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REAL-TIME ULTRASONIC SENSING OF ARC WELDING PROCESSES

by

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NDE techniques are being investigated for fusion zone sensing of arc welding processes for closed-loop process control. An experimental study of pulse-echo ultrasonics for sensing the depth of penetration of molten weld pools in structural metals during welding indicates that real-time ultrasonic sensing is feasible. Results on the detection of liquid/solid weld pool interfaces, the determination of interface location, and effects of high temperature gradients near the molten zones on ultrasonic wave propagation are presented. Additional work required and problems associated with practical application of the techniques are discussed.

MODERN AUTOMATIC ARC WELDING equipment is very sophisticated, controlling the major machine functions such as welding current, arc voltage, travel speed, filler wire speed, mechanical motions of the torch, etc. Some machines are even microprocessor controlled. However, with few exceptions, information about the physical state of the weld fusion zone is not used in real-time process control. (Exceptions to this are systems which use optical or IR sensors to measure the size or temperature of the fusion zone surface on the opposite side from the torch of thin materials being welded.¹) In almost all cases, the human operator "closes the loop" manually, adjusting the welding parameters during the process based on his observations. Thus weld quality is still strongly dependent on operator skill and experience for many automated arc welding applications.

Weld bead penetration is often critical. Unfortunately, the weld operator rarely is able to determine visually the extent of penetration. A sensing technique which can directly measure the extent of weld bead penetration (preferably from the

same side of the part as the welding torch) and provide real-time information for closed-loop control of the machine parameters to maintain the desired weld penetration configuration is a real need.

In addition to the sensing technology, the implementation of such a system would require

- o microprocessor control hardware (this is already available)
- o a model of process parameter/bead geometry relationships² (how must the welder parameters be changed to achieve a desired change in bead geometry)
- o a process sensing algorithm (what must be done with the sensor signal to extract the desired penetration information)
- o a process control algorithm (selection of the optimum parameters taking into account the process model, sensing, welding hardware and inherent process limitations).

Such an automatic welding machine is diagrammed in Fig. 1; the basic feedback loop consists of the molten weld pool, the process control sensor, the sensor data acquisition and signal processing system, the process controller, the welder power supply, the welding torch and arc, and back to the molten weld pool.

Ultrasonics shows promise for weld penetration sensing, as described in this paper. Ultrasonics has the potential to locate the edge of a molten weld zone by virtue of the unique ability of ultrasonic waves to propagate through thick metal structures and be reflected at

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Fig. 1 - Ultrasonic controlled welding process concept

discontinuities in ultrasonic impedance such as occur at liquid/solid interfaces. By the detection and accurate timing of ultrasonic pulses reflected from the liquid/solid interface of a molten weld pool, the position of the interface could be determined and a process control signal generated to maintain the desired weld penetration. At liquid/solid interfaces of typical structural steels, the differences in density and longitudinal ultrasonic wave velocity between the liquid and solid phases are such that the amplitude reflection coefficients are approximately 0.1, or 10%.³⁻⁷ For ultrasonic shear waves, the theoretical reflection coefficient is 1.0, or 100%, since the liquid state will not support shear wave propagation.

BACKGROUND

Ultrasonic techniques have been used to detect liquid/solid interfaces in a variety of different materials for applications including basic solidification studies, monitoring of crystal growth, and monitoring of metal casting processes. Bailey and Dula⁸ followed the motion of the liquid/solid interface during the freezing of water using 1.0 MHz longitudinal ultrasonic waves incident from the liquid side. Bailey and Davila^{9,10} also observed this interface during the freezing of mercury and paraffin under unidirectional heat flow conditions using 2.25 MHz longitudinal waves. Kurz and Lux⁵⁻⁷ detected longitudinal wave reflection from liquid/solid interfaces in Wood's Metal, a Pb-Sn alloy, and steel. They found that reflected ultrasonic signals were reduced by the geometry of the interface and by high attenuation in the solid material at high temperatures. At low solidification rates during the casting of steel, they found that rough surfaces at the interface due to

dendritic grain growth and the presence of a "mushy" transition zone between the solid and liquid reduced the reflected ultrasonic signal. They also observed a decrease in sound velocity in the solid of up to 25% caused by high temperatures which must be accounted for in thickness or interface location measurements.

