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WIRE CHAMBER REQUIREMENTS AND TRACKING SIMULATION STUDIES FOR TRACKING SYSTEMS AT THE SUPERCONDUCTING SUPER COLLIDER.

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Limitations placed on wire chambers by radiation damage and rate requirements in the SSC environment are reviewed. Possible conceptual designs for wire chamber tracking systems which meet these requirements are discussed. Computer simulation studies of tracking in such systems are presented. Simulations of events from interesting physics at the SSC, including hits from minimum bias background events, are examined. Results of some preliminary pattern recognition studies are given. Such computer simulation studies are necessary to determine the feasibility of wire chamber tracking systems for complex events in a high-rate environment such as the SSC.

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1. INTRODUCTION

Tracking at the SSC at the full design luminosity is expected to be a difficult problem. The limitations imposed by rates and radiation damage are severe. However, the dominant constraint is the combination of occupancy and double-hit resolution. Single events from new physica at the SSC have many (several hundred) charged particle tracks and are further complicated by curling tracks in a magnetic field, photon conversions, hits from events from out-of-time bunch crossings, and multiple interactions within the same bunch crossing [1]. It has not been established how well one can find tracks in complex SSC events. These problems can be addressed through computer simulation studies.

A large solenoid detector based on more-or-less "conventional" technology was discussed at the 1987 Berkeley Workshop [2]. The central tracking system for this detector was envisioned to be built of superlayers consisting of layers of straw tubes. With such a design it should be possible to identify local track segments with a high degree of redundancy even in complex SSC events while at the same time rejecting hits from background. We report here on computer simulation studies of tracking in such a detector.

2. WIRE CHAMBER REQUIREMENTS

2.1. The SSC Environment

I he design luminosity, \mathcal{L} , of the SSC is 10^{33} cm⁻² s⁻¹ with an energy of 40 TeV in the center of mass. The inelastic cross section, σ_i at 40 TeV is expected to be about 100 mb, which gives 10^8 interactions per second at the design luminosity. The bunch separation is 4.8 m, so the time between bunch crossings, t_B , is 16 i.e.



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which leads to an average number of interactions per bunch crossing, n_I , of 1.6 at the design luminosity. Most of these interactions are minimum bias events or low- p_T hard scattering processes in which particle production is expected to be uniform in rapidity with an average charged particle multiplicity per unit of rapidity, n_c , of 7.5 over the pseudorapidity range $|\eta| < 6$ [3]. Figure 1 (from ref. [3]) shows the resulting charged particle flux and annual radiation dose as a function of perpendicular distance from the beam for standard SSC operating conditions.

2.2. Rates and Radiation Damage

Radiation damage and rate limitations impose severe constraints on charged particle tracking detectors at the SSC, as described in several references [1,4]. These constraints are summarized here since they are necessary considerations for the design of any SSC tracking system.

A tracking system for the SSC is assumed to be made up of wires running (nearly) parallel to the beam line. The width, w, of the cell is assumed to be equal to the height, h, and the drift distance, d, is half the cell width. The ionization rate, a, in the gas is assumed to be 100 electrons/cm. The gas gain, G, is assumed to be 2×10^4 .

The flux of particles per unit length (ℓ) of wire in a cell at radius r is given by

$$\frac{d^2n}{d\ell\,dt} = \frac{n_c\,w\,\sigma\,\mathcal{L}\sin\theta}{2\,\pi\,r^2} \quad , \tag{1}$$

where θ is the angle relative to the beam direction. The ionization produced by a charged particle at angle θ is $h\alpha/\sin\theta$, so the ionization per unit length of wire

is independent of θ . Thus the current draw per wire, I, for a layer of wires of length L at radius r is given by

$$I = \frac{n_c w h \sigma \mathcal{L} G e \alpha L}{2 \pi r^2} \quad , \tag{2}$$

where e is the electron charge. A layer of 4 mm wide cells at a radius of 50 cm covering $|\eta| < 1.5$ ($L \approx 213$ cm) will draw 0.52 μ A/wire. The limit of acceptable current draw before breakdown will occur is about 1 μ A/wire.

