# Beta-Delayed Proton Emission in Neutron-Deficient Lanthanide Isotopes. 

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Phillip Alan Wilmarth


#### Abstract

Forty-two $\beta$-delayed proton precursors with $56 \leq 7 \leq 71$ and $63 \leq N \leq 83$ were produced in heavy-ion reactions at the Lawrence Berkeley Laboratory SuperHILAC and their radioactive decay properties studied at the on-line mass separation facility OASIS. Twenty-five isotopes and eight delayed proton branches were identified for the first time. Delayed proton energy spectra and proton coincident $\gamma$-ray and x-ray spectra were measured for all precursors. In a few cases, proton branching ratios were also determined. The precursor mass numbers were determined by the separator, while the proton coincident $x$-ray energies provided unambiguous $\mathbf{Z}$ identifications. The proton coincident $\gamma$-ray intensities were used to extract final state branching ratios. Proton emission from ground and isomeric states was observed in many cases. The majority of the delayed proton spectra exhibited the smooth bellshaped distribution expected for heavy mass precursors. The experimental results were compared to statistical model calculations using standard parameter sets. Calculations using Nilsson model/RPA $\beta$-strength functions were found to reproduce the spectral shapes and branching ratios better than calculations using either constant or gross theory $\beta$-strength functions. Precursor half-life predictions from the Nilsson model/RPA $\beta$-strength functions were also in better agreement with the measured half-iives than were gross theory predictions. The ratios of positron coincident proton intensities to total proton intensities were used to determine $\mathrm{Q}_{\mathrm{EC}}-\mathrm{B}_{\mathrm{p}}$ values for several precursors near $N=82$. The statistical model calcalations were not able to reproduce the experimental results for $\mathrm{N}=81$ precursors, which decay to $\mathrm{N}=82$ closed shell proton emitters; instead, pronounced structure in the delayed


proton spectra of ${ }^{147} \mathrm{EDy}$, ${ }^{149} 8 \mathrm{Er}$ and ${ }^{151 g Y b}$ could be explained by shell model configurations of the emitting states which have strongly hindered $\gamma$-decay channels resulting in enhanced proton emission from these states. The odd-odd $\mathrm{N}=81$ precursors ${ }^{148} \mathrm{Ho},{ }^{150} \mathrm{Tm}$, and ${ }^{152} \mathrm{Lu}$ had proton branching ratios a factor of $\sim 10$ larger than predicted and the calculations did not reproduce the spectral shapes. The branching ratio discrepancies could be resolved by reducing the level densities in the emitters or by decreasing the $\gamma$ widths.

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## 1. INTRODUCTION

Nuclei far from stability provide stringent tests of the predictive capabilities of present nuclear structure theories. An understanding of fundamental processes such as nucleosynthesis [Tru84, Mat85] and stellar evolution requires accurate predictions of $Q$ values, $\beta$-decay half-lives and etrength functions, branching ratios, and reaction rates. The five conference proceedings [For66, CRN70, CRN76, CRN81, Tow87] dedicated to nuclei far from stability contain numerous examples of the nuclear structure information that has been learned from studies of such nuclei. The limits of particle stability beyond which nuclei become unbound with respect to proton or neutron emission are known as the the proton and neutron drip lines, respectively. There are approximately 8000 nuclei predicted to lie within the confines of these drip lines yet only about 3000 have been observed so far. Because of the repulsive Coulomb force, the proton drip line lies closer to the line of $\beta$ stability than does the neutron drip line. Using fusion reactions between neutron-deficient targets and projectiles, heavier nuclei near the proton drip line can be produced in the laboratory but naclei near the neutron drip line, due to the large neutron to proton ratios, may never be synthesized outside of stellar environments (with the exception of the lightest elements). Nuclei near the drip lines may exhibit properties not found in nuclei closer to stability such as decay medes involving particle emission.

The present investigation is concerned with nuclei in the vicinity of the proton drip line where, due to small proton binding energies, modes of radioactivity involving proton emission are observed. In an early review article [Gol66], three modes of proton emission were discussed: $\beta$-delayed proton emission, direct proton emission, and direct two proton emission. Delayed proton emission was first discovered in the early 60's [Kar63, Bar63] and the number of precursors tabulated in review articles about delayed proton emission [Har72, Kar74, Har74, Cer77] has increased steadily to nearly 100 in the most recent review [Har87]. Direct proton emission was first observed in the decay of 53 mCo in 1970 [Jac70, Cer70] and five additional proton decaying nuclei have been identified [Fae84, Hof84] more recently. Beta-delayed two proton emission was discovered in 1983 [Cab83, Mol87] and the search for direct two proton emission is still in progress.

Beta-delayed proton emission is a decay process that can occur when the $\beta$ decay energy $Q_{E C}$ of the parent nucleus (the precursor) exceeds the proton binding energy $B_{p}$ in the $\beta$-decay daughter nucleus (the emitter). If levels are populated by $\beta$
decay at an excitation energy that is greater than the proton binding energy, then it becomes energetically possible for these levels to de-excite by proton emission. The conditions necessary for delayed proton emission, namely large Qec's and small $\mathbf{B}_{\mathrm{p}}$ 's, are characteristic of nuclei near the proton drip line. In fact, delayed proton emission is expected to be a common decay mode in nearly all nuclei near the proton drip line. Delayed proton emission provides a very sensitive signal to identify isotopes far from stability since the increasing branching ratios for proton emission and large detection efficiency for charged particles compensate for the decreasing half-lives and production cross sections. For the most neutron-deficient nuclei, data from delayed proton decay are frequently all that is known. In addition to precursor half-life determinations, delayed proton emission is a sensitive method to study the $\beta$-decay process in nuclei with large $Q_{\text {EC }}$ values and the properties of proton emitting levels.

In light delayed proton emitters, the spacing of levels in the emitter is typically greater than the particle detector resolution and the spectrum of the delayed protons consists of resolved peaks corresponding to proton transitions from individual states in the emitter to levels in the proton decay daughter. The energies and intensities of these peaks yield direct information about the preceding $\beta$-decay process and the level structure of the emitter at high excitation energies. The partial proton width $\Gamma_{p}$ is usually much larger than the partial $\gamma$ width $\Gamma_{\gamma}$ since the proton emitting levels are typically at excitation energies well above the Coulomb barrier. In precursors where $\mathbf{Z}<\mathbf{N}$, the superallowed Fermi transition to the isobaric analog state often dominates the proton spectrum and delayed proton branches can approach 100\%. In many of these cases it has been possible to determine the isospin purity of excited levels and perform precise mass measurements using the isobaric multiplet mass formula. In some medium mass emitters ( $40 \leq \mathrm{A} \leq 100$ ) it has been possible to measure the lifetimes of proton emitting levels by observing $\mathrm{K} \times$ ray intensity ratios following electron capture in coincidence with protons [Har76].

Delayed proton emilters with $\mathbf{Z}>50$, in contrast to the lighter emitters, have level spacing -- at excitation energies sufficient for proton emission -- that are typically less than the detector resolution. The high level density and absence of a superallowed branch result in a proton energy spectrum that is no longer composed of discrete peaks but instead becomes a bell-shaped distribution and proton branches seldom exceed a few percent. The proton spectrum is composed of many unresolved transitions and contains information about the average properties of the proton emitting levels. A study of emitters with $\mathrm{Z}>50$ should yield information about $\beta$ -
strength functions, $\gamma$-strength functions, and level densities at high excitation energies [Kar73, Kar74, Kar75, Jon76, Har81]. The Coulomb barriers for proton emission are often larger than $Q_{E C}$ so $\Gamma_{\gamma}$ will typically be larger than $\Gamma_{\mathrm{p}}$ for all proton emitting levels. Proton emission in heavy precursors is, therefore, much more sensitive to $\Gamma_{\boldsymbol{\gamma}}$ than in light emitters. Models of sub-barrier proton penetrability can be tested also. Since individual proton transitions cannot be resolved for heavy precursors, it may be worthwhile studying many emitters in a given region and looking for systematic trends rather than detailed studies of individual emitters. A systematic study of delayed proton emitters in the neutron-deficient lanthanides was undertaken with this goal in mind.

Neutron-deficient nuclei with $50 \leq \mathbf{Z} \leq 71$ and $50 \leq N \leq 84$ exhibit three main decay modes: $\beta$ decay, direct particle ( $\alpha$ or proton) emission, and $\beta$-delayed particle ( $\alpha$ or proton) emission. Beta decay (electron capture or positron emission) is the most common decay mode with $\mathrm{Q}_{\mathrm{Ec}}$ values around 10 MeV and half-lives on the order of a few seconds in the vicinity of the proton drip line. Although difficulties associated with small cross sections and short half-lives can be overcome with current techniques, $\beta$ decays with such large $Q$ values are quite complicated and little detailed spectroscopic information is available for the nuclei near the protori drip line. Some nuclei near $\mathrm{Z}=64$ have been well studied because of the interest in the $\mathrm{Z}=64$ subshell closure. The nuclei midway between the $\mathrm{Z}=50$ and $\mathrm{N}=82$ shells are highly deformed and a mapping of the rotational levels of even-even nuclei over a large part of this region has recently been completed [Lis85]. Also the search for superdeformation in nuclei near ${ }^{134} \mathrm{Nd}$ has focused considerable attention on the spectroscopy of high-spin states in this region [Wad87a, Bec87].

There exists an island of $\alpha$ emission with $52<Z \leq 55$ and $54 \leq N \leq 60$ [Mac65, Kar67, Kir77, Sch79, Sch81] due to the influence of the $\mathrm{Z}=50$ shell closure (and the lower Coulomb barriers). Alpha emission in nuclei with $\mathbb{Z} 60$ and $\mathrm{N} \geq 84$, due in part to the $\mathrm{N}=82$ shell closure, has been well known for many years. Direct proton emission has been observed for ${ }^{109}$ a and ${ }^{113} \mathrm{Cs}$ [Fae84], and for ${ }^{147 \mathrm{~m}, \mathrm{BTm},}{ }^{151 \mathrm{mLu} \text {, }}$ and ${ }^{150} \mathrm{Lu}$ [Hof84]. A comprehensive review of direct proton emission can be found in [Hiof87].

The large $\mathrm{Q}_{E C}$ and small $\mathrm{B}_{\mathrm{p}}$ values near the proton drip line in this region result in many nuclei with known delayed particle branches. In addition to delayed proton emission (observed in all elements from $\mathrm{Z}=52$ to $\mathrm{Z}=71$ ) which is the subject of this thesis, delayed $\alpha$ emission has been observed in a study of delayed particle emission in nuclei near $\mathrm{Z}=\mathrm{N}=50$ [Tid85] where the $\alpha$ binding energies are low.

There is preliminary evidence [Vie88b] that delayed $\alpha$ emission also occurs near $\mathrm{N}=82$.

Using compound nucleus reactions between neutron-deficient projectiles and targets, 42 delayed proton precursors with $56 \leq Z \leq 71$ have been produced at the $\mathrm{Q}_{\mathrm{n}}$ line Apparatus for SuperHILAC Isotope Separation (OASIS) facility [Nit83a] at the Lawrence Berkeley Laboratory SuperHILAC. Because of the broad distribution of products from heavy-ion reactions and the short half-lives encountered, on-line mass separation was required (for an excellent review of mass separator studies of nuclei far from stability, see [Han79]). Of the 42 delayed proton precursors, 25 were identified for the first time and 8 new delayed proton branches were also measured. The region of the chart of the nuclides studied is shown in Fig. 1.1.

A description of the mass separator and the experimental setup is given in chapter 2. A more complete discussion of the delayed proton emission process for heavy mass precursors and of the statistical model is presented in chapter 3. The results of the measurements are presented in chapters 4 (even mass number precursors), 5 (odd mass number precursors). Conclusions from this study will be discussed in chapter 6.


Figure 1.1. Region of the chart of the muclides showing the delayed proton precursore produced in this study.

## 2. EXPERIMENTAL

### 2.1. INTRODUCTION

Highly neutron-deficient lanthanide isotopes were produced as evaporaticn residues in reactions of neutron-deficient heavy-ion projectiles (such as ${ }^{40} \mathrm{Ca}$ or ${ }^{59} \mathrm{Ni}$ ) and neutron-deficient targets (such as 92 Mo or ${ }^{9}{ }^{6} \mathrm{Ru}$ ). The broad distribution of products from such reactions required chemical or mass separation to improve the sensitivity for detecting the isotopes of interest. The half-lives for many of the nuclei studied were a few seconds or less making chemical separations impocsible.
Lanthanide elements could be surface ionized with reasonable efficiencies due to their low first ionization potentials and, therefore, studied wing mass separation. Because of their similar chemical properties and thus similar ionization potentials, many different lanthanide elements could be studied in the same expeciment.

Using $\mathrm{Q}_{\mathrm{EC}}$ and $\mathrm{B}_{\mathrm{p}}$ values from current mast formula such as [Lir76], it was possible to predict which lanthanide isotopes may have delayed proton branches. Selection of the optimum target/projectile combirations and incident beam energies for the production of these isotopes was based on cross section calculations from [Win72]. The choices for target and projectile were based on beams that the SuperHILAC could produce with sufficient intensities and targets that could withstand these high beam intensities (up to ~200 paA). The SuperHII_AC beams which were used are summarized in Table 2.1 and the target materials (physical forms, thicknesses, purities, etc.) are listed in Table 2.2. In most experiments, an enriched molybdenum metal foil served as the target with the beam varied to produce the nuclei of interest. In certain caser, gas-cooled targets [Nit76, Mol81] of ruthenium or other materials were employed. The incident beam energy in all experiments had a center of target energy matching the calculated excitation function peak energy to optimize the production of the isotope of most interest.

### 2.2. THE SEPARATOR

The OASIS mass separator [Nit83a] on-line at the Lawrence Berikeley Laboratory SuperHILAC is shown schematically in the lower half of Fig. 2.1. In addition to the usuai components, the OASIS beamlinc had a "wobbler" (a three phase motor with the beam replacing the rotor) to move the beam spot uniformly over the target surface. This allowed higher beam intensities and was crucial when using
fragile targets. Located between the collimator and target was an RF pickup electrode to measure the beam intensity. The microstructure of the SuperfillaC beam induced an RF voltage in a pick-up electrode which was proportional to the beam intensity. The electrode was calibrated against a Faraday cup at least once during each experiment to avoid errors caused by the varying microstructure of the SuperHIILC beam from experiment to experiment. In many experiments, a beam intensity limiting circuit was used to prevent fluctuations in beam intensity from damaging the target thereby allowing a higher average beam intensity on target.

The separator used an integrated targetion source combination. Surface ionization was used for all elements in the lanthanide region and a typical surface ionization source with an $\mathrm{N}_{2}$ gas cooled target is shown in Fig. 2.2. In experiments using free standing Mo foils, no target cooling was needed and the Havar foil and cooling gas would not be present. The target was followed by two heat shields (carbon foils, $\sim 40 \mu \mathrm{~g} / \mathrm{cm}^{2}$ ) and a bundle of thiii-walled Ta capillary tubes ( 22.23 mm in length by 1.14 mm outside diameter, wall thickness of 0.076 mm ). After traversing the heat shields and capillary tubei, the recoiling products entered the ion source and stopped in a suitable catcher material (usually the Ta anode endplate). The source was heated to very high temperatures near the melting point of Ta (~3000 C) by electron bombardment (EB) resulting in fast diffusion of the recoils from the catcher, short hold-up times inside the source, and high ionization efficiencies. After diffusing out of the catcher, the lanthanide atoms were surface ionized in collisions with the walls of the ion source. The capillary tubes prevented the atoms from diffusing back towards the target and getting trapped in cooler regions of the ion source, while the compound nucleus reaction recoils from the target entered the catcher/ionization region nearly unimpeded due to their small angular divergence. The coaxial construction of the ion source resulted in tight mechanical tolerances at high temperatures. All insulators in the hot sections of the source were replaced by narrow gaps of about 0.25 mm that acted as "molecular flow barriers". This enabled operation of the source at temperatures greater than 2500 C , a temperature where most insulating materials start to become conductive and break down mechanically. Typical ion sources lasted $\mathbf{- 2 4}$ hours before most of the Ta anode (and catcher) had been evaporated due to the strong local heating caused by the EB and the stopping of the SuperHILAC beam. This would cause a noticeabie drop in ion source output over a relatively short time span. A typical ion source change and minor readjustment of the ion opsics required 1-2 hours. The ion source region was pumped by a baffled $250 \mathrm{~mm}, 7000 \mathrm{ls}$ diffusion pump.

After being ionized, the recoils were extracted axially and sccelerated to 50 keV . An einzel lens and an electrostatic quadrupole triplet focused the ion beam onto the entrance slit of the magnetic spectrometer. The main analyzing magnet had a sector angle of 1800 , a mean radius of curvature of 0.66 m , a field index of 0.5 , and was typically cperated at $50 \%$ of its design field. Wiun object and image slit widths of 1.5 mm and no corrective ccils on the pole faces, a mass resolution of about 880 could be obtained routinely. Located at the $135^{\circ}$ pcsition of the magnet were two $16^{\circ}$ wide, wedge-shaped pole pieces so create a region of sufficiently homogeneous magnetic field to operate an NMR probe for mass measurements. A Hall probe was located next to the NMR probe to automatically tune the NMR probe as the magnetic field was changed. For an ion energy of 50 keV , masses from 45 to 380 u could be determined with a precision of $\pm 0.001 u$ from the NMR frequency and the accelerating voltage measured with a $61 / 2$ digit DVM. Mass calibrations were usually accomplished by introducing a small amount of a suitable rare earth oxide directly into the ion source. This provided a stable mass marker at the desired mass number or, at worst, only a few mass units away from the desired mass. Corrections for mass defects within an isobaric chain, calculated from [Lir76], were applied in many cases. A second $250 \mathrm{~mm}, 2000 \mathrm{ls}$ diffusion pump was located at the entrance to the magnet and a small 150 ls turbo pump was connected to a port at the $90^{\circ}$ position of the magnet. The pressure tal the separator was maintained in the $10^{-6}$ torr range to minimize beam losses due to scattering.

Surrounding the focal plane of the spectrometer was a detector box located 1.5 m (line of sight) from the target region; vacuum was maintained by a cryopump with speeds of $15001 / \mathrm{s}$ for air and 4000 ls for water. Due to the high background of neutrons and $\gamma$ rays from the target, only charged particie spectroscopy could be performed here. In order to detect $x$ rays and $\gamma$ rays, the radioactive products had to be transported to a lower background counting location. A suitable room was located 4 m directly above the cave. The ion beam exiting the separator was deflected $90^{\circ}$ vertically via an electrostatic mirror operated at about $80 \%$ of the accelerating potential and transported to a fast-cycling tape cystem for coliection and counting. The transfer line from the spectrometer to the tape system consisted of two electrostatic quadrupole triplets at either end of the transfer line, two (270 and 500 $1 / s$ ) turbomolecular pumps to maintain high vacuum and Faraday cups at the midpoint and collection points to aid in tuning the beam optics. The counting area was shielded from the cave radiation by the 46 cm concrete roof blocks of the cave, large quantities of polyethylene for neutren thermalization located between the cave roof
blocks and the mezzanine floor, 15 crn of additional concrete, and $\sim 10 \mathrm{~cm}$ of lead near the detectors.

The separator was controlled by a PDP 11/10 minicomputer which monitored all important parameters. The ion soucce parameters (arc, electron bombardment, and filament current and voltage), accelerating poiential, magnetic field (NMR and Hall probes), and vacuum gauges were all continuously monitored. Two different computer controlled stabilization modes were possible; the accelerating potential could be stabilized at 50 keV and the magnet manually tuned to the desired mass, or the accelerating potential could be varied to keep the computer calculated mass at a constant value. The two modes are called voltage stabilization and mass stabilization, respectively. The usuai mode of operation was mass stabilization. Optical isolation from the separator prevented high voltage sparks from damaging the computer.

A number of significant improvements in ion source design have occurred since [Nit83a] was publisted. The source now uses a slit geometry for ion extraction which has improved the yield by at least $50 \%$. Older ion source designs used a W liner to increase the surface ionization yield compared to Ta but mechanical problems at the high operating temperatures negated any increased yields. The high temperature region of the ion source is now constructed entirely of Ta and Mo components. As previously mentioned, the bundle of capillary tubes inside the ion source keeps the thermalized recoils in the high temperature region of the source after they have diffused out of the catcher, based on the principle of molecular flow restriction. This technique avoided the problems associated with a thin entrance window close to the hot ion source while allowing very low energy recoils to enter the source. However, the finite wall thickness ( $\sim 0.09 \mathrm{~mm}$ ) of the capillary tubes stops a small fraction of the recoils (and the beam) so the use of very thin walled capillary tubes ( -0.045 mm wall thickness) improved the transmission from the target to the catcher in later experiments. For fragile targets which can't handle as much beam intensity or for more exotic beams which have a lower intensity, the same effective yield can be obtained with about $25 \%$ less beam current using the thinner capillaries.

### 2.3. THE TAPE SYSTEM

A fast-cycling tape system was located inside the shielded room above the separator (see Fig. 2.1). As stated above, this reduced the high background of fast neutrons and $\gamma$ rays present near the target by several orders of magnitude. Long-
lived activities, usually of little interest, were removed from the detection position simply by moving the tape, and many defectors could be placed in clowe geometry to the collected products (both sides of the thin tape were accessible). The mass separated products, after the $-30 \mu$ s flight time through the transfer line, were implanted directly into the tape and periodically moved inside an array of detectors.

The tape system consisted of an IBM 729 tape drive modified so that the tape ran through an evacuated detector chamber where the activity was collected and counted. The magnetic tape from the supply reel was guided through a differentiallypumped vacuum feed-through into the detector chamber. The vacuum of $\sim 10^{-6}$ torr in the detector chamber was maintained by a 500 Vs turbo pump attached to the top of the chamber. The tape from the chamber went through a second vacuum feedthrough and was spooled onto the take-up reel. Magnetic computer tape with a conductivity of $1-10 \mathrm{~K} \Omega$ per $\varepsilon$ quare ( Scoth 720 ) was used to prevent electrostatic charge build-up at the collection point; the spot size of the collected activity was typically less than 6 mm in diameter. The distance from the collection point to the counting position between the detectors was 17.5 cm and the iravel time, at a tape speed of $2.86 \mathrm{~m} / \mathrm{s}$, was 65 ms .

The tape movement was controlled by an Intel 8085 microprocessor. The tape usually ran in a stepping mode where the activity was collected for a fixed period of time and then moved to the detectors to be counted while the next sample was being collected. The counting intervals were selected bused on the known or predicted [Tak73] half-lives of the activities of interest. The measured half-lives were obtained by resetting and starting a digital timer when the tape was advanced and time-tagging each decay event as it occurred during the counting interval. The shortest activities that could be studied were on the order of 0.1 s . In studies of short-lived isotopes where the counting interval was a few seconds or less, the tape could be automatically rewound after $\sim 4000$ advances and counting continued without intervention. The time between tape advances was que tz controlled and could be internally timed by the control computer or externally strobed. A tape positioning accuracy of $\pm 1 \mathrm{~mm}$ was possible at the fastest tape advance speeds and reduction gearing was available to produce slower tape speeds and improved positioning when necessary. The tape controller inhibited all counting during the actual tape movement plus $\sim 10 \mathrm{~ms}$ settling time.

### 2.4. DETECTORS AND ELECTRONICS

The $\beta$-decay process of neutron-deficient lanthanides produces positrons, $x$ rays, $\gamma$ rays, conversion electrons, and delayed particles in many cases. Proton or $\alpha$ particles (direct or $\beta$-delayed) along with any coincident photons or positrons were of primary importance. However, singles data for the determination of absolute $x$-ray and $\gamma$-ray intensities in addition to $\beta \gamma, \gamma \gamma$, and $X \gamma$ coincidence information are also required to complement the particle data. The detectors used in this study have evolved from the rather modest configuration used in the first experiments in 1983 to the current configuration described below. The three main configurations used since 1983, along with the dates each was used, are shown in Fig. 2.3. Only the present configuration witl be described in detail since the others were earlier subsets. Unfortunately, conversion electron spectroscopy (a great aid in assigning $\gamma$-ray multipolarities) was not possible with any of the detector arrangements.

Facing the collection side of the sape was a three element telescope capabie of detecting protons, $\alpha$ 's, positrons, or photons. Closest to the tape was a $10.4 \mu \mathrm{~m}$ thick fully-depleted silicon transmission detector. The middle element was a $718 \mu \mathrm{~m}$ thick fully-depleted tilicon detector followed by a high purity germanium (HPGe) detector. The silicon detectors were operated at room temperature and separated from the HPGe detector by a $50 \mu \mathrm{~m}$ Be window. The first two elements of the ielescope detected and identified protons ( $0.7<\mathrm{E}<8.0 \mathrm{MeV}$ ) and $\alpha^{\prime} \mathrm{s}(2.0<\mathrm{E}<8.0 \mathrm{MeV})$ using a standard particle ID formula, $\mathrm{PI}=(\Delta E+E)^{1.73}-(E)^{1.73}$. This formula gives different values for $\beta$ 's, $\alpha$ 's, and protons and the values for a given type of particle are essentially independent of particle energy. The $10.4 \mu \mathrm{~m}$ detector thickness was selected to provide a very clean separation between positrons, protons and $\alpha$ particles. The identification of ${ }^{149} \mathrm{Er}$ delayed protons from the background of positrons and $\alpha$ particles is shown in Fig. 2.4. The $718 \mu \mathrm{~m}$ detector was used with the HPGe detector as a telescope for $\beta$ particles ( $0.2<\mathrm{E}<10.0 \mathrm{MeV}$ ). The HPGe detector also measured $\gamma$ rays and $x$ rays ( $5<\mathrm{E}<500 \mathrm{keV}$ ). The pulsed optical preamplifier signal from the HPGe was electronically split and sent to two separate amplifiers, one for $\beta$-particle detection (low gain) and one for low-energy photons (high gain). Similarly, the signal from the $718 \mu \mathrm{~m}$ detector was split into low gain for proton and $\alpha$ energies and high gain for $\beta$-particle energy losses $(20 \leq E \leq 2500$ keV).

A large (52\% relative efficiency) n-type coaxial germanium detector faced the backside of the tape. A thin ( 1 mm Pilot F) plastic scintillator coupled to a PMT was located directly in front of the germanium detector. The scintillator was used to detect positrons coincident with protons or, in anticoincidisnce, to reduce the highenergy positron background in the germanium detector, thus improving the signal to noise ratio for high-energy $\gamma$ rays. The signal from the preamp of the Ge detector was split into a high gain channel for x rays ( $5<\mathrm{E}<250 \mathrm{keV}$ ) and a low gain channel for $\gamma$ rays ( $50<\mathrm{E}<5000 \mathrm{keV}$ ).

A second n-type germanium detector ( $24 \%$ relative efficiency) was located about 50 mm to one side of the source at $90^{\circ}$ to the other detectors. Photons with energies from $\sim 100$ to $\mathbf{2 5 0 0} \mathbf{~ k e V}$ couid be detected for $\gamma$ coincidence information. Table 2.3 lists the detector sizes, resolutions, etc. for the current detector configuration. The absolute efficiency curves for the three Ge detectors are shown in Fig. 2.5.

The detectors were surrounded by at least 5 cm of lead to shield against background room radiation and also to shield the detectors from the activity being collected on the tape a few centimeters below the detectors and from the previous activity present on the tape $\sim 15 \mathrm{~cm}$ above the detectors. The biekground of $\alpha$ particles and delayed protons was on the order of one event per day and the coincident event rate for all combinations of pairs of germanium detectors was typically about one per second. Background lines from ${ }^{40} \mathrm{~K}$, the Th and U daughters in the lead, and some neutron capture $\gamma$ rays from Ge and Al caused no difficulties in the analysis of the singles data. Energy calibrations of all germanium detectors were performed before and after each experiment using standard $\gamma$ sources and the silicon detectors were calibrated with a precision pulser. This pulser was periodically calibrated using standard $\alpha$ sources and its long term stability was very good. Absolute detector efficiencies were determined about once per year using special thin sources attached to the computer tape and moved into the actual counting position. There were little, if any, changes in detector efficiencies with time.