Lynnworth and Carnevale⁴ observed both longitudinal and shear wave reflections at liquid/solid interfaces of steel in a study of continuous casting processes. They also observed that interface roughness due to dendritic grain growth reduced the reflected ultrasonic signal. They saw little advantage of shear waves despite the theoretical 100% reflectivity at the interface. Jeskey et al.¹¹ considered ultrasonic pulse-echo reflectivity measurements for monitoring steel ingot solidification. However, because of ultrasound propagation problems associated with coupling, high absorption, grain scattering, and ill-defined and irregular surfaces, a method based on through-transmission transit time was used for solidification rate measurement. Parker³ studied the feasibility of pulse-echo ultrasonics for process control in continuous casting of metals. He succeeded in determining the position of the liquid/solid interface in 99.9 Sn during both freezing and melting to ± 1 mm using 5 MHz longitudinal ultrasound.

Katz¹² considered the possibility of ultrasonic measurement and control of weld penetration in a study similar to this work. He gave a good analysis and discussion of the concept and reported some experimental results on molten zones at the ends of cylindrical rods. He failed to detect molten weld pools in flat plate specimens but, nonetheless, concluded that ultrasonic weld pool dimensional measurement is potentially feasible.

The scope of the work described here is to study the problem of ultrasonically detecting, locating, and determining the dimensions of molten weld zones in structural steel. The main objectives are to determine the feasibility of the method and to obtain preliminary information needed as a first step toward developing an automatic closed-loop welding system controlled by ultrasonic sensors. The work is an experimental laboratory study in which stationary spot-on-plate welds are formed on the surface of steel specimens simultaneously with ultrasonic monitoring of the weld zone.

EXPERIMENTAL METHODS

The experimental measurements are performed with the test specimens suspended in a conventional ultrasonic immersion

testing tank as shown schematically in Fig. 2. This is done in such a way that the bottom surface is immersed in water to facilitate coupling of ultrasonic waves into the sample, while leaving the top surface dry for welding. The welder and torch are common gas tungsten arc welding (GTAW) equipment and are operated manually during experimental runs. The torch and ultrasonic transducer are mechanically connected so that after initial setup and alignment, the assembly can be easily moved from point to point on the test specimen between test runs while maintaining alignment.

Fig. 2 - Schematic diagram of experimental system

The test specimens are 25 mm (1 in.) thick by 100 mm (4 in.) wide by 360 mm (14 in.) long plates of carbon steel or 304 stainless steel. One specimen was prepared with a series of four evenly spaced holes 1.6 mm (0.063 in.) in diameter and approximately 25 mm (1 in.) deep drilled into the side of the specimen as shown in Fig. 3. When welding on the specimen directly above the holes and monitoring with ultrasonics from directly below as shown in Fig. 3, reflected ultrasonic signals from the weld pool region are received at the same time as reflections from the side drilled hole reflections. In this way the side drilled hole reflections serve as internal markers of known position with which the position of the weld pool reflections can be calibrated.

The data acquisition system is shown schematically in Fig. 4. Standard 0.5-in. diameter ultrasonic immersion transducers of nominal frequencies of 1, 2.25, 5, and 10 MHz are used with a standard ultrasonic testing pulser-receiver unit. The ultrasonic data acquisition is completely automatic and computer controlled. The pulser is triggered by a signal from the computer and specified portions of the received A-scans are digitized to 8-bit accuracy at a maximum rate of 20 MHz by a

Fig. 3 - Test sample configuration

Fig. 4 - Data acquisition system

waveform digitizer whose output is then stored in the computer. The data are stored on disk or magnetic tape and recalled at a later time for display and posttest processing. A purchased interactive data processing software package (ILS, Signal Technology, Inc.) is used for data acquisition, file manipulation and management, processing, and display.

After initial setup and alignment of the welding torch, transducer, and sample, the computer is instructed to trigger the pulser at regular intervals and digitize and store windowed portions of the radio frequency A-scans. Typically, 20 or 30 A-scans are taken at 1-s intervals. Once the data acquisition cycle is initiated, the welder is turned on for a period of time, typically 10 s, and then turned off. Thus, a data record of 20 s, for example, consists of one or two A-scans showing the reflected signal from the top sample surface (no weld pool), then ten scans showing the reflected

signal from the weld pool region as the pool forms and grows, and finally several more scans as the weld pool solidifies and cools.

