant pH. The partial pressures of CO_2 , O_2 , and CH_4 are calculated if these gases are present. If oxidation-reduction reactions are included, one of a number of possible measures of the electron activity must be input.⁶

Because WATEQF does not determine the amounts of solid phases that are formed, it is not directly suitable for modeling precipitation in geothermal systems. The systems modeled here were all very simple, with only one precipitate; calculations with WATEQF were relatively easy for these systems. It was necessary to adjust total concentrations of ions contributing to the precipitate in each case so that the solution was just at saturation to obtain the correct ionic strength and activity coefficients. This process required a few repeated calculations for each case. The pH used was estimated from results for other programs. Additional problems were encountered for the CaCO_3 solubility calculations where a specific CO_2 pressure was desired. The other three programs allow a CO_2 pressure or its equivalent for these simple systems to be specified; with WATEQF, the CO_3^{2-} total concentration must be adjusted to achieve the desired CO_2 pressure. In spite of the difficulties, WATEQF was included in these tests because it is widely used and has a well-documented thermodynamic data base.

D. SENECA2

SENECA2 is a modification of SENECA made at the Los Alamos National Laboratory. SENECA was originally written by Ma and Shipman;⁷ it computes equilibrium compositions in a two-step process. The first step uses the free-energy minimization procedure proposed by Naphtali to obtain an approximate composition for a system.¹⁰ The second step uses this approximate composition as an initial estimate for solving the set of mass-balance and mass-action equations by the Newton-Raphson method.²

The modifications made at Los Alamos included a permanent arrangement for an aqueous phase, a

gas phase, and multiple solid phases; an activity coefficient calculation for aqueous species, oxidation-reduction reactions, and a thermodynamic data base. The solid phases present are determined during the first step of the calculation. They are added or rejected during free-energy minimization as successively better estimates of the composition are obtained. Solid phases can be rejected during the second step, but no new solid phases can be added.

Thermodynamic data for 70 complexes, gases, and solids of interest in geothermal systems are available with the version used for these tests. Free-energy data from 25 to 300°C were obtained from Helgeson.¹¹⁻¹³ Activity coefficients for charged species are calculated using Eq. (2), where A , B , and B° are calculated as functions of temperature.¹¹ Values of the parameter a ranging from $2.5-9 \times 10^{-8}$ are used for the various ions and complexes.³ The activity of water is determined from data on the osmotic coefficient.¹¹ The activity coefficients of neutral species are calculated from the activity coefficient of CO_2 in NaCl solutions.¹¹ Composition data are input and output in units of molality. Only temperature and total pressure are required input data along with the total concentrations of the species defining the solution. Potential solid phases, gas phases, and complexes to be considered during the calculation are not automatically selected from the data base by SENECA2 as with the other three programs. A list specifying which species are to be considered must be input. If a gas phase (CO_2 or H_2S are in the data base) is present at equilibrium, water vapor at its equilibrium vapor pressure is included as one of the components. If oxidation-reduction reactions are included, the solution E_h , the oxygen partial pressure, or the sulfate-sulfide ratio must be specified to set the electron activity.

III. EXPERIMENTAL DATA FOR TEST CASES

Seven test cases were chosen for which calculated results from the four chemical-equilibrium codes could be compared with experimental data. Each of the cases involves precipitation of a single solid phase from water, an NaCl, or an HCl solution (up to 4 molal). Solution temperatures

ranged from 25–300°C. Table I summarizes the conditions employed for the seven cases. The following sections discuss each of the test cases and the sources of the experimental data. For each test case, the experimental data are plotted and a smoothed curve drawn through the data. The smoothed curves were employed for later comparison with the calculated results. The plots are presented to establish the magnitude of scatter or uncertainty in the experimental data. This experimental uncertainty can be compared with the differences between the calculated results and experimental curves in Sec. IV.