Conventional fast/slow electronics, shown schematically in Fig. 2.6, were used. The fast timing signals from each detector, after going through appropriate siaping amplifiers and constant fraction descriminators, were used to generate timing information between all detectors pairs of interest. The fast timing signals were also used to define events of interest. A typical event consisted of pairwise coincidences ( $\sim 2 \mu \mathrm{~s}$ overlap) between the germanium detectors (each pair was individually selectable and more than one pair could be logically combined) logically ORed with a
coincidence between the 10.4 and $718 \mu \mathrm{~m}$ detectors. Each detector had an externally strobed pulser to help set up and test the coincident logic. High quality linear electronic components were used for all energy signals resuling in good resolution and stability. The detectors, detector chamber, and electronics were electrically isolated from the separator and the SuperHILAC to prevent ground loops. All preamplifier cables were run from the detectors to the main amplifiers inside a heavy copper pipe to prevent noise pickup.

### 2.5. DATA ACQUISITION AND REDUCTION

After appropriate amplification, the analog signals from the detectors were converted to digital information and stored as histogram and event-mode data. Muitiparameter even-by-event data associated with $\beta \gamma, X \gamma$, and $\gamma \gamma$ coincidences and charged particle related data were recorded in all experiments. But the importance of absolute $\gamma$-ray and $x$-ray intensities in level scheme construction and in proton or $\alpha$ particle branching ratio determinations was realized and singles data (collected as histograms) were roitinely acquired after the addition of the $52 \%$ n-type Ge detector.

In the singles measurements, the tape cycle was typically split into eight equal time intervals and histograms were collected for each interval. Figure 2.7 shows an 8-s tape cycle [Fig. 2.7(a)] divided into 1-s intervals [Fig. 2.7(b)] for the singles data. Thus, half-life information in addition to intensity information was obtained. Both the singles and multiparameter data collection were interrupted during the tape movement and during the 5 ms wide SuperHILAC beam pulses [Fig. 2.7(c)]. The beam blanking was usually a few ms wider then the SuperHILAC pulses to allow for neutron thermalization and reduce the background from slow neutron capture processes. The $52 \%$ detector was connected to an 8 by 8192 charnel histogramming memory. This memory was located in CAMAC, readout by a ModComp computer, and its contents saved on magnetic tape. Singles information from the x-ray region of the HPGe detector was also recorded in a multispectrum mode ( $8 \times 512$ channels), while the $24 \%$ detector generated a singıe 2048 channel spectrum. The HPGe and $24 \%$ detector were connected to multichannii analyzers which were interfaced to an Apple Macintosh personal computer for permanent storage of spectra. The 2iquisition hardware used in the singles measurements is shown in Fig. 2.6.

The multiparameter event-mode data were written to magnetic tape by a ModComp Classic computer using appropriate data acquisition software. The ModComp computer could be interfaced to the experiment in two ways, using an

LBL multiplexer/ADC combination (32 parameters per event maximum) or via CAMAC. For the eatlier experiments reported here, the multiplexer/ADC was used but the quality of the system for high resolution data needed in $\gamma$ ray spectroscopy was not adequate so a transition to CAMAC was made. A simplified version of the CAMAC system is shown in the lower part of Fig. 2.6. About 20 parameters were recorded for each event. There were typically 4 high resolution ( 13 bit ) ADCs for the $x$-ray and $\uparrow$-ray detectors, 5 lower resolution ( 11 bits) ADCs for particle data, 8 TAC signals, 3 scalers (relative lab time, half-life time tagging [Fig. 2.7(d)], and beam intensity), and a tag word to separate one event from the next. The CHAOS data acquisition software [Map79] was used until the number of parameters per event and the event rates exceeded the capabilities of this software. In experiments since January 1987, the CDAS software package [Be186], originally developed for the HERA facility at Lawrence Berkeley Laboratory, was used during data acquisition. This software ran much faster than CHAOS but was less flexible for interactive monitoring.

After acquisition, the methods for data reduction and analysis depended on the type of data. The majority of the multiparameter data on magnetic tape was fy and $\gamma$ coincident events with only about one in $10{ }^{4}$ events sescociatied with a $\beta$ delayed proton decay. This low concentration of particle related events to other events makes a form of data reduction called filtering especially appropriate. The original data tapes were scanned for events of interest (using very general criteria) which were written to a new event tape. This new tape had only a few thousand events instead of the few million events typically recorded during an experiment. The sorting programs could analyze the highly compressed data much more quickly and many different sorts of the same data in a short period of time were possible. A Fortran program was written to filter proton or $\alpha$ related events from the $\beta \gamma$ data using either a simple coincidence requirement between telescope elements or using the standard particle identification technique described above.

The large volume of $\beta \gamma$ and $\gamma$ coincident data required a fast sorting program with space for up to about 300 spectria and the EVA software package [Bel87a] was used almost exclusively. After the histograms were generated, peak fitting was done interactively using the computer program SUSIE [Bel87b]. There were two main methods to assign the large number of unknown $\gamma$ rays associated with $\beta$ decay of large Q $_{E C}$ nuclei, by grouping $\gamma$ rays with similar half-lives or by $x$-ray coincidences (from electron capture). The multiparameter data gave both types of information whereas the time resolved singles data gave only half-life and intensity information.

The singles spectra were analyzed with a Vax version of SAMPO [Rou69], a $\boldsymbol{\gamma}$-ray peak fitting program, to obtain reliable peak areas and centroids. The SAMPO program was particularly useful in resolving $\gamma$-ray multiplets often present in the singles data. The spectra were originally recorried on magnetic tape or on a floppy disc and had to be transferred to the Vaxes before they could be analyied. A Fortran program to read magnetic tapes written by the ModComps was developed. The data on floppies were sent to the Vax via the file transfer program Kermit and then converted to a format that could be read by SAMPO.

Table 2.1 SuperHILAC beams used in this work.

| Beam | Injector | $(\mu \mathrm{A})^{\text {Intensity }}(\mathrm{pnA})^{\text {b }}$ |  |
| :---: | :---: | :---: | :---: |
| ${ }^{36} \mathrm{Ar}^{\text {c }}$ | Adam | $\sim 3{ }^{\text {d }}$ | 200 |
| ${ }^{40} \mathrm{Ca}$ | Adam | $\sim 4{ }^{\text {d }}$ | 300 |
| ${ }^{46}{ }^{\text {Ti }}$ | Abel | ~2 | 150 |
| ${ }^{52} \mathrm{Cr}$ | Abel | $\sim 3 \mathrm{~d}$ | 150 |
| ${ }^{54} \mathrm{Fe}$ | Abel | $\sim 1$ | 100 |
| 56 Fe | Abel | $\sim 3 \mathrm{~d}$ | 200 |
| ${ }^{58} \mathrm{Ni}$ | Abel | $\sim 4^{d}$ | 200 |
| ${ }^{64} \mathrm{Zn}$ | Abel | $\sim 2$ | 100 |

${ }^{2}$ electrical current.
${ }^{b}$ particle current.
c isotopically enriched source.
dimited by target stebility.
Table 2.2 Properties of targets used in this work. Target diameter was 6 mm for all experiments.

| Target | Thickness ( $\mathrm{mg} / \mathrm{cm}^{2}$ ) | Enrichment (\%) | Form | Backing |
| :---: | :---: | :---: | :---: | :---: |
| ${ }^{58} \mathrm{Ni}$ | 2.0 | $\geq 95$ | metal | HAVAR |
| ${ }^{93} \mathrm{Nb}$ | 2.0 | 295 | metal | self supporting |
| 92Mo | 2.0 | $\geq 95$ | metal | self supporting |
| ${ }^{94} \mathrm{Mo}$ | 2.0 | 295 | metal | self supporting |
| 96 Ru | 0.6 | 295 | metal | beryllium |
| 96 Ru | 0.8 | $\geq 95$ | metal | carbon |
| ${ }^{96} \mathrm{Ru}$ | 1.5 | 295 | metal | HAVAR |

Table 2.3 Selected properties for each of the detectors at OASIS.

| Detector | Material | Diameter (mm) | Thickness (mm) | Resolution (keV) | Efficiency |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\Delta \mathrm{E}_{\mathrm{p}}$ | Si | 8.0 | 0.0104 | $\sim 50^{2}$ | $0.127^{2}$ |
| $\mathrm{Ep}_{\mathrm{p}}$ | Si | 16.0 | 0.718 | 15a | $0.127^{2}$ |
| $x$ ¢2y | HPGe | 36.0 | 12.5 | 0.69b | 0.128 c |
| $\Delta \mathrm{E}_{\beta}$ | Pilot F | 38.2 | 1.0 | n.a. | 0.400 |
| $\gamma$ ray (52\%) | n -Ge | 64.9 | 57.8 | $2.5{ }^{\text {d }}$ | $0.230{ }^{\text {b }}$ |
| $\gamma$ ray (24\%) | n -Ge | 51.6 | 55.3 | $2.0{ }^{\text {d }}$ | $0.011^{\text {b }}$ |

[^0]${ }^{2}$ for $5.8 \mathrm{MeV}{ }^{241}$ Am a particles.
b for the 122 keV ${ }^{57}$ Co line.
$c$ for the 59.5 keV 241 Am line.
${ }^{d}$ for the $1332 \mathrm{keV}{ }^{60} \mathrm{Co}$ line.


1. Supmery ac bean
2. TARGET
3. NSULATORS (BEO)
4. ION SOUPCE ANODE (Ta)
5. ION SOUACE CATHODE (TA)
6. CAPILLARY TUBES (Ta)
7. EB FLANENT (TM)
8. EXTRACTION ELECTRODE
9. EXTRACTION AND FOCUSNG
10. ANALYZNG MAGNET
11. FOCRL PLANE DETECTOA BOX
12. ELECTROSTATIC MPRPOR
13. ELECTROSTATIC OLIADRUPOLE
14. TRANSFERLME
15. CONCRETE SHELDMVG
16. TAPE DFIVE (EM T29)
17. MAGNETIC TAPE

1a. DCTECTOR BOX
19. N-TYPE Ca DETECTOR (52\%)
20. N-TYPE G* DETECTOR (24\%)
21. HPGe DEIECTOR
$22.718 \mu \mathrm{~m}$ SI DETECTOR
23. $10.4 \mu \mathrm{~m}$ SI DETECTOR
24. 1 mm PLOT F SCWTLLLATOR

Figure 2.1. Simplified representation of the OASIS mass separator online at the Lawrence Berkeley Laboratory SuperHILAC. The separator and tape system are approximately to scale. The major components are labeled.

## OASIS Ion Source



Figure 2.2. Typical OASIS surface ionization source shown with a gas cooled target.
A) 9/83-11/84


$$
\Omega_{p}=2.7 \%, \Omega_{x}=13.8 \%
$$


C) 10186 - present


Figure 2.3. Detector configurations used at OASIS. The dates that each configuration was in use are in the upper left coriers of the three drawings. The effective solid angles corresponding to the maximums in the efficiency curves are represented by solid lines from the source to the dete-tors.


Figure 2.4. Separation of beta particles, protons, and alphas obtained using the particle telescope is shown for ${ }^{149} \mathrm{Er}$; (a) the $13.8 \mu \mathrm{~m}$ detector spectrum, (b) the $718 \mu \mathrm{~m}$ detector spectrum, (c) sum of (a) and (b) after gain matching, (d) the particle ID distribution (alphas are off scale to the right), and (c) the spectrum from (c) subject to the proton gate shown in (d). The spectrum in (e) has a proton resolution of 35 keV . These spectra are from filiered data (see text). The positron peaks would se $\sim 10^{3}$ larger in the "raw" data.

## OASIS Detector Efficiencies



Figure 2.5. Absolute efficiency curves from 22 to 1000 keV in the current counting geometry for the three germanium detectors used in OASIS experiments.


Figure 2.6. Simplified block diagram of the componems for the lisear, fath timing, sad event definition electronics used at OASIS. The deta acquistion herumare for both even-by-event and siagles deta is also shown.


Figure 2.7. Diagram of the various counting and timing intervals used in OASIS experiments; (a) tape advance pulses for an 8-s counting interval, (b) the subgroups (typically 8) for singles data, (c) counting inhibit pulses during tape movement and during SuperHILAC beam pulses (the shaded rectangles), and (d) the scaler for time-tagging of events.

## 3. BETA-DELAYED PROTON EMISSION

### 3.1. GENERAL

The $\beta$-delayed proton emission process for a gencralized heavy mass precursor is shown schematically in Fig. 3.1(a). The precursor ( $Z, N$ ) must have an electron capture $Q$ value $Q_{E c}$ that exceeds the proton binding energy $B_{p}$ in the emitter ( $Z-1, N+1$ ). The precursor, with spin and parity $J x$, will $\beta$ decay predominendly by allowed Gamow-Teller GT transitions to levels with spin and parity $(\mathrm{J}-1, \mathrm{~J}, \mathrm{~J}+1)^{\mathrm{x}}$ in the emitter at an excitation energy $E^{*}$. If $E^{*}$ is less than $B_{p}$, only $\gamma$-ray emission is possible, but, if $\mathrm{E}^{*}$ is larger than $\mathrm{B}_{\mathrm{p}}$, the level can de-excite by $\gamma$ ray or proton emission. The emitted protons may leave the daughter nucleus ( $\mathrm{Z}-2, \mathrm{~N}+1$ ) in the ground or in excited states (at an energy Ef relative to the daughter nucleus ground state, which will subsequently decay by $\gamma$-ray emission or internal conversion). For nuciei with ${ }^{\mathbf{Z}} \mathbf{- 6 0}$, the Coulomb barrier for protons is around 10 MeV and the emitted protons must tunnel through this barrier. Because of the Coulomb barrier there is a threshold energy $\Theta_{\mathrm{p}}=\mathrm{E}^{+}-\mathrm{B}_{\mathrm{p}}$ of about 2 MeV before proton emission starts to compete with $\gamma$-ray emission. A good estimate of this threshold is when calculated valuer of $\Gamma_{\mathbf{p}} \Gamma_{\gamma}$ in the emitter are greater than $10^{-4}[\mathrm{Nit88}]$. Before proton branches $\mathrm{P}_{\mathrm{p}}$ defined as the number of protons per $\beta$ decay, are large enough to be experimentally observable, $\mathrm{Qec}_{\mathrm{ec}}-\mathrm{B}_{\mathrm{p}}$ needs to be 1 to 2 MeV larger than $\Theta_{\mathrm{p}}$. The energetics for delayed proton decay of ${ }^{123} \mathrm{Ce}$ with Qec and $\mathrm{B}_{\mathrm{p}}$ values from [Lir76] along with the measured proton spectrum are shown in Fig. 3.1(b).

The effects of pairing in the nucleus strongly influence the energetics for delayed proton emission. The criterion of $\mathrm{Q}_{\mathrm{Ec}}-\mathrm{B}_{\mathrm{p}}-\Theta_{p} \geqslant 0 \mathrm{MeV}$ can be satisfied by any sufficiently neutron-deficient nucleus, be it even-even (ee), even-odd (eo), oddeven (oe), or odd-odd (oo) but the majority of known delayed proton precursors are even-odd or odd-odd. In general terms, this is easy to understand by considering $Q_{E C}$ and $\mathrm{B}_{\mathrm{p}}$ values for the four typer of precursors as shown in Fig. 3.2. Since ar everi-odd precursor is the most favorable case, it will be used as a reference [Fig. 3.2(b)] with $Q_{E c}$ and $B_{p}$, denoted by $Q^{\prime}$ and $B$ ', respectively. The minimum energy required to break a pair $2 \Delta$ is equal to about 2 MeV in this mass region, where $\Delta$ is the gap parameter ( $-12 \mathrm{~A}-1 / 2 \mathrm{MeV}$ ). Assuming the nuclei are near each other on the mass surface, the approximate $Q_{E C}$ values are: $Q^{\prime}-2 \Delta$ for an even-even precursor (a proton pair is broken) [Fig. 3.2(a)], $Q^{\prime}$ for an even-odd precursor (one proton pair broken and one neutron pair formed), $Q^{\prime}$ for an odd-even precursor (no pairs broken
or formed) [Fig. 3.2(c)], and $Q^{\prime}+2 \Delta$ for an odd-odd precursor (one neutron pair formed) [Fig. 3.2(d)]. The proton binding energies are approximately $B$ ' for eveneven or even-odd precursort (the emitter has an unpaired proton) and $B^{\prime}+2 \Delta$ for odd-even or odd-odd precurcors (the emitter has to break a proton pair). The $\mathrm{Q}_{\text {Ec }}-\mathrm{B}_{\mathrm{p}}$ values for even-odd or odd-odd precursors will be similar and, in general, about 2A larger than $Q_{\text {Ec }}-B_{p}$ values for neighboring even-even or odd-even precursors. Large $\mathrm{Q}_{\mathrm{Ec}}-\mathrm{B}_{\mathrm{p}}$ values and small $\mathrm{B}_{\mathrm{p}}$ values favor delayed proton emission so the order from largest proton branch to smallest, for the hypothetical precursors in Fig. 3.2, would be even-odd, odd-odd, even-even, and odd-even. General features of the $\beta$-strength function discussed below also favor even-odd or odd-odd precursors. The energetics for a typical even-odd precursor ${ }^{151} \mathrm{Yb}$ and an odd-odd precursor ${ }^{150} \mathrm{Tm}$ are shown in Fig. 3.3.

In practice, the production cross sections are as important as the energetics in determining whether a given precursor can be experimentally observed. In Fig. 3.4 a region of the chart of the nuclides around ${ }^{129} \mathrm{Nd}$ is shown where each nucline is assigned a "figure of merit" estimating the experimentally observable delayeu proton intensity. This value is the product of the calculated [Win72] maximum cross section (using the best possible target/projectile combination) and the predicted proton branching ratio from statistical model calculations discussed below (assuming constant $\beta$-strength functions), normalized to 100 for ${ }^{129} \mathrm{Nd}$. Other factors affecting the experimental yield of a particular isotope such as the diffusion rate of the different elements in the ion source, which affects short half-lives more strongly, or the different surface ionization efficiencies are not included.

### 3.2. MEASURABLE QUANTTITES

In order to extract information from the shape of the delayed proton spectrum which can be calculated in the framework of a statistical model discussed below, other relevant information about the precursor, emitter, and daughter nuclei need to be measured. A proton spectrum from an isolated precursor must be first obtained. For the relatively high $\mathbf{Z}$ precursors discussed here, most of the population of proton emitting levels occurs via electron capture. The characteristic $\mathbf{K} \mathbf{x}$ rays following electron capture measured in coincidence with the delayed protons, therefore, uniquely identify the $\mathbf{Z}$ of the emitter and can be used to determine if there is more than one precursor present in a given isobaric chain. In cases where there is more than one precursor present, a different reaction (or projectile energy) or different
counting intervals, if the half-lives are different, can be used to enhance one of the precursors. A more difficult situstion is shown in Fig. 3.3 where both ${ }^{151 Y} \mathrm{Yb}$ and 150 Tm have $\beta$-decaying isomers that also have delayed proton branches. In these cases, both the isomer and the ground state would give rise to $\mathbf{K} \times$ rays with the same energy and would appear as a single precursor. Other information from such decays can be used to decide whether there is an isomer present but obtrining separate proton spectra from the isomer and the ground state is usually difficult.

The large fraction of $\beta$ decays that occur via electron capture make possible a method of measuring the proton emitting level lifetimes known as the Particle X-ray Coincidence Technique (PXCT) [Har76]. This technique has been used in medium mass precursors ( $A=70$ ) to test the level density, partial proton widths, and parrial $\gamma$ widths used in statistical model calculations. A K shell atomic vacancy is created approximately $80 \%$ of the time during electron capture for the range of elements discussed here. If the lifetime of the $K$ vacuncy is on the same order as the proton emitting level lifetime, then the $\mathbf{K}$ vacancy may be filled before the proton is ejected (Z-1 $x$ rays are observed) or it may be filled afier the proton has been ejected (Z-2 $x$ rays are observed). Since the $\mathbf{K}$ vacancy lifetimes can be calculated precisely, a measurement of the (Z-1)(Z-2) K x-ray intensity ratios can be used to determine the proton emitting level lifetimes. For the range of $\mathbf{Z}$ discussed here, the $K$ vacancy filling is faster than the proton emission so only Z-1 $x$ rays are expected. A second source of 7,-2 energy $x$ rays is the internal conversion of transitions from excited levels populated in the proton daughter nucleus. For many even-odd precursors studied here, the even-even proton daughters will have low-lying 2+ levels and the subsequent E2 transitions will be converted (at Z-60, a 200 keV E2 transition will have a $K$ conversion coefficient of 0.15 ) and produce $\mathbf{Z - 2} \mathbf{x}$ rays. Knowledge of the final states populated in proton emission and the multipolaritiet of the transitions between them is, therefore, necessary before reliable PXCT results can be obtained.

The relative intensities of levels populated in the proton daughter nucleus (final state branches), from a measurement of $\gamma$-rays in coincidence with the delayed protons, can be used to determine or restrict the range of values for the precursor spin and parity. The experimental final state branches can be compared with the predicted branches from statistical model calculations for a series of precursor spins. Typically osif; one or two precursor spins will be consistent with the measured values. For even-odd precursors, the proton daughter is an even-even nucleus and the level energies, spins, and parities are often known from in-beam $\gamma$ or from $\beta$ decay experiments. Final state branches have been measured for all even-odd
precursors presented here. Corrections for detection efficiency, internal conversion, summing in the close counting geometries, and feedings from higher levels have been taken into account in extracting final state branches from the observed $\gamma$-ray intensities. For odd-odd precursors, the odd-even proton daughters are, in general, poorly studied and little is know about their low-lying level structure. Given the small number of proton events observed for most odd-odd precursors, it was impossible to measure final state branches in most cases.

The maximum proton decay energy that is observed (the endpoint of the proton spectrum) is related to the $\mathrm{Q}_{\mathrm{Ec}}-\mathrm{B}_{\mathrm{p}}$ value and in principle the proton spectrum can be used to determine this quantity in nuclei far from stability. Unfortunately, this requires very good statistics in the endpoint region. The $\mathrm{Q}_{\mathrm{Ec}}-\mathrm{B}_{\mathrm{p}}$ value is determined by calculating a proton spectrum with varying values for $\mathrm{Q}_{\mathrm{Ec}}-\mathrm{B}_{\mathrm{p}}$ until the best fit to the proton spectrum in the endpoint region is obtained. An example of this type of analysis can be found in [Jon76]. A more general method to determine $\mathrm{Q}_{\mathrm{Ec}}-\mathrm{B}_{\mathrm{p}}$ is to measure the electron capture to positron ratio of the proton emitting levels as a function of proton energy. The EC/ $\beta+$ ratio over a small proton energy interval determines the average $\beta$-decay energy to the proton emitting levels and when added to the average proton energy in the interval gives $\mathrm{Q}_{\mathrm{Ec}}-\mathrm{B}_{\mathrm{p}}$. The $\mathrm{EC} / \beta+$ ratio is usually determined by counting protons in coincidence with positrons or 511 keV annihilation radiation and comparing to the total number of protons. Since a coincidence measurement is required, this technique is again limited to cases where the proton rate is high. When more than one final state in the proton daughter is fed, there are additional complications and the accuracy to which the final state branches are known will contribute to the uncertainty in $\mathrm{Q}_{\mathrm{Ec}}-\mathrm{B}_{\mathbf{p}}$. Examples of this technique can be found in [Hor72a, Kar74, Tid85, Har87]. Both methods require that the $\beta$ strength function vary slowly with energy over the proton emitting region before reliable $\mathrm{Q}_{\mathrm{Ec}}-\mathrm{B}_{\mathrm{p}}$ values can be obtained. The number of protons observed for most of the precursors presented here was not sufficient for precise Qec- $_{\mathbf{p}}$ determinations.

A very important quantity that can be measured is the proton branching ratio, $\mathbf{P}_{\mathbf{p}}$. The requires a measurement of the total proton intensity and total $\beta$-decay intensity for a particular precursor under identical experimental conditions. The total $\beta$-decay intensity is the sum of the positron intensity and the electron capture intensity. Since practically all isotopes in an isobaric chain will give rise to positrons, multicomponent decay analysis of the positrons must be used to get the fraction associated with a particular isotope. Limitations in such an analysis are that the half-lives of the isotopes in an isobaric chain must be sufficiently different and the
$\beta$ intensity of the isotope of interest must be a significant fraction of the total $\beta$ intensity or the multicomponent analysis may fail. The electron capture intensity for each element can be determined from the intensities of the $\mathrm{K} \times$ rays for each element in an isobaric chain. Although the $\mathrm{K} \times$ rays can be clearly resolved and peak intensities accurately measured, the K x ray intensities may have contributions from internal conversion of transitions in the $\beta$-decay daughters. If these contributions are not known or cannot be measured, they will be a serious source of error. For precursors produced with large cross sections where detaiied information on the precursor $\beta$ decay is known or can be measured in the same experiment, reliable proton branching ratios can be determined. A very favorable case is a high-spin oddodd precursor since the even-even $\beta$-decay daughter will not have any high spin levels at low excitation energies. Any levels poppulated in $\beta$ decay will eventually decay through the $2^{+}$to $0^{+}$transition so the intensity of these $\gamma$ rays will equal the total $\beta$-decay intensity. Many of the odd-odd precursors presented here were produced in early experiments before $\gamma$-ray singles measurements were recorded so proton branching ratios could not be determined.

### 3.3. THE STATISTICAL MODEL

The density of states in a heavy mass emitter at excitation energies sufficient for proton emission is expected to be large enough for a compound nucleus or statistical model to apply. If there is no correlation between the preceding $\beta$ decay and the subsequent level de-excitation (compound nucleus assumption), then delayed proton emission can be considered as a two step process: (i) $\beta$ decay to an excited state in the emitter (ii) the de-excitation of this state via proton or $\gamma$-ray emission. The $\beta$ intensity decreases rapidly as the excitation energy increases due to the decreasing available phase space whereas $\Gamma_{p} \Gamma_{\text {tot }}$ is zero below the proton emission threshold, increases rapidly with increasing proton energy above the threshold, and then changes more slowly as the proton energy approaches the Coulomb barrier. The product of these two factors gives the beli-shaped proton distribution characteristic of heavy precursors as shown in Fig. 3.5 for ${ }^{123} \mathrm{Ce}$. The main features of a statistical description of delayed proton emission were first proposed in [Hor72b] with later refinements to include fluctuation phenomena [Kar73, Jon76] and improved prescriptions for quantities such as level densities and average radiation widths [Har81, Har82]. This model can predict the spectral shape, the proton branching ratio, and final state branches.

It is convenient to discuss the intensity distribution of the preceding $\beta$ decay in terms of a $\beta$-strength function $S_{\beta}$ [Han73] defined as a reciprocal $f$-value calculated per MeV of final levels at excitation energy $\mathrm{E}^{*}$ in the emitter. The strength function contains the nuclear structure information while the kinematic effects are contained in the statistical rate function. Then the normalized total $\beta$ intensity per MeV at excitation energy $\mathrm{E}^{*}$ in the emitter can be written as

$$
\begin{equation*}
I_{\beta}\left(E^{*}\right)=S_{\beta}\left(F^{*}\right) f\left(Z-1, Q_{E c}-E^{*}\right) / \int_{0}^{Q_{\text {ac }}} S_{\beta}(E) f\left(Z-1, Q_{E c}-E\right) d E, \tag{3.1}
\end{equation*}
$$

where $f=f_{\beta^{+}+} f_{E C}$ is the sum of the statistical rate functions for $\beta^{+}$and $E C$ decay calculated according to [Gov71]. In order to evaluate eqn. 3.1, some assumption about the form of $S_{\beta}$ must be made. The simplest form is $S_{\beta}$ equal to a constant above a lower energy cutoff value. The cutoff values are chosen to be $60 \%$ of $0 \Delta$, $2 \Delta$, or $4 \Delta$ for even-even, odd-mass, and odd-odd precursors, respectively [Han73]. These cutoff values are multiples of the pairing energy since most of the protons that can $\beta$ decay are in paired orbitals and most of the $\beta$ strength, therefore, originates from the paired system. This form of $\mathrm{S}_{\boldsymbol{\beta}}$ has been shown to be a reasonable approximation to measured electron capture strength functions using total absorption spectroscopy of neutron-deficient elements with 77SZS86 [Duk70].

Another form of $S_{\beta}$ that may be used is from the gross theory of $\beta$ decay [Tak73]. This model assumes the $\beta$-strength function can be represented by sums of single-particle strength functions. The single-particle strength functions are approximated with Gaussian or modified-Lorentz functions (several MeV wide) centered near the isobaric analog states. An appropriate single-particle model such as the Fermi-gas model is used to calculate level densities and the effects of the Pauli exclusion principle. Pairing effects are also incorporated in the model and calculations for both allowed and first-forbidden transitions are possible.