EXPERIMENTAL RESULTS

In carbon steel and 304 stainless steel, reflected ultrasonic signals from at least two interfaces in the weld pool region are received for normally incident longitudinal waves. A typical result is shown in Fig. 5, a display of a computerized data record for a 16-s weld spot experiment on a stainless steel sample for 10 MHz longitudinal waves. The A-scans were taken at 1-s intervals before, during, and after a molten weld spot was formed in the sample.

Fig. 5 - Ultrasonic A-scans of weld spot in 304 stainless steel

The first scan (time zero) was obtained before the welder was turned on and shows only the reflection from the upper solid/air surface of the sample. The next nine scans were taken while the welder was on and a molten weld pool formed and grew in size. As the pool started to form, the single reflected signal split into two reflected

pulses which separated further in time as the pool grew in depth. After the welder was turned off, the two reflected pulses coalesced into a single signal as the pool solidified and cooled. The final reflected pulses are distorted because of the nonplanar surface of the weld spot and disturbance of the beam by the weld zone microstructure. Note also that in addition to separating in time during welding, both reflected pulses moved to the right (Fig. 5), corresponding to longer time delays. This effect is caused by the high temperatures present in the sample; ultrasonic wave velocities are known to decrease with increasing temperature,⁵ thus producing the shift to longer time delays. This is discussed in more detail below under Analysis and Interpretation.

The two reflected pulses from the molten weld pool are more easily distinguishable in Fig. 6 which shows two of the A-scans of Fig. 5 plotted in different time and amplitude scales. The first A-scan of Fig. 6, which is the first A-scan of Fig. 5, shows the reflected pulse from the top surface of the sample before the welder was turned on; the other A-scan is the tenth scan of Fig. 5, which was taken just before the welder was turned off when the weld pool was deepest. The two pulses are easily distinguishable in the later scan and the time interval between them (approximately 1 μ s) can be measured. There is a noticeable difference in shape between the two pulses: the first being similar (however attenuated) to the original solid/air reflected pulse, but the second distinctively different in both damping

Fig. 6 - Selected ultrasonic A-scans of Fig. 2 at different amplitude and time scales (scans #0 and #9)

(number of peaks in the pulse) and phase (largest peak negative instead of positive). This implies that a pattern recognition technique based on these features might be successful in discriminating between the various signals received in an actual weld monitoring application, if necessary.

In the later scan of Fig. 6, an area of low level signal can be seen ahead in time of the two main reflecting pulses, indicating the presence of a third interface in the weld pool region. The interpretation of the ultrasonic data and the identification of the three interfaces are discussed in the next section.

ANALYSIS AND INTERPRETATION

An understanding and interpretation of the experimental data require calculation of the temperature gradients around the weld pool and of the effects of the gradients on the sound field. The gradients are calculated by numerically solving the heat flow equations. A numerical ray-tracing program is then used to determine the effects of the gradient.

TEMPERATURE GRADIENT CALCULATIONS - The thermal-hydraulics code STEALTH¹³ is used to calculate the temperature gradients as a function of time. The problem is modeled by a fixed weld-pool boundary which is at the melting temperature of the steel. The heat flow from this boundary into the solid steel is calculated as a function of time, and from this the temperature distribution in the solid steel is calculated.

The mesh used in this calculation is shown in Fig. 7. (Note: Figs. 7 and 8 are oriented upside down relative to all other figures.) The horizontal axis is the radial distance from the centerline of the weld pool and the vertical axis is the distance from the top of the weld pool. The left boundary is the axis of symmetry for this axially symmetric model. The curved portion of the mesh boundary represents the liquid/solid interface which is at the melting temperature (1400°C) of 304 stainless steel. The bottom horizontal boundary, which is actually adjacent to room temperature air in the experiment, is modeled as an adiabatic boundary. The remaining boundaries are in water at 20°C and are isothermal.

The STEALTH code requires that the material properties and the initial conditions of the mesh be input. The properties are those of 304 stainless steel as given in References 14 and 15 and Table 1. The entire solid steel volume is assumed to be at 20°C at the start of the problem.