A. Test Case 1

The first test case involved the solubility of CaCO_3 in 0–4-molal NaCl solutions at 25°C and 1-atm CO_2 pressure. Data were obtained from four sources.^{14–17} Figure 1 shows a plot of the data as a function of total NaCl content of the solution. The solid line represents a smoothed curve through the data. Two of the four sources identified the solid phase as calcite;^{15,16} the other two sources mentioned only CaCO_3 . The data of Cameron, et al., were considered unreliable by Frear and Johnston.¹⁵ However, they represent the only data available at high ionic strength.

B. Test Case 2

The second test case involved the solubility of CaCO_3 in water at 25–300°C and 1-atm CO_2 pressure. Data were obtained from three sources.^{15,18,19} Figure 2 shows a plot of the data as a function of temperature. The solid line represents a smoothed curve through the data. All three sources identified the solid phase as calcite.

TABLE I
TEST CASES

Test Case	Precipitate	Solution	Temperature °C	Remarks
1	CaCO_3	0–4 m NaCl	25	1 atm CO_2
2	CaCO_3	water	25–300	1 atm CO_2
3	CaCO_3	1 m NaCl	25–300	12 atm CO_2
4	SiO_2	water	25–200	–
5	SiO_2	0–4 m HCl	25 and 90	–
6	BaSO_4	0–4 m NaCl	25 and 95	–
7	CaSO_4	0–4 m NaCl	25, 100 and 250	–

C. Test Case 3

The third test case involved the solubility of CaCO_3 in a 1-molal NaCl solution at 100–300°C and 12-atm CO_2 pressure. Data were available from only one source.¹⁸ Figure 3 shows a plot of the data as a function of temperature. The solid line represents a smoothed curve through the data. The solid phase was calcite. These data are from the same source as the high-temperature data in Test Case 2.

D. Test Case 4

The fourth test case involved the solubility of amorphous SiO_2 in water at 25–200°C. Data were obtained from three sources.^{20–22} One was a composite curve generated from a number of earlier investigations.²⁰ Figure 4 shows a plot of the data as a function of temperature. The solid line represents a smoothed curve through the data. The agreement among the various investigators is generally quite good.

E. Test Case 5

The fifth test case involved the solubility of amorphous SiO_2 in 0–4-molal HCl solutions at 25 and 90°C. Data from only one source were found.²³ Figure 5 shows a plot of the data as a function of total HCl content of the solution. The solid lines represent smoothed curves through the data. The data for water (0-molal HCl) are a little above the experimental curve in Fig. 4.

F. Test Case 6

The sixth test case involved the solubility of BaSO_4 (barite) in 0–4-molal NaCl solutions at 25 and 95°C. Data from two sources were employed.^{24,25} Figure 6 shows a plot of the data as a function of total NaCl content of the solution. The solid lines represent smoothed curves through the data. The systematic difference between the data of Templeton and Blount necessitated a rather arbitrary line. This uncertainty, however, was not significant in comparison with the scatter in calculated results.

G. Test Case 7

The seventh test case involved the solubility of CaSO_4 in 0–4-molal NaCl solutions at 25, 100, and 250°C. Data from three sources were used.^{26–28} Figure 7 shows a plot of the data as a function of total NaCl content of the solution. The solid lines represent smoothed curves through

Fig. 1. Experimental data for Test Case 1.

Fig. 2. Experimental data for Test Case 2.

Fig. 3. Experimental data for Test Case 3.

Fig. 4. Experimental data for Test Case 4.

Fig. 5. Experimental data for Test Case 5.

Fig. 6. Experimental data for Test Case 6.

Fig. 7. Experimental data for Test Case 7.

the data. At 25°C, the data are for gypsum; at 100 and 250°C, the data are for anhydrite.

IV. TEST CASE RESULTS

An attempt was made to use each of the four chemical-equilibrium computer programs to calculate the solubility of the solid phase for each test case. In some instances, the limitations of the program precluded its use; for example, GEOCHEM is usable only at 25°C. The following sections discuss the results for each of the test cases.

