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PREDICTED PROPERTIES OF THE W^{\pm} and z^{0}

William J. Marciano

Brookhaven National Laboratory, Upton, New York 11973

and

DE83 002842

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Zohreh Parsa

Taman 07107

Summary

Fredicted properties of the W^{\pm} and 2^{0} bosons in the standard SU(2) × U(1) model are presented. For the current value of the weak mixing angle,

 $\sin^2 \theta_{\rm W}(m_{\rm W}) = 0.215 \pm 0.014$, one finds

$$m_W = 83.0^+_{-2.8}$$
 GeV and $m_Z = 93.8^+_{-2.4}$ GeV.

Implications of deviations from these predictions are discussed. Decay rates and branching ratios for the W^{\pm} and Z^0 are given. Radiative corrections, higher order rare decays and exotic possibilities are described.

1. If and Z⁰ Masses

The standard SU(2) \times U(1) electroweak model makes rather definite predictions regarding the masses of the W[±] and 2⁰ intermediate vector bosons. In the case of the W[±], one has the following lowest order relationship

$$\mathbf{m}_{W}^{0} = \left[\frac{\pi \alpha^{0}}{\sqrt{2} c_{W}^{0} \sin^{2} \theta_{W}^{0}}\right]^{1/2}$$
(1)

where the superscript zero signifies bare (unrenormalized) parameters. For $\alpha = 1/137.036$,

 $G_{\mu} = 1.116632 \times 10^{-5} \text{ GeV}^{-2}$ (the muon decay constant) and $\sin^2 8 \text{gerp} = 0.227$ (the lowest order result from v_u-hadron scattering¹), one finds

 $m_{y} = 78.3 \text{ GeV}$ (lowest order). (2)

However, the O(a) radiative corrections to the above relationships are sizesble². Employing the renormalized weak mixing $angle^{3-4}$ $sin^2\theta_{4}(m_{4})$, defined by $\overline{\text{MS}}$ (modified minimal subtraction) with $\mu = m_{4}$, gives to O(a)²⁻⁵

$$\mathbf{m}_{\mathcal{U}} = \frac{38.5 \text{ GeV}}{\sin\theta_{\mathcal{U}}(\mathbf{m}_{\mathcal{U}})} \tag{3}$$

A two parameter fit to v_{μ} and \widetilde{v}_{μ} scattering data yields $^{1},^{6}$

$$\rho^{exp.} = 1.010 \pm 0.020$$
 (4a)

$$\sin^2 \theta_{\rm W}(m_{\rm W}) = 0.236 \pm 0.030$$
 (4b)

where $\rho^0 = \frac{0^2}{m_W^0} / \frac{1}{m_Z^0} \cos^2 \theta_W^0$. Combining Eqs. (3) and (4), we find $m_W^0 = 79.3 + 5.5 \text{ GeV}$. One can do better by employing the standard model's constraint $\rho^0 = 1$ and appending the O(α) rediative corrections to the analysis of deep-inelastic v_{μ} -hadron scattering above. In that way one finds⁷

$$\sin^2 \theta_{\rm g}(m_{\rm g}) = 0.215 \pm 0.014$$
 (5b)

which implies the rather precise prediction7

$$t_{W} = 83.0^{+}_{-2.8} GeV$$
 (6)

The difference between Eqs. (2) and (6) is about 62; a large shift induced by radistive corrections. We see that a precise measurement of my will test the standard model at the level of its quantum loop corrections.

The prediction for mg follows from the lowest order relation $m_Z^{0^2} = m_W^{0^2}/\cos^2\theta_W^{0^2}$. Employing $\rho^0 = 1$ implies the lowest order prediction via Eq. (1)

$$m_{\chi} = 89.0 \text{ GeV}$$
 (lowest order) (7)

However, including radiative corrections one finds²⁻⁵

$$\mathbf{a}_{Z} = \frac{77.1 \text{ GeV}}{\sin 2\theta_{W}(\mathbf{m}_{W})} (1 + \Delta)^{-1/2}$$
(8)

where Δ represents possible corrections to ρ not included in the standard model's radiative corrections (in the simplest case $\Delta = 0$). Comparing Eqs. (4a) and (5a) we find $\Delta = 0.02 \pm 0.02$ which when correlated with Eq. (4b) leads to $m_Z = 89.9 \pm 4.4$ GeV. If we assume $\Delta = 0$, i.e. nothing unexpected in ρ , then Eq. (5b) implies⁷

$$n_{Z} = 93.8^{+}_{-} \frac{2.5}{2.4} \text{ GeV}$$
 (9)