Fig. 7 - Mesh used in numerical calculation of temperature distribution

Table 1 - 304 Stainless Steel Properties

Density	
Solid	8.0 g/cm ³
Liquid	6.9 g/cm ³
Bulk Modulus	1.63 x 10 ¹² dyne/cm ²
Shear Modulus	7.31 x 10 ¹¹ dyne/cm ²
Heat Capacity	4.0 x 10 ⁷ erg/cm ³ °C
Thermal Conductivity	1.62 x 10 ⁵ erg/cm-°C

Given the initial conditions, the code calculates the temperature at the center of each mesh quadrilateral and the heat flux through each edge of each quadrilateral. This information is recalculated at time intervals of 0.01 s using the information from the previous cycle.

The results of the calculation can be plotted or printed. Fig. 8 shows the isotherms around the weld pool at 5.0 s after the start of the problem. The five contour levels correspond to 1100, 900, 700, 500, and 300°C moving away from the weld pool. The calculated temperatures at the center of each mesh cell are then used as input to the ray-tracing program described next.

RAY TRACING - The ray-tracing program calculates the effects of the temperature distribution on the rays of the sound field. In general, two effects occur: Changes in the sound speed with temperature and the consequent refraction of the sound

Fig. 8 - Isotherms around a 4 mm deep weld at 5.0 s

beam due to the sound-speed changes. The first affects the timing of the returning echoes and the second affects the apparent lateral position of the reflectors.

The sound field is modeled by a point source of sound at the bottom surface of the part on the centerline of the beam of the actual transducer. Rays are traced from this point into the material at any angle, accounting for the variation of the sound speed due to the temperature distribution in the part.

The material is divided up into a large number of thin layers. Within each layer the sound is assumed to travel in a straight line at a speed determined by the temperature at the center of the layer on the line of the ray. The time for the ray to traverse the layer is then calculated from the sound speed, thickness, and ray direction.

The refraction of the rays at the boundary between layers is shown in Fig. 9. A linear least-squares fit in two dimensions is made to the temperature distribution using the four temperature values nearest the intersection of the ray and the layer boundary. These values are taken from the output of the STEALTH program as described above. The expression for the temperature distribution in the neighborhood of the ray/boundary intersection is then

$$T = ax + by + c$$

where a , b , and c are the coefficients derived in the fitting process and x and y are the Cartesian coordinates. From this an

Fig. 9 - Refraction of a ray at a boundary between layers

expression for the gradient is found to be

$$\vec{\nabla}T = a\hat{i} + b\hat{j}$$

The angle of the temperature gradient relative to the axis is

$$\alpha = \tan^{-1} \frac{a}{b}$$

The direction of the gradient is in the same direction as the normal to a plane surface, shown in Fig. 9. This plane surface is the boundary between the two regions of different temperature in this numerical model. It is also then the dividing line between two regions with different sound speeds. Thus the incident and refracted angles used in Snell's law must be calculated relative to the normal to this plane or relative to the direction of the temperature gradient.

The incident ray is assumed to be at angle ϕ relative to the y axis as shown in Fig. 9. The angle relative to the surface normal as required by Snell's law to calculate the refracted angle in the next layer is:

$$\theta_i = \phi_i - \alpha$$

Using Snell's law the refracted angle relative to the surface normal can be found

$$\sin \theta_t = \frac{v_t}{v_i} \sin \theta_i$$

where v_i is the sound speed in the incident layer and v_t is the sound speed in the next layer. Finally the angle relative to the y axis in the next layer is calculated.

$$\phi_t = \theta_t + \alpha$$

The sound speeds are calculated from the temperature at the center of the layer along the line of the incident ray using a straight-line fit to the measurements of Kurz and Lux for X5 CrNi 18/9 steel.⁵ These data are assumed to approximate that for 304 stainless steel.

For rays entering the liquid phase, the same procedure is followed except that the temperature is assumed to be constant in the weld pool. This temperature is chosen to be approximately the average temperature of the pool or 1900°C. By extrapolating the data of Kurz and Lux⁵ to 1900°C, the velocity in the liquid is found to be 3.6 mm/s. The path of any ray entering the liquid is extended 0.7 mm above the level surface of the part to account for the meniscus formed above the pool due to the expansion of the steel upon melting.

