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DESIGN CHARTS FOR VACUUM PLATES

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INTRODUCTION

This paper presents design charts to aid designers in selection of a wall thickness for flat plates used on vacuum vessels.

These charts display both stress and deflections for a given wall thickness and plate dimensions. Since both stress and deflection are plotted on a single graph, one may select the proper wall thickness quite readily.

Precautions for use of the charts are also presented.

DESCRIPTION OF DESIGN CHARTS

A recurring design problem encountered by vacuum vessel designers is the selection of a plate thickness for a vacuum vessel wall.

Often a plate thickness is selected based upon what "looks about right". In many applications, the designer must consider deflections as well as the stress. The writer has prepared design charts for circular plates and rectangular plates under a pressure differential of one atmosphere.

The edge constraint for plates may be either fixed or simply supported. Most practical designs have edge conditions that are neither fixed nor simply supported, therefore, the designer should check both the fixed edge chart and the simply supported edge chart to make certain that a safe design has been obtained.

The equations used have all been selected from R. J. Roark.⁽¹⁾ Each chart shows a shaded area. In this shaded area the plots are not completely valid. The plates behave as diaphragms in this area and the deflections and stresses are somewhat less than shown. In other words, if one uses the chart as is, it would result in a safe design in that the stresses would be below those shown.

If one must select extremely thin plates for a chamber, a more intricate design study should be made based upon diaphragm stresses rather than use these charts.

All charts assume a Young's modulus of 30×10^6 psi. While the stresses shown on the plots are valid for every Young's moduli, the deflections are not. When using a material with a different Young's modulus, one must multiply the chart deflections by the following ratio:

$$\frac{E_{30 \times 10^6}}{E_{\text{material}}}$$

(1) Roark, R.J. Formulas for Stress And Strain

The rectangular plate charts show "safe" values. In other words, the plotted values are for b to a ratio of zero. Most designs have b to a ratios considerably more favorable than this. The plotted values can be corrected by using the chart in the upper left hand corner. Stresses and deflections may be reduced, in the case of square plates by as much as a factor of 3. However, it is pointed out that failure to use these "correction factors" results in a conservative design.

PRECAUTIONS

In summary, the following precautions should be noted:

1. One should check both the fixed edge and simply supported edge charts prior to selecting a wall thickness.
2. For Young modulus, other than 30×10^6 psi, apply the following correction factor for the deflections shown:

$$\frac{E_{30 \times 10^6}}{E_{\text{material}}}$$

3. No Young's modulus correction is required for stresses.
4. In the use of rectangular plates, one may reduce the stresses and deflections by using the correction chart in upper left hand corner.
5. In unusual applications, where extremely thin windows are to be used, one should consult diaphragm equations.

6. The plotted values are valid for deflections up to $y = 1/2t$. They are conservative for greater deflections.
7. The chart shows deflections at the plate center. In some applications, deflections at other locations cause the loss of O-ring sealing pressures or similar problems. In such applications, the designer should do further analysis.

The following examples demonstrate the use of these charts:

Example 1:

Select plate thickness for circular plate 9" diameter, fixed edges $E = 30 \times 10^6$. Maximum allowable stress is 20,000 psi.

Enter chart $d = 9"$

Select $t = 1/8"$

Read stress 15,000 psi

Read deflection .019"

Example 2:

Select plate thickness for 7" x 10" plate. Rectangular plate. Fixed edges. $E = 30 \times 10^6$. Maximum allowable stress is 20,000 psi.

Enter correction chart at $\frac{b}{a} = \frac{7"}{10"} = .7$

Read $C_s = .85$

$C_d = .8$

Enter large chart at $b = 7"$

Select $t = 1/8"$

Read stress $22,500 \times C_s = 19,125$ psi

Read deflection $.016 \times C_d = .013"$

I wish to acknowledge the efforts made by Alexander Baron in checking the accuracy of these charts.

DEFLECTION "y" INCHES
(for $E = 30 \times 10^6$ p.s.i. only)

ORIGINATOR	NAME	DATE
DRAWN	N ENGLER	4-20-71
CHECKED		
APPROVED

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Max. $y = \frac{3W(m^2 - 1)d^2}{64\pi E m^2 t^3}$ maximum deflection at center

Max. $s = \frac{3W}{4\pi t^2}$ maximum stress at edge.

$W = \frac{w\pi d^2}{4}$

w = unif. applied load (= 14.7 P.S.I.)

d = diameter — inches

t = plate thickness — inches

$m = \frac{1}{1 - \nu}$ reciprocal of Poisson's ratio

E = mod. of elasticity (= 30×10^6 P.S.I.)

REF: "FORMULAS FOR STRESS & STRAIN" R.J. Roark, 4th edition

In the shaded area, stress and deflection are less than shown due to Peripheral Stresses.

**STRESSES AND DEFLECTIONS
CIRCULAR PLATES, EDGES FIXED
ONE ATMOSPHERE PRESSURE DIFFERENTIAL**

UNCORRECTED DEFLECTION "y" INCHES
(for $E = 30 \times 10^6$ p.s.i. only)

	NAME	DATE
ORIGINATOR	J. O'NEARA	4-20-71
DRAWN	N. ENGLER	4-20-71
CHECKED	L. J. [signature]	5-3-71
APPROVED	S. [signature]	3-7-71

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Max $y = \frac{1422 w b^4}{E t^3 (1 + 22 \frac{b^3}{a^3})}$ = maximum deflection at center

Max $s = \frac{75 w b^2}{t^2 (1 + 162 \frac{b^3}{a^3})}$ = maximum stress at center

- w = unit applied load (= 14.7 PSI.)
- b = short span — inches
- a = long span — inches
- t = plate thickness — inches
- E = mod of elasticity (= 30×10^6 PSI.)

REF: "FORMULAS FOR STRESS & STRAIN," R. J. Roark, 4th edition

Plots are valid for $\frac{b}{a} = 0$. For other ratios multiply values by correction factor. SEE CORRECTION CHART

In the shaded area, stresses and deflections are less than shown due to Peripheral Stresses.

STRESSES AND DEFLECTIONS
RECTANGULAR PLATES, ALL EDGES SUPPORTED
ONE ATMOSPHERE PRESSURE DIFFERENTIAL