A more microscopic approach to allowed GT $\beta$-strength function calculations has recently become available [Kru84]. The Nilsson model, using the modified oscillator potential, is used to calculated the single-particle energy levels and wavefunctions used in the subsequent $\beta$-strength function calculation. The parameters of the potential are adjusted to reproduce the experimento? ringle-particle levels for both spherical and deformed nuclei in the region of interest. The $\beta$ strength function calculation involves evaluating the GT $\beta$-decay operator between the Nilsson model generated initial and final state wavefunctions. Pairing is treated
in the BCS approximation and a simple residual interaction is included by use of the Random Phase Approximation (RPA). The strength of the residual interaction is adjusted so that 'te calculation reproduces the experimental energies of the giant GT resonances for ${ }^{208 P b}$ and ${ }^{144} \mathrm{Sm}$. Further detrils of this model can be found in [Kru84]. The results from these calculations (discrete transition intensities from the $\beta$-decay parent to the calculated $\beta$-decay daughter levels) are smoothed with a
Gaussian function before incorporation into the statistical model calculations. Figure 3.6 shows $\mathrm{I}_{\beta}\left(\mathrm{E}^{*}\right)$ for ${ }^{123} \mathrm{Ce}$ based on 2 constant $\mathrm{S}_{\beta}$ [Fig. 3.6(a)], a gross theory $\mathrm{S}_{\beta}$ [Fig. 3.6(b)], and a Nilsson/RPA calculated $\mathrm{S}_{\beta}$ [Fig. 3.6(c)].

The compound nucleus expression for the intensity of an individual proton transition ${\underset{P}{i f}}^{\mathrm{f}}$ from a state i in the emitter to a state f in the proton daughter is given by

$$
\begin{equation*}
\mathrm{I}_{\mathrm{p}}^{\mathrm{if}}\left(\mathrm{E}_{\mathrm{p}}\right)=\omega\left(\mathrm{J}, \mathrm{~J}_{\mathrm{i}}\right) \mathrm{I}_{\beta}\left(\mathrm{E}^{*}\right) \frac{\Gamma_{\mathrm{p}}^{\mathrm{if}}\left(\mathrm{E}_{\mathrm{p}}\right)}{\Gamma_{\gamma^{\prime}}^{\mathrm{j}}\left(\mathrm{E}^{*}\right)+\sum_{\mathbf{f}^{\prime}} \Gamma_{p}^{i f^{\prime}\left(E_{p}^{\prime}\right)},} \tag{3.2}
\end{equation*}
$$

where $\mathrm{E}_{\mathrm{p}}$ is the energy of the emitted proton, $\mathrm{r}_{\mathrm{p}}\left(\mathrm{E}_{\mathrm{p}}\right)$ is partial proton width for a transition between initial state $i$ and final state $f, \Gamma^{i},\left(E^{*}\right)$ is the total $\gamma$ width for state $i$, and the second term in the denominator is the sum over all final states of all open proton channels. The statistical weight factor for feeding of levels in the emitter with a spin $J_{i}^{\pi}$ from a precursor with spin and parity $\mathrm{J}^{\pi}$ is approximated by

$$
\begin{equation*}
\omega\left(\mathrm{J}, \mathrm{~J}_{\mathrm{i}}\right)=\left(2 \mathrm{~J}_{\mathrm{i}}+1\right) /[3(2 \mathrm{~J}+1)] . \tag{3.3}
\end{equation*}
$$

The proton energy is related to the excitation energy $\mathrm{E}^{*}$ through the relationship

$$
\begin{equation*}
E^{*}=B_{p}+E_{f}+\frac{A}{A-1} E_{p} \tag{3.4}
\end{equation*}
$$

where $B_{p}$ is the proton binding energy, $\mathrm{E}_{\mathrm{f}}$ is the energy of state f in the daughter, and $A$ is the emitter mass number. The proton partial width can be calculated in the optical model by means of the relationship

$$
\begin{equation*}
\Gamma_{p}^{i f}\left(E_{p}\right)=\left[2 \pi p_{i}\left(E^{*}\right)\right]^{-1} \sum_{j} T_{1, j}\left(E_{p}\right), \tag{3.5}
\end{equation*}
$$

where $\mathrm{p}_{\mathrm{i}}\left(\mathrm{E}^{*}\right)$ is the density of levels with spin and parity $\mathrm{J}_{\mathrm{i}}^{\pi}, \mathrm{T}_{\mathrm{l}}\left(\mathrm{E}_{\mathrm{p}}\right)$ are the optical model transmission coefficients for protons of energy $\mathrm{E}_{\mathrm{p}}$ and angular momentum 1 , and the sum extends over the partial waves permitted by the selection rules in spin and parity. The total $\gamma$ width of state $i$, assuming E1 radiation dominates at high level densities, is given by [Bar73] as

$$
\begin{equation*}
\Gamma_{\gamma}^{i}\left(E^{*}\right)=\int_{0}^{E_{m 2 x}} E_{\gamma}^{3} f_{E 1}\left(E_{\gamma}\right) \sum_{j^{\prime}=j-1}^{j^{\prime}=j+1} \frac{\rho_{j}\left(E^{*}-E_{\gamma}\right)}{\rho_{j}\left(E^{*}\right)} d E_{\gamma} \tag{3.6}
\end{equation*}
$$

where $\rho_{j}$ is the density of spin J states, $\mathrm{f}_{\mathrm{EI}}$ is the strength function for $\mathrm{E} 1 \psi$-decay; $f_{E 1}\left(E_{\gamma}\right)=8.7 \times 10^{-8} \sigma\left(\mathrm{E}_{\gamma}\right) / \mathrm{E}_{\gamma}$, and $\sigma\left(\mathrm{E}_{\gamma}\right)$ is the photoabsorption cross section in mb [Har82].

Equation 3.2 is valid when individual proton transitions can be resolved, however, when the average spacing between levels in the emitter is less than the detector resolution, what is experimentally observed is a statistical average over many such transitions and the total proton intensity over a proton energy interval $\mathrm{dE}_{\mathrm{p}}$ is

$$
\begin{equation*}
I_{p}\left(E_{p}\right) d E p=\sum_{i} \sum_{f} \omega\left(J, J_{i}\right)\left\langle I_{\beta}\left(E^{*}\right)\right\rangle\left\langle\frac{\Gamma_{p}^{i f}\left(E_{p}\right)}{\Gamma_{\gamma}^{i}\left(E^{*}\right)+\sum_{\mathbf{f}^{\prime}} \Gamma_{p}^{i f^{\prime}}\left(E_{p}^{\prime}\right)}\right\rangle d E_{p}, \tag{3.7}
\end{equation*}
$$

where the sum is taken over all possible initial and final states that can give rise to a proton with energy in the interval $\mathrm{E}_{\mathrm{p}}, \mathrm{E}_{\mathrm{p}}+\mathrm{d} \mathrm{E}_{\mathrm{p}}$ and the brackets 〈〉 denote statistical averages of the enclosed quantities over the excitation energy associated with proton energies in the interval $\mathrm{E}_{\mathrm{p}}, \mathrm{E}_{\mathrm{p}}+\mathrm{E}_{\mathrm{p}}$. The total proton intensity per $\beta$ decay is

$$
\begin{equation*}
P_{p}=\int_{0}^{E_{p}, \max } I_{p}\left(E_{p}\right) d E_{p} \tag{3.8}
\end{equation*}
$$

The $\beta$ intensity and the individual partial widths are proportional to the squares of nuclear matrix elements and are expected to have Porter-Thomas distributions about their means. The Porter-Thomas distribution is very skew and may give rise to significant fluctuations in the measured proton intensities. Attempts to extract quantities such as the level density from the magnitude of the fluctuations can be found in [Kar73, Jon76, Elm78].

A computer code that originated at CERN and GSI which calculates delayed proton spectra according to eqn. 3.7 was made available [Sch83] and calculations of spectral shapes, proton branching ratios, and final state feedings were performed with the input parameters discussed next. The precursor spin is considered as a variable unless known from previous experiments. The final state energies, spins, and parities are usually taken from the literature or from systematics. The different forms of $S_{\beta}$ which could be used in the calculations were discussed above. Particle separation energies and $\beta$-decay $Q$ values from the mass formula of [Lir76] were used based on comparisons with measured masses [Hau84] indicating that this model is better than other formulae at predicting masses in this region. In [Hor72b] the level density formula of [Gi165] and average radiation widths taken from [Cam57] were used but PXCT results [Har81, Har82] suggest that the back-shifted Fermi level densities [Dil73] and the the average radiation width based on photoabsorption cross sections, eqn. 3.6, give better agreement with experiment (for A=70 precursors) and have been used for the calculations presented here. Transmission coefficients can be calculated from the optical model with many different sets of parameters [Per63, Bec69, Joh70, Joh79]. The calculations presented here used the parameters from [Bec69]. In Fig. 3.7, the measured proton spectrum for ${ }^{123} \mathrm{Ce}$ is compared to statistical model calculations using a constant $\mathrm{S}_{\beta}[$ Fig. 3.7(a)], a gross theory $\mathrm{S}_{\beta}$ [Fig. 3.7(b)], and a Nilsson/RPA calculated $\mathrm{S}_{\beta}$ [Fig. 3.7(c)].


Figure 3.1. (a) Generic decay scheme for $\beta$-delayed proton emission from a single state at excitation energy $E^{*}$ and (b) delayed proton decay of ${ }^{123} \mathrm{Ce}$. Notation and symbols are explained in the text. Energies are in MeV with Q values and separation energies from [Lir76].


Figure 3.2. Effects of pairing on the energetics for delayed proton emission; (a) even-even precursor, (b) even-odd precursor, (c) odd-even precursor, and (d) odd-odd precursor. Electron capture $Q$ values and proton binding energies are shown relative to the values for the even-odd precursor (denoted by $Q^{\prime}$ and $\mathbf{B}^{\prime}$, respectively). Excitation energies greater than the proton emission threshold in each emitter are shaded. The energy required to break a pair $2 \Delta$ is about 2 MeV for $\mathrm{A}=130$ nuclei.


Figure 3.3. Schematic representation of delayed proton decay for (a) an odd-odd precursor and (b) for an even-odd precursor. Both precursors shown here have isomers with beta-delayed protor: branches.


Figure 3.4. Region of the chart of nuclides around ${ }^{129} \mathrm{Nd}$ with a "figure of merit" assigned to each nuclide (shown in bold) estimating the relative intensity of delayed protons that would be experimentally observed. The "figure of merit" is the product of the maximum calculated cross section value and the calculated proton branching ratio normalized to the value for ${ }^{129} \mathrm{Nd}$. The known delayed proton precursors are shaded. The QEC , Bp , and QEC - $\mathrm{Bp}_{\mathrm{p}}$ values from [Lir76] are shown in parentheses for each nuclide.


Figure 3.5. Beta intensity $\mathrm{I}_{\beta}$ (for a constant $\mathrm{S}_{\beta}$ ) and a factor related to the competition between proton emission and gamma emission $\Gamma_{\mathrm{p}} / \Gamma_{\text {tot }}$ as a function of excitation energy in the emitter for ${ }^{123} \mathrm{Ce}$. The product of the two factors (the shaded curve) represents the characteristic shape of delayed proton spectra from heavy mass precursors.


Figure 3.6. Beta-strength functions and total beta intensities for ${ }^{123} \mathrm{Ce}$; (a) constant, (b) gross theory [Tak73], and (c) Nilsson/RPA calculated [Kru84]. The histogram in (c) is the calculation binned in 50 keV wide channels and the curve labeled $\mathrm{S} \beta$ is the result of a Gaussian smoothing of the histogram with a sigma equal to 0.7 MeV .


Figure 3.7. Comparison of calculated delayed proton spectra with experiment for ${ }^{123} \mathrm{Ce}$. Calculations are for (a) constant, (b) gross theory, and (c) Nilsson/RPA calculated beta-strength functions. All calculations used $Q$ values from [Lir76] and a precursor spin of $5 / 2+$. Also shown are the calculated contributions to the proton spectrum from decays to each of the final states in ${ }^{122} \mathrm{Ba}$.

## 4. EVEN MASS PRECURSORS

### 4.1. GENERAL

Twenty precursors with even mass numbers have been studied; 17 of the precursors were odd-add and 3 were even-even. In most cases the number of observed protons was a few hundred or less and half-lives and proton spectra were all that could be obtained. For two precursors, ${ }^{148} \mathrm{Ho}$ and ${ }^{150} \mathrm{Tm}$, final state branching ratios were also measured. The reactions used to produce these precursors are summarized in Table 4.1. Also listed in Table 4.1 are the calculated cross sections, detector configurations, and dates when the bombardments were performed.

The measured half-lives of the delayed proton activities are given in Table 4.2. Information from the experiment that gave the best data for a given precursor is tabulated. For each precursor the date of the expsriment (to correlate with entries in Table 4.1), counting intervals and the number of events observed at each counting interval is also given. The last two columns are predicted half-lives from the gross theory of $\beta$ decay and values obtained from Nilsson/RPA $\beta$-strength function calculations. The gross theory values [Tak73, Tak88] were calculated using the modified Lorentz strength function with Q values from [Lir7G]. The values in the last column were obtained by integrating the Nilsson/RPA calculated $\beta$-strength functions [Kru84] from 0 to $\mathrm{Q}_{\mathrm{Ec}}$ with an assumed Gamow-Teller quenching factor of 0.5 and $Q$ values from [Lir76].

The delayed proton decay for each precursor is summarized in Table 4.3. The proton energy range is an estimate of the lowest and highest proton energies that were observed. The mean $\overline{\mathbf{x}}$ and vidth $\overline{\mathbf{w}}$ were calculated from the expressions:

$$
\overline{\mathbf{x}}=\mathrm{A}^{-1} \Sigma \times \mathrm{C}_{\mathrm{x}} \quad \text { and } \quad \overline{\mathbf{w}}=2.355 \sqrt{\mathrm{~A}^{-1} \Sigma \mathrm{C}_{\mathrm{x}}(\mathrm{x}-\overline{\mathrm{x}})^{2}},
$$

where the area $A$ is the spectrum integral, $C_{x}$ is the contents of channel $x$, and the sums are over all channels. Proton branching ratios and precursor spins are listed when known. The input parameters for statistical model calculations are given in Table 4.4. In many cases the precursor spin was not known and could only be estimated from systematics. In this region, $1+$ low-spin and 4 ; 5 ; or 6 - high-spin isomers are known in many odd-odd nuclei closer to stability and for the odd-odd precursors near $\mathrm{N}=82$. Heavy-ion reactions are expected to strongly favor high-spin
production, so spins of $5^{-}$were assumed for precursors with $\mathbf{Z}<64$ and spins of $6^{-}$ for precursors with $\mathbf{Z}>64$.

The experimental results are presented in figures 4.1 though 4.18 which have a similar format. The top of each figure shows a delayed proton spectrum (the entries in Table 4.3 correspond to the spectra shown in the figures) plotted from 0 to 8 MeV at 36 keV per channel. Overlaying the measured proton spectrum are calculated proton spectra, normalized to the observed proton intensity, with the input parameters to the statistical model listed in Tabie 4.4. Each calculated proton spectrum is labeled with the respective $\beta$-strength function used in the calculation. Ghown next is a representative proton coincident $x$-ray spectrum used for unambiguous $\mathbf{Z}$ indentifications. Due to the difficulty of gain shifting spectra with low statistics, data from different detectors or different experiments were not combined unless necessary. The measured $x$-ray energies are given in the figures while the literature values for each element are reproduced in Tabie 4.5. A decay curve of the delayed proton activity is shown for data corresponding to the counting interval listed in Table 4.2. In cases where final state feedings were observed, a proton coincident $\gamma$-ray spectrum is also shown.

### 4.2. DISCUSSION OF INDIVIDUAL PRECURSORS

Pertinent information for each precursor is given in Tables 4.1 to 4.4 and will not be repeated below. Half-lives for many of the precursors discussed here and in chapter 5 have been published in [Nit87] and complementary information from $\beta$ decay for some of the precursors is discussed in [Gil87] and [Tot87d].

120La: This isotope was first reported in [Nit84] and is shown in Fig. 4.1.
122La: The proton spectrum from an experiment using a dual telescope cetector arrangement described in [Nit83b] is shown in Fig. 4.2(a) along with the calculated proton spectra. The results from a second experiment using the detector configuration listed in Table 4.1 are shown in Fig. 4.3. There were only 63 events observed in the second experiment and since the 10 -s counting interval is about one half-life it was difficult to confirm the 8.7 s half-life from the first experiment. The decay curve in Fig. 4.3 was fitted with a fixed half-life of 8.7 s . Both experiments were first reported in [Nit84]. The $\mathrm{QEC}_{\mathrm{Ec}}$ of 9.99 MeV from [Lir76] results in calculated half-lives that are too short and the calculated proton spectra do not match the measured spectrum in the endpoint region. Using a $\mathrm{Q}_{\mathrm{EC}}=9.49 \mathrm{MeV}$ resulted in a gross theory half-life of 7 s and an improved fit to the proton spectrum [Fig. 4.2(a)].

The $\beta$ decay of ${ }^{122}$ La has been studied in [Gen87] with a half-life of 8.5( 6 ) $s$ in agreement with the value listed in Table 4.2. The $\beta$-decay information suggests a possible precursor spin of 4 or 5 .
${ }^{124}$ Pr: The delayed proton data are shown in Fig. 4.4. Lanthanum $\mathrm{K} x$ rays and $\gamma$ rays of 70,113 , and 166 keV were also observed in coincidence with the protons but the $\gamma$ transitions cannot be uniquely placed since the level scheme of ${ }^{123} \mathrm{La}$ is not known. The $\beta$ decay of ${ }^{123} \mathrm{Ce}$ was reported in [Gen87] and $\gamma$-rays of 66, 113, and 178 keV were observed but no level scheme for ${ }^{123}$ La was given. Assuming any combination of M1 or E2 multipolarities for the above $\gamma$ transitions, all La K x rays can be accounted for by internal conversion. The possibility that the La $\mathrm{K} x$ rays could originate from a weak delayed proton branch in ${ }^{124} \mathrm{Ce}$ can be excluded for the following reasons: (i) internal conversion can account for all La K x rays, (ii) statistical model calculations indicate that the proton branching ratio for ${ }^{124} \mathrm{Ce}$ should be about 103 times weaker than for ${ }^{124} \mathrm{Pr}$ (folding in cross section predictions, ${ }^{124}$ Ce should still be 16 times weaker), and (iii) the decay of the proton activity gives, within the statistical uncertainty, no indication of a second, longer lived activity.

A weak $142 \operatorname{keV} \gamma$-ray decaying with a $\sim 1 \mathrm{~s}$ half-life can be assigned to ${ }^{124} \mathrm{Pr}$ $\beta$ decay and confirms the $\mathbf{2 +}^{+}$to $0^{+}$transition in ${ }^{124} \mathrm{Ce}$ [Yin86].
${ }^{126} \mathrm{Pr}$ : This isotope was first identified in [Nit83a] from experiments completed prior to the construction of the tape system. The precursor $Z$ assignment was based on systematics and predicted cross sections; no additional studies of this isotope have been performed. The proton spectrum is shown in Fig. 4.2(b). A recent $\beta$-decay study [Bér88] has reported a half-life of $3.0(4)$ s for ${ }^{126 p r}$, in excellent agreement with the value in Table 4.2. The $\beta$-decay results also indicate a likely precursor spin of greater than 5 or 6 .

128Pr: The proton activity at this mass number was at first assigned to ${ }^{128} \mathrm{Nd}$ [Nit83b] but a later experiment shown in Fig. 4.5 indicates delayed proton emission from only ${ }^{128} \mathrm{Pr}$ [Wi185]. No evidence for delayed proton decay from ${ }^{128} \mathrm{Nd}$ can be seen in the proton coincident $x$-ray spectrum and the decay curve appears to be a single component. The 3.1 (3) \& $\beta$ decay of ${ }^{128} \mathrm{Pr}$, which populated levels in ${ }^{128} \mathrm{Ce}$ most consistent with a spin of 4 or 5 , has been recently reported in [BEr88].
${ }^{130} \mathrm{Pm}$ : The discovery of this isotope, shown in Fig. 4.6, was reported in [Wil85]. The proton spectrum was highly distorted in this experiment. It appeared that the protons were degraded in energy but, during an examination of the telescope at the end of the experiment, no absarbing material between the detectors and
collection tape was found. Protons from ${ }^{129} \mathrm{Nd}$ were also produced and could be compared with the ${ }^{129} \mathrm{Nd}$ proton spectrum from a later experiment. A gain shifting procedure that was able to approximately reproduce the ${ }^{129} \mathrm{Nd}$ spectrum was also applied to ${ }^{130} \mathrm{Pm}$ and the result is shown in Fig. 4.6(a). No attempt was made to compare this proton spectrum with calculations.

132Pm: This isotope was first identified by decay analysis of the Nd x rays associated with electron capture [Bog77]. A delayed proton branch was first identified in [Wil85] and is shown in Fig. 4.7. Recent studies [Ber87, Ker87b, Kor87] of the $\beta$ decay of ${ }^{132 \mathrm{Pm}}$ have been completed but little information other than half-lives was given. In both studies, the $4^{+}$level in ${ }^{132} \mathrm{Nd}$ but not the $6^{+}$was fed perhaps indicating a spin of 3 or 4 for ${ }^{132} \mathrm{Pm}$.
${ }^{134} \mathrm{Eu}$ : A weak proton activity is assigned to ${ }^{134} \mathrm{Eu}$ (Fig. 4.8); further details can be found in [Vie88a].

136Eu: The delayed proton decay of this isotope is shown in Fig. 4.9 and is reported in [Vie88a]. The $\beta$ decay of ${ }^{136 \mathrm{Eu}}$ was also studied in [Vie88a] where tentative $3^{+}, 7^{+}$spin assignments for the low- and high-spin isomers were proposed. Other recent studies of ${ }^{136} \mathrm{Eu} \beta$ decay have also been reported [Bér87, Ker87a, Ker87b].

140 Tb : Identification of this isotope was first published in [Wi186] and is shown in Fig. 4.10.
$\mathrm{A}=142$ : Two delayed proton activities, ${ }^{142 \mathrm{~Tb}}$ (Fig. 4.11) and ${ }^{142} \mathrm{Dy}$ (Fig. 4.12) have been identified at this mass number [Wil86]. Analysis of the $\beta$ decay data yielded a ${ }^{142}$ Dy half-life of $2.3(8) s$ and this value was used in the decay curves shown in Figs. 4.11 and 4.12. A high-spin isomer ( $6^{-}$) and the ground state ( $1^{+}$) in ${ }^{142} \mathrm{~Tb}$ with half-lives of $0.3(1) \mathrm{s}$ and $0.6(2) \mathrm{s}$, respectively, were also identified [Gi187] in the $\beta$-decay analysis. The high spin isomer must have a weak $\beta$-decay branch due to the short half-life and the proton decay curves are more consistent with a 0.6 s component so the ${ }^{142} \mathrm{~Tb}$ precursor is tentatively assigned to the $1^{+}$ground state. It was not possible to obtain a clean proton spectrum associaied with ${ }^{142} \mathrm{~Tb}$ decay [Fig 4.11(a) is only $\sim 33 \% \mathrm{~Tb}$ ] therefore no calculations for ${ }^{142} \mathrm{~Tb}$ are shown in Fig. 4.11. The proton spectrum in Fig. 4.12(a) associated with ${ }^{142} \mathrm{Dy}$ decay is composed of $\sim 82 \%$ Dy and $\sim 18 \% \mathrm{~Tb}$ based on the decay curve analysis (the Tb admixture to the proton spectrum may affect comparisons with the calculations).
$\mathrm{A}=144$ : A proton emitter with a half-life of $0.7(1) \mathrm{s}$ was assigned to ${ }^{144} \mathrm{Ho}$ on the basis of Dy K x rays observed in coincidence with the protons [Wi186]. A second delayed proton activity with a half-life of $7(3) \mathrm{sw}$, assigned to ${ }^{144} \mathrm{Dy}$
[Wil85] from proton coincident Tb $\mathrm{K} \times$ rays. In the $3 / 84$ experiment, a GeLi detector with poorer resolution and efficiency had to be used and the assignment of the longer lived proton activity via coincident x mys was difficult. In a later experiment, using a reaction where the production of ${ }^{144} \mathrm{Ho}$ was predicted to be negligible, the proton activity could be assigned to ${ }^{144} \mathrm{Dy}$ and the data from this experiment are shown in Fig. 4.13. The $\beta$ decay of ${ }^{144}$ Dy was reported in [Red86, Gil87] with a half-life of 9.1(5) s. Using this half-life value in the decay analysis shown in Fig. 4.14(c), it can be calculated that the proton spectrum in Fig. 4.14(a) contains $\sim 15 \%{ }^{144} \mathrm{Dy}$ and $85 \%{ }^{144} \mathrm{Ho}$. The proton spectrum associated with ${ }^{144} \mathrm{Dy}$ [Fig. 4.13 (a)] is quite narrow and may distort the ${ }^{144} \mathrm{Ho}$ proton spectrum in Fig. 4.14(a). The statistics are too low to subtract the experimental ${ }^{144}$ Dy spectrum [Fig. 4.13(a)] from the spectrum in Fig. 4.14(a) in order to get a better estimate of the ${ }^{144} \mathrm{Ho}$ proton spectrum. Instead, the calculations shown in Fig. 4.14(a) are a mixture of ${ }^{144} \mathrm{Dy}$ and ${ }^{144} \mathrm{Ho}$ ( $15 \%$ and $85 \%$, respectively). No conclusive evidence for a delayed proton branch in ${ }^{144} \mathrm{~Tb}$, which has a $\mathrm{Q}_{\mathrm{EC}}-\mathrm{S}_{\mathrm{p}}$ similar to ${ }^{144} \mathrm{Dy}$ was obtained.
${ }^{146} \mathrm{Ho}$ : The $\beta$-decay of ${ }^{146} \mathrm{Ho}$ was first reported in [Gui82]. The delayed proton branch was identified in [Wil86] and is shown in Fig. 4.15.

A=148: The high-spin isomer of ${ }^{148} \mathrm{Ho}$ was first observed in [Tot79] with a half-life of $9(1) \mathrm{s}$. The low-spin $\left(1^{+}\right)$isomer with a half-life of $2(1)$ : was identified in [No182b]. Detailed studies of ${ }^{148} \mathrm{Ho} \beta$ decay [Tot88] and ${ }^{148} \mathrm{Ho}$ delayed proton decay [Nit88] have been recently carried out. The presence of a delayed proton branch in ${ }^{148} \mathrm{Er}$ was also found in [Nit88] and the delayed protons shown in Fig 4.16(a) are $\mathbf{2 0 \%} \mathrm{Er}$ and $\sim 80 \%$ Ho from decay analysis and $x$-ray intensities. Since a clean ${ }^{148} \mathrm{Er}$ spectrum could not be obtrained, only calculated spectra for ${ }^{148} \mathrm{Ho}$ are shown.

Weak $\gamma$ transitions in ${ }^{147} \mathrm{~Tb}$ were observed in coincidence with ${ }^{148} \mathrm{Ho}$ protons with the following intensities: $6(4) \%$ to the $7 / 2+$ level, $1(4) \%$ to the $5 / 2^{+}$ level, $3(5) \%$ to the $3 / 2^{+}$level, and $90(20) \%$ to both the $1 / 2^{+}$and $11 / 2^{*}$ levels. The calculated values for a 6 precursor are: $2 \%$ to the $7 / 2^{+}$level, $2 \%$ to the $5 / 2^{+}$level, $1 \%$ to the $3 / 2^{+}$level, and $95 \%$ to the $11 / 2^{-}$level. The calculated feedings are in good agreement with the measured values.

150 Tm: The isotope ${ }^{150} \mathrm{Tm}$ was first identified in [Nol82a] with a more extensive study of its $\beta$ decay reported in [Tot87b] where a half-life of 2.2(2) $s$ for the 6 - state of ${ }^{150} \mathrm{Tm}$ was obtained. There was indirect evidence that a low-spin ( ${ }^{+}$) isomer in ${ }^{150} \mathrm{Tm}$ was also present but no isomeric transition was observed and no half-life determined. A detailed study of the delayed proton decay [Nit88] was
recently completed. The delayed proton spectrum, etc. are shown in Fig. 4.17. The final state feedings to levels in ${ }^{149} \mathrm{Ho}$ are summarized in Table 4.6 where a mixture of $20 \% 1+$ and $80 \% 6$-precursors $g$ ave the best result.
${ }^{152} \mathrm{Lu}$ : The first observation of ${ }^{152} \mathrm{Lu}$ and its $\beta$ decay to levels of ${ }^{152 \mathrm{Yb}}$ was reported in [Tot87a]. From the observation of an allowed transition to a $5^{-}$level it was concluded that the spin/parity of ${ }^{152} \mathrm{Lu}$ is $4 ; 5$; or 6 . No evidence for a lowspin isomer was seen. The delayed proton decay was reported in [Nit88] and the data are shown in Fig. 4.18.