Wire chamber lifetimes are measured in deposited charge per unit length of wire before a decrease in gain occurs due to the buildup of material on the wires. For the above example, the collected charge over a chamber lifetime of five years (5 × 10⁷ s) would be 0.12 C/cm. Chamber lifetimes of 1.0 C/cm have been measured under very clean laboratory conditions [5], but for the purposes of a realistic experiment, it is probably best to assume a chamber lifetime about an order of magnitude less than this.

Changes in gain for wire chambers have been observed at the level of 10^5 particles/cm-s at a gas gain of $\sim 4 \times 10^5$ due to space charge buildup [6]. The particle flux is given by eq. (1). For the above example, the flux would be 1.9×10^4 particles/cm-s at $\theta = 90^\circ$ where the flux is maximum. Since the gas gain must be much smaller than 4×10^5 because of current draw and lifetime considerations, space charge should not be an important limitation.

The hit rate per wire, R, for SSC central tracking chambers is quite large and is given by

$$R = \frac{n_c \, \eta_{\text{max}} \, \sigma \, \mathcal{L} \, w}{\pi \, \tau} \tag{3}$$

for chambers covering $|\eta| < \eta_{max}$. For the above example, the hit rate per wire would be 2.9 Mhz. Existing electronics can probably handle rates of ~ 10 Mhz.

A very serious limitation for tracking systems at the SSC is occupancy. Since the time between bunch crossings at the SSC is shorter than the resolving time of a typical drift chamber cell, the cell is sensitive to several bunch crossings. The occupancy, O, is given by

$$O = \frac{2n_c \eta_{max} n_I n_B d}{\pi r} , \qquad (4)$$

where n_B is the number of bunch crossings during the resolving time of the cell. n_B is given by

$$n_B = 1 + \inf(t_R/t_B)[2 - t_B/t_R - (t_B/t_R)\inf(t_R/t_B)]$$
, (5)

where t_R is the resolving time of the cell, d/v_D , for drift velocity v_D , and int (x) is the largest integer $\leq x$. Actually, n_B is very close to $t_R/t_B = d/(v_D t_B)$. A 4 mm wide cell (2 mm drift) has a resolving time of 40 ns for a typical drift velocity of 50 μ m/ns and is therefore sensitive to 2.6 bunch crossings. A layer of such cells at a radius of 50 cm and covering a rapidity range $|\eta| < 1.5$ would have an occupancy of 12% per cell. It is guessed that an occupancy of \sim 10% is reasonable, but a realistic answer depends on the effects on pattern recognition and track finding, which are discussed in more detail in sec. 3. The real limitation to occupancy is due to the double-hit resolution because of the loss of information.

The rates given above are based only on particles produced in an interaction and must be increased by a factor of 2-4 because of curling tracks in a magnetic

field, converted photons, and albedo particles leaking out of the front face of the calorimeter. Regardless of pattern recognition considerations, the effects on current draw and chamber lifetime must be carefully considered in the design of any SSC tracking system based on wire chambers.

2.3. Tracking System Considerations

A large solenoid detector based on more-or-less "conventional" technology was discussed at the 1987 Berkeley Workshop [2]. Calorimetry and tracking were located inside a large superconducting solenoid with 2 Tesla field. A schematic view of the Large Solenoid Detector is shown in fig. 2. An examination of the requirements for momentum resolution based on the physics led to the criterion that the sign of the charge for electrons should be measured for $p_T \leq 0.5$ -1.0 TeV/c. The momentum resolution is given by [7]

$$\frac{\sigma_{p_2}}{p_T^2} = \sqrt{\frac{720}{1+5/N}} \left(\frac{\sigma_x}{0.3 \, q \, B \, D^2 \, \sqrt{N}} \right) \quad , \tag{6}$$

where p_T is the transverse momentum of the particle in GeV/c, q is the charge in units of the electron charge, σ_x is the spatial resolution in m, B is the magnetic field in Tesla, D is the track length in m, and N is the number of measurements, assumed to be equally spaced.

The tracking detector design for the Large Solenoid Detector was divided into central tracking ($|\eta| \lesssim 1.2$) and intermediate tracking (1.2 $\lesssim |\eta| < 2.5$). The central tracking system was assumed to be built of straw tubes of radii from 2 to 3.5 mm parallel or nearly parallel to the beam direction. There are many advantages to a straw tube design for tracking at the SSC, as discussed in ref. [1].

