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FUTURE ete- LINEAR COLLIDERS AND BEAM-BEAM EFFECTS

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### 1. Introduction

As designers of the high energy accelerators of the future, the first question we must ask is, "What do the particle physicists want?" It is a fundamental fact of nature that the cross sections for the production of interesting events in electronpositron collisions in the TeV energy range tend to fall-off inversely as the square of the particle energy.2 The luminosity for two colliding beams, either in a storage ring or from a linear collider, is defined as the event rate divided by the cross section. In order to keep the event rate at an accoptable level, the luminosity must therefore increase approximately as the square of the beam energy. In Table 1 the luminosities which follow this scaling are shown for four collider energies. The first row gives the energy and luminosity, at turn-on and after potential luminosity up-grades, for the Stanford Ligear Collider (SLC). The next three rows give parameters for future and far future linear colliders. The machines that have been suggested for more detailed parametric studies in general fall into the three energy and luminosity categories shown in the table.

Table I. Present and Future High Energy Linear Colliders

Energy	Luminosity	Total Length (3 linus) in km			
Per Linae	(cm <sup>-2</sup> sec <sup>-1</sup> )	G=20 MV/m	G=200 MV/m	G=1 GV/m	
50 GaV	6 × 10 <sup>29-30</sup>	5	0,5	0.1	
350 GeV	·10 <sup>52</sup>	25	3.5	0.7	
1-1.5 TeV	1022	100-150	10-18	2-3	
5 TeV	1054	500	50	10	

Numerous concepts, ranging from conventional to highly exotic, have been proposed for the acceleration of electrons and positrons to very high energies. For any such concept to be viable, it must be possible to produce from it a set of consistent parameters for one of these "benchmark" machines. In this paper our attention will be directed to the choice of parameters for a collider in the 300 GeV energy range, operating at a gradient on the order of 200 MV/m, using X-band power souces to drive a conventional disk-loaded accelerating structure. These RF power sources, while not completely conventional, represent a reasonable extrapolation from present technology.

The choice of linac parameters is strongly coupled to various beam-beam effects which take place when the electron and positron bunches collide. We summarise these beam-beam effects in the next section, and then return to the RF design of a 650 GeV center-of-mass collider.

# 1. Summary of Beam Beam Effects

## LUMINOSITY

The luminosity for the collision of two gaussian bunches is given by

$$L_1 = N^2 f_r H_D / 4\pi A , \qquad (2.1)$$

where N is the number of particles per bunch,  $f_r$  is the bunch collision rate,  $H_D$  is the pinch enhancement factor due to disruption (see next section) and  $A = \sigma_x \sigma_y$  is the beam area. The area is in turn related to the normalized emittance  $\epsilon_n = \epsilon_{ng} = \epsilon_{ng}$  by

$$A = \epsilon_n \left(\beta_n^* \beta_n^*\right)^{1/2} / \gamma \quad , \tag{2.2}$$

where  $\gamma$  is the ratio of electron energy to rest energy and  $\beta_z^*$  and  $\beta_z^*$  are the beta functions at the collision point.

If a single bunch is accelerated during each linec pulse, then fr is also the linac repetition rate and the luminosity is the single bunch luminosity  $\mathcal{L}_1$ . The situation is more complex if. rather than single bunches, a train of b bunches is accelerated during each linac pulse. There are then several options for producing bunch collisions. Successive bunches can be switched to collide at different interaction points, as shown at (a) in Fig. 1. The luminosity summed over all interaction regions is then  $\mathcal{L}_{sum} = 5\mathcal{L}_1$ . A second option is to collide bunches at an angle a, as shown at (b) in Fig. 1, where a is less than the transverse to longitudinal aspect ratio  $\sigma_x/\sigma_x$ . Only corresponding bunches in each of the two bunch train will collide. Noncorresponding bunches will miss each other, although if the collisions are nighly disruptive bunches at the rear of the train will pass through debris from earlier collisions. For this option the total luminosity at the single interaction point is  $\mathcal{L}_{tot} = \delta \mathcal{L}_1$ . A third option is to collide a train of bunches head on as shown at (c) in Fig. 1. There are 2b-1 interaction points spaced a distance  $\Delta s/2$  apart, where  $\Delta s$  is the bunch spacing. If the collisions are sufficiently nondisruptive, then the luminosity summed over all interaction point is  $\mathcal{L}_{sum} = b^2 \mathcal{L}_1$ . The luminosity is different at each interaction point, the luminosity at the mth interaction point being given by

$$\mathcal{L}_{m} = \mathcal{L}_{1} \times \{1, 2, \dots b-1, b, b-1, \dots 2, 1\}$$