154 Lu : In a prejiminary experiment, fifteen delayed proton events and a few possible delayed $\alpha$ events were assigned to ${ }^{154} \mathrm{Lu}$ based on energetics, half-life, and cross section predictions [Vie88b]. No particle coincident x rays were observed due to the poor statistics so the Z assignment is somewhat uncertain at this time. This is the first evidence for delayed $\alpha$ emission near the $\mathrm{N}=82$ closed shell.

Table 4.1. Reactions used to prodece even-mass delayed proton precmens; Thickness = target thickness, EHILAC = beam energy at machine exil, ETaget = catculmed bemenergy at triget center, $\sigma=$ calculated cross section, Detectors $=$ detector configuration used.

| Lsotope | Reaction | Thickness $\left(\mathrm{mg} / \mathrm{cm}^{2}\right)$ | $\begin{aligned} & \text { EHMAC } \\ & \text { (MeV) } \end{aligned}$ | ETarget (MeV) | $\begin{gathered} \sigma^{2} \\ (m b) \end{gathered}$ | Dand | Detectars ${ }^{\text {c }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ${ }^{120}{ }_{\text {La }}$ | ${ }^{58} \mathrm{Ni}\left({ }^{64} \mathrm{Zn}, \mathrm{pn}\right)$ | 2 | 380 | 253 | 3.5 | 983 | A |
| 122 La | ${ }^{92} \mathrm{Mo}\left({ }^{36} \mathrm{Ar}, 3 \mathrm{p} 3 \mathrm{n}\right)$ | 2 | 196 | 188 | 7 | 9883 | A |
| ${ }^{124} \mathrm{Pr}$ | $\left.{ }^{92} \mathrm{Mo}^{36} \mathrm{Ar}, \mathrm{p} 3 \mathrm{n}\right)$ | 2 | 186 | 174 | 0.4 | 486 | B |
| ${ }^{128} \mathrm{Pr}$ | ${ }^{92} \mathrm{MO}\left({ }^{40} \mathrm{Ce}, 3 \mathrm{pn}\right)$ | 2 | 195 | 186 | 100 | 10884 | A |
| ${ }^{130} \mathrm{Pm}$ | $92 \mathrm{Mo}\left({ }^{40} \mathrm{Capm}\right)$ | 2 | 182 | 170 | 0.2 | 7184 | A |
| ${ }^{132} \mathrm{Pm}$ | ${ }^{96} \mathrm{Ru}\left({ }^{40} \mathrm{Ca}, 3 \mathrm{pn}\right)$ | 0.8 | 195 | 175 | 90 | 10184 | A |
| ${ }^{134} \mathrm{Eu}$ | ${ }^{92} \mathrm{Mo}{ }^{46} \mathrm{Ti}, \mathrm{p} 3 \mathrm{n}$ ) | 2 | 223 | 212 | 0.8 | $11 / 86$ | C |
| ${ }^{136} \mathrm{Eu}$ | ${ }^{92} \mathrm{Mo}\left({ }^{46} \mathrm{Ti}, \mathrm{pa}\right)$ | 2 | 204 | 192 | 1.5 | 11/86 | C |
| 140 Tb | $\left.{ }^{92} \mathrm{Mo}{ }^{(54} \mathrm{Fe}, 3 \mathrm{p} 3 \mathrm{n}\right)$ | 2 | 312 | 297 | 5 | 12185 | B |
| ${ }^{140} \mathrm{~Tb}$ | ${ }^{92} \mathrm{Mo}\left({ }^{52} \mathrm{Cr}, \mathrm{p} 3 \mathrm{n}\right)$ | 2 | 244 | 230 | 2 | $2 / 87$ | C |
| ${ }^{142} \mathrm{Dy}$ | ${ }^{92} \mathrm{MO}\left({ }^{54} \mathrm{Fe}, 2 \mathrm{p} 2 \mathrm{n}\right)$ | 2 | 277 | 261 | 5 | 2184 | A |
| ${ }^{142} \mathrm{~Tb}$ | ${ }^{92} \mathrm{Mo}\left({ }^{54} \mathrm{Fe}, 3 \mathrm{pa}\right)$ | 2 | 277 | 261 | 35 | 284 | A |
| ${ }^{142} \mathrm{Dy}$ | ${ }^{92} \mathrm{Mo}\left({ }^{54} \mathrm{Fe}, 2 \mathrm{p} 2 \mathrm{n}\right)$ | 2 | 261 | 247 | 4.5 | $12 / 85$ | B |
| 142 Tb | ${ }^{92} \mathrm{Mo}\left({ }^{54} \mathrm{Fe}, 3 \mathrm{pn}\right)$ | 2 | 261 | 247 | 60 | 12885 | B |
| ${ }^{142} \mathrm{Dy}$ | ${ }^{92} \mathrm{Mo}\left({ }^{52} \mathrm{Cr}, 2 \mathrm{n}\right)$ | 2 | 224 | 210 | 1 | 2/87 | C |
| 142 Tb | ${ }^{92} \mathrm{Mo}\left({ }^{52} \mathrm{Cr}, \mathrm{pn}\right)$ | 2 | 224 | 210 | 10 | $2 / 87$ | C |
| ${ }^{144} \mathrm{Ho}$ | ${ }^{92} \mathrm{Mo}\left({ }^{56} \mathrm{Fe}, \mathrm{p} 3 \mathrm{n}\right)$ | 2 | 273 | 257 | 0.4 | $2 / 84$ | A |
| ${ }^{144}$ Dy | ${ }^{92} \mathrm{Mo}\left({ }^{56} \mathrm{Fe}, 2 \mathrm{p} 2 \mathrm{n}\right)$ | 2 | 273 | 257 | 17 | 2184 | A |
| 144 Tb | ${ }^{92} \mathrm{Mo}\left({ }^{56} \mathrm{Fe}, 3 \mathrm{pn}\right)$ | 2 | 273 | 257 | 80 | 2184 | A |
| ${ }^{144} \mathrm{Ho}$ | ${ }^{92} \mathrm{Mo}\left({ }^{51} \mathrm{Ni}, 3 \mathrm{p} 3 \mathrm{n}\right)$ | 2 | 342 | 325 | 0.8 | 3/84 | A |
| ${ }^{144} \mathrm{Dy}$ | ${ }^{92} \mathrm{Mo}\left({ }^{58} \mathrm{Ni}, 4 \mathrm{p} 2 \mathrm{n}\right)$ | 2 | 342 | 325 | 11 | 3184 | A |
| ${ }^{144} \mathrm{~Tb}$ | ${ }^{92} \mathrm{Mo}\left({ }^{58} \mathrm{Ni}, 5 \mathrm{Sn}\right)$ | 2 | 342 | 325 | 23 | 384 | A |
| ${ }^{144} \mathrm{Dy}$ | ${ }^{92} \mathrm{Mo}\left({ }^{56} \mathrm{Fe}, 2 \mathrm{p} 2 \mathrm{n}\right)$ | 2 | 261 | 245 | 18 | 6185 | B |
| 144 Tb | $\left.{ }^{92} \mathrm{Mo}{ }^{56} \mathrm{Fe}, 3 \mathrm{pn}\right)$ | 2 | 261 | 245 | 100 | 6185 | B |
| ${ }^{146} \mathrm{Ho}$ | ${ }^{92} \mathrm{Mo}\left({ }^{58} \mathrm{Ni}, 2 \mathrm{p} 2 \mathrm{n}\right)$ | 2 | 278 | 262 | 40 | 11/84 | A |
| ${ }^{148} \mathrm{Er}$ | ${ }^{94} \mathrm{Mo}\left({ }^{58} \mathrm{Ni}, 2 \mathrm{p} 2 \mathrm{n}\right)$ | 2 | 275 | 257 | 9 | 11/85 | B |
| ${ }^{148} \mathrm{Ho}$ | $\left.{ }^{94} \mathrm{Mo}{ }^{58} \mathrm{Ni}, 3 \mathrm{pm}\right)$ | 2 | 275 | 257 | 80 | 11/85 | B |
| ${ }^{150} \mathrm{Tm}$ | ${ }^{96} \mathrm{Ru}\left({ }^{58} \mathrm{Ni}, 3 \mathrm{pn}\right)$ | 1.5 | 372 | 267 | 22 | 11/85 | B |
| ${ }^{152}$ Lu | ${ }^{96} \mathrm{Ru}\left({ }^{58} \mathrm{Ni,pn}\right)$ | 1.5 | 354 | 244 | 0.4 | $4 / 85$ | B |
| ${ }^{154} \mathrm{Lu}$ | ${ }^{92} \mathrm{MO}\left({ }^{64} \mathrm{Zn}, \mathrm{pn}\right)$ | 2 | 285 | 267 | 0.6 | $12 / 87$ | C |

${ }^{2}$ Calculated from [Win72].
${ }^{\text {b }}$ To indicate when more then one experiment was performed a a given mass chain and to correlate with entries in Table 4.2.
${ }^{c}$ The symbols $A, B$, and $C$ refer to the detector configurations shown in Figure 3.3.

Table 4.2. Half-lives of evea-mass delryed proton precursors; Trmait Time $=$ tipe trensport time,
Cycle Time $=$ length of collection and counting intervals, No. of Events $=$ number of delayed protons at the respective counting cycle, $\mathrm{T}_{1 / 2}$ Exp. $=$ memured half-life, $\mathrm{T}_{1 / 2}$ 2.t. $=$ predicted halflife from the gross theory of $\beta$ decay, $T_{1 / 2} R P A=$ half-life from Nikson/RPA $\beta$-strength function calculations.

| Isotope | Date | Transit <br> Time (s) | Cycle $\text { Time ( } \mathrm{s})^{2}$ | No. of Events | $\begin{gathered} \mathrm{T}_{1 / 2} \\ \text { Exp. }{ }^{6}(\mathrm{~s}) \end{gathered}$ | $\begin{gathered} \mathrm{T}_{1 / 2} \\ \mathrm{~g} \cdot \mathrm{~L}^{c}(\mathrm{~s}) \end{gathered}$ | $\begin{gathered} \mathrm{T}_{1 / 2} \\ \mathrm{RPA}^{d}(\mathrm{~s}) \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ${ }^{120}{ }_{\text {La }}$ | 9/83 | 0.07 | 5,10 | 62,441 | 2.8(4) | 1.4 | 1.8 |
| ${ }^{122} \mathrm{La}^{\text {e }}$ | 5/83 | -- | - | 1809 | 8.7(7) | 4.2 | 5.5 |
| ${ }^{124} \mathrm{Pr}$ | $4 / 86$ | 0.25 | 4 | 493 | 1.2(2) | 1.0 | 0.6 |
| ${ }^{126} \mathrm{Pr}^{\text {f }}$ | 10182 | -- | . | 171 | 3.2(6) | 3.0 | 2.0 |
| ${ }^{128} \mathrm{Pr}$ | 10184 | 0.25 | 12 | 126 | 4 (1) | 9.2 | 7.7 |
| ${ }^{130} \mathrm{Pm}$ | $7 / 84$ | 0.25 | 8 | 62 | 2(1) | 2.3 | 1.7 |
| ${ }^{132} \mathrm{Pm}$ | 10184 | 0.25 | 12 | 287 | $5(1)$ | 5.7 | 3.7 |
| ${ }^{134} \mathrm{Er}$ | 11/86 | 0.07 | 4 | 34 | $0.5(2)$ | 1.4 | 1.3 |
| ${ }^{136} \mathrm{Eu}$ | 11/86 | 0.07 | 4,16 | 44,167 | 4(1) | 3.8 | 1.8 |
| 140 Tb | $12 / 85$ | 0.25 | 8 | 206 | $2.015)$ | 2.2 | 2.0 |
| ${ }^{142} \mathrm{~g}_{\mathrm{Tb}} \mathrm{Tb}$ | 287 | 0.07 | 2.4 | 1445 | $0.6(2)^{\text {h }}$ | 4.9 | 3.5 |
| 142 Dy | $12 / 85$ | 0.25 | 8 | 1158 | $2.3(3)^{\text {h }}$ | 4.2 | 2.7 |
| 144 Dy | 6185 | 0.25 | 12 | 668 | $9.1(5)^{\mathrm{h}}$ | 9.3 | 9.7 |
| ${ }^{144} \mathrm{Ho}$ | 3/84 | 0.07 | 2.4,5,50 | 428,3458,678 | 0.7(2) | 1.5 | 1.3 |
| ${ }^{146} \mathrm{Ho}$ | 11/84 | 0.25 | 12 | 288 | $3.1(5)$ | 2.6 | 2.9 |
| ${ }^{148} \mathrm{Ho}^{\text {i }}$ | 11/85 | 0.25 | 16 | 19755 | $9.7(3)^{\text {h }}$ | 4.8 | 5.9 |
| ${ }^{148} \mathrm{Er}$ | 11/85 | 0.25 | 16 | 19758 | 4.4(2) ${ }^{\text {h }}$ | 4.2 | 2.4 |
| ${ }^{150} \mathrm{Tm}^{\text {i }}$ | 11/85 | 0.25 | 8 | 6191 | 2.2(2) | 1.5 | 0.9 |
| ${ }^{152} \mathrm{Lu}^{\text {i }}$ | 4/85 | 0.25 | 4 | 353 | 0.7(1) | 0.6 | 0.3 |
| ${ }^{154} \mathrm{Lu}$ | 1287 | 0.07 | 2.56 | -15 | -1 | 3.1 | 1.4 |

${ }^{\text {a }}$ Decay curves are shown in Figures 4.1 to 4.18. When more than one tape cycle was used only the underlined cycle time is presented in the corresponding figure.
${ }^{b}$ Best value from all available proton data.
${ }^{c}$ Values from the gross theory [Tak73, Tak88] using the modified Lorentz strength functioa.
${ }^{\text {d }}$ Calculated by integraling $\beta$-strengin functions from [Ku84] assuming a Gamow-Teller quenching factor of 0.5 .
${ }^{e}$ Data taken fros 1 Nit84].
f Data taken from [Nit83b].
$\mathbf{g}$ Mixture of all delayed protons in this isobaric chain.
${ }^{\mathrm{h}}$ Half-lives quoted are values from $\beta$-delayed $\gamma$ rays given in [Nit87] and references cited therein.
i Decay dominated by high spin ( $-6^{-}$) isomer.

Table 4.3. Summary of the delayed prowa decay of even-mass precursors; Type $=$ type of. precursor: odd-odd ( 00 ) or even-even (ee), $\mathrm{T}_{\mathbf{z}}=1 / 2(\mathrm{~N}-\mathrm{Z}$ ) procursor isorpin projection, No. of Events n number of protons shown in Fiqures 4.1(a) to 4.18(a), Rage $=$ approximale lowest and highest observed proton energies, $\bar{x}=$ average proton energy, $\bar{w}=$ FWHM of proton distribution, $P_{p}=$ measured proton branching ratio, and $\mathrm{J}^{\boldsymbol{*}}=$ precursor spin and parity.

| Isotope | Type | $\mathrm{T}_{\mathbf{z}}$ | No. of Events | $\begin{aligned} & \text { Range } \\ & \text { (MeV) } \end{aligned}$ | $\begin{gathered} \overline{\mathrm{x}} \\ (\mathrm{M} \subset \mathrm{~V}) \end{gathered}$ | $\begin{gathered} \bar{W} \\ (\mathrm{MeV}) \end{gathered}$ | $\mathbf{P r}_{\mathbf{p}}$ | $\mathrm{J}^{\boldsymbol{\pi}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ${ }^{120} 0_{\text {La }}$ | - | 3 | 508 | 2.0,5.6 | 3.71(3) | 1.67(8) | - | - |
| ${ }^{122} \mathrm{La}$ | 00 | 4 | 1813 | 2.0,4.8 | 3.42(2) | 1.46(4) | - | - |
| ${ }^{124} \mathrm{Pr}$ | 00 | 3 | 493 | 2.1,7.0 | 3.73(3) | 1.68(8) | - | - |
| $126 \mathrm{Pr}{ }^{\text {b }}$ | © | 4 | 191 | 2.1,5.4 | 3.67(5) | 1.61(9) | - | -- |
| ${ }^{128} \mathrm{Pr}$ | © | 5 | 123 | 1.9,4.2 | 3.24 (4) | 1.11(9) | - | - |
| ${ }^{130} \mathrm{Pm}^{\text {c }}$ | 00 | 4 | 62 | , | (1) |  | - | - |
| ${ }^{132} \mathrm{Pm}$ | - | 5 | 286 | 2.1,5.0 | 3.60(3) | 1.26(9) | - | - |
| ${ }^{134} \mathrm{Eu}$ | 00 | 4 | 35 | 2.1,6.0 | 3.7(2) | 2.2(4) | - | - |
| ${ }^{136} \mathrm{Eu}$ | 00 | 5 | 211 | 2.4,5.7 | 3.90(5) | 1.66(9) | $9(3) \times 10^{-4}$ | (3+) |
| ${ }^{140} \mathrm{~Tb}$ | 00 | 5 | 350 | 2.0,6.6 | 4.18(4) | 1.85(9) | $7(3) \times 10^{-3}$ | (6) |
| 1428 Tb | - | 6 | 144 ${ }^{\text {d }}$ | 2.0,5.1 | -3.7 | -1.4 | (3) | $\left({ }^{+}\right)$ |
| ${ }^{142} \mathrm{Dy}$ | e | 5 | $115^{e}$ | 2.5,5.2 | -3.9 | -1.4 | - | $0^{+}$ |
| ${ }^{144} \mathrm{Dy}$ | c | 6 | 66 | 2.5,4.5 | 3.25(5) | 1.00(9) | - | $0^{+}$ |
| ${ }^{144} \mathrm{Ho}$ | - | 5 | 345f | 2.2,7.0 | 4.15(5) | 2.12(9) | - | - |
| ${ }^{146} \mathrm{Ho}$ | - | 6 | 288 | 2.3,6.3 | 4.13(4) | 1.76(9) | - | - |
| ${ }^{148} \mathrm{Ho}$ | $\infty$ | 7 | 19758 | 2.2,5.4 | 4.07(1) | 1.27(3) | $8(2) \times 10^{-4}$ | (6) |
| ${ }^{148} \mathrm{Er}$ | ¢ | 6 | - | - | - | - | - | $0^{+}$ |
| ${ }^{150} \mathrm{Tm}$ | $\infty$ | 6 | 6182 | 2.2,7.5 | 4.71(1) | 2.09(3) | 1.2(4) $\times 10^{-2}$ | $\left(1^{+}, 6^{-}\right)^{\text {h }}$ |
| ${ }^{152} \mathrm{Lu}$ | $\infty$ | 5 | 353 | 2.3,7.9 | 4.56(5) | 2.28(9) | $1.5(7) \times 10^{-1}$ | (6) |
| ${ }^{154} \mathrm{Lu}$ | O | 6 | ~15 | - | -4.3 | - | $\sim 6 \times 10^{-4}$ | (7) |

${ }^{2}$ Data taken from [Nit84].
${ }^{b}$ Data taken from [Nit83b].
c Proton energies could not be determined. See text for details.
d Proton activity is $67 \%{ }^{142}$ Dy and $33 \%{ }^{142} \mathrm{~Tb}$.
${ }^{\text {e Proton activity is }} 82 \%{ }^{142}$ Dy and $18 \%{ }^{142} \mathrm{~Tb}$.
${ }^{\mathrm{f}}$ Proton activity is $85 \%{ }^{144} \mathrm{Ho}$ and $15 \%{ }^{144}$ Dy.
8 Pioton activity is $82 \%{ }^{148} \mathrm{Ho}$ and $18 \%{ }^{148} \mathrm{Er}$.
${ }^{h}$ Relative position of high- and low-spin isomers is unknown. High-spin decay is expected to dominate and proton branching ratio is for the 6 precursor.

Table 4.4. Input parameters for statistical model calculations of even-mass precursors; $\mathrm{J}^{\boldsymbol{\pi}}=$ precursor spin and parity, QEC $=\boldsymbol{\beta}^{+}$/EC decay energy, $\mathrm{B}_{\mathrm{p}}=$ proton binding energy, Final States = references where energies, spins, and paritier of levels in the final nucleus can be found. All calculations used level density paramesers from [Di173], optical model parameters from [Bec69], average radiation widths from [Har82], and gross heory or Nilsson/RPA $\beta$-strength functions (as indicated in Figures 4.1 to 4.18).

| Isotope | J ${ }^{\text {\% }}$ | $\begin{aligned} & \mathbf{Q E C}^{\mathbf{a}} \\ & (\mathrm{MeV}) \end{aligned}$ | $\begin{gathered} \mathbf{B p}^{\mathbf{a}} \\ (\mathrm{MeV}) \end{gathered}$ | Find States |
| :---: | :---: | :---: | :---: | :---: |
| ${ }^{120} \mathrm{La}^{\text {a }}$ | 5 | 11.37 | 3.75 | [Gax78, Gar79] |
| ${ }^{122} \mathrm{La}$ | 5 | 9.99 | 4.49 | [Eks77, Gar78, Gar79] |
| ${ }^{124} \mathrm{Pr}$ | 5 | 11.76 | 3.40 | [Gen87], systematics |
| ${ }^{126} \mathrm{Pr}_{\mathrm{r}}$ | 5 | 10.43 | 4.08 | [Lei73, Gen87] |
| ${ }^{128} \mathrm{Pr}$ | 5 | 9.21 | 4.72 | [War75, Smi85, Gen87] |
| ${ }^{130} \mathrm{Pm}$ | 5 | 10.92 | 3.60 | systematics |
| ${ }^{132} \mathrm{Pm}$ | 5 | 9.75 | 4.20 | [God87] |
| ${ }^{134} \mathrm{Eu}$ | 5 | 11.44 | 3.09 | [Lis85, Wad876] |
| ${ }^{136}$ Eu | $3+$ | 10.30 | 3.67 | [Lis85, Wad87b, Wad88, Vie88a] |
| ${ }^{140} \mathrm{~Tb}$ | 6 | 10.88 | 3.18 | [Red86, Bis88] |
| ${ }^{142} \mathrm{~g}_{\mathrm{Tb}}$ | $1^{+}$ | 9.91 | 3.76 | [Lun86, Red86, Gil87, Tur81] |
| 142 Dy | $0^{+}$ | 7.13 | 0.93 | [Gi187, Tur87] |
| $1^{144}$ Dy | $0^{+}$ | 6.24 | 1.55 | [O185, Red86, Tur87] |
| ${ }^{144} \mathrm{Ho}$ | 6 | 11.48 | 2.76 | [OH185, Red86] |
| ${ }^{146} \mathrm{Ho}$ | 6 | 10.57 | 3.35 | [Alk82, Nol82b] |
| ${ }^{148} \mathrm{Ho}$ | 6 | 9.90 | 3.98 | [Nag81, Tot82, All883, Sty83, Sch84a] |
| ${ }^{148} \mathrm{Er}$ | $0^{+}$ | 7.04 | 1.21 | [ $\mathrm{No182b]}$ |
| ${ }^{150} \mathrm{Tn}_{\mathrm{s}^{\text {b }}}$ | $1^{+}, 6^{-}$ | 11.36 | 2.99 | [Wil80, Tot85] |
| ${ }^{152} \mathrm{Lu}$ | 6 | 12.75 | 2.02 | [ $\mathrm{Nol82}$ c] |

${ }^{2}$ Reference [Lir76].
${ }^{\mathrm{b}}$ The calculations shown in Fig. 4.17 are for the 6 - precursor.

Table 4.5. Energies (and approximate intensities) of $\mathrm{K} \times$ rays for lanthanide elements from Ref. [TOI78] appendix III. Energies are given in keV.

| Element | $\begin{gathered} \mathbf{K}_{\alpha 1} \\ (I-100) \end{gathered}$ | $\begin{aligned} & \mathbf{K}_{02} \\ & (\mathbf{l}-55) \end{aligned}$ | $\mathbf{K}_{\text {c,ave }}$. | $\underset{(\mathbb{1}=31)}{\mathbf{K}_{\boldsymbol{\beta} 1}}$ | $\begin{aligned} & \mathbf{K}_{\mathbf{\beta 1}} \\ & (\mathbf{I}=8) \end{aligned}$ | $\mathbf{K}_{\boldsymbol{\beta}, \mathrm{ave}}$. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Cesium | 30.97 | 30.63 | 30.85 | 35.0 | 35.8 | 35.2 |
| Barium | 32.19 | 31.82 | 32.06 | 36.4 | 37.3 | 36.6 |
| Lanthanum | 33.44 | 33.02 | 33.30 | 37.8 | 38.7 | 38.0 |
| Cerium | 34.72 | 34.28 | 34.56 | 39.2 | 40.2 | 39.5 |
| Praseodymium | 36.03 | 35.55 | 35.86 | 40.7 | 41.8 | 41.0 |
| Neodymium | 37.36 | 36.85 | 37.18 | 42.2 | 43.3 | 42.5 |
| Promethium | 38.72 | 38.17 | 38.52 | 43.8 | 44.9 | 44.1 |
| Samarium | 40.12 | 39.52 | 39.91 | 45.4 | 46.6 | 45.7 |
| Europium | 41.54 | 40.90 | 41.31 | 47.0 | 48.3 | 47.3 |
| Gadolinium | 43.00 | 42.31 | 42.75 | 48.7 | 50.0 | 49.0 |
| Terbuim | 44.48 | 43.74 | 44.21 | 50.3 | 51.7 | 50.7 |
| Dysprosium | 46.00 | 45.21 | 45.72 | 52.1 | 53.5 | 52.4 |
| Holmium | 47.55 | 46.70 | 47.24 | 53.8 | 55.3 | 54.2 |
| Erbium | 49.13 | 48.22 | 48.80 | 55.6 | 57.2 | 56.3 |
| Thulium | 50.74 | 49.77 | 50.39 | 57.5 | 59.1 | 57.8 |
| Ytterbium | 52.39 | 51.35 | 52.01 | 59.3 | 61.0 | 59.7 |
| Lutetium | 54.07 | 52.97 | 53.67 | 61.2 | 63.0 | 61.6 |

Table 4.6. Relative experimental and calculated $\beta$-delayed proton branches from 150 Tm to levels in ${ }^{149} \mathrm{Ho}$. The last column represents a mixture of $80 \% 6^{-}$decay and $20 \% 1+$ decay.

| Levels in ${ }^{149} \mathrm{Ho}$ |  | Relative Proton Branches (\%) |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{J} \pi$ | Energy (keV) | Experiment | $\begin{gathered} 150 \mathrm{Tm}\left(6^{-}\right) \\ \text {calc. } \end{gathered}$ | $\begin{gathered} 150 \mathrm{Tm}(1+) \\ \text { calc. } \end{gathered}$ | $\begin{gathered} {\left[0.8\left(6^{-}\right)+0.2\left(1^{+}\right)\right]} \\ \text {cacl. } \end{gathered}$ |
| $\begin{aligned} & 1 / 2^{+} \\ & 11 / 2^{-} \end{aligned}$ | 0 | 78(5) | 92 | 46 | 83 |
| 3/2+ | 171.5 | 7(3) | 2 | 41 | 9 |
| 5/2+ | 515.4 | 4(2) | 2 | 12 | 4 |
| 7/2+ | 952.1 | 5(2) | 2 | 1 | 2 |
| 15/2+a | $1380^{6}$ | 5(3) | 2 | -- | 1 |
| 15/2-a | $1560^{6}$ | 1(1) | 1 | -- | 1 |

${ }^{\text {a }}$ Spin and parity assignments of these levels are uncertain; the statistical model calculations are, however, not sensitive to variations of $\pm 1$ unit of angular momentum because of the small relative branches.
${ }^{\mathrm{b}}$ Reference [Wil80].




Figure 4.1. Decay of ${ }^{120} \mathrm{La}$; (a) beta-delayed proton spectrum, (b) proton coincident $x$-ray spectrum, and (c) decay of the proton activity. The smooth curves in (a) are the results of statistical model calculations using the indicated beta-strength functions.



Figure 4.2. Delayed proton spectra of (a) ${ }^{122} \mathrm{La}$, and (b) ${ }^{126} \mathrm{Pr}$ from experiments performed before the tape system was completed. The smooth curves in each figure are the results of statistical model calculations using the indicated beta-strength functions. The data were first reported in [Nit84] and [Nit83b], respectiveley.