Two of the programs (REDEQL.EPAK and GEOCHEM) deal in molarity units, but the experimental data are all in molality units. Considering the uncertainty in equilibrium constants and activity coefficients, the differences between molality and molarity are often ignored. For the comparisons reported here, results from the two codes were corrected to molality units. The correction was calculated as

$$\frac{C_M}{C_m} = \rho_s w_s,$$

where C_M is the concentration in molarity units, C_m is the concentration in molality units, ρ_s is the density of the solution, and w_s is the mass of water per unit mass of solution. The quantity w_s was determined as

$$w_s = \frac{1000}{1000 + M_s C_m},$$

where M_s is the molecular weight of the solute. For these calculations, M_s was taken as the molecular weight of NaCl, 58.44. The density of the solution at the temperature of the test and C_m molality was calculated from the correlation of Haas.²⁹ Figure 8 shows a plot of the molarity/molality ratio (C_M/C_m) as a function of the solution molality at various temperatures. This ratio was employed for corrections to REDEQL.EPAK and GEOCHEM results.

A. Test Case 1 Results

Figure 9 shows a plot of CaCO_3 solubility as a function of total NaCl content of the solution for Test Case 1. The solid line is the same curve

Fig. 8. Molarity-molality correction factors.

^aIndicates Davies equation.

Fig. 9. Results for Test Case 1.

that is drawn through the experimental data in Fig. 1. The results from SENECA2 are in reasonable agreement with the experimental curve over the entire range of NaCl content. The results from REDEQL.EPAK and WATEQF show reasonable agreement up to 1-m NaCl content, but drop significantly below the experimental curve at higher ionic strengths. The differences between the results from SENECA2 and the results from WATEQF and REDEQL.EPAK are mainly in the activity-coefficient calculation. The three programs agree relatively well at 0-1-m NaCl content, but diverge at higher values. The results from WATEQF were independent of the choice of method for calculating activity coefficients because all the influential species in the test case are members of the group whose activity-coefficient calculation does not vary. WATEQF has solubility data for both calcite and aragonite. The results reported here represent calcite solubilities. Aragonite solubility is about twice that of calcite at 25°C.

The results from GEOCHEM are slightly high for water, but they diverge rapidly at higher NaCl content. One result, 0.045-molal CaCO_3 solubility at 4.35-molal NaCl content, was not plotted. The cause of the high solubility is consideration of the formation of the CaCl^+ complex by GEOCHEM. This complex contains about one-half the calcium in solution at 2-molal NaCl content and about two-thirds of the calcium at 4-molal NaCl content. The equilibrium constant used by GEOCHEM for the reaction

is about 4. No references were found for this formation constant. Based on results presented here, it appears to be too high. None of the other three programs consider the formation of CaCl^+ . Activity coefficients calculated by GEOCHEM are similar to those of SENECA2. The slight discontinuity in the GEOCHEM results between 0.5 and 1-molal NaCl content occurs from a change in the activity-coefficient equation in this range.

B. Test Case 2 Results

Figure 10 shows a plot of CaCO_3 solubility as a function of solution temperature for Test Case 2. The solid line is the same curve as is drawn through the experimental data in Fig. 2.

GEOCHEM was not included in this comparison because it is usable only at 25°C; Test Case 1 includes that comparison. The results from SENECA2 are a little high at 25°C, but are generally in reasonable agreement over the entire temperature range. The results from WATEQF are in good agreement from 25-200°C, but are somewhat high at 300°C. Because of the necessity to fix pH and the inability to fix the CO_2 pressure with WATEQF, these calculations required additional time and effort. The results from REDEQL.EPAK are slightly high at 25°C. From 100-300°C, their trend is opposite to that of the experimental curve; that is, the calculated solubility increases with increasing temperature rather than decreasing. These problems may be related to equilibrium-constant data. The formation constant of solid CaCO_3 is not available as a function of temperature in REDEQL.EPAK. Also, the temperature variation of the formation constant for HCO_3^- (from H^+ and CO_3^{-2}) appears quite different from that in WATEQF or SENECA2. Activity coefficients calculated by the three programs are in relatively good agreement for this test case because the solutions are at low ionic strength. The results from WATEQF were independent of the choice of activity-coefficient calculation.