The straws are made of aluminized polyester film (Mylar) or polycarbonate (Lexan) with wall thicknesses of about 30 um and are assumed to be at atmospheric pressure. Eight layers of straws are glued together to form superlayers. Within each superlayer the layers are staggered by half the cell width in order to allow hits from out-of-time bunch crossings to be rejected and resolve left-right ambiguities, as illustrated in fig. 3. By dividing the chamber into eight-straw-thick superlayers locally identifiable track segments can be obtained with a high level of redundancy. The track segments can then be linked to form tracks. Every other superlayer is small-angle stereo (~ 3°) in order to measure the coordinate along the wire. Azimuthal cathode pads or strips, included on the outer surfaces of the superlayers, will be useful for bunch assignment and reducing stereo ambiguities. The central tracking system extends radially from 40 cm to 160 cm with 15 superlayers in all. Assuming a spatial resolution of 150 µm, the momentum resolution which can be obtained with such a system is 0.54 p_T (TeV/c) using only wires at radii larger than 50 cm. If the particles are constrained to come from the interaction region, the momentum resolution would improve to 0.26 p_T . The total number of cells is 122,368. The total number of radiation lengths is 8% for a particle traversing the central tracking chambers at 90°. The Large Solenoid Detector central tracking system geometry is summarized in table 1.

In order to provide momentum measurement for $1.2 \lesssim |\eta| < 2.5$, the Large Solenoid Detector included tracking in the intermediate region to take over where the central tracking ends. Two options were considered: planes of parallel wires and radial chambers. The options for intermediate tracking have not yet been worked out in as much detail as the central tracking.

The central and intermediate tracking systems for the Large Solenoid Detector are shown in fig. 4(a), and the momentum resolution as a function of polar angle and rapidity is shown in fig. 4(b).

3. TRACKING SIMULATION

3.1. Simulation of a Central Tracking System for the SSC

The simulation of an SSC central tracking system design was based on that for the Large Solenoid Detector [2], described in sec. 2.3, although it is quite general and can be used for any system of cylindrically oriented sensing elements. All parameters of the detector, such as number of superlayers, number of layers in each superlayer, minimum and maximum radius and length of each superlayer, and azimuthal spacing between sense wires can be specified independently. The parameters used are as shown in table 1, except that we included only the outer 13 superlayers. We used a solenoidal magnetic field of 2 Tesla. The spatial resolution was taken to be 150 μ m. So far, we have simulated only axial wires, that is, wires parallel to the cylinder axis.

We used ISAJET [8] to generate events from interesting physics processes, such as high- p_T two-jet events or Higgs boson production, and from inelastic scattering background, for which we used minimum bias events. We used the GEANT3 [9] general-purpose detector simulation package running on the SLAC IBM 3081 to simulate the interactions of the particles with the detector.

Using GEANT, the particles interact in the 8% of a radiation length of material due to straw tube walls, wires, and gas (the material was assumed to be

distributed uniformly throughout the tracking volume), including photon conversion and multiple Coulomb scattering. The digitizations consist of a wire number and a drift time, calculated from the distance of closest approach of a track to a wire using a drift velocity of 50 µm/ns, for each track in each layer. Background from inelastic scatterings in the same and out-of-time bunch crossings is included by superimposing the digitizations from minimum bias events. The number of bunch crossings is determined by the resolving time of the straw tube cell. At each bunch crossing the number of events to be included is determined from a Poisson distribution with a mean of 1.6 interactions per bunch crossing. Drift times from background events are then corrected for the time difference between the bunch crossing of the background event and the bunch crossing of the event of interest. The double-hit resolution is equal to the cell width, that is, only the earliest hit on a wire is kept. The simulation program is described in more detail in ref. [9].

3.2. Results of the Simulation

We used the simulation described above to study tracking in SSC events. First we examined high- p_T ($p_T > 1$ TeV/c) two-jet events. Figure 5(a) shows such an event in the detector described in sec. 2.3. Figure 5(b) shows an enlargement of the same event in the outer two superlayers in the area of the dense jet. Figure 5(c) shows the earliest hits in the cells for the tracks shown in fig. 5(b). Hits from background events and converted photons are not shown in fig. 5.