Figure 4.3. Decay of 122 La ; (a) beta-delayed proton spectrum, (b) proton coincident $x$-ray spectrum, and (c) decay of the proton activity.


Figure 4.4. Decay of ${ }^{124} \mathrm{Pr}$; (a) beta-delayed proton spectrum, (b) proton coincident gamma-ray spectrum, (c) proton coincident x-ray spectrum, and (d) decay of the proton activity. The smooth curves in (a) are the results of statistical model calculations using the indicated beta-strength functions.


Figure 4.5. Decay of ${ }^{128} \mathrm{Pr}$; (a) beta-delayed proton spectrum, (b) proton coincident $x$-ray spectrum, and (c) decay of the proton activity. The smooth curves in (a) are the results of statistical model calculations using the indicated beta-strength functions.


Figure 4.6. Decay of ${ }^{130} \mathrm{Pm}$; (a) beta-delayed proton spectrum, (b) proton coincident $x$-ray spictrum, and (c) decay of the proton activity. The energy scale for the protons is only approximate, see text for details.


Figure 4.7. Decay of ${ }^{132} \mathrm{Pm}$; (a) beta-delayed proton spectrum, (b) proton coincident $x$-ray spectrum, and (c) decay of the proton activity. The smooth curves in (a) are the results of statistical model calculations using the indicated beta-strength functions.


Figure 4.8. Decay of ${ }^{134} \mathrm{Eu}$; (a) beta-delayed proton spectrum, (b) proton coincident $x$-ray spectrum, and (c) decay of the proton activity. The smooth curves in (a) are the results of statistical model calculations using the indicated beta-strength functions.


Figure 4.9. Decay of ${ }^{136} \mathrm{Eu}$; (a) beta-delayed protons, (b) proton coincident x rays, and (c) decay of the proton activity. The smooth curves in (a) are the results from statistical model calculations.


Figure 4.10. Decay of ${ }^{140} \mathrm{~Tb}$; (a) beta-delayed proton spectrum, (b) proton coincident $x$-ray spectrum, and (c) decay of the proton activity. The smooth curves in (a) are the results of statistical model calculations using the indicated beta-strength functions.



Figure 4.11. Decay of ${ }^{142} \mathrm{~Tb}$ (and ${ }^{142} \mathrm{Dy}$ ); (a) beta-delayed proton spectrum, (b) proton coincident $x$-ray spectrum, and (c) decay of the proton activities. The spectrum in (a) is only $\sim 33 \%{ }^{142} \mathrm{~Tb}$ decay, see text for details.


Figure 4.12. Decay of ${ }^{142}$ Dy (and ${ }^{142} \mathrm{~Tb}$ ); (a) beta-delayed proton spectrum, (b) proton coincident $x$-ray spectrum, and (c) decay of the proton activities. The smooth curves in (a) are the results of statistical model calculations for ${ }^{142}$ Dy using the indicated beta-strength functions. See text for details.


Figure 4.13. Decay of ${ }^{144} \mathrm{Dy}$; (a) beta-delayed proton spectrum, (b) proton coincident x -ray spectrum, and (c) decay of the proton activity. The smooth curves in (a) are the results of statistical model calculations using the indicated beta-strength functions.


Figure 4.14. Decay of ${ }^{144} \mathrm{Ho}$ (and ${ }^{144}$ Dy); (a) beta-delayed proton spectrum, (b) proton coincident x-ray spectrum, and (c) decay of the proton activities. The smooth curves in (a) are the combined results of statistical model calcuiations for both precursors using the indicated beta-strength functions. See text for details.


Figure 4.15. Decay of ${ }^{146} \mathrm{Ho}$; (a) beta-delayed proton spectrum, (b) proton coincident $x$-ray spectrum, and (c) decay of the proton activity. The smooth curves in (a) are the results of statistical model calculations using the indicated beta-strength functions.


Figure 4.16. Decay of ${ }^{148} \mathrm{Ho}$ (and ${ }^{148} \mathrm{Er}$ ); (a) beta-delayed proton spectrum, (b) proton coincident gamma-ray spectrum, (c) proton coincident $x$-ray spectrum, and (d) decay of the proton activities. The smooth curves in (a) are the results of statistical model caculations for ${ }^{148} \mathrm{Ho}$ using the indicated beta-strength functions (see text).


Figure 4.17. Decay of ${ }^{150} \mathrm{Tm}$; (a) beta-delayed proton spectrum, (b) proton coincident gamma-ray spectnum, (c) proton coincident x-ray spectrum, and (d) decay of the proton activity. The smooth curves in (a) are the results of statistical model calculations using the indicated beta-strength functions.


Figure 4.18. Decay of ${ }^{152} \mathrm{Lu}$; (a) beta-delayed proton spectrum, (b) proton coincident $x$-ray spectrum, and (c) decay of the proton activity. The smooth curves in (a) are the results of statistical model calculations using the indicated beta-strength functions.

## 5. ODD MASS PRECURSORS

### 5.1. GENERAL

Twenty-two precursors with odd mass numbers have been studied; 21 of the precursors were even-odd and one was odd-even. For all even-odd precursors, final state branches were determined from the intensities of proton coincident $\gamma$ rays. The reactions, calculated cross sections, detector configurations, and dates when the bombardments were performed are listed in Table 5.1.

Half-life related information for the delayed proton activities is given in Table 5.2, delayed proton information for each precursor is summarized in Table 5.3, and input parameters for statistical model calculations are given in Table 5.4. All three tables are similar to the corresponding Tables in chapter 4. The measured final state branches for precursors with $\mathrm{Z}<64$ are listed in Table 5.5 along with the calculated values from statistical model calculations. The calculations used Nilsson/RPA $\beta$ strength functions and masses from [Lir76]. Final state branches for precursors with $\mathbf{Z} 264$ are presented in Table 5.6. In even-odd isotopes in the region $Z \geq 64$ and $\mathrm{N} \leq 82,1 / 2^{+}$and $11 / 2^{-}$isomer pairs are well established [Tot87d] and calculations (using Nilsson/RPA $\mathrm{S}_{\beta}$ 's and [Lir76] masses) for these spins are also listed in Table 5.6. In most cases, a mixture of $1 / 2+$ and $11 / 2$ - precursor spins (the last column) results in much improved agreement with experiment.

The experimental results are presented in figures 5.1 though 5.20 which have a format similar to the figures in chapter 4. The delayed proton spectra are plotted from 0 to 8 MeV at 36 keV per channel in the deformed region and at 18 keV per channel for precursors near $\mathrm{N}=82$. The statistical model calculated proton spectra shown in the figures correspond to the precursor spins given in Table 5.4 (or combination of spins deduced from Table 5.6). Proton coincident $\psi$-ray spectra (with the peaks labeled by energy) are shown for most precursors. The transitions in the proton daughter nuclei associated with the $\gamma$ rays are also shown. Sum peaks in the coincident $\boldsymbol{\gamma}$-ray spectra are denoted by a $\boldsymbol{\Sigma}$.

### 5.2. DISCUSSION OF INDIVIDUAL PRECURSORS

${ }^{119} \mathrm{Ba}:$ This isotope was first identified in [Bog75] with a more complete study of its delayed proton decay reported in [Bog78a]. The data shown in Fig. 5.1
confirm the half-life and Z assignment of the earlier work and the proton coincident $\gamma$ rays indicate a precursor spin of $1 / 2^{+}$.
${ }^{123} \mathrm{Ce}$ : The discovery of this precursor was first reported in [Nit84] and is shown in Fig. 5.2. From the final state feedings in Table 5.5, a $5 / 2^{+}$precursor spin could be determined. The half-life for ${ }^{123} \mathrm{Ce}$ has been confirmed in a recent study of its $\beta$ decay [Gen87].
${ }^{125} \mathrm{Ce}$ : The identification and half-life determination of ${ }^{125} \mathrm{Ce}$ was first reported in [Bog78b] and its delayed proton branch first measured in [Nit83b]. The results of a much improved study [Wil86] are shown in Fig. 5.3 and, from Table 5.5, a precursor spin of $5 / 2^{+}$seems most likely. Preliminary results from studies of ${ }^{125}$ Ce $\beta$ decay [Gil87, Gen87] have confirmed the half-life of $9.8(8)$ s from the delayed proton studies.

127 Nd: Figure 5.4 shows the delayed proton decay of ${ }^{127} \mathrm{Nd}$ [Nit83b, Wil86]. A $\gamma$ ray of 170 keV was observed in coincidence with the protons and confirms the first $2+$ to $0^{+}$transition in ${ }^{126} \mathrm{Ce}$ [Lis85]. The final state feedings are most consistent with a low-spin ( $1 / 2^{+}$) precursor.
${ }^{129} \mathrm{Nd}$ : A $\beta$-delayed proton activity with a half-life of $5.9(6) \mathrm{s}$ at this mass was previously assigned to ${ }^{129} \mathrm{Nd}$ [Bog77] based on systematics for delayed proton emission. Subsequently, the $Z$ assignment was confirmed and proton coincident $\gamma$ rays measured in [Wil85]. The data are presented in Fig. 5.5. A comparison of the final state branches with statistical model calculations in Table 5.5 indicates that a precursor spin of $5 / 2^{+}$is the most compatible with the experiment.

A=131: Delayed protons from ${ }^{131} \mathrm{Nd}$, previously reported in [Wil86, Bog77], from a ${ }^{94}{ }^{M O}\left({ }^{40} \mathrm{Ca}, 2 \mathrm{pn}\right)$ reaction are shown in Fig. 5.6. A. 1.2(2) s delayed proton activity coincident with $\operatorname{Pm~K~x-rays,~observed~in~a~}{ }^{96} \mathrm{Ru}\left({ }^{40} \mathrm{Ca}, 2 \mathrm{p} 3 \mathrm{n}\right)$ bombardment (which also produced ${ }^{131} \mathrm{Nd}$ ), was identified as ${ }^{131} \mathrm{Sm}$ [Wi186] and is shown in Fig. 5.7. The final state feedings in Table 5.5 suggest a $5 / 2+$ spin for ${ }^{131} \mathrm{Nd}$ but ${ }^{131} \mathrm{Sm}$ shows relatively strong feeding of both the $0^{+}$and $4+$ levels in ${ }^{130} \mathrm{Nd}$. A single precursor spin cannot reproduce this feeding pattern which may indicate a low- and high-spin isomer pair in ${ }^{131} \mathrm{Sm}$. A 75\% 1/2+, 25\% 11/2precursor combination gives calculated final state branches of $36 \%\left(0^{+}\right), 41 \%\left(2^{+}\right)$, $17 \%\left(4^{+}\right)$, and $6 \%\left(6^{+}\right)$which are in much better agreement with the measured values. However, the $0^{+}$feeding, which is determined from the difference in the total number of protons and the number feeding excited states, is dependent on the subtraction of the ${ }^{131} \mathrm{Nd}$ activity to determine the proton intensity associated with ${ }^{131} \mathrm{Sm}$. A reduction in the total number of protons from ${ }^{131} \mathrm{Sm}$ would decrease the
$\mathrm{O}^{+}$branch and raise the $\mathbf{4}^{+}$and 2+ branches which would then be more consistent with a $7 / 2$ assignment. Due to this ambiguity, a spin of $5 / 2+$ for ${ }^{131} \mathrm{Sm}$ was used in the statistical model calculations shown in Fig. 5.7.
${ }^{133} \mathrm{Sm}$ : Delayed proton emission from ${ }^{133} \mathrm{Sm}$ was first reported in [Bog77] and later studied in more detail [Wil85] where proton coincident $\gamma$ rays and x rays were measured. The data are shown in Fig. 5.8. From Table 5.5, a precursor spin of $3 / 2+$ gives the best agreement with experiment but other precursor spins ( $1 / 2$ or 5/2) cannot be ruled out.
$\mathbf{1 3 5}_{5 m}$ : Delayed proton emission from ${ }^{135} \mathrm{Sm}$ was first observed in [Bog77]. The results of the present experiments are shown in Fig. 5.9. Beta-decay studies [Gil87, Vie88a] indicate a high-spin ( $\sim 11 / 2^{-}$) isomer with a half-life similar to that of the delayed protons but the final state feedings are more consistent with a lower-spin precursor such as $3 / 2$ or $5 / 2$. This discrepancy cannot be resolved with the present data and a spin of $5 / 2^{+}$was used in the statistical model results shown in Fig. 5.9.
${ }^{137} \mathrm{Gd}$ and ${ }^{139} \mathrm{Gd}$ : Both isotopes were first reported in [Nit83b] from experiments completed prior to the construction of the tape system. The precursor $\mathbf{Z}$ assignments were based on systematics and predicted cross sections; no additional studies have been performed. The proton spectra are shown in Fig. 5.10. The halflife for ${ }^{139} \mathrm{Gd}$ has been recently confirmed [Bér88] in a study of its $\beta$ decay.
$\mathrm{A}=141$ : Two delayed proton precursors, ${ }^{141} \mathrm{Gd}$ and ${ }^{141} \mathrm{Dy}$ [Nit84, Wil86], have been identified at this mass number and are shown in Figs. 5.11 and 5.12, respectively. The $\beta$ decay ${ }_{2}^{f}{ }^{141} \mathrm{Gd}$ was first studied in [Red86] and additional results have been recently reported [Tur87, Gil87]. There is an 11/2-isomer located 378 keV above the $1 / 2^{+}$ground state; both states $\beta$ decay and have similar half-lives. The delayed proton half-life is consistent with the $1 / 2^{+}$ground state value and the final state branches in Table 5.6 support the $1 / 2^{+}$precursor assignment.

The final state feedirgs for ${ }^{141}$ Dy are more consistent with a combination of $1 / 2^{+}$and $11 / 2^{-}$precursors but additional evidence of an isomer pair could not be found. The calculated proton spectra in Fig. 5.12(a) originate from a mixture of precursors with sping of $1 / 2^{+}$and $11 / 2^{-}$.

143Dy: Figure 5.13 shows the result of ${ }^{143}$ Dy [Nit83b, Nit84] delayed proton decay. The proton coincident $\gamma$ rays suffered from poor resolution and the $2^{+}$ to $0^{+}$transition at 515 keV was difficult to resolve from the 511 annihilation radiation but the final state feedings in Table 5.6 suggest a $1 / 2^{+}, 11 / 2^{-}$isomer pair. The calculated proton spectra in Fig. 5.13(a) are from a combination of $1 / 2^{+}$and 11/2-
precursors in the relative proportions that gave the best agreement with the final state feedings.

A=145: The delayed proton branch in ${ }^{145}$ Dy was first reported in [Sch84b] but coincident x and $\boldsymbol{\gamma}$ rays were not measured. This decay was reinvestigated and the results are shown in Fig. 5.14. There is an 11/2- isomer (at an excitation energy of $\sim 120 \mathrm{keV}$ ) above the $1 / 2^{+}$ground state. The final state feedings seem to indicate an equal mixture of both precursors whereas the 8 s half-life of the protons is the same as the $1 / 2^{+}$ground state half-life; a $50 \%$ admixture of an $\sim 14 \mathrm{~s} 11 / 2$ isomer [Nol82b, Alk82] would result in a proton half-life longer than 8 s . Analysis of the $\beta$-decay data is in progress and may help clear up this discrepancy.

The delayed proton precursor ${ }^{145} \mathrm{Er}$ was identified for the first time with a half-life of $\sim 0.9 \mathrm{~s}$ (see Fig. 5.15). The low production cross section made it impossible to obtain a clean ${ }^{145}$ Er proton spectrum. Even at the shortest cycle times, a significant fraction of the protons were due to ${ }^{145}$ Dy decay. The protoris spectrum in Fig. 5.15(a), obtained from a subtraction of the ${ }^{145}$ Dy contribution, should, therefore, be considered as a qualitative rather than quantitative representation of the ${ }^{145} \mathrm{Er}$ delayed proton distribution. The final state feedings suggest the delayed proton decay originates predominantly from a high-spin precursor (11/2-) but the existence of a $1 / 2^{+}$precursor cannot be ruled out.
$A=147$ : The delayed proton precursor ${ }^{147} \mathrm{Dy}(\mathrm{N}=81)$, shown in Fig. 5.16, has been the focus of many studies [Kle82, Sch84a, Sch84b, Tot84a, Tot84b, Alk86, Nit87, Sch87] because of the pronounced structure in its delayed proton spectrum. The proton spectrum is associated with the decay of the $1 / 2^{+}$ground state only and the nature of the structure will be discussed in the next chapter. Even though the assumptions of the statistical model appear to be invalid in this case, the results from such calculations are shown in Fig. 5.16(a).

A second delayed proton activity at this mass number, ${ }^{147} \mathrm{Er}$ [Sch84b, Tot87d], is shown in Fig. 5.17. From the final state feedings in Table 5.6, the 11/2isomer is the predominant precursor but there is a possible contribution from the $1 / 2^{+}$ ground state. The direct proton emission from ${ }^{147} \mathrm{Tm}$ [Kle82, Hof84, and references therein] can also be seen in Fig. 5.17(a).

A=149: The delayed proton results from a detailed study [Fir88] of ${ }^{149 \mathrm{mEr}}$ and ${ }^{149} \mathrm{gEr}$ decays are shown in Fig. 5.18. Earlier studies of this $\mathrm{N}=81$ even-odd precursor focused on the structure in the delayed proton spectrum [Sch84b, Tot84a, Tot84b] or single particle states in ${ }^{149} \mathrm{Er}$ and ${ }^{149} \mathrm{Ho}$ [Sch84a, Tot85]. Based on the observed final state feedings, about $30 \%$ of the delayed protons follow $\beta$ decay of
${ }^{149} \mathrm{~m} \operatorname{Er}\left(11 / 2-\right.$ ) with the remaining protons from ${ }^{149} \mathrm{EEr}\left(1 / 2^{+}\right)$decay. The peak-like structure in the delayed proton spectrum is associated with ${ }^{149}$ ger decay and will be discussed in the following chapter. It is impossible to experimentally separate the delayed proton spectra of ${ }^{149} \mathrm{mEr}$ and ${ }^{149 \mathrm{gEr}}$ and the calculations shown in Fig. 5.18(a) represent a mixture of both precursors.

Delayed proton emission was also observed in ${ }^{149} \mathrm{Tm}$ [Tot87c] but its protcal spectrum could not be measured due to the intense ${ }^{149} \mathrm{Er}$ activity also present.
${ }^{151 Y}$ Y: Delayed proton studies [Tot84a, Tot86] and $\beta$-decay studies [Kle85, Ako88] have been performed for this $\mathrm{N}=81$ precurscr which exhibits structure in its delayed proton spectrum [Fig. 5.19(a)] analogously to other $\mathrm{N}=81$ even-odd precursors. In [Tot86] it was shown that the delayed proton spectrum is composed of a structureless component associated with the $11 / 2$ - isomer and a structured component due to the $1 / 2^{+}$ground state decay. This structure in $\mathrm{N}=81$ precursors will be discussed in the next chapter.
${ }^{153 Y} \mathrm{Y}$ : A thoreugh report on the delayed proton branch in this isotope can be found in [Wil88] and the data are shown in Fig. 5.20 and Table 5.7.

Table 5.1. Reactions used to produce odd-mass delayed proton precursors; Thickness $=$ target thickness, EHILAC = beam energy at machine exit, ETarget = calculated beam energy at target center, $\sigma=$ calculated cross section, Detectors $=$ detector configuration used.

| Isotope | Reaction | $\begin{aligned} & \text { Thickness } \\ & \text { (mg/cmin) } \end{aligned}$ | $\begin{aligned} & \mathrm{E}_{\mathrm{HOLAC}} \\ & (\mathrm{MeV}) \end{aligned}$ | ETarget ( MeV ) | $\begin{gathered} \boldsymbol{\sigma}^{\mathbf{a}} \\ (\mathrm{mb}) \end{gathered}$ | Date ${ }^{\text {b }}$ | Devectiors |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ${ }^{119} \mathrm{Ba}$ | $\left.{ }^{58} \mathrm{Ni}^{(64} \mathrm{Z}_{\mathrm{n}, 2 \mathrm{pma}}\right)$ | 2 | 380 | 253 | 40 | 9/83 | A |
| ${ }^{123} \mathrm{Ce}$ | $\left.{ }^{92} \mathrm{Mc}^{36} \mathrm{Ar}, 2 \mathrm{p} 3 \mathrm{n}\right)$ | 2 | 196 | 188 | 3 | 9183 | A |
| ${ }^{125} \mathrm{Ce}$ | ${ }^{92} \mathrm{Mo}\left({ }^{36} \mathrm{Ar}, 2 \mathrm{pn}\right)$ | 2 | 165 | 153 | 80 | 4186 | B |
| ${ }^{127}$ Nd | ${ }^{92} \mathrm{Mo}\left({ }^{40} \mathrm{Ca}, 2 \mathrm{p} 3 \mathrm{n}\right)$ | 2 | 223 | 208 | 1.5 | $2 / 85$ | B |
| ${ }^{129} \mathrm{Nd}$ | ${ }^{92} \mathrm{Mo}\left({ }^{40} \mathrm{Ca}, 2 \mathrm{pn}\right)$ | 2 | 182 | 170 | 40 | $7 / 84$ | A |
| ${ }^{129} \mathrm{Nd}$ | ${ }^{92} \mathrm{Mo}\left({ }^{40} \mathrm{Ca}, 2 \mathrm{pn}\right)$ | 2 | 184 | 172 | 40 | 10184 | A |
| ${ }^{131}$ Sm | ${ }^{96} \mathrm{Ru}\left({ }^{40} \mathrm{Ca}, 2 \mathrm{p} 3 \mathrm{n}\right)$ | 0.6 | 288 | 208 | 0.6 | $2 / 85$ | B |
| ${ }^{131} \mathrm{Nd}$ | ${ }^{96} \mathrm{Ru}\left({ }^{40} \mathrm{Ca}, 4 \mathrm{pn}\right)$ | 0.6 | 288 | 208 | 80 | 2885 | B |
| ${ }^{131} \mathrm{Nd}$ | ${ }^{54} \mathrm{Mo}\left({ }^{40} \mathrm{Ca}, 2 \mathrm{pn}\right)$ | 2 | 180 | 168 | 60 | $2 / 85$ | B |
| ${ }^{133}$ Sm | ${ }^{96} \mathrm{Ru}\left({ }^{40} \mathrm{Ca}, 2 \mathrm{pn}\right)$ | 0.8 | 195 | 175 | 30 | 10884 | A |
| ${ }^{135}$ Sm | ${ }^{92} \mathrm{Mo}\left({ }^{46} \mathrm{Ti}, 2 \mathrm{pn}\right)$ | 2 | 204 | 192 | 80 | 11/86 | C |
| ${ }^{141} \mathrm{D}$ | ${ }^{92} \mathrm{Mo}\left({ }^{54} \mathrm{Fe}, 2 \mathrm{p} 3 \mathrm{n}\right)$ | 2 | 292 | 276 | 0.7 | 10:83 | A |
| 1419 | ${ }^{92} \mathrm{Mo}\left({ }^{54} \mathrm{Fe}, 4 \mathrm{pn}\right)$ | 2 | 292 | 276 | 62 | $10 \times 83$ | A |
| $14 . \mathrm{Dy}$ | ${ }^{92} \mathrm{Mo}\left({ }^{54} \mathrm{Fe}, 2 \mathrm{p} 3 \mathrm{n}\right)$ | 2 | 291 | 276 | 0.7 | 286 | B |
| ${ }^{141} \mathrm{Gd}$ | ${ }^{92} \mathrm{Mo}\left({ }^{54} \mathrm{Fe}, 4 \mathrm{pn}\right)$ | 2 | 291 | 276 | 62 | 2186 | B |
| ${ }^{141}$ Gd | ${ }^{92} \mathrm{Mo}\left({ }^{52} \mathrm{Cr}, 2 \mathrm{pn}\right)$ | - | 224 | 210 | 100 | 2187 | C |
| ${ }^{143} \mathrm{Dy}$ | ${ }^{92} \mathrm{Mo}\left({ }^{56} \mathrm{Fe}, 2 \mathrm{p} 3 \mathrm{n}\right)$ | 2 | 290 | 275 | 4 | 10183 | A |
| ${ }^{145} \mathrm{Er}$ | ${ }^{92} \mathrm{Mo}\left({ }^{58} \mathrm{Ni}, 2 \mathrm{p} 3 \mathrm{n}\right)$ | 2 | 325 | 297 | 0.2 | 3/88 | C |
| 145 Dy | ${ }^{92} \mathrm{Mo}\left({ }^{58} \mathrm{Ni}, 4 \mathrm{pn}\right)$ | 2 | 310 | 283 | 58 | 3/88 | C |
| ${ }^{147}{ }^{\text {Er }}$ | ${ }^{92} \mathrm{Mo}\left({ }^{58} \mathrm{Ni}, 2 \mathrm{pn}\right)$ | 2 | 261 | 245 | 18 | 4/87 | C |
| ${ }^{147}$ Dy | ${ }^{92} \mathrm{Mo}\left({ }^{58} \mathrm{Ni}, \mathrm{xpyn}\right)^{\text {d }}$ | 2 | 261 | 245 | 100 | $4 / 87$ | C |
| 187 Dy | ${ }^{3} \mathrm{Nb}\left({ }^{58} \mathrm{Ni}, 3 \mathrm{pn}\right)$ | 2 | 268 | 250 | 100 | 10886 | C |
| 149 Tm | ${ }^{94} \mathrm{Mo}\left({ }^{58} \mathrm{Ni}, \mathrm{p} 2 \mathrm{n}\right)$ | 2 | 259 | 242 | 1.5 | 1086 | C |
| ${ }^{149} \mathrm{Er}$ | ${ }^{94} \mathrm{Mo}\left({ }^{58} \mathrm{Ni}, 2 \mathrm{pr}\right)$ | 2 | 259 | 242 | 38 | 10186 | C |
| ${ }^{149} \mathrm{Er}$ | ${ }^{94} \mathrm{Mo}\left({ }^{58} \mathrm{Ni}, 2 \mathrm{pn}\right)$ | 2 | 278 | 262 | 5 | 11/84 | A |
| ${ }^{151} \mathrm{Yb}$ | ${ }^{96} \mathrm{Ru}\left({ }^{58} \mathrm{Ni}, 2 \mathrm{pn}\right)$ | 0.8 | 275 | 248 | 8.5 | 11/84 | A |
| ${ }^{151} \mathrm{Yb}$ | ${ }^{96} \mathrm{Ru}\left({ }^{58} \mathrm{Ni}, 2 \mathrm{pn}\right)$ | 1.5 | 360 | 250 | 8.5 | $4 / 85$ | B |
| ${ }^{153} \mathrm{Yb}$ | ${ }^{92} \mathrm{Mo}\left({ }^{64} \mathrm{Zn}, 2 . \mathrm{nn}\right)$ | 2 | 285 | 267 | 45 | 12/87 | C |

${ }^{2}$ Calculated from [Win72].
${ }^{\mathrm{b}}$ To indicate when more than one experimment was performed at a given isobaric chain and to correlate with eizinies in Table 5.2.
${ }^{\mathbf{c}}$ The symbols $A, B$, and $C$ refer to the detector configurations shown in Figure 3.3.
${ }^{d}$ Not produced directly. The cross section is the sum of all 3-particle reaction channels.