If the collisions are highly disruptive, then the only effective collisions take place at the central interaction point, where  $\mathcal{L}_{tot} = b\mathcal{L}_1$ .

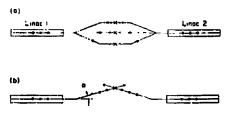


Fig. 1. Possible collision modes for bunch trains in a linear collider

(c)

<sup>\*</sup>Work supported by the Department of Energy, contract DE-AC03-76SF00515.

When an electron bunch collides with a positron bunch, the collective field from the particles in one beam acts like a lens to focus the particles in the opposing beam toward the axis. For particles near the the axis in a gaussian bunch, the focal length of this lens is  $\sigma_x/D_z$  where  $\sigma_x$  is the bunch length and D is the disruption parameter defined as

$$D = D_{\theta} = \frac{r_0 N o_s}{\gamma A} \left(\frac{2R}{1+R}\right) \quad . \tag{2.3}$$

Here  $A=\sigma_X\sigma_y$ ,  $R=\sigma_X/\sigma_y\geq 1$  is the aspect ratio and  $\tau_0=2.83\times 10^{-15}$  cm is the classical electron radius. If the disruption parameter is on the order of one the bunches pinch substantially as they pass through each other, reducing the effective transverse bunch area and enhancing the luminosity. The vahancement factor  $H_D$  has been computed from a simulation by R. Hollebeck,  $^{2,3}$  and is shown in Fig. 2. For a flat beam  $\{R>>1\}$  one would expect the pinch enhancement for a round beam, as shown by the dashed line in Fig. 2. Agreement with simulation results is seen to be reasonable. For intermediate values of R an approximate analytic expression for  $H_D(R)$  in terms of  $H_D(R=1)$  is given in Ref. 4.

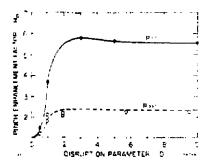


Fig. 2. Pinch enhancement factor as a function of disruption parameter for round and flat beams. Points shown are simulation results from Ref. 3.

#### BEAMSTRAHLUNG.

An electron or positron moving in the collective field of the oncoming beam emils synchrotron radiation, in this case called beamstrahlung. In classical synchrotron radiation, the power spectrum for the emission of photons of energy has increases as w1/3 for photons of low energy to a peak near the critical energy at  $\hbar \omega_c = 3h\gamma^2 eB/2mc$ . Above the critical energy the spectrum lain oil exponentially. By integrating the power spectrum over all frequencies, the total rate at which energy is radiated is obtained as  $P \sim \gamma^2 B^2$ . As either energy or magnetic field strength is increased, the critical energy will also increase until at some point has exceeds your?. One photon at the critical energy would then have to carry away more than the entire energy of the electron. A correct quantum calculations shows, however, that the radiation spectrum is suppressed for he > \gammamc2, as shown in Fig. 3. The total radiated power is reduced by an amount corresponding to

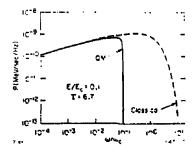


Fig. 3. Synchrotron radiation spectrum for a 5 TeV electron moving in a magnetic field of 30 MG. Dashed and solid lines show the difference between classical and quantum calculations.

the area between the solid and dashed lines. Define a scaling parameter T by

$$T = \frac{2\hbar\omega_c}{3\gamma mc^2} = \frac{\gamma B}{B_c} , \qquad (2.4)$$

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where  $B_c=4.4\times 10^{13}$  G. In the classical regime (T << 1) the total radiated power is proportional to  $T^2\sim \gamma^2 B^2$ , while for T>>1 the power is proportional to  $T^{2/3}$ . In the quantum limit, the radiated power is reduced compared to the classical radiation rate by the factor 0.556  $T^{-4/3}$ . This reduction factor,  $H_T$ , is plotted as a function of T in Fig. 4.