It is anticipated that my will be determined to within 0.1 GeV at e^+e^- colliders⁸; such a measurement will provide a value of $\sin^2\theta_{\rm W}(m_{\rm H})$ to within 0.37 via Eq. (8) but only under the assumption $\Delta = 0$. What would be interesting is to have an independent precise determination of $\sin^2\theta_{\rm W}(m_{\rm H})$ which when combined with my would yield Δ . For example, by precisely measuring both my (which determines $\sin^2\theta_{\rm W}(m_{\rm H})$ via Eq. (3) and my one can obtain Δ using



$$\Delta = 1 - \frac{m_W^2}{m_Z^2 [m_W^2 - (38.64 \text{ GeV})^2]}$$
(10)

A determination of w_{ij} to within 0.5 GeV at hadron colliders combined with a 0.1 GeV measurement of w_{ij} at e⁺e⁻ colliders will determine Δ to within 0.01.

An interesting example of an effect that could contribute to Δ is the possibility $m_{t} > m_{y}$. (t = top quark). (Eq. (5a) assumes $m_{t} \approx 20$ GeV.] In that case, a one loop calculation gives⁹

$$\Delta = \frac{3\pi}{16\pi \sin^2 \theta_{\rm H}(m_{\rm H})} = \frac{m_{\rm c}^2}{m_{\rm H}^2} = 0.002 \frac{m_{\rm c}^2}{m_{\rm H}^2}$$
(11)

Other potential contributions to Λ are additional fermion generations, higher dimensional Higgs representations, dynamical symmetry breaking effects¹⁰ etc.

Clearly, precise measurements of my, m2, Δ , and $\sin^2\theta_V(my)$ by as many methods as possible should be high priority experiments at future collider facilities. Those fundamental parameters test the standard model at the level of its quantum loop corrections and provide tight constraints on the structure of electroweak interactions.

2. F and 20 Decays

In this section we review the anticipated decay properties of the W^{\pm} and Z^{0} in the standard model. Since high luminowity colliders will produce about 10^{7} W^{\pm} and Z^{0} bosons per year, one may anticipate precise measurements of branching ratios, total widths, and decay asymmetries⁸. Perhaps rare higher order decays may even be observed. In addition, if the Higgs scalar is light it should be detectable through Z^{0} decays. The most exciting possibility would be a distinct deviation from the standard model, signaling new physics.

2.1 W= Decays

including QCD -corrections and lowest order top quark mass effects, the badronic decay width of the W² is predicted to $be^{1.1-1.2}$

$$\Gamma(\forall + hadrons) = \frac{3G_{m} m_{W}^{3}}{2/2\pi} \left(1 - \frac{m_{C}^{2}}{2m_{W}^{2}} + \frac{1}{6} \frac{m_{C}^{6}}{m_{W}^{6}}\right) \left(1 + \frac{\alpha_{s}(m_{W})}{\pi}\right)$$

= 2.28 GeV (for m₊ Ξ 20 GeV) (12)

for 2 generations. (Eq. (12) assumes $m_{\rm t}$ < mg.) The leptonic partial widths are

$$\Gamma(W + t\bar{v}_{t}) = \frac{G_{\mu}W_{\mu}}{6/2r} = 0.25 \text{ GeV}, \quad (t = e_{,\mu}, \tau) \quad (13)$$

Together these imply a total width

$$\Gamma(W + all) = 3.03 \text{ GeV}$$
 (14)

and leptonic branching ration

$$\frac{\Gamma(W + L_{\nu})}{\Gamma(W + a11)} = 0.083$$
(15)

The electroweak radiative corrections to these results are small, provided one measures inclusive rates i.e. including soft and hard bremsstrahlung. However, severely constraining the final state energy configurations can lead to significant QED effects (see Ref. 11).