C. Test Case 3 Results

Figure 11 shows a plot of CaCO_3 solubility as a function of solution temperature for Test Case 3. The solid line is the same curve as is drawn through the experimental data in Fig. 3. Only results from WATEQF and SENECA2 are included because GEOCHEM is usable only at 25°C and REDEQL.EPAK does not allow CO_2 pressures above 1 atm. The CO_2 pressure was 12 atm for this test case. The SENECA2 results are high at 100°C, but those at 200-300°C are in reasonable agreement with the experimental curve. The WATEQF results are quite low at 100°C and appear to be increasing with increasing temperature at 200-300°C. Again, difficulties were encountered in obtaining results with WATEQF. A number of differences in equilibrium-constant data appear to be the cause of the differences between SENECA2 and WATEQF. Activity coefficients were similar for the two programs.

D. Test Case 4 Results

Figure 12 shows a plot of amorphous SiO_2 solubility as a function of temperature for Test

Fig. 10. Results for Test Case 2.

Fig. 11. Results for Test Case 3.

Fig. 12. Results for Test Case 4.

Case 4. The solid line is the same curve as is drawn through the experimental data in Fig. 4. GEOCHEM and REDEQL.EPAK data are shown for 25°C only; REDEQL.EPAK does not have data for the temperature variation of the formation constant of amorphous silica. The results of all four programs are in relatively good agreement with the experimental curve for this test case. WATEQF has solubility data for a number of solid SiO₂ phases.⁶ The results in Fig. 12 are for the "silglas" phase, which gave the best overall agreement with the experimental curve. The "silgel" phase showed better agreement at 25°C, but was quite high at 100–200°C. The activity coefficients for the significant species were similar from all four programs owing to the low ionic strengths involved.

E. Test Case 5 Results

Figure 13 shows a plot of amorphous SiO₂ solubility as a function of total HCl content of the solution at 25°C for Test Case 5. The solid line is the same curve as is drawn through the experimental data at 25°C in Fig. 5. Figure 14 shows a similar plot for the 90°C data.

At 25°C (Fig. 13), the results of GEOCHEM and SENECA2 are in good agreement with the experimental curve. The results of REDEQL.EPAK are also in relatively good agreement, but they are almost constant with increasing HCl content rather than decreasing as the experimental curve does. This is because the precipitation reaction for SiO₂,

involves only neutral species, and REDEQL.EPAK assumes neutral species have unit activity coefficients at all ionic strengths.⁴ The results from WATEQF (using the "silglas" solid) are low over the entire range.

At 90°C (Fig. 14), only results from SENECA2 and WATEQF were available. These results are low except at the highest HCl content. The Davies equation was used for the WATEQF activity coefficients. Because the major species are neutral in this test case, the choice of activity-coefficient method in WATEQF is immaterial.

Fig. 13. Results for Test Case 5 at 25°C.

Fig. 14. Results for Test Case 5 at 90°C.

F. Test Case 6 Results

Figure 15 shows a plot of BaSO_4 solubility as a function of total NaCl content of the solution at 25°C for Test Case 6. The solid line is the same curve as is drawn through the experimental data at 25°C in Fig. 6. Figure 16 shows a similar plot for the 95°C data.