Table 5.2. Half-lives of odd-mass delayed proton precwrsors; Transit Tine = tupe trasport dime, Cycle Time $=$ lengh of collection and counaing inerval, No. of Events = number of defayed protons
 the gross theory of $\beta$ decay, T $_{1 / 2}$ RPA $=$ half-life from Nilscon/RPA $\beta$-strength function calculations.

| Isotope | Date | Trassit <br> Time (s) | Cycle <br> Time (s) ${ }^{1}$ | No. of Events | $\begin{gathered} \mathrm{T}_{1 / 2} \\ \text { Exp. }{ }^{\mathrm{b}}(\mathrm{~s}) \end{gathered}$ | $\begin{aligned} & T_{1 / 2} \\ & e_{2 . c^{c}(s)} \end{aligned}$ | $\begin{gathered} \mathrm{T}_{1 / 2} \\ \operatorname{RPA}^{\mathrm{d}}(\mathrm{~s}) \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ${ }^{119} \mathrm{Ba}$ | 9/83 | 0.07 | 10,50 | 14255,1263 | 6.0(3) | 7.3 | 8.3 |
| ${ }^{123} \mathrm{Ce}$ | 9/83 | 0.07 | 10 | 2611 | 3.8(2) | 4.6 | 1.9 |
| ${ }^{125} \mathrm{Ce}$ | 4/86 | 0.25 | 16 | 5487 | 9.8(8) | 13.9 | 10.2 |
| ${ }^{127}{ }^{\text {Nd }}$ | $2 / 85$ | 0.25 | 6 | 302 | 1.8(4) | 3.0 | 1.7 |
| ${ }^{129} \mathrm{Nd}$ | 10184 | 0.25 | 12 | 1915 | 4.9(3) | 8.3 | 6.8 |
| ${ }^{131}{ }^{\text {Nd }}$ d | $2 / 85$ | 0.25 | 24 | $2167{ }^{\text {c }}$ | 25(5) | 25.2 | 18.5 |
| ${ }^{131}$ Sm | 2885 | 0.25 | 6 | 849 | 1.2(2) | 1.9 | 1.6 |
| ${ }^{133} \mathrm{Sm}$ | 10184 | 0.25 | 8 | 838 | 2.8(5) | 5.5 | 3.5 |
| ${ }^{135}$ Sm | 11/86 | 0.07 | 16.40 | 475,148 | 10(2) | 13.0 | 5.6 |
| ${ }^{137} \mathrm{Gd}^{\text {f }}$ | $12 / 82$ | -- | - | 358 | 7(3) | 3.1 | 1.2 |
| ${ }^{139}$ Gdf | $12 / 82$ | -- | - | 315 | 5(1) | 7.5 | 4.5 |
| 1418Gd | 2187 | 0.07 | 128 | 426 | 23(3) | 15.6 | 16.3 |
| ${ }^{141} \mathrm{Dy}$ | 286 | 0.25 | 24,4 | 790e, 1180 | 0.8(2) | 1.8 | 1.4 |
| ${ }^{143} \mathrm{Dy}$ | 10883 | 0.07 | 10 | 1486 | 3.1(3) | 4.1 | 2.9 |
| 145 mbDy | 3/88 | 0.07 | 16,40 | 2251,673 | B(1) | 7.6 | 11.2 |
| ${ }^{145} \mathrm{Er}$ | 3/88 | 0.07 | 1.6,4 | 1570¢, $1223{ }^{\text {e }}$ | $0.9(3)$ | 1.2 | 0.7 |
| $1478^{\text {dy }}$ | 10186 | 0.25 | 160 | 4699 | -406 | 22.5 | 32.9 |
| 147 mbEr | $4 / 87$ | 0.07 | 1.28,4 | 3001,6817 | 2.6.2) | 2.2 | 2.5 |
| 149 msEr | 10186 | 0.25 | 4,16 | 20990,9912 | 8.8(5) | 4.8 | 3.2 |
| ${ }^{149} \mathrm{Tm}$ | 10886 | 0.25 | 4 | 2099 e | 0.9(2) ${ }^{\text {h }}$ | 1.6 | 0.9 |
| 151meYb | 4/85 | 0.25 | 4 | 5745 | 1.6 (1) | 1.2 | 0.9 |
| ${ }^{153} \mathrm{Yb}$ | 12887 | 0.07 | 1.28,12.8 | 295,506 | 3.9(5) | 13.6 | 8.9 |

[^1]Table 53. Summary of the delayed proton decay of odd-mass precursors; Type $=$ type of precursor: even-odd (eo) or odd-even (oe), $\mathrm{T}_{\mathbf{z}}=1 / 2(\mathrm{~N}-\mathrm{Z})$ precursor isospin projection, No. of Events $=$ number of protons shown in Figures 5.1(a) to 5.20(a), Range $=$ approximate lowest and highest observed proton energies, $\bar{x}=$ average proton energy, $\bar{w}=F W H M$ of proton distribution, $P_{P}=$ measured proton branching ratio, $\mathrm{J}^{\pi}$ Exp. $=$ deduced precursor spin and parity, $\mathrm{J}^{\pi}$ Calc. $=$ predicted precursor spin and parity from [See75]

| Isotope | Type | $\mathrm{T}_{2}$ | Ne. of Events | Range (MeV) | $\underset{(\mathrm{MeV})}{\overline{\mathrm{M}}}$ | $\begin{gathered} \overline{\mathbf{w}} \\ (\mathrm{MeV}) \end{gathered}$ | $\mathbf{P}_{\mathbf{p}}$ | $\begin{gathered} \mathrm{J} \pi \\ \text { Exp. } \end{gathered}$ | $\begin{gathered} \mathrm{J}^{\pi} \\ \text { Calc. } \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ${ }^{119} \mathrm{Ba}$ | eo | $7 / 2$ | 15526 | 1.9,5.6 | 3.43(1) | 1.55(1) | - | $\left(1 / 2^{+}\right)$ | $3 / 2^{+}$ |
| ${ }^{123} \mathrm{Ce}$ | $\infty$ | 7/2 | 2611 | 2.0,6.2 | 3.61(1) | 1.66 (3) | - | ( $5 / 2{ }^{+}$) | $5 / 2^{+}$ |
| ${ }^{125} \mathrm{Ce}$ | $\infty$ | 9/2 | 5487 | 1.8,4.8 | 3.33(1) | 1.28(2) | - | (5/2+) | $1 / 2^{+}$ |
| 127 Nd | $\infty$ | $7 / 2$ | 302 | 2.2,15.0 | 3.66(4) | 1.78(9) | - | - | $1 / 2^{+}$ |
| 129 Nd | ¢ | $9 / 2$ | 1916 | 1.9,5.5 | 3.66(2) | 1.51(4) | - | $\left(5 / 2^{+}\right)$ | $5 / 2^{+}$ |
| ${ }^{131}$ Nd | $\infty$ | 11/2 | 2167 | 1.8,4.2 | 3.13(1) | 1.04(2) | - | (5/2+) | $5 / 2^{+}$ |
| ${ }^{131} \mathrm{Sm}^{\text {a }}$ | $\infty$ | $7 / 2$ | 673 | 2.0,6.5 | 3.85(3) | 1.81(7) | - | - | $7 / 2^{-}$ |
| ${ }^{133} \mathrm{Sm}$ | eo | $9 / 2$ | 836 | 2.0,6.2 | 3.77(j) | 1.80 (6) | - | - | $5 / 2^{+}$ |
| ${ }^{135} 5 \mathrm{Sm}$ | eo | 11/2 | 623 | 1.8,5.1 | 3.54(2) | 1.366 ) | $2(1) \times 10^{-4}$ | - | 9/2- |
| ${ }^{137} \mathrm{Gd}^{\text {b }}$ | co | 912 | 358 | 2.2,6.7 | 3.83(5) | 2.16(9) | - | - | 9/2* |
| ${ }^{139} \mathrm{Gd}^{\text {b }}$ | Co | 11/2 | 313 | 1.8,6.0 | 3.80(5) | 1.86(9) | - | - | 7/2+ |
| 141 gGd | Co | 13/2 | 433 | 1.8,4.8 | 3.52(3) | 1.26 (6) | $3(1) \times 10^{-4}$ | (122) | $3 / 2^{-}$ |
| ${ }^{141} \mathrm{Dyc}$ | e0 | $9 / 2$ | 790 | 2.3,7.1 | 4.14(3) | 1.90(7) | - | - | $7 / 2^{+}$ |
| ${ }^{143} \mathrm{Dy}$ | co | 11/2 | 1487 | 2,2,6,8 | 4.17(2) | 1.86(5) | - | - | $3 / 2^{+}$ |
| 145 gDy |  |  |  |  |  |  | - | (1/2+) | 3/2+ |
| 145 mby | 0 | 13/2 | 2923 | 1.8,6.0 | 3.99(1) | 1.69(3) |  | (11/2) | - |
| ${ }^{145} \mathrm{Er}^{\text {d }}$ | $\infty$ | $9 / 2$ | 839 | 2.5,7.6 | 4.34(3) | 2.00(7) |  | - | 3/2 |
| 147 gDy | Co | 15/2 | 4699 | 2.0,4.4 | 3.50(1) | 1.03(2) | $2(1) \times 10^{-3}$ | $1 / 2^{+}$ | 11/2- |
| 147 gEre |  |  |  |  |  |  | -- | (1/2+) | 1/2- |
| 147 mer | $\infty$ | 11/2 | 5899 | 2.2,7.9 | 4.32((1) | 1.96(3) | - | (11/2) |  |
| ${ }^{149} \mathrm{~g} \mathrm{Er}$ |  |  |  |  |  |  | $7(2) \times 10^{-2}$ | $1 / 2^{+}$ | 11/2- |
| 149 mer | $\infty$ | 13/2 | 9912 | 2.0,7.3 | 4.28(1) | 1.87(2) | $1.8(7) \times 10^{-3}$ | 11/2- | - |
| ${ }^{149} \mathrm{Tm}$ | - | 9/2 | - | - | - | - | - | (11/2) | 11/2- |
| ${ }^{151 g Y b}$ |  |  |  |  |  |  |  | $1 / 2^{+}$ | 11/2- |
| ${ }^{151 m Y}$ | ¢0 | 11/2 | 5745 | 2.2,7.8 | 4.52(1) | 1.92(3) |  | 11/2- | - |
| ${ }^{153} \mathrm{Yb}$ | Co | 13/2 | 801 | 2.1,5.8 | 3.88(2) | 1.53(5) | $8(2) \times 10^{-5}$ | 7/2 | 712 |

${ }^{2}$ Contribution from ${ }^{131}$ Nd decay was subtracted.
${ }^{6}$ Data taken from [Nit83b].
${ }^{c}$ Proton spectrum contains less than $12 \%{ }^{141} \mathrm{Gd}$ decay.
${ }^{\text {d }}$ Conrribution from ${ }^{145}$ Dy decay was subtracted.
${ }^{e}$ Contribution from ${ }^{147}$ Dy decay was subtracted.

Table 5.4. Input parameters for statistical model calculations of odd-mass precursors; $\mathrm{J}^{\pi}=$ precursor spin and parity, QEC $=\beta^{+} / \mathrm{EC}$ decay energy, $\mathrm{B}_{\mathrm{p}}=$ proton binding energy, Final Sumes $=$ references where energies, spins, and parities of levels in the final nucleus can be found. All calculations used level density parameters from [Dil73], optical model parameters from [Bec69], iverage radiation widths from [Har82], and gross theary or Nilsson/RPA $\beta$-strength functions (as indiczted in Figures 5.1 to 5.20 ).

| Isotope | $\mathrm{j}^{\boldsymbol{\pi}}$ | $\begin{gathered} \mathrm{O}_{\mathrm{EC}}{ }^{\mathrm{a}} \\ (\mathrm{MeV}) \end{gathered}$ | $\begin{array}{r} \mathrm{B}_{\mathrm{p}} \mathbf{a}^{( } \\ (\mathrm{MeV}) \end{array}$ | Final Stutes |
| :---: | :---: | :---: | :---: | :---: |
| ${ }^{119} \mathrm{Ba}$ | 12+ | 8.05 | 1.69 | [Cien77, Kersi] |
| ${ }^{123} \mathrm{Ce}$ | $5 / 2^{+}$ | 8.53 | 1.47 | [Con74, Gen87] |
| ${ }^{125} \mathrm{Ce}$ | $5 / 2^{+}$ | 7.27 | 2.20 | [Con74, Gil87, Mar87] |
| ${ }^{127}$ Nd | 1/2+ | 9.05 | 1.13 | [Lis85] |
| ${ }^{129} \mathrm{Nd}$ | $5 / 2^{+}$ | 7.83 | 1.80 | [Wa75] |
| ${ }^{131} \mathrm{Nd}$ | 5/2+ | 6.71 | 2.43 | [Kor87, Tod84] |
| ${ }^{131} \mathrm{Sm}$ | 5/2+ | 9.60 | 0.72 | [Lis85] |
| ${ }^{133} \mathrm{Sm}$ | $3 / 2^{+}$ | 8.43 | 1.35 | [Lis85, Mak86, Ber87, Ker87b, Kor87, Wad87b, Wad88] |
| ${ }^{135}{ }_{\text {S }}$ m | 5/2+ | 7.35 | 1.96 | [Ber87, Bil87, Ker87b, Kor87, Pau87, Wad8\%, Vie88, Wad88] |
| ${ }^{137}$ Gd | $5 / 2^{+}$ | 9.04 | 0.91 | [Lit85, Mer86, Ber87, Ker87a, Ker87b, Wad87b, Vie88a] |
| ${ }^{139} \mathrm{Gd}$ | $5 / 2^{+}$ | 8.01 | 1.51 | [Cha85, Lis85, Mak86, Resióa, Bér87, Ker87b, Pau87] |
| 141 gGd | 1/2+ | 7.08 | 2.12 | [Mar76, Ker87a, Ker87b, St287] |
| $141^{\text {Dy }}$ | 1/2+,11/2- | 9.65 | 0.50 | [Lis85, Bis88] |
| ${ }^{143} \mathrm{Dy}$ | 1/2+,11/2- | 8.68 | 1.12 | [Lun86, Gil87, Goes7, Sta87] |
| 145 Dy | 1/2+,11/2 | 7.81 | 1.74 | [ $\mathrm{NoL82b}$, Lac84, Red86] |
| ${ }^{145} \mathrm{Er}$ | $1 / 2^{+}, 11 / 2^{-}$ | 10.29 | 0.16 | [Goe87] |
| ${ }^{147} 7_{\text {g }} \mathrm{Py}$ | $1 / 2^{+}$ | 6.55 ${ }^{\text {b }}$ | $2.08{ }^{\text {b }}$ | [Jul80] |
| ${ }^{147} \mathrm{Er}$ | $1 / 2^{+}, 11 / 2^{-}$ | 9.39 | 0.79 | [Gui82] |
| ${ }^{149}{ }^{\text {E }}$ Er | $1 / 2^{+}$ | $8.40{ }^{\text {c }}$ | $1.40^{\text {c }}$ | [Dal78, Tot88] |
| ${ }^{149} \mathrm{~mm}_{\mathrm{Er}}$ | 11/2- | $9.10^{\text {c }}$ | $1.40{ }^{\text {c }}$ | [Da178, Tor88] |
| ${ }^{149} \mathrm{Tm}$ | 11/2- | 9.76 | 2.58 | [Bro84] |
| 151 gYb | 1/2+ | 10.11 | 0.39 | [Nol82a, Nol82b] |
| ${ }^{151 m Y}$ | 11/2- | $10.86^{\text {d }}$ | 0.39 | [ $\mathrm{Nol822}, \mathrm{Nol82b]}$ |
| ${ }^{153} \mathrm{Yb}$ | 7/2 | 6.91 | 0.94 | [Hor81, No182c, Tot87a] |

${ }^{2}$ Reference [Lir76].
${ }^{6}$ Reference [Wap87].
${ }^{c}$ Reference [Fir88].
disomer assumed to be $\sim 750 \mathrm{keV}$ above ground.

Table 5.5. Comparison of experimental and calculated proton final state branches; Precursor $\rightarrow$ Daughter $=$ delayed prown precursor and prowon dengher, $\mathrm{J}^{\pi}=$ spin and parity of level in procon daughter, Energy = excitation energy of level in proton daughter, Exp. = measured branch to level in proton daughter, and calculated branches for various precursor spins.

| Precursar <br> $\rightarrow$ Daughter | $\mathbf{J}^{\boldsymbol{\pi}}$ | $\begin{aligned} & \text { Energy } \\ & \text { (keV) } \end{aligned}$ | Exp. <br> (\%) | $\begin{aligned} & 1 / 2^{+} \\ & \text {calc. } \end{aligned}$ | $\begin{aligned} & 3 / 2^{+} \\ & \text {calc. } \end{aligned}$ | $\begin{aligned} & 5 / 2^{+} \\ & \text {calc. } \end{aligned}$ | $\begin{aligned} & 7 / 2^{+} \\ & \text {calc. } \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & { }^{119} \mathrm{Ba} \\ & \rightarrow{ }^{118} \mathrm{Xe} \end{aligned}$ | $0^{+}$ | 0 | 71(10) | 60 | 46 | 21 | - |
|  | $2+$ | 337 | $29(5)$ | 33 | 45 | 60 | - |
|  | 4+ | 810 | 1(1) | 1 | 1 | 9 | - |
| $\begin{aligned} & { }^{123} \mathrm{Ce} \\ & \rightarrow{ }^{122} \mathrm{Ba} \end{aligned}$ | $0^{+}$ | 0 | 23(6) | - | 37 | 14 | 9 |
|  | $2+$ | 197 | 66(6) | - | 55 | 66 | 54 |
|  | $4^{+}$ | 570 | $9(3)$ | - | 3 | 14 | 32 |
|  | $6^{+}$ | 1083 | 2(1) | - | - | - | 1 |
| $\begin{aligned} & { }^{125} \mathrm{Ce} \\ & \rightarrow{ }^{124_{\mathrm{Ba}}} \end{aligned}$ | $0^{+}$ | 0 | 36(4) | - | 49 | 20 | 14 |
|  | $2^{+}$ | 197 | 53(4) | _ | 50 | 72 | 65 |
|  | $4^{+}$ | 570 | 9(3) | - | 1 | 8 | 21 |
|  | $6^{+}$ | 1228 | 1(1) | - | - | - | - |
| $\begin{aligned} & { }^{127} \mathrm{Nd} \\ & \rightarrow{ }^{126} \mathrm{Ce} \end{aligned}$ | $0^{+}$ | 0 | 60(15) | 50 | 37 | 14 | - |
|  | $2^{+}$ | 170 | $35(13)$ | 48 | 60 | 70 | - |
|  | $4+$ | $520$ | $5(5)$ | $2$ | $3$ | 16 | - |
| $\begin{aligned} & { }^{129} \mathrm{Nd} \\ & \rightarrow{ }^{128} \mathrm{Ce} \end{aligned}$ | $0^{+}$ | 0 | 23(7) | - | 44 | 17 | 12 |
|  | $2+$ | 207 | 68(7) | - | 54 | 71 | 61 |
|  | 4+ | 607 | $9(3)$ | - | 2 | 12 | 27 |
| $\begin{aligned} & { }^{131} \mathrm{Nd} \\ & \rightarrow{ }^{130} \mathrm{Ce} \end{aligned}$ | $0^{+}$ | 0 | 32(7) | - | 57 | 26 | 20 |
|  | $2^{+}$ | 254 | $67(7)$ | - | 41 | 68 | 67 |
|  | $4^{+}$ | 710 | 1(1) | - | 1 | 4 | 11 |
| $\begin{gathered} { }^{131} \mathrm{Sm}^{130} \mathrm{Nd} \end{gathered}$ | $0^{+}$ | 0 | 41(15) | 47 | 35 | 13 | 7 |
|  | $2+$ | 158 | 36(15) | 51 | 61 | 68 | 52 |
|  | $4^{+}$ | 483 | 21(8) | 2 | 4 | 19 | 39 |
|  | $6^{+}$ | 938 | 3(3) | - | - | 1 | 2 |
| $\begin{aligned} & { }^{133} \mathrm{Sm} \\ & \rightarrow{ }^{132} \mathrm{Nd} \end{aligned}$ | $0^{+}$ | 0 | 35(9) | 56 | 43 | 18 | - |
|  | $2^{+}$ | 213 | 63(9) | 43 | 54 | 70 | - |
|  | $4^{+}$ | 611 | 1(1) | 1 | 3 | 12 | - |
| $\begin{aligned} & { }^{135} \mathrm{Sm} \\ & \rightarrow{ }^{134} \mathrm{Nd} \end{aligned}$ | $0^{+}$ | 0 | 42(13) | 64 | 52 | 24 | - |
|  | $2+$ | 294 | 41(14) | 31 | 41 | 61 | - |
|  | $2^{+}$ | 754 | 10(6) | 4 | 6 | 8 | - |
|  | $4^{+}$ | 789 | 7(5) | - | 1 | 5 | - |

Table 5.6. CTaratison of experimental aod calculmed proton final state branches; Precursor $\rightarrow$ Daughter = delayed proton precursor and proton denghter, $\mathrm{J}^{\pi}=$ spin and perity of level in proton deughter, Energy $=$ excitation energy of the level, Exp. $=$ measured branch to the level, $1 / 2^{+}$calc. $=$ calculated final state branches for a $1 / 2^{+}$precursor, $11 / 2$ calc. = caclulwed final stane branches for \&n $11 / 2^{-}$precursor, Mixing = fractions (in percenc) of $1 / 2^{+}$and $11 / 2^{-}$proton invensities that give improved finai state branches, and Total calc. $=$ combined calculaied final stane branches.

| Precursor <br> $\rightarrow$ Daughter | $\mathrm{J}^{\pi}$ | Energy <br> (keV) | Exp. <br> (\%) | $\begin{gathered} 1 / 2^{+} \\ \text {cak.( }(\%) \end{gathered}$ | $\begin{gathered} 11 / 2^{-} \\ \text {calc. (\%) } \end{gathered}$ | Mixing (\%) | $\begin{aligned} & \text { Total } \\ & \text { calc. (\%) } \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & { }^{181} \mathrm{Fd} \\ & \rightarrow{ }^{140} \mathrm{Sm} \end{aligned}$ | $0^{+}$ | 0 | 79(11) | 87 | 8 | 1000 | 87 |
|  | $2^{+}$ | 530 | 21(10) | 12 | 66 |  | 12 |
|  | $4^{+}$ | 1246 | -- | - | 6 |  | - |
| $\begin{aligned} & { }^{141} \mathrm{Dy} \\ & \rightarrow^{140} \mathrm{Gd} \end{aligned}$ | $0^{+}$ | 0 | 32(12) | 60 | 1 | $57 / 43$ | 34 |
|  | $2^{+}$ | 329 | 42(15) | 39 | 26 |  | 34 |
|  | $4^{+}$ | 837 | 26(10) | 1 | 61 |  | 27 |
|  | $6^{+}$ | 1465 | - | - | 12 |  | 5 |
| $\begin{aligned} & { }^{143} \mathrm{Dy} \\ & \rightarrow{ }^{142} \mathrm{Gd} \end{aligned}$ | $0^{+}$ | 0 | 24(10) | 76 | 3 | 26774 | 22 |
|  | $2+$ | 515 | 34(12) | 20 | 42 |  | 36 |
|  | $2+$ | 980 | 11(3) | 4 | 7 |  | 6 |
|  | $4^{+}$ | 1209 | 31(7) | - | 42 |  | 31 |
|  | $6+$ | 1964 | - | - | 4 |  | 3 |
| $\begin{aligned} & { }^{145} \mathrm{Dy} \\ & \rightarrow{ }^{144} \mathrm{Gd} \end{aligned}$ | $0^{+}$ | 0 | 56(8) | 91 | 14 | 50150 | 53 |
|  | 2+ | 743 | 44(8) | 9 | 71 |  | 40 |
|  | $4^{+}$ | 1745 | $<2$ | - | 11 |  | 5 |
| $\begin{aligned} & 145 \mathrm{Er} \\ & \rightarrow{ }^{144} \mathrm{Dy} \end{aligned}$ | $0^{+}$ | 0 | 17(14) | 67 | 2 | 20180 | 15 |
|  | $2+$ | 493 | 38(18) | 33 | 38 |  | 37 |
|  | $4^{+}$ | 1165 | 44(12) | - | 53 |  | 43 |
|  | $6+$ | 1916 | - | - | 7 |  | 5 |
| $\begin{aligned} & 147 \mathrm{Er} \\ & \rightarrow{ }^{146} \mathrm{Dy} \end{aligned}$ | $0^{+}$ | 0 | 19(6) | 81 | 6 | 15/85 | 17 |
|  | $2^{+}$ | 683 | 54(7) | 19 | 57 |  | 52 |
|  | $4^{+}$ | 1608 | 27(4) | - | 30 |  | 25 |
|  | 3- | 1783 | $<2$ | - | 3 |  | 3 |
|  | 5 | 2283 | $<2$ | - | 3 |  | 2 |
| $\begin{aligned} & { }^{149} \mathrm{Er} \\ & \rightarrow{ }^{148} \mathrm{Dy} \end{aligned}$ | $0^{+}$ | 0 | 71(5) | 99 | 24 | 70130 | 76 |
|  | $2^{+}$ | 1678 | 4(3) | 1 | 11 |  | 4 |
|  | 3 | 1688 | $9(5)$ | - | 31 |  | 9 |
|  | 5 | 2349 | 5(3) | - | 15 |  | 5 |
|  | $4+$ | 2428 | 7(2) | - | 10 |  | 3 |
|  | $6^{+}$ | 2732 | 2(1) | - | 6 |  | 2 |

Table 5.6. (Concinued).

| Precursor/ <br> $\rightarrow$ Daughter | $\mathrm{J}^{\pi}$ | Energy <br> (keV) | Exp. <br> (\%) | $1 / 2^{+}$ <br> calc.(\%) | $11 / 2^{-}$ <br> calc. (\%) | Mixing <br> (\%) | Total <br> calc.(\%) |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ${ }^{151 \mathrm{Yb}}$ | $0^{+}$ | 0 | $51(5)$ | 95 | 5 | 50150 | 51 |
| $\rightarrow{ }^{150} \mathrm{Er}$ | $2^{+}$ | 1579 | $14(3)$ | 3 | 10 |  | 7 |
|  | $3^{-}$ | 1786 | $10(1)$ | 2 | 14 |  | 8 |
|  | $5-$ | 2261 | $9(3)$ | - | 18 |  | 9 |
|  | $4^{+}$ | 2295 | $11(3)$ | - | 25 |  | 13 |
|  | $6^{+}$ | 2621 | $5(2)$ | - | 19 |  | 9 |

Table 5.7. Experimental and calculated $\beta$-delayed proton branches from ${ }^{153} \mathrm{Yb}$ to levels in ${ }^{152} \mathrm{Er}$. The precursor spin was assumed to be $7 / 2^{-}$and calculations for three different forms of $S_{\beta}$ are listed.

| Levels in ${ }^{152} \mathrm{Er}$ |  | Final State Branches (\%) |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{J} \pi$ | Energy (keV) | Experiment | Gross Theory 7/2- | Nilsson/RPA $72^{-}$ | $\begin{gathered} \text { Constant } \\ 7 / 2^{-} \end{gathered}$ |
| $0{ }^{+}$ | 0 | 57(17) | 50 | 66 | 49 |
| $2^{+}$ | 808 | 40(12) | 44 | 32 | 45 |
| 4+ | 1481 | 3(3) | 4 | 2 | 4 |



Figure 5.1. Decay of ${ }^{119} \mathrm{Ba}$; (a) delayed proton spectrum, (b) proton coincident gamma-ray spectrum, (c) proton coincident x-ray spectrum, and (d) decay of the proton activity. The smooth curves in (a) are from statistical model calculations using the indicated beta-strength functions.


Figure 5.2. Decay of ${ }^{123} \mathrm{Ce}$; (a) delayed proton spectrum, (b) proton coincident gamma-ray spectrum, (c) proton coincident x-ray spectrum, and (d) denay of the proton activity. The smooth curves in (a) are from statistical model calculations using the indicated beta-strength functions.


Figure 5.3. Decay of ${ }^{125} \mathrm{Ce}$; (a) delayed proton spectrum, (b) proton coincident gamma-ray spectrum, (c) proton coincident x-ray spectrum, and (d) decay of the proton activity. The smooth curves in (a) are from statistical model calculations using the indicated betn-strength functions.


Figure 5.4. Decay of ${ }^{127} \mathrm{Nd}$; (a) delaved proton spectrum, (b) proton coincident gamma-ray spectrum, (c) proton coincident x-ray spectrum, and (d) ciecay of the proton activity. The smooth curves in (a) are f:om statistical model calculations using the indicated beta-strength funstions.


Figure 5.5. Decay of 129 Nd ; (a) delayed proton spectrum, (b) proton coincident gamma-ray spectrum, (c) proton coincident x-ray spectrum, and (d) decay of the proton activity. " he smooth curves in (a) are from statistical model calc'lations using the indicated beta-strength functions.


Figure 5.6. Decay of ${ }^{131} \mathrm{Nd}$; (a) delayed proton spectrum, (b) proton coincident gamma-ray spectrum, (c) proton coincident x-ray spectrum, and (d) decay of the proton activity. The smooth curves in (a) are from statistical model calculations using the indicated beta-strength functions.


Figure 5.7. Decay of ${ }^{131} \mathrm{Sm}$ (and ${ }^{131} \mathrm{Nd}$ ); (a) delayer proton spectrum, (b) proton coincident gamma-ray spectrum, (c) proton coincident $x$-ray spectrum, and (d) decay of the prolon activity. The smooth curves in (a) are from statistical model calculations using the indicated beta-strength functions. Spectrum in part (a) was obtained after subtracting the ${ }^{131} \mathrm{Nd}$ contribution.