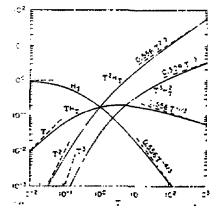


Fig. 4. Several useful functions of the quantum beamstrahlung parameter T

The preceeding discussion was valid for a single electron moving in a constant magnetic field. When two gaussian bunches collide, particles see a range of collective fields from zero on the axis to a maximum near one sigma in the transverse direction. Using the power spectrum for classical synchrotron radiation, Bassetti and Gygi-Hanney<sup>6</sup> have calculated the average energy loss per particle, divided by the incident energy, to be

$$\delta_{cd} = \frac{F_1 r_0^3 \gamma N^2}{g_s A} \left[ \frac{4R}{(1+R)^2} \right] , \qquad (2.5)$$

where  $F_1 = 0.22$  is a form factor independent, to within a few percent, of the aspect ratio R.

It is expected that the radiation will be significantly reduced when single particle values for T at the position of maximum transverse field in the opposing bunch are on the order of one. In a breamstrahlung simulation, R. Noble<sup>7</sup> has shown that the reduction in energy loss per particle, averaged over the entire bunch, can be expressed by the single particle reduction factor  $H_T$  if an effective T, denoted by T, is defined in terms of the bunch parameters as

$$\overline{T} = \frac{F_2 r_0 \lambda_c \gamma N}{\sigma_f A^{1/2}} \left[ \frac{2R^{1/2}}{1+R} \right] H_D^{1/2} . \qquad (2.6)$$

Here  $\lambda_c = 3.86 \times 10^{-11}$  is the Compton electron wavelength divided by  $2\pi$  and  $F_2 = 0.43$  is a form factor determined from the simulation. A factor  $H_D^{1/2}$  is included to take plach enhancement into account. Thus the beamstraklung parameter for colliding gaussian bunches can be expressed as

$$\delta = \delta_{e\ell} H_D H_T(\overline{\Upsilon})$$
 , (2.7)

where again a factor HD is included to take pinch into account. CENTER-OF-MASS RMS ENERGY SPREAD

For particle physics, the center-of-mass rms energy spread,  $\sigma_W$ , is of more importance then the average energy loss per electron calculated after the bunches have collided. The relation between  $\delta$  and  $\sigma_W/W$  for gaussian bunches depends only on  $\overline{\mathbf{T}}$ . In the classical limit ( $\overline{\mathbf{T}} \ll 1$ )  $\sigma_W/W = 0.55\,\delta^{1/2}$ . These contrasting limits on  $\sigma_W/W$  are a consequence of the strong variation in average number of photons,  $N_p$ , emitted per electron as a function of  $\overline{\mathbf{T}}$ . In the classical limit,  $N_p = 2.1\,\delta/\overline{\mathbf{T}}$ , while in the quantum limit  $N_p = 3.9\,\delta$ . Thus in the classical limit,  $\sigma_W/W = 0.12$  for  $\delta = 0.30$ . For  $\delta = 0.30$  in the quantum limit, however,  $N_p = 1.1$  and  $\sigma_W/W = 0.30$  (see Ref. 8).

# SUMMARY AND COMBINED RELATIONS

From Eqs. (2.1), (2.5) and (2.6) we note that  $\mathcal{L}_1$ ,  $\delta_{c\ell}$  and  $\overline{T}$  all depend on  $\mathbb{R}^3/A$ . This makes it possible to combine these parameters in various useful ways. In Table II the beambeam parameters and some of these combinations are written in practical units. Of special importance are the functions  $\bar{T}H_T \sim \delta(f_r/\mathcal{L}_1)^{1/2} \sim A^{1/2} \, \delta/N$  and  $\bar{T}^2H_T \sim E_0\delta/\sigma_z$ . These function are plotted in Fig. 4. Also plotted is  $T^3H_T^2 \sim \delta^2/A^{1/2}D$ .