2.2 Z^Q Decays

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In the case of the Z^0 , the partial decay widths are predicted to be (for three generations and $m_L \leq m_Z/2)^{11-12}$

$$\Gamma(z^{0} + \tilde{zz}) = \frac{G_{\mu} z^{3} (1 - 4s^{2} + 8s^{4})}{12 \sqrt{2\pi}} = 0.092 \text{ GeV} (16)$$

$$\Gamma(Z^{0} + v_{\underline{z}}v_{\underline{z}}) = \frac{G_{\underline{u}}m_{\underline{z}}^{3}}{12\sqrt{2\pi}} \approx 0.181 \text{ GeV}$$

$$(Z^{0} + \text{hsdrons}) = \frac{G_{\underline{u}}m_{\underline{z}}^{3}}{4\sqrt{2\pi}} F(s^{2}, m_{\underline{z}}^{2}/m_{\underline{z}}^{2}) (1 + \frac{a_{\underline{s}}(m_{\underline{z}})}{\pi}) \quad (17)$$

= 2.20 GeV, (for $m_{\rm g}$ = 20 GeV)

where $s^2 \equiv \sin^2\theta_y(my) = 0.215$ and 12

$$\mathbb{P}(s^{2}, \mathbf{u}_{L}^{2}/\mathbf{u}_{Z}^{2}) = 5 - \frac{28}{3}s^{2} + \frac{80}{9}s^{4} + (1 - \frac{4\mathbf{u}_{L}^{2}}{\mathbf{u}_{Z}^{2}})$$

$$[1 - \frac{8}{3}s^{2} + \frac{32}{9}s^{4} - \frac{\mathbf{u}_{L}^{2}}{\mathbf{u}_{Z}^{2}}(1 + \frac{16}{3}s^{2} - \frac{64}{9}s^{4})] \quad (18)$$

Adding these contributions, one finds

 $\Gamma(2^0 + all) = 3.02 \text{ GeV}$ (19)

$$\frac{F(Z^{0} + L\bar{L})}{F(Z^{0} + z11)} = 0.030 \text{ GeV}$$
(20)

The t quark mass effect can be important, an illustrated by Eq. (18). If $\mathbf{n}_{\rm C} = 40$ GeV rather than 20 GeV, then the total width is reduced by 0.18 GeV i.e. the equivalent of 1 neutrino species. The statements made above regarding electroweak corrections to W^{\pm} decay also apply to the Z^0 .

2.3 QCD Jets

In the hadronic decays of the W^{\pm} and Z^{0} , one expects to observe rather well collimated streams of jets in the final states. Indeed, it is a straightforward exercise to apply all of the QCD jet calculations originally carried out for $e^{+}e^{-}$ + hadrons to such decays. (Only heavy quark mass effects modify the formulas.) For example, using the Sterman-Weinberg¹³ criterion for a two jet event as one in which all but at most ε of the total available energy, w_{Z} , is emitted within a pair of oppositely directed cones of opening half-angle $\delta \ll 1$, one finds to order $a_g(w_{Z})$

$$\frac{\Gamma(Z^0 + 2 \text{ jets})}{\Gamma(Z^0 + \text{hadrons})}$$
(21)

$$1 - \frac{4}{3} \frac{\alpha_s(m_Z)}{\pi} \left[(4 \ln 2\epsilon + 3) \ln \delta + \frac{\pi^2}{3} - \frac{5}{2} \right]$$

(the same result with $m_Z + m_Y$ holds for W^{\pm} decays). From this expression we learn that for $\varepsilon = 0.1$ and $\delta = 0.2$ (i.e. = 12°), about 70% of all hadronic decays are expected to form two narrow jets with energy ≥ 0.9 m_Z and opening angle $\delta \leq 0.2$. Other jet parameters such as thrust, sphericity etc, which have been analyzed in great detail for e⁺e⁻ annihilation similarly apply to Z⁰ and W[±] decays. In particular, for the decay Z⁰ + q + \bar{q} + gluon which materializes as three distinct hadronic jets, one finds the familiar differential decay rate¹¹

$$\frac{d^2\Gamma(Z^0 + 3 \text{ jets})}{dxdy} =$$
(22)
$$2\pi (m_1) = 2$$

$$\Gamma(Z + hadrons) = \frac{2n}{3\pi} \frac{(m_Z)}{2\pi} = \frac{x^2 + y^2}{(1 - x)(1 - y)}$$

where $x = 2E_q/m_Z$ and $y = 2E_q/m_Z$, with E_q and E_q the energies contained in the quark and antiquark initiated jets, $0 \le x \le 1$ and $0 \le y \le 1$. In such three jet configurations, one expects the gluon jet to be somewhat broader than those initiated by quarks, because gluons carry more color and should therefore fragment more¹⁴. Clearly, the 2^3 and W^{\pm} provide excellent settings for studying perturbative QCD and jet phenomenology.