Figure 5.8. Decay of ${ }^{133} \mathrm{Sm}$; (a) delayed proton spectrum, (b) proton coincident gamma-ray spectrum, (c) proton coincident x-ray spectrum, and (d) ciecay of the proton activity. The smooth curves in (a) are from statistical model calculations using the indicated beta-strength functions.


Figure 5.9. Decay of ${ }^{135} \mathrm{Sm}$; (a) delayed proton spectrum, (b) proton coincident gammanay spectram, (c) proton coincident x-ray spectrum, and (d) decay of the proton activity. The smooth curves in (a) are from statistical model calculations using the indicated beta-strength functions.


Figure 5.10. Deiayed proton spectra of (a) ${ }^{137} \mathrm{Gd}$, and (b) ${ }^{139} \mathrm{Gd}$ from experiments before the completion of the tape system. The smooth curves are from statistical model calculations using the indicated beta-strength functions. The data were first reported in [Nit83b].


Figure 5.11. Decay of ${ }^{141} \mathrm{Gd}$; (a) delayed proton spectrum, (b) proton coincident gamima-ray spectrum, (c) proton coincident x-ray spectrum, and (d) decay of the proton activity. The smooth curves in (a) are from statistical model calculations using the indicated beta-strength functions.


Figure 5.12. Decay of ${ }^{141} \mathrm{Dy}$ (and ${ }^{141} \mathrm{Gd}$ ); (a) delayed proton spectrum, (b) proton coincident gamma-ray spectrum, (c) proton coincident $x$-ray spectrum, and (d) decay of the proton activity. The smooth curves in (a) are from statistical model calculations using the indicated beta-strength functions.


Figure 5.13. Decay of ${ }^{143} \mathrm{Dy}$; (a) deiayed proton spectrum, (b) proton coincident gamma-ray spectrum, (c) proton coincident $x$-ray spectrum, and (d) decay of the proton activity. The smooth curves in (a) are from statistical model calculations using the indicated beta-strength functions.


Figure 5.14. Decay of ${ }^{145}$ Dy; (a) delayed proton spectrum, (b) proton coincident gamma-ray spectrum, (c) proton coincident x-ray spectrum, and (d) decay of the proton activity. The smooth curves in (a) are from statistical model calculations using the indicated beta-strength functions.


Figure 5.15. Decay of ${ }^{145} \mathrm{Er}$ (and ${ }^{145} \mathrm{Dy}$ ); (a) delayed proton spectrum, (b) proton coincident gamma-ray spectrum, (c) proton coincident $x$-ray spectrum, and (d) decay of the proton activity. Spectrum in part (a) was obtained after subtracting the 145 Dy contribution. The emooth curves in (a) are from statistical model calculations using the indicated beta-strength functions.


Figure 5.16 . Decay of ${ }^{147}$ Dy; (a) delayed proton spectrum, (b) proton coincident $x$-ray spectrum, and (d) decay of the proton activity. The smooth curves in (a) are from statistical model calculations using the indicated beta-strength functions. A discussion of the structured -ve-statistical nature of the proton spectrum in (a) can be found in chapter 6.


Figure 5.17. Decay of ${ }^{147} \mathrm{Er}$ (and ${ }^{147} \mathrm{Dy}$ ); (a) delayed proton spectrum, (b) proton coincident gamma-ray spectrum, (c) proton coincident x-ray spectrum, and (d) decay of the proton activity. The spectrum in (a) was obtained after subtracting the 147 Dy contribution. Direct proson erniscion from 147 Tm (monoenergetic peak at 1.05 MeV ) is also shown in (a). The smooth curves in (a) are from statistical model calculations.


Figure 5.18. Decay of ${ }^{149} \mathrm{Er}$; (a) delayed proton spectrum, (b) proton coincident gamma-ray spectrum, (c) proton coincident $x$-ray spectrum, and (d) decay of the proton activity. The smooth curves in (a) are from statistical model celculations using the indicated beta-strength functions. The structure in the proton spectrum (a) is discussed in chapter 6 .


Figure 5.19. Decay of ${ }^{151 Y b ;}$ (a) delayed proton spectrum, (b) proton coincideat gamma-ray spectrum, (c) proton coincident $x$-ray spectrum, and (d) decay of the proton activity. The emooth curves in (a) are from statistical model calculations using the indicaved beta-strength functions. The structure in the proton spectrum (a) is discussed in chapter 6 .


Figure 5.20. Decay of ${ }^{153} \mathrm{Yb}$; (a) delayed proton spectruim, (b) proson ccincident gamma-ray spectrum, (c) proton coincident $x$-ray spectrum, and (d) decay of the proton activity. The smooth curyer in (a) are from statistical model calculations using the indicated beta-strength functions.

## 6. DISCUSSION

### 6.1. STRUCTURE IN N=81 EVEN-ODD PRECURSORS

Mout of the delayed protom apestra (shown in the figwes in chapters 4 and 5) have the typical smooth spectrum expected from hervy mass precursors due to the high level demsities at excitation emergies surficiendy high for proton emietion. However, inspection of Figmes 5.16, 5.18, and $5.19\left({ }^{147} \mathrm{Dy},{ }^{149 \mathrm{Er}}\right.$, and ${ }^{151} \mathrm{Yb}$, respectively) shows that the $\mathrm{N}=81$ even-odd precunsors exhibit pronounced structure in their delayed pronoa epactra. Before mempting suy interpretation of the nature of this structure, isomer energies and sequeaces, Q values, and final strie feedings have to be determined for each precurnor before proton emergies cma be related to excitation energies in the emitter.

The even-odd $\mathrm{N}=81$ ieotopes ${ }^{147 \mathrm{Dy}}$, ${ }^{149 \mathrm{Er}}$, and 151 Yb have $11 / 2$ - high-spin isomers located about 750 keV above a $1 / 2^{+}$gromed state. The proton dingetier nuclei are eveo-even cloeed shell macki mad have lange eneryy gape ( -1.5 MeV ) between the $0^{+}$ground atime and highorepin excited atmen. Dese to the hrge agulir momentum berrier for the emision of $m 1=5$ proton froes $m 11 / 2$ - peacurvor to a $0^{+}$ daughter stme, decay to higher-apin excited athes in favored effioctively increacing the $\mathrm{B}_{\mathrm{p}}$ for proton emistion from the 11/2-inomers. This cman be seen in Fig. 3.3(b) for ${ }^{151} \mathrm{Yb}$. This shift in the effictive $B_{p}$ implies that proton earicion of the $1 / 2^{+}$ precursor can start from states in the eaniter roughly 1.5 MeV lower in excitation energy than proton emission for the $11 / 2$-ieomer. Due to the different energy dependencies for positron and eloctroa capheme decay, lurge decay energies (feeding to low excitation energies in the emitter) occer preferentislly via positron emission while decays to high excitation energies occur via electron capture. Requiring protons to be in coincidence with positrons is therefore expected to eahance the fraction of protons emitted from low excitation energies, i.e. to enhance the low-spin $\left(1 / 2^{+}\right)$precursor component. Figure 6.1(a) shows the proton singles spectrum from ${ }^{149} \mathrm{Er}$ decay and Fig. 6.1(b) shows the spectram of prowns in coincidence with positrons (reconded in the platic scintillator). The structured component is clearly enhanced and cem be asocismed with the $1 / 2^{+}$precursor decaying to the $0^{+}$ground state in ${ }^{148} \mathrm{Dy}$. This method was first reported in [Tot86] for ${ }^{151 \mathrm{Yb}}$ and the resulting proton spectra sre shown in Fig. 6.2. For this isotope, the structure is again associated widh the $1 / 2^{+}$precursor decay. In contrast, the $11 / 2-$ precursor decay (protons obverved in coincidence with the $3^{-}$to $2^{+}$transition in ${ }^{150} \mathrm{Er}$ ) was
structureless [Toti6]. Le the cane of ${ }^{147} \mathrm{Dy}$, the Qace is relatively low and the effiective decay window for the high spin proton decay is rmall ( -3.5 MeV ) 20 thit only $1 / 2^{+}$proton decaly is obencved. Since the peats (or narrow resonances) in the proton spectra for all three procurvors are firom the $1 / 2^{+}$precurvor gromod state decaying to the $0^{+}$gromad smest in the pecton dmeghere, their caergies con be unembiguously retaned to excination emersy in the emitter, i.e. $\mathrm{E}^{*}=\mathrm{B}_{\mathrm{p}}+\mathrm{E}_{\mathrm{p}} \mathrm{A}(\mathrm{A}-1)$.

The spectra for ${ }^{149 \mathrm{Er}}$ [Fig. 6.1(a)] and ${ }^{151} \mathrm{Yb}$ [Fig. 6.2(a)] appear to have a larger fraction of "statistical" delayed protome then the 1473Dy decay [Fig 5.16(a)] which is due to the increming fraction of delayed provons from the 112 - isomer decays as the precursor Z incremes. There were no proton coincident $\gamma$ rays obeerved for ${ }^{147} \mathrm{Dy}$ indicuing very livele $11 / 2$ - precurnor decky, wherens the fraction (in \%) of $1 / 2+$ protort 10 11/2- protoms (tured on predicted fimel state feedings in Table 5.6) were 7030 and 50550 for ${ }^{164}$ Er and ${ }^{151 Y b}$, reepectively. One remon for this increase in 11.2-precustor pectoa impanity is then the IT brmaches decrease from
 ion reactions predominmidy produce bidh-apin products, the IT decay in a major source of the $1 / 2^{+}$procursor production so there in simply leos $1 / 2+$ precursor produced for ${ }^{149} \mathrm{Er}$ and ${ }^{151} \mathrm{Y} \mathrm{H}$ complered to ${ }^{141} \mathrm{Dy}$. Another remon is tint the energetics which are mafavoreble for high-epin protom emimion in 147 my ( $\mathrm{Qec}_{\mathrm{e}}-\mathrm{B}_{\mathrm{p}}-1.5=-3.5$ in MeV ) are much more favorable in ${ }^{149 \mathrm{mr}}$ ( $\mathrm{Qaxc}_{\mathrm{E}}-\mathrm{E}_{\mathrm{p}}-1.5=-6$ in MeV) and ${ }^{151 m \mathrm{Mb}}$ ( $\mathrm{Q}_{\mathrm{Bc}}-\mathrm{B}_{\mathrm{p}}-1.5=-\mathrm{O}$ in MeV ). Givea the more favorable energetics, decreasing IT branchet, and the production of predominmatly high spin products in heavy-ion reactions, the increase in the obeerved fraction of $11 / 2^{-}$ precursor proton intensity from ${ }^{147} \mathrm{Dy}$ to ${ }^{151} \mathrm{Yb} \mathrm{cm}$ be readily explained.

Now that the atructured component is seen to follow the $1 / 2+$ decay of all $\mathrm{N}=81$ even-odd precinsons, what gives rise to this ytucture? It is most likely relnted 10 the $\mathrm{N}=82$ closed neutron chell in the emiters - either the lower level densities in closed shell nuclei or tome properties of the low hing levels in the emitter that are unique to $\mathrm{N}=82$ nuciei. Two different experixnemen approwches to understand this structure were undertiken. A study of other even-odd precursors with neutron numbers near $\mathrm{N}=81$, namely $\mathrm{N}=79$ and $\mathrm{N}=83$ procursors, was performed. In addition, a study of the odd-odd $\mathrm{N}=81$ precursors, which probe higher regions of excitation energy (and higher level density) in the emitter, was also performed. The $\mathrm{N}=79$ even-odd precursors have $11 / 2^{-}$isomers and $1 / 2^{+}$ground states but the $11 / 2^{-}$ states decreme in energy rapidly with decreasing neutron number away from the cloted shell. In ${ }^{145} \mathrm{Dy}$, the $11 / 2$ - isomer is only about 117 keV above ground. There
thould be no apprecieble II bruaches in the $\mathrm{N}=79$ even-odd ieomers. The final state energiet are siso dificment the first $2+$ levels me at $\sim 700 \mathrm{keV}$ with the 3 - and $4+$ levels remaining at -1.5 MeV . The predicted feedings (see Table 5.6) for an 11/2precursor indicate considernble proton intensity to the $2+$ levels 10 thet the separation in the excitation energies from which low- and high-epin preaursor proton emistion occurs is not as lerge as for N - 81 precursors. Figme 6.3 shows the proton siagles
 structure $\frac{\text { at }}{} 2.6$ mad 2.9 MeV in Fig. 6.3 (e) which is also preeent in Fig. 6.3(b) and could perhaps be amocinted with the $1 / 2+$ docay. However, about half of the observed protions are due to the high-mpin inoamer which probebly addy a "statistical" background to the $1 / 2^{+}$decay and any ponentiol structure in the prowon spectrum would then be more difficult to obeerve. In ${ }^{147} \mathrm{Er}$ decay, Table 5.6 augeets $\sim 85 \%$ of the protons follow the 11/2-inonarr $\beta$ decay. In Fig. 6.4(a) there is weak, brond structure at 3.1 and 3.7 MeV is fone pronan singles spectra which is slso enhanced in the positron coincident protom epectran, Fig. 6.4(b). The low-epin decavs in 145Dy and ${ }^{147}$ Er should probe similar regions of excitation emergies in the emitur as the $\mathrm{N}=81$ low-spin decays but the structure is moch low pronounced at $\mathrm{N}=79$. The only known even-odd $\mathrm{N}=83$ precursor, ${ }^{153} \mathrm{Yb}$, has no clemr indication of any structure is the delayed proton spectrum [Pig. $5.20(\mathrm{a})$ ]. The ground state of 153 Yb is expected to be 7/2- and there are no known $\beta$-decaying isomers. Thus the decays of $\mathrm{N}=83$ precursors are probably similar to the decsy of $11 / 2$ - precursors discussed above and little structure should be present.

The delayed prown deciy of the inee $\mathrm{N}=81$ odd-oud precursors ${ }^{149} \mathrm{Ho}$ (Fig. 4.15), ${ }^{150} \mathrm{Tm}$ (Fig. 4.17), and 152 ${ }^{\text {m (Fig. 4.18) is discussed in detail in [Nit88] and }}$ briefly summarized below. The decays of odd-odd precursors probe regions of higher excitation eseryy in the emitter due to the larger $\mathrm{B}_{\mathrm{p}}$ values [see Fig. 3.2(d) and compare the $\mathrm{B}_{\mathrm{p}}$ values for the $\mathrm{N}=\$ 1$ odd-odd precursors (in Table 4.4) with the $\mathrm{N}=81$ even-odd precursors (in Table 5.4)]. All three precursors have low-and highspin isomers, typically $1+6$ pairs, which are expected to be close to one another in energy. The proton decay daughters also have close lying low- and high-spin isomers (1/2+,11/2-pairs) which create decay paths for both the low- and high-spin precursors that have very similar energetics. This can be seen in Fig. 3.3(a) for $\mathbf{1 5 0} \mathrm{Tm}$. It is very dificult to experimentally separate the low- and high-spin decays because of the similar energetict. Heavy-ion reactions are expected to strongly favor the high-spin states, and the observed fingl state feedings and precursor half-lives indicate that the protion decays are indeed dominated by the high-spin precursors.

The delayed proton singles spectrum from ${ }^{150} \mathrm{Tm}$ and the positron coincident proton spectrum are shown in Fig. 6.5. There is perhape some deviation from the smooth behavior at sbout 3 MeV but in gereral the odd-odd precursors show litile structure.

It was alrendy pointed out that the structure in $\mathrm{N}=82$ emitters is associated with low-spin siates at relatively low excitation energies in the emitter (the decays of odd-odd precursors and 11/2-isomers, which are sensitive to higher spin levels at higher excitation energies, exhibit little structure) and is not present in emitters away from the $\mathrm{N}=82$ closed shell. The decay (via proton and $\gamma$-ray emission) of these lowspin states in the emitter muat be different thea the deceys of high-apin states. According to the shell model, the configurations for the $1 / 2^{+}$precursor ground states are $\pi h_{1 / 2} \mathrm{VS}_{1 / 2}{ }^{-1}$ and the $11 / 2$-isomeric precursors have configurations of $\pi h_{11 / 2} \mathrm{vh}_{11 / 2^{-1}}$. The allowed Gamow-Teller $\beta$ decays of both the $1 / 2^{+}$and $11 / 2^{-}$ states should be dominated by $\pi h_{11 / 2} \rightarrow v_{\text {gh2 }}$ GT transitions [Sch84a] to levels at around $4-5 \mathrm{MeV}$ excitation energy in the $\beta$-decay daughers. The states following the $\pi \mathrm{h}_{11 / 2} \rightarrow \mathrm{v}_{\mathrm{h} / 2}$ GT $\beta$ decays of the high-epin isomers will have configurations $\left[\left(\pi h_{11 / 2} v_{h} / 2\right)\right)^{+} \mathrm{x} \mathrm{vh}_{\left.11 / 2^{-1}\right]} \mathrm{M} 2,11 / 2,1322$ which can then decay by fast $\sim 4 \mathrm{MeV}$ M1 vhgh $\rightarrow \mathrm{vh}_{11 / 2^{-1}}$ spin-flip transitions as shown in the top part of Fis, 6.6. The $\left[\left(\pi h_{112} v^{2} h_{22}\right) 1^{+} \mathrm{x} \mathrm{vs}_{12} 2^{-1}\right] 1 / 2^{+}, 32^{+}$low spin stalest in the emitter following the $\pi h_{11 / 2} \rightarrow v_{h} / 2$ GT $\beta$ decays of the $1 / 2+$ precurtor ground states must undergo complex rearrangements to decay to the low-lying low-spin ( $1 / 2^{+}, 3 / 2^{+}$, and $5 / 2^{+}$) single proton states (the bottom of Fig. 6.6). The $\gamma$ decay of these low-spin levels is expected to be much slower than the $\gamma$ decay for the high-rpin states.

In [Sch84a] the $\beta$ decay of ${ }^{147}$ Dy was sudied. The $\beta$ decay of the 11/2isomer had considerable strength to levels at $\sim 4.7 \mathrm{MeV}$ which de-excited by single high energy $\gamma$ transitions to the $11 / 2$-ground state in ${ }^{147} \mathrm{~Tb}$. In contrast, the $1 / 2+\beta$ decay had considerable strength to levels at $\sim 4 \mathrm{MeV}$ which showed frequent $\gamma$ branchings in their de-excitation. The low- and high-spin decays seem to be consistent with the simple shell model description presented above. Because of the slower $\gamma$ decay of the low-spin levels, $\Gamma_{\mathbf{p}}\left(\Gamma_{\mathbf{p}}+\Sigma \Gamma_{\gamma}\right)$ could be much larger than assumed in statistical model calculations and enhanced proton emission from these stabes would occur. A study of 1478Dy [Alk86] using a total absorption spectrometer where the delayed protons and the $\beta$-strength function were independently measured indicutes that the partial proton widths are about an order of magnitude larger than statistical model calculations would predict. In a detailed study of ${ }^{14} 9 \mathrm{Er} \beta$ decay [Fir88], the high-spin decay showed the same pettern as in ${ }^{147 \mathrm{mDy}}$ and the partial proton widths for ${ }^{149} \mathrm{FE}$ Er seemed to be about an order of magnitude larger than
statistical model predictioas. In both [Sch84]] and [Fir88], an atrempt was made to mation the proton energies to corresponding excited levels in the ewitter determined from the $\gamma$-ray analysis. There is some correlation between the lowest energy protion lines and levels placed from the $\gamma$ ray data [Sch87] in ${ }^{1474 D y}$ decay, but for ${ }^{149 \mathrm{cEr}}$ no such correlation could be found [Fird8]. This suggests that the complex $\gamma$ decay of the levels sasociated with the proton structure is slow enough that proton emission dominates. An interpretation of this structurs, in the framework of a "doorway" state model was proposed in [Nit87].

The simple shell model description above and shown in Fis. 6.6 tives a qualitative understanding of what is currently known about the structure in even-cdd $\mathrm{N}=81$ precursors. These low-spin states should occur ar roughly the same excitation energy in the emitter and the most intense proton peaks in ${ }^{147} \mathrm{Dy},{ }^{14} \mathrm{Er}$, and ${ }^{151} \mathrm{Yb}$ should be at essentially the same excitation in the emitter (ree Fig. 6.7 where all six delayed proton spectra from $\mathrm{N}=81$ precursors are shown as a function of excitation energy in the emitter) which is indeed the case. It also explains the difficulties in finding the corresponding $\gamma$ decay of these levels and the large branching ratios
 than statistical model predictives. The lack of structure in the 11/2- decays and in the odd-odd precursort is due to the higher level densities ot higher excitation energies and the faster $\gamma$ decays of the proton-emiting stames in these emitters. It should be pointed out that the proton energies associmed with the 11/2- precursors in Fig. 6.7 are shown $\sim 1.5$ too low in emitter excitaion energy since these protons could not be separated from those astocimed with the $1 / 2^{+}$precursors. There may be weak structure in the $\mathrm{N}=791 / 2^{+}$precursors, but the level densities are higher and there may be additional low-spin levels between the proton emitting region and the ground state in the emitter which could cause faster $\gamma$ decays and reduce the level widths for proton emission.

### 6.2. QEC-Bp DETERMINATIONS

The detailed studies of the precursors near $\mathrm{N}=82$ mace it possible to measure the mass difference $\mathrm{Qagc}_{\mathrm{B}} \mathrm{B}_{\mathrm{p}}$ by comparing the number of protons in coincidence with positrons to the total number of protons $\eta_{p}$. For a series of assumed $\mathrm{Q}_{\mathrm{EC}}$ and $\mathrm{B}_{\mathbf{p}}$ values, the proton energies can be related to excitation encrgies $\mathrm{E}^{\dagger}=\mathrm{B}_{\mathrm{p}}+\mathrm{E}_{\mathrm{p}} \mathrm{A}(\mathrm{A}-1)$ which imply $\beta$-decay energies of $Q^{\prime}=Q_{E C}-E^{*}$. The $\beta+$ to $\left(E C+\beta^{+}\right)$ratios for these decay energies can be precisely calculated [Gov71] and compared to the measured
values. The $\eta_{p}$ values depend on the difference between $Q_{E C}$ and $B_{p}$ since the $\beta+$ to ( $\mathrm{EC}+\beta^{+}$) ratio is determined by the $\beta$-decay energy only. Because the experimental $\eta_{p}$ value is usually an average over the entire proton spectrum and the final states in the proton daughter, proper averaging of the calculated ratios is required [Hor72a]. The $\eta_{p}$ values were calculated according to following formula:

$$
\eta_{p}=\frac{\sum_{x} I_{p}(x)\left[\sum_{f} W_{f}\left(E_{p}, E_{f}\right) \omega\left(Q^{\prime}\right)\right]}{\sum_{x} I_{p}(x)},
$$

where $I_{p}(x)$ is the measured proton intensity as a function of proton energy (or channel number), $W_{f}\left(E_{p}, E_{f}\right)$ are the measured final state branches, $\omega\left(Q^{\prime}\right)$ is the calculated $\beta^{+}$to ( $\mathrm{EC}+\beta^{+}$) ratio, and $Q^{\prime}=\mathrm{Q}_{\mathrm{Bc}}-\mathrm{B}_{\mathrm{p}}-\mathrm{E}_{\mathrm{F}}-\mathrm{F}_{\mathrm{p}} A(\mathrm{~A}(\mathrm{1})$. The sums over x are taken over all channels in the measured proton spectrum and the sum over $f$ is taken over the number of observed final states. The final state branches depend on the proton energy but could not be measured due to the small number of $\gamma$ rays coincident with protons. This dependence is probably strongest at the lowest and highest proton energies where the weighting by the proton spectrum is rather small. It was assumed that the final state branches were constant over the entire proton spectrum.

Using this technique, the results for ${ }^{147} \mathrm{Er}$ and ${ }^{150} \mathrm{Tm}$ are shown in Figs. 6.8(a) and 6.8(b), respectively. The statistical errors of the experimental $\eta_{p}$ 's were used to estimate the errors in $\mathrm{Q}_{\mathrm{EC}}-\mathrm{B}_{\mathrm{p}}$ values. Other $\mathrm{Q}_{\mathrm{sc}}-\mathrm{B}_{\mathrm{p}}$ values are listed in Table 6.1. The values for ${ }^{149} \mathrm{Er}$ and ${ }^{151} \mathrm{Yb}$ were determined in a slightly different way. The areas of the peaks in the proton singles and the positron coincident proton spectra were compared and the $\mathrm{Q}_{\mathrm{Ec}}-\mathrm{B}_{\mathrm{p}}$ values inferred from the ration [Fir88]. Since the peaks represent transitions to the $0^{+}$ground state in the daughter, there is no need to average over the proton spectrum. The extrapolated values from [Wap87] in Table 6.1 seem to offer better agreement with experiment than the values from [Lir76]. The $\mathrm{B}_{\mathrm{p}}$ values quoted in [Wap87] are gencrally smaller than those in [Lir76] in the region near $\mathrm{N}=82$ which may have a slight influence on the interpretation of the $\mathrm{N}=81$ emitters discussed above. A figure similar in layout to Fig. 6.7 using the $\mathrm{B}_{\mathbf{p}}$ values from [Wap87] instead of the values from [Lir76] can be found in [Nit87]. These figures are essentially identical; the region of excitation energy associated with the structure is still roughly the same for the three even-odd precursors and proton
emission for odd-odd precursors occurs at higher excitation energies in the emitters than for tre $1 / 2^{+}$even-odd precursors.

### 6.3. STATISTICAL MODEL CALCULATIONS

Nuclear properties of the deliyed proton emitters near $\mathrm{N}=82$ are of great interest because of the structure discussed above and the close proximity to the proton drip line. However, a major focus of this work was to systematically study delayed proton emission of heary mass precursors and to learn if the proton emission process could be adequately described within a statistical model framework. The emitters in the highly deformed region midway between the $\mathrm{Z}=50$ and $\mathrm{N}=82$ closed shells should satisfy the main requirement of a statistical model, namely, that the level spacing in the emitter be comparable to the level width. The low level densities near closed shells and shell model effects cuch as the slow $\gamma$ decay of low spin states in $\mathrm{N}=82$ emitters ( ${ }^{147 \mathrm{EDy}},{ }^{149} \mathrm{LEr}$, and ${ }^{151 \varepsilon Y b}$ ) cmonot be treated correctly in the simple statistical model presented in chapter 3.

An examination of the delayed proton spectra and the associated calcuinted spectra shown in the rop part of the figures in chapters 4 and 5 indicates that, with the exception of the $\mathrm{N}=81$ precursors, the statistical model calculations agree reasonably well with the measured spectra. In almost every case, the calculations using the Nilsson/RPA $\beta$-streagth functions appear to be in much better agreement with the experiments than calculations using the gross theory $\beta$-strength functions. This is more quantitatively presented in Table 6.2, where the experimental epectra are compared with the results from three seis of calculations using three different forms of the $\beta$-strength function. The centroids from the Nilston/RPA calculations are typically within 100 to 200 keV of the experiment while the groes theory and constant $\mathrm{S}_{\beta}$ calculations result in spectra that have centroids typically $\sim 400 \mathrm{keV}$ too high in energy. A chi squared $X^{\mathbf{2}}$ evaluation was also performed to determine a "goodness of fit" parameter. A slight dependance on the number of counts prevented a comparison of the "goodness of fit" between different precursors but could still be used to judge the agreement between the experiment and the three different calculations for a given precursor. The $\mathrm{X}^{2}$ values for each precursor were normalized to the $X^{2}$ value for the Nilsson/RPA calculation. The Nilsson/RPA results have $\mathrm{X}^{2}$ values that are typically a factor of 2 to 3 better than the other calculations.

Other parameters in the statistical model can also influence the shape of the proton spectrum. Small changes in level densities, optical model parameters, and $\gamma$ widths do not change tine shape of the proton spectrum very much; however, the QEC and $B_{p}$ values can have a significant effect of the spectrum shape, as shown in Fig. 4.2 for ${ }^{122} \mathrm{La}$. The predictions of [Lir76] are generally expected to be reliable [Hau84] and data from the half-life predictions discussed below also indicate the energetics were well described in mont cascs. The strongest influence on the proton spectrum shape is exerted by the different $\beta$-strength functions, and the Nilsson/RPA model is cleariy in better agreement with experiment in this region. However, due to the influences of the other parameters in the statistical model, direct measurements of the $\beta$-strength functions are the only method to determine if the Nilsson/RPA $S_{\beta}$ calculations reliably reproduce the experimental $S_{\beta}$ 's. All that can be concluded from the delayed proton studies thus far is that the Nilsson/RPA $S_{\beta}$ 's in conjunction with the other statistical model parameters listed in Tables 4.4 and 5.4 result in much improved agreement with the experimental data.