A final beam parameter of interest is the beam power,  $P_b = \gamma mc^2 N f_r$ . In the practical units of Table II,

$$P_b(MW) = 1.6 \times 10^{-2} \{N E_0 b f_c\}$$
 (2.16a)

$$= 21.7 \left\{ \frac{bE_0 \mathcal{L}_1 A^{1/2} T H_T}{B_D^{1/2} b} \right\} \left[ \frac{2R^{1/2}}{1+R} \right] . \qquad (2.16b)$$

Table II. Beam-Beam Expressions in Practical Units

E <sub>0</sub> (TeV)	σ <sub>σ</sub> (anm)	N (10 <sup>10</sup> )
£ <sub>1</sub> (19 <sup>23</sup> /cm <sup>2</sup> /sec)	Α (μπ.) <sup>3</sup>	f. (He)
		-

$$\mathcal{L}_{1} = 8.0 \times 10^{-6} \left\{ \frac{N^{3} f_{r} H_{D}}{A} \right\} \tag{2.8}$$

$$D = 1.44 \times 10^{-1} \left\{ \frac{N\sigma_{s}}{E_{c}A} \right\} \left[ \frac{2R}{1+R} \right]$$
 (2.9)

$$\delta = 9.9 \times 10^{-4} \left\{ \frac{R^2 E_0 H_D H_T}{\sigma_g A} \right\} \left[ \frac{4R}{(1+R)^2} \right]$$
 (2.10)

$$T = 9.2 \times 10^{-8} \left\{ \frac{NE_0 H_0^{1/2}}{\sigma_c A^{1/2}} \right\} \left[ \frac{2R^{1/8}}{1+R} \right]$$
 (2.11a)

$$= 3.27 \left\{ \frac{E_0 \mathcal{L}_1^{1/2}}{\sigma_* f_*^{1/2}} \right\} \left[ \frac{2R^{1/2}}{1+R} \right]$$
 (2.11b)

$$\hat{T}H_T = 2.6 \times 10^{-2} \left\{ \frac{f_*^{1/2} \delta}{L_*^{1/2}} \right\} \left[ \frac{1+R}{2R^{1/2}} \right]$$
 (2.12)

$$\tilde{T}^2 H_T = 8.5 \times 10^{-8} \left\{ \frac{E_0 \delta}{\delta} \right\}$$
 (2.13)

$$N = 9.2 \left\{ \frac{A^{1/2} \xi}{H_{\pi}^{1/2} \hat{T} H_{T}} \right\} \left[ \frac{1 + R}{2R^{1/2}} \right]$$
 (2.14)

$$DH_D^{1/2} = 1.13 \times 10^{-9} \left\{ \frac{\delta^2}{\Upsilon^5 H_{Z,A}^{1/2}} \right\} \left[ R^{1/2} \right]$$
 (2.15)

#### 3. RF and Structure Parameters

Energy in an electromagnetic field delivered to some sort of structure is re-uired to accelerate charged particles. The structure can be a metallic waveguide, such as the traditional disk-loaded accelerator structure, an open resonator, a wake-field "transformer," or in a general sense even a plasma. Also required is a driver to convert power from the AC line into the electromagnetic energy delivered to the structure. The driver can be a microwave tube, a laser, or a driving banch as in the wake field accelerator. A conceptual diagram of a generalized driver and accelerating structure is shown in Fig. 5.

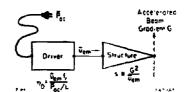


Fig. 5. Conceptual diagram of an accelerator.