At 25°C (Fig. 15), the results of SENECA2 are in good agreement with the experimental curve. Two sets of results are shown for WATEQF, one using Davies equation activity coefficients and the other using Debye-Huckel equation activity coefficients. Both methods give similar results at 0-0.5-molal NaCl content; above that range, results employing the Debye-Huckel activity coefficients show much better agreement with the experimental curve. The results of REDEQL.EPAK are similar to those of WATEQF with the Davies equation activity coefficients. Both problems come from activity coefficients that are too large at high ionic strengths. For REDEQL.EPAK, both Ba^{+2} and SO_4^{-2} activity coefficients are high. For WATEQF, the Davies equation activity coefficient for Ba^{+2} is much too large; the SO_4^{-2} activity coefficient is always calculated with the same equation. The GEOCHEM results are quite low over the entire range of NaCl contents. This is because of a significant difference in the formation constant for solid BaSO_4 in GEOCHEM as compared with the other three programs; it is about an order of magnitude larger.

At 95°C (Fig. 16), the results of SENECA2 are in good agreement with the experimental curve at low ionic strengths, but are high above 1-molal NaCl content. For WATEQF, the results using Davies equation activity coefficients are as low at high ionic strength as they were at 25°C. Results using Debye-Huckel activity coefficients are quite high above 1-molal NaCl content; one result, 7.8×10^{-4} molal BaSO_4 solubility at 4-molal NaCl content, was not plotted. The results of REDEQL.EPAK are also in good agreement up to 1-molal NaCl content, but are quite low at higher ionic strengths. The reasons for this are the same as those noted for the 25°C results.

G. Test Case 7 Results

Figure 17 shows a plot of CaSO_4 solubility as a function of total NaCl content of the solution at 25°C for Test Case 7. The solid line is the

same curve as is drawn through the experimental data at 25°C in Fig. 7. Figures 18 and 19 show similar plots for 100 and 250°C data.

At 25°C (Fig. 17), the results from GEOCHEM, WATEQF, and REDEQL.EPAK are in reasonable agreement with the experimental curve up to 0.5-molal NaCl content. Above that, the results from GEOCHEM are well above the curve and the results from REDEQL.EPAK and WATEQF are below. The best agreement is for WATEQF using Debye-Huckel activity coefficients. GEOCHEM results are high at high NaCl content for the same reason as Test Case 1; the formation of CaCl^+ complex ties up a substantial amount of calcium. The results from SENECA2 are slightly high at low NaCl content and are well above the experimental curve at high ionic strengths. The difference is caused by a combination of formation-constant and activity-coefficient data.

At 100°C (Fig. 18), results from SENECA2 and WATEQF are in reasonable agreement with the experimental curve. Differences at 2-4-molal NaCl content result from activity-coefficient data. REDEQL.EPAK results are high at low ionic strength, and have the wrong variation with NaCl content from 1-4 molal. The results at low ionic strength are related to formation-constant data; the trend at high ionic strength is caused by high activity coefficients for Ca^{+2} and SO_4^{-2} (see Test Case 1 results). GEOCHEM was not usable at 100 or 250°C.

At 250°C (Fig. 19), results from SENECA2 are in reasonable agreement at low ionic strength, but fall well below the experimental curve above 1-molal NaCl content. Activity-coefficient data are the main cause of this difference. The results of WATEQF are very high over the entire range of NaCl content. The equilibrium constant for solid CaSO_4 (anhydrite) formation used by WATEQF is much greater than the value used by SENECA2; this leads to considerably higher solubility. Results from REDEQL.EPAK are so high as to be above the range of the plot except for one point at 4-molal NaCl content. Off-scale points range from 0.06-0.1-molal CaSO_4 solubility. A large equilibrium constant for the formation of solid CaSO_4 is the major reason for the very high solubilities predicted by REDEQL.EPAK.

Fig. 15. Results for Test Case 6 at 25°C.

Fig. 16. Results for Test Case 6 at 95°C.

Fig. 17. Results for Test Case 7 at 25°C.

Fig. 18. Results for Test Case 7 at 100°C.

Fig. 19. Results for Test Case 7 at 250°C.

V. TIMING TESTS

Timing tests, which compared execution times for three of the four chemical-equilibrium programs, were also performed. Test problems used for the timing tests involved solutions from which a number of possible solid phases could precipitate. WATEQF was not included in the timing tests because it does not predict actual solid phases formed (see Sec. II.C).