The shape of the delayed proton spectrum is not the only quantity the statistical model raust reproduce: the $\beta$-to-proton brunching ratios and the relative branches to final states should also be correctly predicted. Very few odd-odd precursors had any $\gamma$ rays in coincidence with delayed protons, so the majority of the final state feedings were obtained for even-odd precursors and are listed in Tables 5.5 and 5.6. The statistical model calculations are indeed capable of predicting the measured final state branches within the experimental uncertainty and could even be used in the region above $\mathrm{Z} \mathbf{- 6 4}$ to determine the fraction of low- and high-spin precursors contributing to the delayed proton decay. The calculations of the final state feedings are, as expected, most sensitive to the optical model parameters and the choice of the precursor spin (see Table 5.5). The effect of the different $\beta$-strength functions on the final state feeding is shown in Table 5.7 for 'ne example of ${ }^{153} \mathrm{Yb}$, and in general there are only small differences in the values from the three calculations. Another indication that the optical model parameters used in the calculations (and to a lesser extent the $\gamma$ widths) are reasonable is that the onset of proton emission is very well predicted by the statistical model calculations which can be seen in the figures in chapters 4 and 5 . Even in cases where the calculation did not match the centroid or the upper part of the measured proton spectrum, the onset of emission was reliably predicted.

The final state feedings observed in delayed proton studies are a very sensitive method to identify the low-lying rotational transitions in even-even nuclei
very far from stability. In all even-odd precursor decays, at least the first $2^{+}$to $0^{+}$ transition in the prown daugher was observed. The $x$-rays, in coincidence with the delayed protons, and the mass separator uniquely identify the precursor and consequently, the even-even proton daughter. The x-ray sum peaks in the proton coincident $\psi$-ray spectra provide additional identification information. In-beam $\psi$-ray spectroscopists may have difficulty identifying band beads in nuclei fer from stability due to the low cross sections and the possibility then transitions from other isotopes could obscure the transition of interest. The data from delayed proton studies may provide important complementary information on the level properties of even-even nuclei.

The other importart quentity in evaluating the reiability of the atatistical model calculations is the proton branching ratio. Unfortunately, proton bruching ratios are difficult to determine with the present experimental setup. Esseatially complete decay scheme work in nuclei with very complicaned $\beta$ decays due to the large QEC values and high level densitien is required. This process is extremely time consuming and there is the potential for large errors in the total $\beta$ intensity (and thus $P_{p}$ ) if there are incorrect assumptions about the decay scheme. The measured and predicted $P_{p}$ 's are listed in Table 6.3. There are only four measured values in the deformed region and the statistical model calculations me in remsonable agreement with experiment. The remainder of the measured values are for nuclei near $\mathrm{N}=82$. The value for ${ }^{153} \mathrm{Yb}$ in in good agreement with the calculations but the $\mathrm{N}=81$ precursors have oranches that are about a factor of 10 larger than predicted. In the case of ${ }^{1498 E r}$, the shell model interpretation discussed above would suggest a branch much larger than predicted. A possible explanation for the other precursors is a lower level density in $\mathrm{N}=82$ muclei than predicted, since the level density has a strong influence on the branching ratio. In [Nit88] the branching ratios for the three odd-odd precursors could be reproduced by decreasing the a parameter in the level density formula to $70 \%$ of the predicted value. Decreasing the $\gamma$ widths will also result in larger branching ratios and may be justified for the odd-odd precursors. The precursor is expected to have a spin $\sim 6$ - in all three cases and is assumed to $\beta$ decay by allowed GT transitions to 5 -, 6 -, or 7 - states in the even-even emitter. The eveneven $\mathrm{N}=82$ nuclei have a $0^{+}$ground state and higher spin states about 1.5 MeV above ground. In the statistical model, the $\gamma$ width is given by equation 3.6 where the $\gamma$ strength function is integrated from 0 to the maximum available $\gamma$-decay energy. Since there is no $\gamma$ decay from high spin levels to the $0^{+}$level, the maximum $\gamma$-decay energy should be $\mathrm{E}^{*}-1.5 \mathrm{MeV}$ rather than $\mathrm{E}^{*}$. The calculations presently do not take
into consideration the low-lying level structure in the emitter and the $\gamma$ strength is probably too large, resulting in low branching ratios.

### 6.4. PRECURSOR HALF-LIVES

While comparing $\beta$-strength functions and their effects on the statistical model calculations, the question of predicting precursor half-lives, with the different $\beta$-strength functions arises. Half-life predictions in nuclei fer firom stability are of importance in s - and r-process calculations. In Tables 4.2 and 5.2 predictions from both the gross theory and Nilsson/RPA calculations are listed along with the measured values. Both models show surprisingly good agreement with the experimental values and, even more surprisingly, the two models usually predict similar values. The $\mathrm{Q}_{\text {Ec }}$ values [ Li i 76 ] were the same in both calculations and, since two very different models ahow similar deviations from the measured values, it was suspected that errors in the $Q$-value predictions are the source of these deviations. For the gross theory calculations, changing the $Q_{E c}$ 's by $\pm 5 \%$ resulted in half-lives that were $\sim 1.5$ times longer with the lower $Q_{E C}{ }^{\prime} s$ and $\sim 0.7$ times shorter with the larger Qec's. The ratios of predicted half-lives to measured half-lives are plotted in Fig. 6.9. The scatter in the two sets of predictions is about the same with the gross theory values consistently a little loager thisn the experimental values. The Nilsson/RPA values could be improved slightly since there is some freedom in the choice of the Gamow-Teller quenching factor used in the calculations.

### 6.5. SUMMARY

Forty-two delayed proton precursors ( 25 new isotopes and 8 new branches) were produced in heavy-ion reactions and, after on-line mass separation, their radioactive decay properties were studied. The precursor $Z$ and $A$ were uniquely identified in all cases. Delayed proton spectra and final state branches were measured for all precursors and, in a few cases, proton branching ratios were determined. The statistical model adequately described the delayed proton emission process in heavy mass precursors with standard parameter prescriptions. Statistical model calculations using Nilsson/RPA model $\beta$-strength functions were compared to calculations using gross theory or constant $\beta$-strength functions. The Nilsson/RPA based calculations reproduced the spectral shapes and branching ratios better than calculations using the other $\beta$-strength functions. Precursor half-ife predictions from the Nilsson/RPA $S_{\beta}$ calculations were in better agreement with the measured values than the gross theory
predictions. Final state feedings and the onset of proton emission were reasonably well predicted indicating the optical model adequately detcribes the low-erergy proton barrier penetrability.

In $\mathrm{N}=81$ precurions, which decay to $\mathrm{N}=82$ chsed winell proton emitters, the statistical model wis not able to reproduce the experimental results. Pronounced atructure associated with the decay of $1 / 2^{+}$even-odd $\mathrm{N}=81$ precuriors could be explained by shell model configurations of the emitting states which have strongly hindered $\gamma$-decay channels resulting in enhanced proton emission from these stater. The odd-odd $\mathrm{N} \times 81$ precursors had proton brapching ratios a factor of $\sim 10$ larger than predicted and the calculations could not reproduce the spectral ahepe. The branching ratio discrepancy can be resolved by reducing the level density in the emitter or decreasing the $\gamma$ widths. Beta-strength functions from Nibson/RPA calculations, which seemed to offer the best agreement with experiment in the majority of cases, may be inappropriate near closed ahells sinve the assumption of the $\beta$-decay parent and daughter having the same deformaion is not valid.

The statistical model has several free parameters and even with the large volume of data amassed for the precursons presented here, the devermination of the best set of parameters was impossible. Additional data such as the direct measurement of $\beta$ - and $\gamma$-strength functions, level widths, and level densities are required before further insight into the delayed proton emission process in heavy nuclei can be gained.

Table 6.1. Comparison between experimental and predicied $\mathrm{Qec}_{\mathrm{E}}-\mathrm{B}_{\mathrm{p}}$ values;
Experimental $=$ Qec- $^{-3}$ value from positron coincident to total proton intensity ratio, Liran-Zelden $=$ value calculated from [Lir76] mass formula, and Wapstra, et al. $=$ value calculated from extrapolated mase values from the 1986-87 mass predictions [Wap87].


Table 6.2. Compmien betweon calculmal and experimantil delayed protan spectra; Experimeat -








| Precmace | $\frac{\text { Experimont }}{\overline{\mathbf{E}}}$ | Nimenalat |  |  | Growe Theory |  |  | Cometat |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | E | $\triangle$ | $\mathrm{x}^{2}$ | E | 4 | $\mathrm{x}^{2}$ | $\overline{\mathbf{E}}$ | $\Delta$ | $\mathrm{x}^{2}$ |
| ${ }^{119} \mathrm{Ba}$ | 3.43(1) | 3.50 | +0.07 | 1.0 | 3.67 | +0.24 | 9.3 | 3.58 | + 0.15 | 4.1 |
| ${ }^{120} \mathrm{La}$ | 3.71(3) | 3.89 | +0.17 | 1.0 | 4.20 | +0.49 | 4.2 | 4.06 | +0.35 | 2.2 |
| ${ }^{122} \mathrm{La}$ | 3.42(2) | 3.64 | +0.22 | $1.0{ }^{0}$ | 3.52 | +0.40 | 2.7 | 3.79 | +0.37 | 2.6 |
| ${ }^{123} \mathrm{Ce}$ | 3.61(1) | 3.75 | +0.14 | 1.0 | 4.2:2 | +0.41 | 6.8 | 3.91 | $+0.30$ | 4.3 |
| ${ }^{124} \mathbf{P r}$ | 3.73(3) | 4.05 | +0.32 | 1.0 | 4.45 | +0.72 | 5.6 | 4.30 | +0.57 | 3.4 |
| ${ }^{125}$ Ce | 3.33(1) | 3.39 | $+0.06$ | 1.0 | 3.50 | +0.17 | 5.9 | 3.50 | +0.17 | 6.5 |
| ${ }^{126} \mathrm{Pr}$ | 3.67(5) | 3.50 | +0.13 | 1.0 | 4.15 | +0.48 | 4.3 | 4.12 | +0.45 | 3.8 |
| ${ }^{127} \mathrm{Nd}$ | 3.66(4) | 3.91 | +0.25 | 1.0 | 4.17 | +0.51 | 2.7 | 4.03 | +0,37 | 1.5 |
| ${ }^{128} \mathrm{Pr}$ | 3.24(4) | 3.27 | $+0.03$ | 1.0 | 3.34 | +0.10 | 1.4 | 3.36 | + + 0.12 | 1.8 |
| ${ }^{129}$ Nd | 3.66(4) | 3.75 | +0.09 | 1.0 | 3.99 | +0.23 | 5.5 | 3.90 | +0.24 | 6.6 |
| ${ }^{131}$ Nd | 3.12(1) | 3.06 | -0.06 | 1.0 | 3.10 | -0.02 | 0.8 | 3.13 | +0.01 | 1.0 |
| ${ }^{131}$ Sm | 3.85(3) | 4.17 | +0.32 | 1.0 | 4.35 | $+0.50$ | 2.2 | 4.19 | +0.34 | 1.0 |
| ${ }^{132} \mathrm{Pm}$ | 3.60(3) | 3.77 | +0.17 | 1.0 | 388 | +0.2s | 1.7 | 3.92 | +0.32 | 2.3 |
| ${ }^{133} \mathrm{Sm}$ | 3.77(3) | 3.93 | $+0.16$ | 1.0 | 4.18 | +0.41 | 5.5 | 4.16 | +0.39 | 5.6 |
| ${ }^{134} \mathrm{Eu}$ | 3.72415) | 4.24 | +0.52 | 1.0 | 4.61 | +0.89 | 1.3 | 4.51 | +0.79 | 1.0 |
| 135 Sm | 3.542) | 3.56 | +0.02 | 1.0 | 3.65 | +0.11 | 2.3 | 3.69 | +0.15 | 3.6 |
| ${ }^{136} \mathrm{E}_{\mathrm{E}}$ | 3.90(5) | 4.12 | +0.22 | 1.0 | 4.25 | +0.38 | 1.8 | 4.23 | +0.33 | 1.5 |
| ${ }^{137}$ Gd | 3.83(5) | 4.02 | +0.19 | 1.0 | 4.36 | +0.53 | 2.6 | 4.33 | +0.50 | 2.4 |
| ${ }^{139}$ Gd | 3.80(5) | 3.85 | +0.05 | 1.0 | 4.09 | +0.29 | 2.7 | 4.15 | +0.35 | 3.7 |
| ${ }^{140} \mathrm{~Tb}$ | 4.18(4) | 4.16 | -0.02 | 1.0 | 4.55 | +0.37 | 3.2 | 4.59 | +0.41 | 4.6 |
| ${ }^{141}$ Gd | 3.52(3) | 3.47 | -0.05 | 1.0 | 3.61 | +0.09 | 1.0 | 3.65 | $+0.13$ | 1.3 |
| $141^{\text {Dy }}$ | 4.14(3) | 4.38 | +0.24 | 1.0 | 4.62 | +0.41 | 3.8 | 4.57 | +0.43 | 3.3 |
| 142Dy | 3.80) | 3.86 | -0.02 | 1.0 | 4.14 | +0.26 | 3.8 | 4.22 | +0.34 | 5.6 |
| 143 Dy | 4.17(2) | 4.09 | -0.03 | 1.0 | 4.41 | +0.24 | 3.5 | 4.49 | +0.32 | 5.6 |
| 144 Dy | 325(5) | 3.43 | +0.18 | 1.0 | 3.54 | +0.29 | 2.2 | 3.57 | +0.32 | 2.7 |
| ${ }^{144} \mathrm{Ho}$ | 4.15(5) | 4.84 | +0.69 | 1.0 | 4.61 | +0.46 | 0.4 | 4.63 | +0.48 | 0.4 |

Tshle 6.2. (cominued)

| Prucursar | $\frac{\text { Expaivent }}{\bar{E}}$ | Ninocarpa |  |  | Grom Thary |  |  | Comerer |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\bar{E}$ | A | $\mathrm{x}^{2}$ | E | $\Delta$ | $\mathrm{x}^{2}$ | $\bar{E}$ | 4 | $\mathrm{x}^{2}$ |
| ${ }^{145} \mathrm{D}_{\text {j }}$ | 3.99(1) | 3.91 | -0.08 | 1.0 | 4.03 | +0.04 | 0.6 | 4.06 | +0.09 | 0.7 |
| ${ }^{145} \mathrm{Er}$ | 4.343) | 4.64 | +0.30 | 1.0 | 4.92 | +0.58 | 3.3 | 4.90 | +0.56 | 3.0 |
| 146 Ho | 4.13(4) | 4.25 | +0.15 | 1.0 | 4.58 | +0.45 | 5.5 | 4.68 | +0.55 | 8.4 |
| 1475Dy | 3.50(1) | 3.37 | -0.13 | 1.0 | 3.46 | -0.04 | 0.5 | 3.48 | -0.02 | 0.4 |
| ${ }^{147} \mathrm{Er}$ | 4.32(1) | 4.52 | +0.23 | 1.0 | 4.76 | +0.44 | 28 | 4.85 | $+0.53$ | 4.0 |
| ${ }^{141} \mathrm{Ho}$ | 4.07(2) | 3.94 | -0.13 | 1.0 | 4.24 | +0.17 | 2.2 | 4.30 | +0.23 | 3.1 |
| $149 \mathrm{~m}+\mathrm{EEr}$ | 4.20(1) | 4.10 | -0.18 | 1.0 | 4.49 | +0.21 | 0.9 | 4.60 | +0.32 | 1.7 |
| 150 Tm | 4.71(1) | 4.49 | -0.22 | 1.0 | 5.02 | +0.31 | 1.4 | 5.15 | +0.44 | 2.9 |
| $151 \mathrm{~m}+5 \mathrm{Yb}$ | 4.52(1) | 4.73 | +0.21 | 1.0 | 5.05 | +0.53 | 8.1 | 5.12 | +0.60 | 12.5 |
| ${ }^{152} \mathrm{Lu}$ | 4.36(5) | 5.16 | +0.60 | 1.0 | 5.43 | +0.57 | 0.8 | 5.39 | +0.83 | 0.6 |
| ${ }^{153} \mathrm{Yb}$ | 3.102) | 3.85 | -0.03 | 1.0 | 4.10 | +0.22 | 4.3 | 4.12 | +0.24 | 5.2 |








| Precmex | $\mathrm{J}^{\text {x }}$ | $\mathbf{P}_{\mathbf{p}}$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Exprimeat | Nineontiph | Geom Treary | Coment |
| ${ }^{119} \mathrm{ga}$ | 1/2+ | - | $4 \times 10^{-2}$ | $8 \times 10^{-3}$ | $8 \times 10^{-3}$ |
| ${ }^{120}$ | 5 | - | $2 \times 10^{-2}$ | $5 \times 10^{-3}$ | $4 \times 10^{-3}$ |
| ${ }^{122} \mathrm{La}$ | 5 | - | $6 \times 10^{-4}$ | $2 \times 10^{-4}$ | 1×10-4 |
| ${ }^{123} \mathrm{Ce}$ | $5 / 2^{+}$ | - | $8 \times 10^{-3}$ | $6 \times 10^{-3}$ | $5 \times 10^{-3}$ |
| ${ }^{124} \mathrm{Pr}$ | 5 | - | $6 \times 10^{-3}$ | $3 \times 10^{-3}$ | $2 \times 10^{-3}$ |
| ${ }^{125} \mathrm{Ce}$ | $52^{+}$ | - | $4 \times 10^{-4}$ | $2 \times 10^{-4}$ | $2 \times 10^{-4}$ |
| ${ }^{126} \mathrm{Pr}$ | 5 | - | $3 \times 10^{-4}$ | $2 \times 10^{-4}$ | 1810-4 |
| ${ }^{127}$ Nd | 1/2+ | - | $4 \times 10^{-2}$ | $2 \times 10^{-2}$ | $1 \times 10^{-2}$ |
| ${ }^{128} \mathrm{Pr}$ | 5 | - | $7 \times 10^{-6}$ | $6 \times 10^{-6}$ | $4 \times 10^{-6}$ |
| ${ }^{129} \mathrm{Nd}$ | 5/2+ | - | $2 \times 10^{-3}$ | $7 \times 10^{-4}$ | $5 \times 10^{-4}$ |
| ${ }^{130} \mathrm{P}$ m | 5 | - | $1 \times 10^{-3}$ | $6 \times 10^{4}$ | $3 \times 10^{-4}$ |
| ${ }^{131} \mathrm{Nd}$ | $512^{+}$ | - | $2 \times 10^{-5}$ | $1 \times 10^{-5}$ | $1 \times 10^{-5}$ |
| ${ }^{131}$ Sm | $5 / 2+$ | - | $8 \times 10^{-2}$ | $2 \times 10^{-2}$ | $2 \times 10^{-2}$ |
| ${ }^{132} \mathrm{Pm}$ | 5 | - | $5 \times 10^{-5}$ | $4 \times 10^{-5}$ | $3 \times 10^{-5}$ |
| ${ }^{133}$ Sm | 3/2+ | - | $9 \times 10^{-3}$ | $4 \times 10^{3}$ | $3 \times 10^{-3}$ |
| ${ }^{134} \mathrm{Ez}$ | 5 | - | $6 \times 10^{-3}$ | $2 \times 10^{-3}$ | $1 \times 10^{-3}$ |
| ${ }^{135}{ }_{\text {S }}$ m | $512+$ | 2(1) $100^{-4}$ | $1 \times 10^{-4}$ | $2 \times 10^{-4}$ | $1 \times 10^{-4}$ |
| ${ }^{136}$ Ee | 3+ | 9(3)=104 | $4 \times 10^{4}$ | $4 \times 10^{-4}$ | $2 \times 10^{-4}$ |
| ${ }^{137} \mathrm{Gd}$ | $512+$ | (3) | $1 \times 10^{-2}$ | $1 \times 10^{-2}$ | $7 \times 10^{-3}$ |
| ${ }^{139} \mathrm{Gd}$ | $512+$ | - | $9 \times 10^{-4}$ | $1 \times 10^{-3}$ | $7 \times 10^{-4}$ |
| ${ }^{140} \mathrm{~Tb}$ | 6 | 7(3) $10^{-3}$ | $3 \times 10^{-3}$ | $1 \times 10^{-3}$ | $7 \times 10^{-4}$ |
| ${ }^{141}$ EGd | $1 / 2^{+}$ | $3(1) \times 10^{4}$ | $4 \times 10^{-4}$ | $1 \times 10^{-4}$ | $1 \times 10^{-4}$ |
| $141_{14}^{\text {Dy }}$ | 1/2+ | - | $1 \times 10^{-1}$ | $4 \times 10^{-2}$ | $3 \times 10^{-2}$ |
| 141 Dy | 11/2- | - | $1 \times 10^{-2}$ | $5 \times 10^{-3}$ | $3 \times 10^{-3}$ |
| ${ }^{1428} \mathrm{~Tb}$ | $1+$ | - | $3 \times 10^{-4}$ | $3 \times 10^{-4}$ | $2 \times 10^{-4}$ |
| 142 Dy | $0^{+}$ | - | $1 \times 10^{-3}$ | $1 \times 10^{-3}$ | $1 \times 10^{-3}$ |
| ${ }^{143} \mathrm{Dy}$ | 1/2+ | - | $2 \times 10^{-2}$ | $8 \times 10^{-3}$ | $6 \times 10^{-3}$ |
| 143 Dy | 11/2- | - | $4 \times 10^{-4}$ | $3 \times 10^{-4}$ | $2 \times 10^{-4}$ |
| ${ }^{144} \mathrm{Dy}$ | $0^{+}$ | - | $1 \times 10^{-4}$ | $6 \times 10^{-5}$ | $7 \times 10^{-5}$ |

Tule 6.3. (cominmal).

| Precuesar | $\mathrm{J} \times$ | $\mathrm{P}_{\mathrm{F}}$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Experiment | NilsaowRPA | Geom Theory | Comatant |
| ${ }^{144} \mathrm{Ho}$ | 6 | - | $9 \times 10^{-3}$ | $5 \times 10^{-3}$ | $3 \times 10^{-3}$ |
| 1458 Dy | 1/2+ | - | $5 \times 50{ }^{-3}$ | $1 \times 10^{-3}$ | $1 \times 10^{-3}$ |
| 145my | 11/2 | - | $2 \times 10^{-5}$ | $6 \times 10^{-6}$ | $6 \times 10^{6}$ |
| 145 Er | 1/2+ | - | $2 \times 10^{-1}$ | $8 \times 10^{-2}$ | $6 \times 10^{-2}$ |
| 145 Er | 112- | - | $2 \times 10^{-2}$ | 7×10 $0^{-3}$ | $4 \times 10^{-3}$ |
| ${ }^{146} \mathrm{Ho}$ | 6 | - | $2 \times 10^{-3}$ | 1×10 ${ }^{-3}$ | $6 \times 10^{-4}$ |
| 1478 Dy | $1 / 2^{+}$ | 2(1) $10^{-3}$ | $5 \times 10^{-4}$ | $9 \times 10^{-5}$ | $9 \times 10^{-5}$ |
| ${ }^{147} \mathrm{Er}$ | 12+ | 20 | $9 \times 10^{-2}$ | $3 \times 10^{-2}$ | $2 \times 10^{-2}$ |
| ${ }^{147} \mathrm{Er}$ | 11/2- | - | $2 \times 10^{-3}$ | 7×10-4 | $5 \times 10^{-4}$ |
| ${ }^{148} \mathrm{Ho}$ | 6 | 8 (2) $100^{-4}$ | $3 \times 10^{-4}$ | \% $\times 10^{-5}$ | $6 \times 10^{-5}$ |
| ${ }^{149} \mathrm{EEr}$ | 1/2+ | 7(2) $10^{-2}$ | $6 \times 10^{-3}$ | $4 \times 10^{-3}$ | $3 \times 10^{-3}$ |
| 149 mer | 11/2- | 1.8(7) $\times 10^{-3}$ | $1 \times 10^{-5}$ | $2 \times 10^{-5}$ | $2 \times 10^{-5}$ |
| 150 Tm | 6 | $1.2(4) \times 10^{-2}$ | $2 \times 10^{-3}$ | $2 \times 10^{-3}$ | $1 \times 10^{-3}$ |
| 151 FYb | 1/2+ | - | $1 \times 10^{-1}$ | $5 \times 10^{-2}$ | $3 \times 10^{-2}$ |
| 151 myb | 11/2- | - | $1 \times 10^{-3}$ | $1 \times 10^{-3}$ | $9 \times 10^{-4}$ |
| ${ }^{152}$ La | 6 | 1.57) $\times 10^{-1}$ | $4 \times 10^{-2}$ | $2 \times 10^{-2}$ | $1 \times 10^{-2}$ |
| ${ }^{153} \mathrm{Yb}$ | 712 | 8(2) $10^{-5}$ | $2 \times 10^{-4}$ | $1 \times 10^{-4}$ | $1 \times 10^{-4}$ |



Figure 6.1. (a) Delayed proton singles spectrum and (b) positron coincident proton spectrum for ${ }^{149}$ Er. From the enhancement of the structured component in spectrum (b), this structure can be sasigned to the decay of the $1 / 2^{+}$ground state in ${ }^{149} \mathrm{Er}$ to the $\mathrm{O}^{+}$ground sfate in ${ }^{148} \mathrm{Ho}$.


Figure 6.2. (a) Delayed proton singles epectrum and (b) positron coincident proton spectrum for ${ }^{151} \mathrm{Yb}$. From the enhancement of the structured component in spectrum (b), this structure can be assigned to the decay of the $1 / 2^{+}$ground state in ${ }^{151} \mathrm{Yb}$ to the $\mathrm{O}^{+}$ground state in ${ }^{150} \mathrm{Er}$.


Figure 6.3. Delayed proton spectra from the combined 40 and $16 s$ counting cycles for ${ }^{145} \mathrm{Dy}$; (a) proton singles spectrum and (b) positron coincident proton spectrum.


Figure 6.4. Delayed proton spectra from the combined 4 and 1.28 s counting cycles for ${ }^{147} \mathrm{Er}$; (a) proton singles spectrum and (b) positron coincident proton spectrum. The contribution to spectrum (a) from ${ }^{147}$ Dy has been subtracted.



Figure 6.5. Delayed proton spectra for ${ }^{150} \mathrm{Tm}$; (a) proton singles spectrum and (b) positron coincident proton epectrum.


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Figure 6.6. Schematic shell model representation of the decay of even $\mathbf{Z}$, $\mathrm{N}=81$ nuclei. The states shown in bold are at excitation energies of $\sim 4-5 \mathrm{MeV}$ in the emitter. Proton emission from the low-spin excited states dominates due to the slow gamma-decay channel associated with these states.


Figure 6.7. Delayed proton spectra of $\mathrm{N}=81$ precursors as a function of excitation energy in the emitter. Proton separation energies were taken from [Lir76].


Figure 6.8. Graphs used to determine $Q_{E C}-B_{P}$ from the ratio of positron coincident to total proton intensity for (a) ${ }^{147} \mathrm{Er}$ and (b) ${ }^{150} \mathrm{Tm}$.


Figure 6.9. Comparison between experimental half-lives and predicted half-lives from (a) the gross theory of beta decay and (b) from Nilscon/RPA beta-strength function calculations for the delayed proton precursors listed in Tables 4.2 and 5.2.

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[^1]:    ${ }^{2}$ Decay curves are shown in Figures 4.19 to 4.38. When more then one tape cycle was used only the underlined cycle time is presented in the corresponding figure.
    ${ }^{b}$ Best value from all available proton datu.
    c Values from the gross theory [Tak73, Tak88] using the modified Lorenta itrength function.
    ${ }^{d}$ From integrating $\beta$-strength functions from [Ku484] with a Gamow-Teller quenching factor of 0.5 .
    ${ }^{\mathrm{e}}$ Mixture of all delayed protons in this isobar.
    ${ }^{f}$ Data taken from [Nir83b].
    8 Fitted with half-lives for ${ }^{147}{ }^{3} \mathrm{Dy}$ and ${ }^{147}$ EDy from [Sch84b].
    ${ }^{h^{\prime}}$ Half-life is the value from $\beta$-delayed $\gamma$ rays given in $[\mathrm{Nit87}]$ and references cited therein.