A figure of merit for the accelerating structure is the efficiency with which it converts average input electromagnetic energy per unit length,  $u_{\rm em}$ , into average accelerating gradient G. The dimension of  $G^2/u_{\rm em}$  is that of an inverse capacitance, or elastance, per unit length. A figure of merit for the driver is the efficiency with which it converts well plug energy into electromagnetic energy delivered to the structure. In this paper we focus on the case of a conventional linac in which the driver is a microwave tube (plus pulse compression) and the structure

is a conventional disk-loaded structure. The parameters  $\eta_D$  and  $\delta$  are, however, more generally useful for comparing the various exotic and conventional acceleration schemes that have been proposed for high energy colliders.

Consider a SLAC-type  $2\pi/3$ -mode disk-loaded traveling wavestructure. As the beam aperture radius <u>a</u> is increased, we find that the group velocity  $v_s$  increases approximately as  $a^{1/4}$ , and the elastance  $s \equiv G^2/u$ , where u is the stored energy per unit length, decreases. The unloaded Q, on the other hand, is approximately independent of the beam aperture radius. Thus

$$a/\lambda \approx 8.42 \times 10^{-2} \left[ v_g (m/\mu s) \right]^{2/4}$$
 (3.1)

$$s\left(\frac{\Omega}{ps-m}\right) \approx \frac{13.24 \left[f(GHz)\right]^2}{1+0.216 \left[v_0(m/\mu s)\right]^{1/2}}$$
 (3.2)

$$T_0(\mu s) \equiv \frac{2Q_0}{\omega} \approx 7.1 [f(GHz)]^{-3/2}$$
 . (3.3)

The above relations are strictly valid only for constant impedance (constant beam aperture) structures. For a constant gradient structure, in which the beam aperture decreases along the structure in order to maintain a constant accelerating field, the situation is more complex. However, if the attenuation parameter (defined by  $\tau \equiv T_f/T_0$  where  $T_f$  is the filling time) is not too large, then an effective group velocity  $\theta_g \equiv L_s/T_f$  can be used in the above expressions to give approximate average values for the structure. The smallest beam aperture at the end of the structure will then be less than that given by Eq. (3.1) by a factor  $e^{-\tau/4}$ .

Because of losses (and the spatial variation in the accelerating field in the case of a constant impedance structure), the effective stored energy in the structure at the end of the filling time is less than the input energy by the structure efficiency factor \( \eta\_i \). For a constant gradient structure

$$\eta_s = \frac{1 - e^{-2\tau}}{2\tau} \quad . \tag{3.4}$$

Note that structure figure of merit, as defined in Fig. 5, is  $s = s\eta_s$ . The peak input power to the structure is now

$$\hat{P}_s = \frac{G^2 L_s}{n_s T_{\ell S}} \quad . \tag{3.5}$$

RF pulse compression can be used to reduce the required peak power using the binary power multiplication (BPM) scheme of Z. D. Farkas.<sup>10</sup> The peak power gain for an n-stage BPM is

$$M = 2^n \eta_s , \qquad (3.6)$$

where  $\eta_c$  is the compression efficiency given by

$$\eta_i = 2^{-n} \left\{ \left[ 1 + \exp\left(-2\alpha T_f\right) \right] \right.$$

$$\left. \left[ 1 + \exp\left(-4\alpha T_f\right) \right] \dots \left[ 1 + \exp\left(-2^n \alpha T_f\right) \right] \right\} .$$

Here  $\alpha$  is the delay line attenuation per unit time. If each RF source feeds  $N_e$  accelerating structures, then the peak source power will be

$$\hat{P}_{k} = \frac{N_{s} L_{s} G^{2}}{M \eta_{s} T_{f} s} . \qquad (3.8)$$

The average source power will be  $\vec{P}_k = 2^a T_f f_* \hat{P}_k$ , and the total AC "wall plug" power per lipac of length  $\hat{L}$  is

$$\overline{P}_{ac} = \frac{N_k \overline{P}_k}{\eta_{rf}} = \frac{f_r L G^2}{\eta_{rf} \eta_c \eta_a s} = \frac{f_r L G^2}{\eta_D s} \quad . \tag{3.9}$$

