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IN A LOW PRESSURE GAS

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NUMERICAL SIMULATION OF SECONDARY ELECTRON ORBITS NEAR
AN ELECTRON BEAM PROPAGATING IN A LOW PRESSURE GAS*

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ABSTRACT

A numerical simulation has been constructed to obtain a detailed, quantitative estimate of the electromagnetic fields generated in a recently-proposed collective accelerator scheme for electrons. The code treats the secondary electrons by particle simulation and the beam dynamics by a time-dependent envelope model. The simulation gives a fully relativistic description of secondary electrons moving in selfconsistent electromagnetic fields. The calculations are made using coordinates t, x, y, z for the electrons and $t, ct-z, r$ for the axisymmetric electromagnetic fields and currents. Code results showing the axial electric field dependence on the configuration of the ultrashort U.V. laser pulse will be given.

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I. OVERVIEW OF A COLLECTIVE ACCELERATOR SCHEME

It has been proposed [1] to use a high-current, medium-energy electron beam as a "charging beam" to accelerate and focus a short, high-energy electron bunch. The accelerator would have very high accelerating field gradients (of order several MeV/cm) with experimentally useful luminosity and high efficiency in transferring energy from the charging beam to the high-energy beam. No quadrupole magnets are required for focusing either the charging beam or the high-energy beam.

Potential energy for the high-energy beam comes from a column of unneutralized ions, produced by the charging beam in three steps. (1) Laser guiding [2] is used to establish the beam axis through the accelerator. (2) Direct beam ionization of a low-pressure high-molecular weight background gas establishes propagation in the ion focused regime (IFR). In this mode, secondary electrons generated by the charging beam are expelled to the accelerator wall by the beam electrostatic field in a time short compared with the pulse length of the charging beam, and the remaining ions focus and partially neutralize the beam electrons. Ion charge densities comparable in magnitude to charging beam densities are produced near the tail of the charging beam. (3) The charging beam pulse is cut off abruptly at the tail, leaving an ion column wake which produces a large positive radial electric field (of order MeV/cm). The proposed accelerator scheme uses this intense radial electric field to generate a negative axial accelerating field of comparable intensity. Before the ions can disperse (which takes on the order of 1 ns), a second laser with a pulse length in the picosecond range creates a photoionization plasma whose electrons rush radially inward, creating a

negative E_z "spike" following the charging beam. The high-energy electron bunch is accelerated in the E_z spike region, which simultaneously has a very large focusing pinch field $E_r - B_\theta$.

II. SELF-CONSISTENT SIMULATION OF THE ACCELERATOR

All beam associated fields, currents, and boundary conditions are assumed axisymmetric. The charging beam and high-energy bunch are described by an envelope model [3], which determines beam radius, energy, and emittance as functions of axial position and time. Secondary electrons are generated through direct ionization in the charging beam body and through photoionization by the guiding laser and by the picosecond laser at the tail of the charging beam. Trajectories of all these electrons are calculated by integration of the relativistic equations of motion for particles in electric and magnetic fields. The ion motion is always non-relativistic and is essentially only radial motion in the potential well of the IFR channel or in the repulsive collective radial electric field after the charging beam passes. Finally, the electromagnetic fields of the beam and secondaries are described by an approximate form of Maxwell's equations in which, with proper choice of beam related coordinates, time appears as a parameter rather than an independent variable (see Eqs. (5-7)).

III. CALCULATION OF ELECTROMAGNETIC FIELDS AND SECONDARY ELECTRON ORBITS

We consider the time evolution of a system consisting of beam associated electromagnetic fields E and B satisfying Maxwell's equations

$$\frac{1}{c} \frac{\partial \vec{E}}{\partial t} = \nabla \times \vec{B} - \frac{4\pi}{c} \vec{J} \quad (1)$$

$$\frac{1}{c} \frac{\partial \vec{B}}{\partial t} = -\nabla \times \vec{E} \quad (2)$$

and N secondary electrons with positions $\vec{r}_j$ and velocities $\vec{v}_j$ satisfying the relativistic equations of motion ($j=1, N$)

$$\frac{d}{dt} \frac{\vec{v}_j}{(1-v_j^2/c^2)^{1/2}} = \frac{e}{m} [\vec{E}(\vec{r}_j, t) + \frac{\vec{v}_j}{c} \times \vec{B}(\vec{r}_j, t)] \quad (3)$$

(The two divergence equations $\nabla \cdot \vec{E} = 4\pi\rho$ and $\nabla \cdot \vec{B} = 0$ are imposed as initial conditions.) The current $\vec{J}$ in Eq. (2) has contributions from secondary and beam electrons and ions.