2.4 Number of Neutrino Species

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An anticipated use of a precise measurement of the Z^{0} 's total width, is to determine the number of distinct neutrino species, N_0 . From the formulas in eqs. (16) - (19), we see that one might interpret deviations from $\Gamma(Z^0 + all) = 3.02$ GeV as being due to additional decays involving 4th, 5th etc. generation neutrinos. If their coupling to the Z^0 is universal, then one expects a 0.181 GeV increase in the width for each new flavor, i.e.

 $(N_v - 3)(0.181 \text{ GeV}) = \Gamma(Z^0 + all) - 3.02 \text{ GeV} (Z3)$

(assuming that additional quarks and leptons are too massive to contribute to the Z^0 's width). Big bang cosmology combined with the observed helium abundance in the universe implies an upper bound of 3 or 4 neutrino species¹⁵; it will be interesting to see whether a precise measurement of $\Gamma(Z^0 + \text{all})$ supports that bound.

Do Z^0 propagator effects presently tell us anything about N_y? Neutrinos contribute to the propagator via loop effects. Within the framework of the standard model too large a number of neutrinos would ruin the excellent agreement between theory and experiment observed in the $e^+e^- + \mu^+\mu^-$ backward-forward asymmetry. A crude analysis gives $N_0 \leq 10^3$; not a very impressive bound.

2.5 Higher Order Rare Decays

A variety of higher order induced decays (in addition to the three jet configuration in Eq. (22) of the W^{\pm} and Z^{0} have been studied. Most important are rare Z^{0} decays, since $e^{+}e^{-}$ colliders will produce $\approx 10^{7} Z^{0}$ events /yr. on resonance with little background¹⁶. Therefore, one will have the opportunity to observe decay modes with branching ratios as small as $\approx 10^{-6}$.

An interesting possibility is the observation of the Higgs scalar, ϕ , in 2⁰ decays. If $w_{\phi} \ll w_Z$, one finds¹⁷⁻¹⁸

 $B(2^{0} + \phi^{0} + \mu^{+} + \mu^{-}) = 7 \times 10^{-5}$ (24)

$$B(Z^{0} + \phi^{0} + \gamma) = 2 \times 10^{-5}$$
 (25)

These appear to be observable; unfortunately, the rates in Eq. (24) decreases rather rapidly with increasing my.⁸

Gluons may be studied at the Z^0 . Calculations find¹⁹

$$B(2^0 + 3 \text{ gluons}) = 10^{-5}$$
 (26)

 $B(2^0 + \gamma + 2 \text{ gluons}) = 2 \times 10^{-6}$ (27)

These rates are detectable. We remark that two body final states such as $Z^0 + \gamma +$ glueball are highly unlikely.

It would be nice to be able to detect the W^{\pm} in the decay products of the Z^0 . In that way one could study the non-Abelian Z^0WW coupling. Unfortunately, this seems to be unlikely, since one finds²⁰

$$B(7^{0} + W^{\pm} + anything) = 2 \times 10^{-7}$$
 (28)

$$B(Z^{0} + W^{+} + e^{-} + v) = 10^{-3}$$
 (29)

Radiative two body decays can be reliably computed. One finds²¹

$$B(2^{0} + \pi^{0} + \gamma) = 3 \times 10^{-11}$$
 (30)

$$B(Z^{0} + \eta + \gamma) = 3 \times 10^{-10}$$
 (31)

$$B(Z^0 + Q\bar{Q} + \gamma) = 10^{-7}$$
 (32)

where $Q\bar{Q}$ is a heavy \simeq 50 GeV pseudoscalar quarkonia state

Finally, one might ask: Will flavor changing decays of the 2⁰ be observable? In particular, if $m_{\rm C} > \omega_{\rm Z}/2$, the decay 2⁰ $\stackrel{\sim}{\rightarrow}$ tt is kinematically forbidden; however 2⁰ + t + light quark may go. Unfortunately, the branching ratio²²

$$B(Z^0 + t + X) \leq 10^{-10}, (a_2 > a_2/2)$$
 (33)

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is extremely suppressed.

It is important to measure as many decays of the 2⁰ and W⁴ as possible. In so doing, one will test the standard model; perhaps even at the level of its quantum corrections. Deviations from the expected may signal exotic new physics such as technicolor, supersymmetry etc.

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