Table II lists total concentrations of species for three test problems. The data were assumed to be in molal units for SENECA2 and molar units for REDEQL.EPAK and GEOCHEM. No attempt was made to compare results of the three programs except for the identity of the solid phases predicted. Thus, the assumption that molal and molar units are equivalent is acceptable here. In Timing Problem 1, possible solid phases are CaCO_3 , MgCO_3 , $\text{CaMg}(\text{CO}_3)_2$, SiO_2 , ZnCO_3 , and PbCO_3 . For Timing Problem 2, sulfide ion was added so that ZnS and PbS were also possible solids. For Timing Problem 3, the concentration of a number of ions was reduced, but possible solid phases remained the same as in Problem 2.

TABLE II

TIMING TEST PROBLEMS

Species	Total Concentration (molal or molar)		
	Problem 1	Problem 2	Problem 3
Na^+	0.500	0.500	0.500
Cl^-	0.504	0.530	0.454
Ca^{+2}	0.050	0.050	0.050
Mg^{+2}	0.030	0.030	2×10^{-3}
H_4SiO_4	0.030	0.030	2×10^{-3}
CO_3^{-2}	0.150	0.150	0.100
H^+	0.240	0.240	0.150
OH^-	0.100	0.100	0.100
Zn^{+2}	1×10^{-3}	2×10^{-2}	1×10^{-5}
Pb^{+2}	1×10^{-3}	2×10^{-2}	1×10^{-5}
S^{-2}	-	2.5×10^{-2}	1.1×10^{-5}

The timing runs were made on a Los Alamos Control Data Corporation (CDC) 7600 computer operating under the LTSS time-sharing system.³⁰ Central processor unit (cpu) times were compared. REDEQL.EPAK and GEOCHEM were compiled as they were received except for a few small changes that were necessary for compatibility with the CDC FTN compiler.

Table III lists the cpu times obtained. The small differences between REDEQL.EPAK and GEOCHEM are not significant; on a time-sharing system like LTSS, small differences of this magnitude can be obtained from repeated runs of the same problem if the system load (number of users) varies. The results from these two programs are essentially the same for the three problems. SENECA2 is competitive for Timing Problem 1, but shows significantly longer cpu times for the second and third problems. SENECA2 had considerable difficulty with species present in small amounts in the third timing problem. Most of the time was spent in the first step of the calculation (see Sec. II.D.). Although this procedure minimizes the free energy of the system, it depends on the definition of a basis set or set of elemental species that must be present.⁷ Much of the additional time is spent changing species in the basis set during early phases of minimization.

Table IV lists the solid phases predicted for Timing Problems 1 and 2. The differences reflect a disagreement in equilibrium-constant data among the three programs. Because there are no experimental data for comparison, it is not possible to establish which solid phases are correct for these problems.

VI. CONCLUSIONS

The purpose of the work was to compare results from four chemical-equilibrium computer programs with experimental solubility data for some simple systems of geothermal interest. The test cases were rather severe on occasion, with ionic strengths up to 4 molal and temperatures up to 300°C. None of the four programs showed consistently good agreement with experimental data. Two causes of disagreement were related to free-energy or equilibrium-constant data and to activity coefficients.

TABLE III
TIMING TEST RESULTS

Program	cpu Time (s)		
	Problem 1	Problem 2	Problem 3
SENECA2	1.63	2.35	15.33
REDEQL.EPAK	1.13	1.15	1.12
GEOCHEM	1.14	1.28	1.12