Here  $N_k=L/N_aL_a$  is the total number of RF sources per linac,  $\eta_{ef}$  is the efficiency for the conversion of wall plug power to RF power,  $\eta_D=\eta_{ef}\eta_c$  is the overall driver efficiency and  $\delta=s\eta_c$  is the net structure elastance. It is also useful to know the average power dissipation per unit length of accelerating structure, given by (constant gradient case)

$$\frac{\overline{P}_{\text{diso}}}{L_{\star}} = \frac{2\tau f_{\star}G^2}{4} \quad . \tag{3.10}$$

As a design example, consider two X-band linars (f = 11.4 GHz) driven by microwave tubes, each with a peak output power of 150 MW and a pulse length of 1.8 µs. Let each accelerating structure be 1.0 m in length, assume four stages of pulse compression, and let each RF source feed four accelerating sections. Thus the filling time is  $T_f = 1.8 \,\mu\text{s}/16 = .112 \,\mu\text{s}$ , and the other structure parameters given in Table III follow. If the attenuation of the delay lines in the pulse compression system is  $\alpha = 0.10$  nepers per microsecond (3 in I.D. overmoded copper pipe), then the compression efficiency is  $\eta_c = 0.85$ , the peak power multiplication factor is M = 13.6, and the gradient G = 186 MV/m follows from Eq. (3.8). The energy of each linac is then 325 GeV. If we assume a repetition rate of 120 Hz and an efficiency  $\eta_{ef} = 0.55$  for conversion of AC power to RF power, then the total wall plug power for both linacs is 50 MW. The RF source parameters are also summarized in Table III.

TABLE III. RF and Structure Parameters for a 325 + 325 GeV Linear Collider

STRUCTURE PARAMETERS		
Length per Linac L	1.75	km
Length Each Section L,	1.0	m
Frequency fr	11.4	GHz
Filling Time Tf	112	20
Internal Time Constant To	184	ED.
Attenuation Parameter 7	0.61	
Average Group Velocity 0,	8.9	m/µe
Ū <sub>α</sub> / c	0.0296	
Structure Efficiency 7,	0.58	
Internal Elastance	1050	V/pC-m
Effective Elastance 3	610	V/pC-m
Disk Hole Radius a	3.82	mm
RF SOURCE PARAMETERS		
Source Spacing N.L.	4.0	m
Total Number of Sources	438	/linac
Peak Source Power   Pk	150	MW
Pulse Length Tk	1.8	μa
Repetition Rate fr	120	Ha
Average Source Power Pk	32	ŁW
Pulse Compression Efficiency 7c	0.85	
Structure Average Power Dissipation	4.8	kW/m
Assumed RF efficiency ye	0.55	
Wall Plug Power Par	25	MW/linas
Net Driver Efficiency nD	0.47	•
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Several important collider parameters depend upon the interaction between the beam and the accelerating structure. The single bunch efficiency  $\eta_b$ , is important because it is a rough measure of the energy apread within the bunch produced by longitudinal wake fields. Also, the bunch-to-bunch energy droop between bunches in a bunch train is  $\Delta E/E \approx \frac{1}{2} \eta_b$ . The single bunch efficiency is

$$\eta_b = \frac{enG}{v} = \frac{eNs}{G} 
= 1.6 \times 10^{-3} \left\{ \frac{N(10^{10}) s(10^{12} \text{ V/C-m})}{G \text{ (MV/m)}} \right\} .$$
(4.1)

The single bunch energy spread can only be obtained exactly by a calculation using the longitudinal deita-function wake potential for the accelerating structure in question, as is explained in Ref. 11. For a short bunch sitting on the crest of the accelerating wave, the energy spread is given roughly by  $(\Delta E/E)_{th} \approx \frac{1}{2}B(\sigma_x)\eta_{th}$  where B is an enhancement factor taking into account the effect of higher-order longitudinal crodes (see Ref. 11). For example,  $B \approx 3$  for a 1 mm bunch in the SLAC structure. However, this energy spread can be reduced by adjusting the relative phase of the bunch with respect to the crest of the accelerating wave, such that the slope of the RF wave tends to compensate for the slope of the wake potential within the bunch. In this way the energy spread can be residuced by at least a factor of 3. A conservative estimate is then  $(\Delta E/E)_{th} < \eta_0/2$ .