The calculation starts by assuming a given position of the point source and of the initial ray angle. The ray is then traced through successive layers until it reaches the top surface of the steel block. The time for the ray to reach any point in the block may be determined and from that the round-trip time for an echo returning from that point calculated. The relative time from different reflectors can then be determined and compared to experimental values.

RESULTS - Fig. 10 shows three rays traced through the steel. The center ray is directed normally to the surface of the part, travels to the weld pool (represented by the dotted line), into the pool, and finally to the top surface. The actual sound field would be partially reflected at the positions of the side-drilled holes, at the solid/liquid interface, and at the top surface. The other rays are at the smallest angle such that the rays will just miss the weld pool and intersect the top surface after traveling only through the solid.

The interpretation of the observed echoes is based on the times for the rays to reach each interface as calculated by the ray tracing program and are shown in Table 2. Fig. 11 shows the interpretation

Fig. 10 - Three rays traced from the bottom of the part through and around the weld pool

Fig. 11 - Interpretation of the three observed echoes

of the observed echoes. The times of the echoes are calculated relative to the time for the echo from the side-drilled hole that is second from the top. These times are then compared to those observed in the experiment and the correlation that is shown in Table 2 is obtained.

Table 2 - Calculated and observed echo times (μ s)

Interface	Relative Time	Observed Relative Time
2nd side-drilled hole	0.0	0.0
1st side-drilled hole	1.83	1.85
Liquid/solid interface (1)	2.42	2.60
Solid/air interface (2)	4.16	4.10
Liquid/air interface (3)	5.04	4.75

Figure 12 shows two A-scans, one taken before the welder was turned on and one at 5 s after. The data from Table 2 are also plotted with the arrow marking the time for the second side-drilled hole aligned with the first positive peak of the echo from that interface. The other arrows can be seen to align closely with the corresponding echoes in the A scan.

Fig. 12 - Comparison of calculated echo times with A-scan

This interpretation is supported by two experimental observations. The last signal received, as seen on an oscilloscope screen during the experiment, was observed to fluctuate rapidly with time in a manner suggesting a signal reflected from a disturbed free liquid surface, which a molten weld pool surface certainly is. Unfortunately, the data acquisition system can take data only about every second and this dynamic action does not appear in the digitized A scans. The small echo due to the liquid/solid interface was observed to move gradually earlier in time relative to the side-drilled hole, corresponding to the expected gradual increase in the depth of the pool.

These signals can be used to measure the weld-pool depth. Unfortunately, the signal from the liquid/solid interface is small and is not always present. However, the time difference between the other two echoes is approximately proportional to the pool depth. The time difference can be calculated relative to the time for the echo from the solid/liquid interface

$$\begin{aligned} t_3 &= t_1 + 2D/V_L \\ t_2 &= t_1 + 2D/V_S \end{aligned}$$

where the subscripts refer to the rays shown in Fig. 11 and D is the pool depth. However, the time through the pool must be modified to account for the meniscus. For a pool depth of 4 mm, the meniscus has been calculated to be 0.7 mm high. The path length through the liquid is then increased

in proportion to the pool depth and the time t_3 is recalculated:

$$\Delta D = \frac{0.7}{4} D$$

$$t_3 = t_1 + \frac{2(D + \Delta D)}{V}$$

The time difference and the pool depth can be calculated.

$$t_3 - t_2 = 2D \frac{1.175 V_S - V_L}{V_S V_L}$$

$$D = \frac{V_S V_L}{2(1.175 V_S - V_L)} \Delta t$$

$$= 3.95 \Delta t$$

where the average value for the speed $V_S = 5.0$ mm/μs around the pool is determined from the ray tracing program and the average value through the pool is the same as estimated above ($V_L = 3.6$ mm/μs).

The results from three weld pools of different depths, made by using three different welder power inputs, are summarized in Fig. 13. The A-scans recorded just before the welder was turned off are shown along with a photomicrograph of the solidified fusion zone for each weld pool. (Note that it is much easier to identify the position of the reflected pulses when the complete series of A-scans can be seen and compared.) A plot of ultrasonic transit times versus weld pool depths for the data of Fig. 13 is shown in Fig. 14. The result is a linear plot with a slope of 4.0 compared to 3.95 calculated above.