Although we have not yet quantified these observations with high-statistics studies, we note:

- Although these events have very dense jets which seem at first to be impossible to resolve, when viewed on the scale of the wire spacings most of the hits appear to lie on identifiable tracks with a 2-Tesla magnetic field, particularly in the outer superlayers.
- 2. Eight layers in a superlayer is probably close to the optimum number because two tracks which are as close as the wire spacings produce hits only on every other layer because of the staggering. Some of these hits may be lost due to nearby curling tracks or background hits. Three tracks within the wire spacing distance would not be resolvable.
- 3. Although a 2-Tesla magnetic field produces curling tracks which obscure the high-pr tracks to some extent, particularly in the inner superlayers, the effect in the outer superlayers is to spread out the tracks and, of course, remove the low-pr tracks from consideration.

We next turned our attention to events from Higgs boson production, $pp \to HX$, with the Higgs decaying to Z^0Z^0 and both Z^{0} 's decaying to e^+e^- or $\mu^+\mu^-$. We used a Higgs mass of 400 GeV/c². Such events allowed us to focus on the measurement of the high- p_T particles from the Higgs decay. Leptons from heavy Higgs decay typically have $p_T > 20$ GeV/c. For these events we used the full simulation as described in the previous Section. An example of a Higgs event in the simulated central tracking system is shown in fig. 6. We generated ~ 200 such events.

The fully-simulated events, including adding digitizations from minimum bias background events and removing digitizations within the double-hit resolution,

had 12,000-30,000 digitizations, as shown in fig. 7(a). The fraction of digitizations from the minimum bias background events is shown in fig. 7(b). On the average 57% of the digitizations were due to background events. For all tracks $(11.6 \pm 0.7)\%$ of the digitizations were lost because of the double-hit resolution, and the loss was about the same in all superlayers. For the leptons from the Higgs decay an average of $(7.3 \pm 0.6)\%$ of the digitizations were lost with the worst losses being in the inner superlayers.

3.3. Pattern Recognition

We began working on pattern recognition algorithms in order to examine our original design goals of finding track segments in superlayers and removing hits from out-of-time bunch crossings. The algorithm for finding track segments was the following:

- 1. In each superlayer we identified "roads" containing hits. There are two parameters which can be varied: the width of the road and the number of hits required on the road. We used a width of five wires and required three or more hits out of eight possible. For isolated tracks one could require more hits; however, if two tracks are close together, as in fig. 5, they will produce hits only on alternate layers and if one is lost due to the double-hit resolution there will be only three hits. The road requirement discriminates against low-pr tracks.
- We required that at least one of the hits be in a layer with the opposite wire stagger from the others so that the left-right ambiguities could be resolved and hits from out-of-time bunch crossings rejected.

3. We required that the hits be consistent with a straight line to within an error and in the process resolved the left-right ambiguities.

Figure 8(a) shows all of the digitizations [11] for the event shown in fig. 6, including those from minimum bias background events. Figure 8(b) shows only those digitizations which are included in segments. Keeping only those digitizations which form segments cleans up the events considerably. Figure 8(c) shows the tracks from the original event in the outer five superlayers in the region around the muon at the lower right. Figure 8(d) shows all of the digitizations in the event in the enlarged region (the digitizations are displayed at the locations of the hit wires). Finally, fig. 8(e) shows only those digitizations in the enlarged region which form track segments; here, the left-right ambiguities have been resolved, the drift times have been converted to distances, and the digitizations are displayed at the positions of closest approach of the tracks to the wires. One can clearly identify the muon track, and most of the extra hits have been removed.

Next, we applied our segment-finding algorithm to the ϵ and μ tracks from Higgs boson decays. We defined two classes of segments: a "good" segment was one with at least five hits from a lepton track and no other hits, and an "OK" segment was one with at least five hits from the lepton track and one hit from another track. The effects of hits from other tracks remain to be studied; we plan to compare measured momenta with produced momenta in future work. With these definitions, we counted the number of segments found for each lepton track.