In order to obtain a high luminosity with a reasonable repetition rate and number of particles per bunch, a very small transverse emittance will be required. Significant growth in emittance as the bunch travels through the linar can lead to an unacceptable degradation in luminosity. A number of effects care produce such an emittance growth, but there is space here to focus on just one representative effect. The quadrupoles in the focusing lattice of the linar will jitter randomly in transverse position due to high frequency components in ground motion arising from both ratural and man-made causes. The excursions off-axis by the head of the bunch will produce a transverse wake which wiggles the tail of the bunch. The growth in transverse beam size is given by 12

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$$\frac{\Delta z}{\sigma_f} = \frac{\sqrt{2} \tau_0 N W_{\perp} \gamma d_{rms}}{\pi^{3/2} \epsilon_n^{1/2} (d\gamma/dz)^{3/2}} . \tag{4.2}$$

Here  $W_{\perp}$  is the transverse wake potential in cgs units (cm<sup>-3</sup>),  $d_{rms}$  is the rms jitter amplitude, and  $\sigma_f$  is the brach size at the end of the linac. For short bunches the transverse wake can be estimated from  $W_{\perp} = 2\sigma_s W_{\perp}^s$ , where  $W_{\perp}^s$  is the slope of the delta function transverse wake potential. For the SLAC structure ( $\lambda = 10.5$  cm, a = 1.165 cm), this slope is  $W_{\perp}^s = 2.1$  cm<sup>-4</sup> and scales as

$$W_{\perp}^{I} \sim \omega^{4} (a/\lambda)^{-3.6}$$
 (4.3)

The emitance grawth due to magnet jitter can be reduced substantially by introducing an energy apread between the head and the tail of the bunch (Landau damping)<sup>13</sup>. However, Eq. (4.2) provides a measure of the severity of transverse wake field effects and is useful for scaling.

### 5. A 325 GeV Collider Example

Although it may seem like the backward way to do it, the RF parameters for our example collider were calculated first in Sec. 3 before the beam-beam parameters were considered. The RF frequency was chosen a priori, and the peak source power and pulse length were chosen to give the gradient necessary to reach 300° GeV in a linac 1.75 km in length. The repetition rate was fixed at 120 Hz to give a reasonable AC wall plug power. The energy and repetition rate, together with a luminosity per bunch of 1032/cm2/sec and a beamstrahlung parameter  $\delta = 0.3$ , fix  $\Upsilon = 0.16$  and  $\sigma_s = 0.6$  mm from Eqs. (2.12) and (2.13). The logical next step would be to fix  $\eta_t$  at a reasonable value of 1-2%, determine N through Eq. (4.1) and then A and hence  $\epsilon_n$  from Eq. (2.14). We instead fix  $\epsilon_n$  at  $3 \times 10^{-6}$ m-rad (one-tenth the SLC damping ring emittance), choose  $\beta$ = 1 mm, find  $A^{1/2} = 0.07 \mu m$  and show that N, D and  $\eta_0$ are reasonable. From Eq. (2.15) and Fig. 2 we find D = 5.4,  $H_D = 5.5$ . From Eq. (2.14) it follows that  $N = 9.4 \times 10^9$ , and from Eq. (4.1) \$\eta\_b = 0.85\%\$. These results are summarized in Table IV. Following a similar procedure for a flat beam with R = 10, we obtain the results shown in the second row of Table IV. The last column gives  $\sigma_W/W$  obtained from data in Ref. 7.

Transverse emittance growth was checked by inserting these parameters in Eq. (4.2). The result is  $\Delta x/\sigma_f \approx 0.06$  for the round beam case assuming  $d_{rms} = 10^{-2} \, \mu \text{m}$ . The high gradient and larger than normal disk hole radius help to keep emittance growth tolerable.

