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ON COMPTON PROFILE MEASUREMENTS**

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The Assessment of Geometrical Effects on Compton Profile Measurements

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ABSTRACT

Energy dispersive measurements of Compton scattered x rays for analyses have become important with the development of high efficiency, high energy resolution detectors for 50-200 keV x rays. The Compton scattered x ray peak is an inherently broad peak resulting in part from the momentum distribution of the target electrons, referred to as the Compton profile. Hence, information from the width of the Compton peak can be used to study the momentum distribution. The actual peak width also depends on geometrical and attenuation effects. We have begun to assess the geometrical effects and present some of the results.

THE ASSESSMENT

One of the basic interactions between x rays and electrons is Compton scattering. This scattering is incoherent resulting in a phase change of the x ray along with a transfer of energy. When the target electron is free and stationary, the energy of a Compton scattered x ray can be given by:

$$\left(\frac{E}{E_o}\right) = \frac{1}{1 + \gamma(1 - \cos \theta)} \quad (1)$$

where E is the energy of the scattered x ray, E_o is the energy of the incident x ray, $\gamma = \frac{E_o}{m_o c^2}$, and θ is the scattering angle. The scattering of x rays by bound electrons is greatly complicated by the Compton profile of the bound electrons. The Compton profile is the distribution of electron momenta relative to the momentum of the incident x ray. The scattering then results in a distribution of scattered x-ray energies with respect to the most probable energy, E , of equation 1.

Equation 1 illustrates that there is an angular dependence on the energy of the scattered x rays. Because of this angular dependence, we expect a geometry contribution to the spread in the energy of the observed scattered x rays resulting from the solid angle subtended by the detector. One must be aware of this "geometrical spread" so that it is not attributed to the Compton profile being measured. The contribution from the geometrical spread (ΔE_{geom}) resulting from the detector accepting $\Delta\theta$ about θ with can be determined

with equation 2.

$$\Delta E_{geom} = \frac{dE}{d\theta} \Delta\theta \quad (2)$$

In order to evaluate equation (2) we must either be able to describe the sample in θ space or describe θ in an "easy" geometry. An appropriate geometry was presented in ref. 1 and is reproduced in figure 1. In this geometry the axis of symmetry is the line between the source and the detector. We can then relate the angle of scatter, θ , to r and z through the relationship:

$$\tan \theta = \frac{\frac{r}{b}}{\frac{z}{b}(1 - \frac{z}{b}) - (\frac{r}{b})^2} \quad (3)$$

As was illustrated in ref. 1 we can generate contours of constant scattering angle in the two dimensions of r and z . This is of interest in this work since there is a 1:1 correlation, through equation 1, between the contours of constant scattering angle and contours of constant scattering energy. Drawing the sample in relation to contours of constant scattering energy is useful since it helps to determine the number of contours lines subtended by the sample and hence ΔE .

The R and Z axes are Cartesian and hence we can easily describe two of the three dimensions of the sample in r and z . This approach is quite useful since now we can describe θ in terms of r and z and can describe the dimensions of the sample in terms of Δr and Δz instead of $\Delta\theta$. ΔE is then calculated by differentiating E with respect to r and z .

The third dimension is dealt with by recognizing that we have azimuthal symmetry about the source-detector axis (1,2). Therefore the three dimensional surfaces of constant scattering angle are toroids. The third dimension is dealt with by projecting along the toroidal surface to the R-Z plane while maintaining the same scattering angle.

As an illustration, figure 2 shows a contour plot of constant $\frac{\Delta E}{E}$ for 60 keV x rays as a function of $\frac{r}{b}$ and $\frac{z}{b}$. This plot was generated assuming $\frac{\Delta r}{b} = 0.023$ and $\frac{\Delta z}{b} = 0.03$. These values were selected since they are related to measurements on plexiglass that are being carried out and will be reported separately. These calculations are for plexiglass with a thickness of 1.6mm. These calculations are strictly from geometrical considerations and great care must be used in interpreting their meaning since they are totally independent of the attenuation of the x ray beam. If the geometry of the measurements is such that $z=0$ and the sample

is mounted normal to the incident x ray beam, then $\frac{\Delta x}{b}$ is the sample thickness normalized to b . $\frac{\Delta x}{b}$ is determined by source and detector aperture sizes.

In order to determine the most appropriate geometry, we must balance the geometrical spread with the efficiency of the system. If A_S and A_D are the areas of the source and detector apertures respectively, we can write the efficiency as:

$$\epsilon = \left(\frac{A_S}{r^2 + z^2} \right) \left(\frac{A_D}{r^2 + (b - z)^2} \right) \quad (4)$$

Figure 3 shows a contour plot of isoefficiency as a function of $\frac{r}{b}$ and $\frac{z}{b}$ for a source area, normalized to b^2 , of 0.01 and a detector area, normalized to b^2 , of 0.023.

CONCLUSIONS

We have been working on methods of assessing the contributions to the already naturally broad Compton scatter peak resulting from geometrical effects. This work will be useful in Compton profile measurements so that the broadening of the scatter peak due geometrical effects will not be included in the measurement of the actual Compton profile. This work should also prove useful x ray analytical techniques where the Compton scattered x rays are used as part of the analysis. In analytical techniques it is important to understand the Compton peak in order to accurately measure the peak.

ACKNOWLEDGEMENTS

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REFERENCES

1. A.L. Hanson, G.E. Gigante, and M. Meron, "Contours of Constant Scattering Angle", Phys. Rev. Lett. 61 (1988) 135-137.
2. A. Ghose, "Optimisation and Symmetry in Experimental Radiation Physics", Chapter 1, EUR-10968.

FIGURES

1. The geometry illustrating the source-detector line as the axis of symmetry.
2. A contour plot of $\frac{\Delta E}{E}$ for 60 keV x rays as a function of $\frac{r}{b}$ and $\frac{z}{b}$. This plot was generated assuming $\frac{\Delta r}{b} = 0.023$ and $\frac{\Delta z}{b} = 0.03$.
3. A contour plot of isoefficiency as a function of $\frac{r}{b}$ and $\frac{z}{b}$ for a source area, normalized to b^2 , of 0.01 and a detector area, normalized to b^2 , of 0.023.

Figure 1

Figure 2