The distribution of the number of good segments for the e's and μ 's in the Higgs events is shown in fig. 9(a). The corresponding distribution of total (good or OK) segments is shown in fig. 9(b). We see that the lepton tracks from Higgs decay

have an average of about 8 good segments and 10 total segments out of 13 possible. Typically 30-50% of segments were good in the inner superlayers, increasing to almost 80% for the outer superlayers. When OK segments are counted as well, 50-60% of segments are accepted for inner superlayers and over 80% for outer superlayers.

3.4. Future Work

We are planning to continue our tracking simulation studies using the software we have developed. Future work will include simulation of small-angle stereo wires and cathode strips for reconstruction of the direction along the wires; linking of segments, both axial and stereo, to form tracks; studying how much additional information is needed from cathode strips to link the stereo segments properly; a more realistic simulation of electron drift in small-cell or straw tube drift chambers, including the effects of $E \times B$; and conceptual design and simulation of intermediate tracking, as described briefly in sec. 2.3. In addition, we will study tracking for different physics processes, such as new heavy fermions, supersymmetric particles, and high-p_T two-jet events, and begin to develop a realistic design for a tracking system for a complete SSC detector, including other detector components.

4. CONCLUSIONS

We have shown that an SSC tracking system design based on a pattern recognition strategy of finding track segments in superlayers appears to provide a powerful means of finding tracks in complex SSC events, even in an environment of multiple events from several bunch crossings. So far, detailed simulations have verified the concepts developed over several years for SSC tracking detectors. An algorithm

for finding track segments such as that described here could be used in the trigger for high-pr tracks. Depending on the effects on the physics analyses, we might envision making this requirement at the processor level, reading out only the hits that form track segments. Although a great deal of work remains to be done, we are hopeful that an SSC tracking system based on conventional wire chambers will enable us to explore the new physics which awaits us in the SSC regime.

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Table 1
Summary of Large Solenoid Detector Central Tracking System (from ref. [2])

Superlayer Number	Inner Radius (cm)	Module Thickness (cm)	Half Length (cm)	Straw Diameter (mm)	Rapidity Range	Cell Occup ancy (%)
ì	40	2.7	85.2	3.92	1.50	12.1
2	48	2.7	85.2	3.92	!.34	9.1
3	56	2.7	119.0	3.92	1.50	8.8
4	64	2.7	119.0	3.92	1.38	7.0
5	72	4.1	119.0	5.89	1.28	13.0
6	80	4.2	170.0	6.04	1.50	14.5
7	88	4.2	170.0	6.17	1.41	12.9
8	96	4.3	170.0	6.28	1.34	11.6
9	104	4.4	170.0	6.38	1.27	10.5
10	112	4.5	238.5	6.47	1.56	11.9
11	120	4.5	238.5	6.55	1.44	10.9
12	128	4.6	238.5	6.61	1.38	10.0
13	136	4.6	238.5	6.68	1.33	9.3
14	144	4.6	238.5	6.73	1.28	8.5
15	152	4.7	238.5	6.78	1.23	7.9

FIGURE CAPTIONS

- Fig. 1. The charged particle flux and annual radiation dose as a function of perpendicular distance from the beam under standard SSC operating conditions (from ref. [3]).
- Fig. 2. Schematic view of the Large Solenoid Detector from the 1987 Berkeley Workshop [2].
- Fig. 3. Layers of straw tubes in a superlayer with every other layer staggered by the straw tube radius. A single in-time track will appear as a series of hits on the wires on alternate sides of the track. The left-right ambiguity is easily resolved locally. A track from an out-of-time bunch crossing will produce hits which are displaced from possible tracks by at least 16 ns in drift time.
- Fig. 4. (a) Schematic view of central and intermediate tracking systems in the Large Solenoid Detector. (b) Momentum resolution as a function of polar angle and rapidity in the Large Solenoid Detector for the 13 superlayers at radii > 50 cm in the central tracking system and including intermediate tracking (from ref. [2]).
- Fig. 5. (a) Two-jet event from ISAJET with $p_T > 1$ TeV/c in a 2-Tesla magnetic field in a detector of the geometry of the Large Solenoid Detector. There are 223 particles with $p_T > 200$ MeV/c and $|\eta| < 1.5$. Converted photons and background from minimum bias events are not shown. (b) Enlargemer* of the event in the outer two superlayers in the area of the dense jet at the top of the detector. (c) Earliest hit in each cell for the tracks shown in (b).
- Fig. 6. Example of a Higgs event in the simulated central tracking system. The leptons from the Higgs decay are indicated by the heavier lines. Converted photons and other interactions with the material are included.