SUMMARY AND CONCLUSIONS

We have demonstrated that molten weld pools in structural steels can be detected ultrasonically and the data understood, both qualitatively and quantitatively, in terms of the weld pool configuration and the surrounding temperature gradients. Using longitudinal ultrasonic waves, information about weld pool depth, or penetration, for a simple weld configuration can be obtained during welding which might be used for closed-loop process control.

Before practical application of the techniques on realistic welding processes, however, additional work needs to be done in several areas. The high temperature environment near a weld zone presents both hardware and data interpretation problems. The hardware problems are associated with the process of coupling ultrasonic energy into a hot test piece. These problems should be solvable by the use of cooled ultrasonic search heads, momentary contact

Fig. 13 - Comparison of three weld pools of different depths

techniques, or noncontact techniques such as electromagnetic acoustic transducers or laser techniques for generation and detection of ultrasonic waves. For welding geometries more complex than the stationary flat plate weld spots considered in this study, a more detailed knowledge of the effects of temperature gradients on wave

Fig. 14 - Correlation of weld-pool depth and time difference between echoes

propagation will be necessary. Realistic weld configurations will also likely require the use of ultrasonic shear waves entering from the top surface of the structure being welded, and an investigation of weld zone detection by shear waves will be necessary.

The fact that the ultrasonic signals reflected from liquid/solid interfaces of molten weld pools are quite small will likely require the use of sophisticated signal processing techniques for detection and analysis of the data. Development of such techniques remains to be done. Finally, much work must be done to develop algorithms for specific process control applications, i.e., exactly how must the ultrasonic data be acquired, interpreted in terms of weld zone configuration, and converted to an optimum process control signal.

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REFERENCES

1. Vilkas, E. P., *Welding Journal*, 45, 410-16 (1966).

2. Smartt, H. B. and J. F. Key, "An Investigation of Factors Controlling GTA Weld Bead Geometry," ASM Conference on Trends in Welding Research in the United States, November 1981, New Orleans, LA.
3. Parker, R. L. , "Physics in the Steel Industry," pp. 254-271, F. C. Schwerer (ed.), (1982) published by American Institute of Physics, New York, as AIP Conference Proceedings No. 84.
4. Lynnworth, L. C. and E. H. Carnevale, "Proceedings of the Fifth International Conference on Nondestructive Testing," pp. 300-307, The Queen's Printer, Ottawa, Canada (1969).
5. Kurz, W. and B. Lux, Berg-und Huttenmannische Monatshefte, 114, 123-130 (1969) (in German).
6. Kurz, W. and B. Lux, Translated from Archiv f. d. Eisenhüttenwesen, 39, 521-530 (1968), Available in English from Henry Bratcher Translations, ASM, Metals Park, Ohio as HB No. 7528.
7. Kurz, W. and B. Lux, Zeits. Metallkunde, 57, 70-73 (1968), (in German).
8. Bailey, J. A. and A. Dula, Rev. Sci. Instruments, 38, 535-538 (1967).
9. Bailey, J. A. and J. R. Davila, Appl. Sci. Res., 25, 245-261 (1971).
10. Bailey, J. A. and J. R. Davila, Journal of the Institute of Metals, 97, 248-251 (1969).
11. Jeskey, G. V., L. C. Lynnworth, and K. A. Fowler, AFS International Cast Metals Journal, 2, 26-30 (1977).
12. Katz, J. M., "Ultrasonic Measurement and Control of Weld Penetration," M.S. thesis, Massachusetts Institute of Technology, 1982.
13. R. Hoffmann, "STEALTH, A Language Explicit Finite-Difference Code for Solids, Structural and Thermodynamic Analysis," EPRI NP-260, August 1976.
14. "Metals Handbook," 9th Edition, Vol. 3, pp. 34-35, American Society of Metals, Metals Park, Ohio (1980).
15. "Marks' Standard Handbook for Mechanical Engineers," p. 5-5, Theodore Baumeister (ed.), McGraw-Hill, New York (1978).