Suppose the beam propagates in the $+z$ direction. If the currents and boundary conditions are axisymmetric, then all field quantities depend only on $r = (x^2 + y^2)^{1/2}$, z , and t . However, it is convenient to use as independent variables r , ζ , and t , where

$$\zeta = ct - z \quad (4)$$

is the (positive) distance behind the beam front. In the axisymmetric case a closed set of equations may be obtained for the three field components E_r , E_z , B_θ and the two current components J_r and J_z . For beam particles with axial velocities essentially equal to c , $\partial/\partial t \ll c \partial/\partial \zeta$ for any field quantity. In the limit that $\partial/\partial t$ terms are negligibly small, Maxwell's equations become

$$\frac{\partial}{\partial r} E_z = \frac{4\pi}{c} J_r \quad (5)$$

$$\frac{\partial}{\partial \zeta} (E_r - B_\theta) = -\frac{4\pi}{c} J_r \quad (6)$$

$$\frac{1}{r} \frac{\partial}{\partial r} r B_\theta = \frac{4\pi}{c} J_z + \frac{\partial}{\partial \zeta} E_z \quad (7)$$

All fields and currents in Eqs. (5-7) are functions of r, ζ, t . However, t is no longer an independent variable in the field equations but rather a parameter: the fields at time t are produced solely by the currents at time t . Time is, of course, the appropriate independent variable for secondary particle motion. As the particles move the associated currents are generally time-dependent, which injects a parametric time-dependence into the fields via Eqs. (5-7). (Any external accelerating and focusing fields affect the secondary electron motion through Eq. (3), but the external fields are not included in Eqs. (5-7).)

Since the ions are nonrelativistic and respond essentially only to E_r it is inappropriate to treat the ion motion with the relativistic equation of motion Eq. (3) and the complete Maxwell's equations Eqs. (1-2). Accordingly ions are treated by the non-relativistic equation of motion

$$\frac{d}{dt} \vec{r}_j = \frac{q_{ion}}{m_{ion}} \vec{E}_r(\vec{r}_j) \quad (8)$$

where E_r is calculated from the ion and electron charge densities ρ_i and ρ_e using Poisson's equation

$$\frac{1}{r} \frac{\partial}{\partial r} r E_r = 4\pi [\rho_i + \rho_e] \quad (9)$$

IV. SIMULATION DETAILS AND RESULTS

The field equations (5-7) are solved implicitly in r and ζ . To obtain a fully centered differencing scheme for Eqs. (5-7), four separate interlaced grids are used, and non-linear gridding in r is used to increase the number of points near the beam axis. Appropriate boundary conditions on the fields are specified on the beam axis, beam wall, and beam head. The two-dimensional array is protected on all four sides by guard cells so that physical particles always lie in interior cells of the field array and never on edge cells. A completely relativistic particle push [4] valid for arbitrary electric and magnetic fields is used.

For the results shown in this paper, the $\zeta - r$ grid was 101×31 , and secondary electrons were represented by 5000 macro-particles having the electron charge/mass ratio. The code requires around 10 seconds (dependent on graphics requested) of CRAY 1 computer time to advance the complete system 200 time steps.

Figures 1-5 show results of a typical simulation. The ion column had a radius of 1 mm, while the picosecond laser photoionization channel had a radius of 3 mm. The E_z spike is evident in Fig. 1 and lies about 1.5 mm behind the tail of the picosecond laser. All quantities in the figure are in cgs units. The peak E_z spike of around -4000 statvolts/cm corresponds to 1.2×10^8 volts/meter. The high-energy bunch has length 0.5 mm and radius 10 μ m. In this case, oscillations occur after the E_z spike because the high-energy pulse does not load the accelerating E_z field optimally. The photoionization electrons do not lose most of their energy to the high-energy

bunch and therefore oscillate radially about beam axis. For all figures the particles and fields were advanced two hundred time steps for a total of 33 picoseconds.

Work is in progress to optimize the accelerator luminosity and efficiency by varying the beam and photoionization channel profiles by improving the loading of the accelerating field.

FIGURES

Fig. 1. Axial accelerating field E_z in statvolts/cm. (All quantities in Figs. (1-5) are in cgs units.)

Fig. 2. Radial electric field at $r \approx 1$ mm.

Fig. 3. Pinch field $E_r - B_\theta$ at $r = 1$ mm.

Fig. 4. B_θ at $r = 1$ mm.

Fig. 5. Positions of 5000 (macro) electrons after 33 picoseconds.

Figure 1

Figure 2

Figure 3

Figure 4

Figure 5

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