- Fig. 7. (a) Total number of digitizations in Higgs events, including digitizations from minimum bias background events. (b) Fraction of digitizations from the minimum bias background events. The mean is 0.572 ± 0.011.
- Fig. 8. (a) All of the digitizations for the Higgs event shown in fig. 6, including those from minimum bias background events. (b) Digitizations for this event which are included in track segments, as defined in the text. (c) Tracks from the original event in an enlarged region in the outer five superlayers in the region around the muon at the lower right. (d) All of the digitizations in the event in the enlarged region of (c) (the digitizations are displayed at the locations of the hit wires). (e) Only those digitizations in the enlarged region which form track segments. Here, the left-right ambiguities have been resolved, the drift times have been converted to distances, and the digitizations are displayed at the positions of closest approach of the tracks to the wires.
- Fig. 9. (a) Distribution of the number of good segments out of 13 possible for the e's and μ 's from the Higgs decays. (b) Distribution of the number of total segments (good or OK) for the leptons from the Higgs decays.

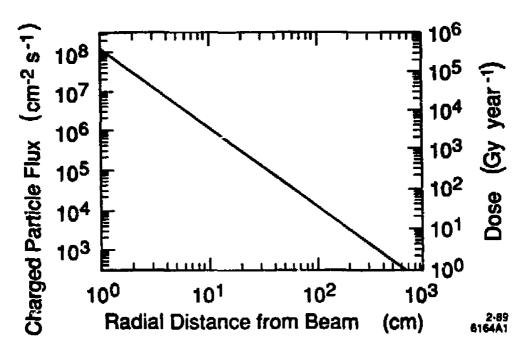


Fig. 1

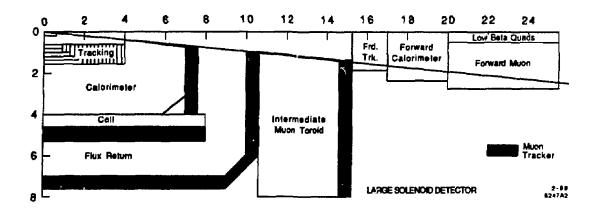


Fig. 2

Fig. 3

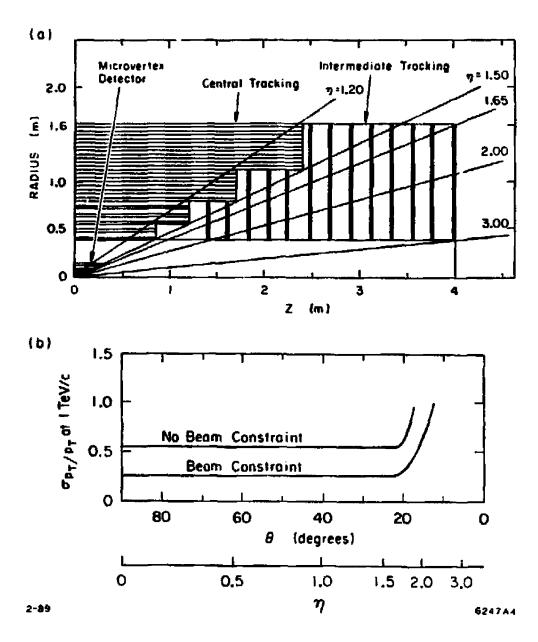


Fig. 4

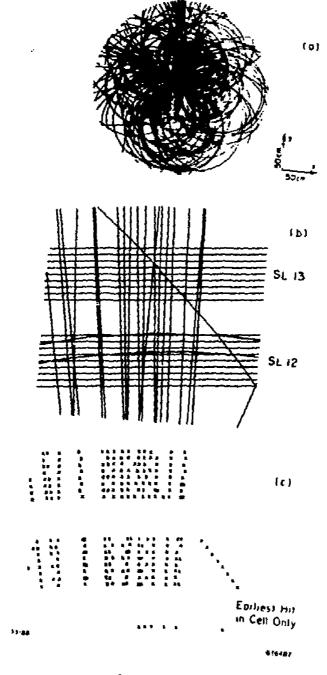
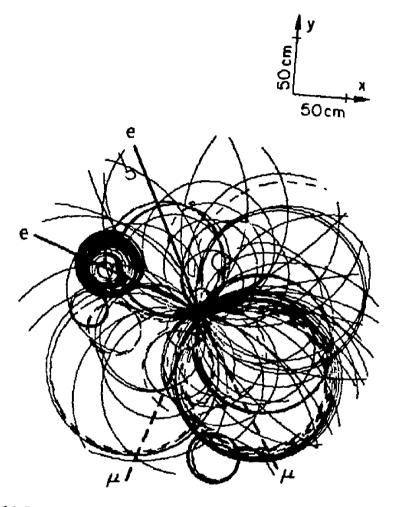


Fig. 5



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Fig. 6

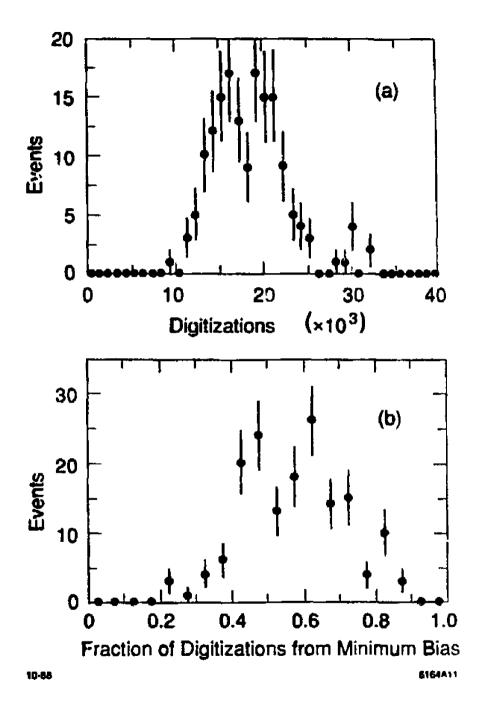


Fig 7

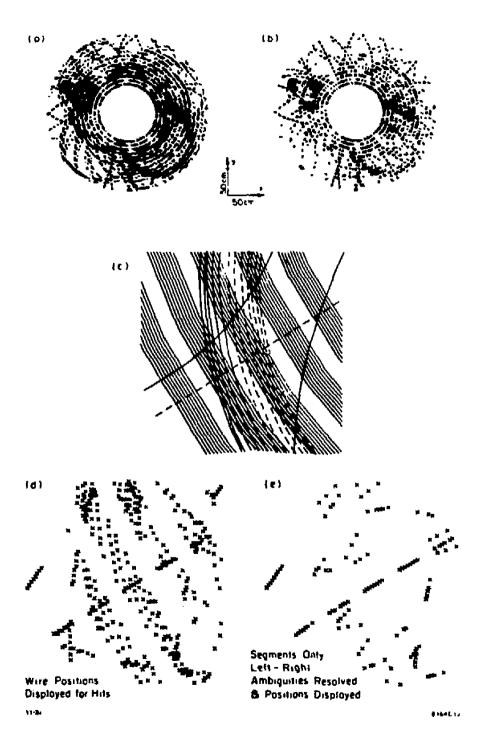


Fig. 8

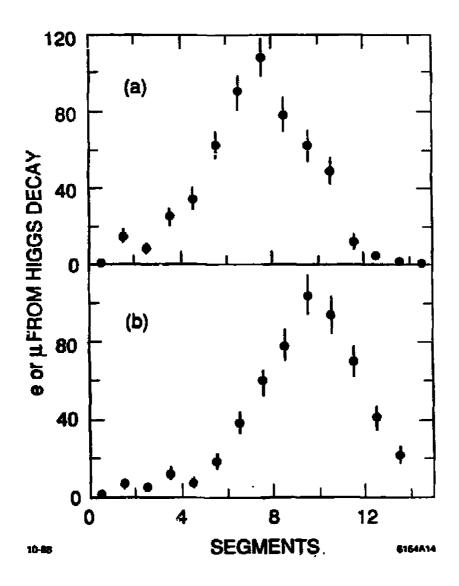


Fig. 9

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