TABLE IV
SOLID PHASES PREDICTED WITH TIMING PROBLEMS

Timing Problem	Solid Phases Predicted		
	SENECA2	REDEQL.EPAK	GEOCHEM
1	CaCO ₃ ZnCO ₃ PbCO ₃ SiO ₂ CaMg(CO ₃) ₂	CaCO ₃ ZnSiO ₃ PbCO ₃ SiO ₂ CaMg(CO ₃) ₂	CaCO ₃ ZnCO ₃ PbCO ₃ SiO ₂
2	CaCO ₃ ZnS PbS PbCO ₃ SiO ₂ CaMg(CO ₃) ₂	ZnS ZnSiO ₃ PbS SiO ₂ CaMg(CO ₃) ₂	CaCO ₃ ZnS ZnCO ₃ PbS SiO ₂

All four programs give similar activity coefficients at ionic strengths in the 0-1-molal range. At higher ionic strengths, the Davies equation and its variants gave activity coefficients that were too large. Thus, REDEQL.EPAK and WATEQF (using the Davies equation) predict solubilities that are too low at high ionic strengths. The SENECA2 activity coefficients appear to yield more reasonable results at high ionic strengths. As an example of some of the differences observed, Table V lists calculated activity coefficients for three species involved in the solubility reactions:

TABLE V
ACTIVITY COEFFICIENTS AT 25°C

	Activity Coefficient at Ionic Strength			
	0.1	0.5	2.0	4.0
Na ⁺				
REDEQL.EPAK	0.772	0.691	0.804	1.169
GEOCHEM	0.780	0.680	0.725	0.820
WATEQF(D) ^a	0.782	0.708	0.789	1.043
WATEQF(D-H) ^a	0.782	0.708	0.789	1.043
SENECA2	0.776	0.681	0.671	0.752
Ca ⁺²				
REDEQL.EPAK	0.356	0.229	0.419	1.868
GEOCHEM	0.371	0.224	0.208	0.207
WATEQF(D) ^a	0.390	0.260	0.289	0.509
WATEQF(D-H) ^a	0.390	0.260	0.289	0.509
SENECA2	0.404	0.262	0.208	0.215
Ba ⁺²				
REDEQL.EPAK	0.356	0.229	0.419	1.868
GEOCHEM	0.371	0.224	0.208	0.207
WATEQF(D) ^a	0.372	0.288	1.069	12.3
WATEQF(D-H) ^a	0.376	0.214	0.135	0.111
SENECA2	0.380	0.225	0.163	0.161

^aD indicates Davies equation and D-H indicates Debye-Huckel equation.

Na^+ , Ca^{+2} , and Ba^{+2} . The large differences at high ionic strengths are apparent.

Inaccurate free-energy or equilibrium-constant data were a major cause of differences between calculated results and experimental data. Data for the solubility reaction itself or for formation of complexes with common ions could be at fault. GEOCHEM provided examples of both situations; a large value for the formation constant of solid BaSO_4 led to low solubilities in Test Case 6, and a large value for the formation constant of CaCl^+ led to high solubilities in Test Cases 1 and 7. The other programs provided similar examples, particularly at high temperatures.

One of the four programs tested, WATEQF, is clearly not suitable for modeling precipitation from geothermal brines because it does not calculate the amounts of solid phases that are formed. Also, the necessity of specifying the pH of the solution complicates its use if pH is unknown. GEOCHEM and REDEQL.EPAK are very similar programs as far as the tests conducted here are concerned. Although REDEQL.EPAK has the capability of calculation at temperatures other than 25°C , only a small percentage of species in the data base have the needed data available. Both programs showed good results in the timing tests. SENECA2 generally showed good results in comparisons with experimental data. The data base for SENECA2 is much smaller than that in the other three programs, but it emphasizes reactions of geothermal interest. SENECA2 might require significant modifications in the calculation procedure to improve its performance in the timing tests.

The overall conclusion of this work is that currently available chemical-equilibrium computer programs can give reasonable results when used for modeling precipitation from geothermal brines. However, considerable care must be taken to check free-energy data and activity coefficients because significant errors can be caused by inaccuracies in either type of data. If chemical modeling of geothermal brines is to become an accurate science, the two greatest needs are accurate free-energy data and an accurate method of calculating activity coefficients at high ionic strength.

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