Table IV. Beam-Beam Parameters for Callider Example

$E_0$ =325 GeV		leV	•		$\mathcal{L}_{\parallel} = 10^{32} / \text{cm}^2 / \text{sec}$				
$\delta = 0.3$					ć <sub>n</sub> :	m (	$(\sigma_z^*\sigma_y^*)^{1/2}=0.07~\mu\mathrm{m}$		
R	Ť	Ит	σ, [mm]	D	$H_D$	N (10 <sup>10</sup> )	A (1W)	7. (%)	ow/W
1	0 16	0.55	0.61	5.4	5.6	0.94	59	0 84	0.14
ı۸	D 49	0.30	0.12	29	24	1.43	AG	13	0.18

#### 6. Some Conclusions

For the next generation of linear collider  $(E_0 \ge 300 GeV)$ , there is an advantage in working at a higher gradien: than the SLC gradient of 20 MV/m in order to keep the total length of accelerating structure within reasonable bounds. In the preceding sections we have developed the design of a collider with a gradient on the order of 200 MV/m using conventional RF technology at 11 GHz (although some might argue that X-band microwave tubes delivering 150 MW are far from conventional). The same technology could be extended to build a 1 TeV collider with a luminosity of 1022 cm-2 see-1, with a wall plug power on the order of 100 MW, if we can learn how to collide a train of 10 or 20 bunches spaced several nanoseconds apart. In the case of a 5 TeV collider, the machine becomes uncomfortably long even with a gradient of 200 MV/m (see Table I), and the wall plug power would approach the GW range. A higher RF frequency with a nonconventional RF power source (e.g., two beam accelerator) may be required, or perhaps such a machine will be based on a completely different acceleration technology derived from one of the many exotic concepts that have been proposed.14

# References and Notes

- B. Richterin Laser Acceleration of Particles, Malibu, CA, 1985, C. Joshi and T. Katsouleas, eds., AIP Conf. Proc. No. 130, (Am. Inst. Phys., New York, 1985), pp.8-22.
- 2. R. Hollebeck, Nucl. Instrum. Methods 184, 333 (1981).
- R. Hollebeek and A. Minten, SLAC Internal Note CN-302 (1985).
- P. Wilson in Larer Acceleration of Particles, Maiibu, CA, 1985, C. Joshi and T. Katsouleas, eds., AIP Conf. Proc. No. 130, (Am. Inst. Phys., New York, 1985), p.562.
- See for example T. Erber et al., Proc. 12th Int. Conf. on High Energy Accelerators, Fermilab, August 1983, p.372;
   also Thomas Erber, Rev. Mod. Phys. 38, 626 (1966).
- M. Bassetti and M. Gygi-Hanney, LEP-Note-221, CERN, Geneva (1980).
- Robert J. Noble, SLAC-PUB-3871 (1986). See also K. Yokoya, KEK Preprint 85-53 (October 1985, also submitted to Nucl. Instrum. Methods), for an analytic calculation of beamstrahlung in the quantum regime.

 For N<sub>p</sub> ≈ 1 higher moments in the electron energy distribution became comparable with σ<sub>W</sub>, and this parameter is then of dubious usefulness.

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- The use of elastance for the ratio G<sup>2</sup>/u was suggested by 2. D. Farkas. See IEEE Trans. Nucl. Sci. NS-32, No. 5, 3225 (1985).
- Z. D. Farkas, MTT Special Transactions Issue on New and Future Applications of Microwave Systems, to be published in October 1986. Also SLAC-PUB-3662.
- See for example P. B. Wilson in Physics of High Energy Accelerators, F. R. Huson and M. Month, eds., AIP Conf. Proc. No. 87, (Am. Inst. Phys., New York, 1982), Secs. 10.2 and 12.3; also SLAC-PUB-2884.
- 12. A. Chao and R. Ruth, private communication.
- See for example K. L. F. Bane, IEEE Trans. Nucl. Sci. NS-32, No. 5, 2389 (1985); also SLAC-PUB-3670.
- For a review of proposed acceleration concepts see articles in Laser Acceleration of Porticles, Molibu, CA, 1985, C. Joshi and T. Katsouless, eds., AIP Conf. Proc. No. 130, (Am. Inst. Phys., New York, 1985).