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MASTER

ELECTRON TRANSFER REACTIONS OF FERROCENE

Ph.D. Thesis Submitted to Iowa State University, August 1971

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Electron transfer reactions of ferrocene

by

John R. Pladziewicz

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TABLE OF CONTENTS

	Page
INTRODUCTION	1
EXPERIMENTAL SECTION	8
Reagents	8
Equipment	20
Methods, Procedures, and Data Treatment	22
RESULTS	36
Formal Electrode Potential Measurements	36
Iron(III)-Ferrocene Reactions	42
Ferrocene-Ferricenium Electron Transfer Reactions	48
Chromium(VI)-Ferrocene Reaction	49
INTERPRETATION AND DISCUSSION	64
Ferrocene-Ferricenium Ion Reactions	64
Iron(III)-Ferrocene Reactions	75
Ferrocene-Chromium(VI) Reaction	81
APPENDIX	83
Exchange Rate Solution to the Marcus Equation	83
BIBLIOGRAPHY	88
ACKNOWLEDGMENT	91

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ABSTRACT

State Univ.

Kinetic studies have been carried out on electron-transfer reactions of eight substituted ferrocenes. The reactions are of three types:

- (a) electron transfer between different ferrocenes, as

- (b) oxidation of ferrocenes by iron(III), as

- (c) chromium(VI) oxidation of ferrocene, as

In the first group, rate measurements were made on 22 of the possible 28 combinations. The rate law corresponds to the process in (a), with rate constants $4.2 - 150 \times 10^6 \text{ M}^{-1} \text{ sec}^{-1}$ at 25° in 1:1 v/v H_2O -n-propanol $\mu = 0.05 \text{ M}$ $\text{Ba}(\text{ClO}_4)_2$. These 22

reaction rates were found to correlate quite well with the Marcus equation. From this correlation exchange rates for the ferricenium ion pairs were computed.

The second reaction, which was studied for $(\pi\text{-C}_5\text{H}_5)(\pi\text{-(3)-1,2-C}_2\text{B}_9\text{H}_{11})\text{Fe(II)}^-$ as well as for the ferrocenes, has the rate law $d[\text{Fe}^{2+}]/dt = k[\text{Fe}^{3+}][\text{FeCp}_2]$, with k between 5.5×10^2 and $4.9 \times 10^6 \text{ M}^{-1} \text{ sec}^{-1}$ in 1:1 v/v H_2O -tetrahydrofuran, $\mu = 1.00 \text{ M}$ (LiClO_4) at 25° . The rates of these reactions were also interpreted in terms of the Marcus equation. For these reactions observed rates were substantially lower than rates calculated from the Marcus equation.

For the third reaction only the oxidation of ferrocene was studied and has the rate law $-d[\text{Cr(VI)}]/dt = k[\text{FeCp}_2][\text{HCrO}_4^-][\text{H}^+]$. The value of k at 25°C in 1:1 v/v H_2O -acetone $\mu = 1.00 \text{ M}$ (LiClO_4) is $1.01 \pm .04 \times 10^4 \text{ M}^{-2} \text{ sec}^{-1}$. A mechanism with three one electron transfer steps is proposed with the first step being rate determining.

INTRODUCTION

Attempts to measure electron transfer rates between various ferrocenes and ferricenium ions have been limited to studies of the ferrocene-ferricenium exchange¹ rate (1,2,3)

Eq. 1.

The methods used in earlier studies have included isotopic exchange (1,3) and nuclear magnetic resonance techniques (2). Only the study by Stranks (3), utilizing isotopic exchange combined with rapid mixing and quenching techniques at very low temperature in methanol, was successful.

Of interest to this study is the measurement of the rates of a family of related electron transfer reactions²,

Eq. 2:

¹Throughout this study the terminology "exchange" will be reserved for electron transfer reactions between species differing only by oxidation state, a process which results in no net observable chemical change.

²The convention will be adopted that all of the reactions are written in the thermodynamically favored direction, in addition rate constants and equilibrium constants will be expressed in k_{ij} and K_{ij} notation respectively, where i, j refer to the numbers 1-8 assigned the ferrocenes in Table 1.

and calculations concerning the rates of the corresponding exchange reactions, Eq. 3.

The electron transfer reactions (Eq. 2), unlike the exchange reactions (Eqs. 1 and 3), lead to net chemical reaction. Consequently, the kinetics can be evaluated by analysis using uv-visible spectrophotometry, for example, without resorting to the rapid quenching and efficient separation techniques required in isotopic exchange studies of these very rapid reactions.

In addition to this group of reactions, two additional kinetic studies have been carried out: (1) a study of the oxidation of ferrocene and certain of its derivatives by iron(III) ions as in Eq. 4, and (2) the oxidation of ferrocene by chromium(VI) as in Eq. 5.

Except for the one study by Stranks on Eq. 1, no data are in the literature concerning the rates or mechanisms of any of these three classes of reaction. With reference to the work by Stranks a second-order rate for exchange was found with a rate constant of $1.7 \pm 0.4 \times 10^6 \text{ M}^{-1} \text{ sec}^{-1}$ at -70°C in methanol. The very high rate of reaction made the measurement quite difficult; the mean half-time for exchange was $2 \pm 0.5 \text{ msec}$ at -70°C at $1 \times 10^{-4} \text{ M}$ reactant concentrations, while the most rapid mixing and quenching time attainable was 3 msec. The present work has been carried out in mixed aqueous-organic solvents, and in every case appropriate stability tests for the reagents have been performed.

The rate constant for reaction 1 ought to be measurable by proton nmr line-broadening measurements. However, in attempts to do so it was found (2) that the transverse relaxation time of the paramagnetic ferricenium ion was much greater than the average lifetime of ferricenium ion with respect to electron transfer. Hence line broadening was controlled by the transverse relaxation process and only a lower limit could be placed on the specific rate for exchange of $\geq 1 \times 10^5 \text{ M}^{-1} \text{ sec}^{-1}$.

The motivations and goals of this work can be summarized

as follows:

(a) To study the oxidation-reduction kinetics of ferrocene, which has been quite neglected. Aside from the exchange study referred to above, only the oxidation of ferrocene by iodine (4), and the reduction of ferricenium ion by Sn(II) (5,6) have been examined kinetically. It is possible that the paucity of data for the ferrocene-ferricenium ion reactions results from the instability of the ferricenium ions in solution (2), and the difficulty involved with studying reactions that are so rapid (3). However, with judicious choice of compounds and conditions some of these studies can be made (these choices are discussed in the experimental section of this thesis).

(b) In recent years several theoretical models have been developed for electron transfer reactions in homogeneous solution (7). Of these the most often applied model has been that developed by Marcus (8) for outer-sphere electron transfer reactions. In this development Marcus has shown that many of the quantities which are difficult to estimate for an "a priori" calculation of rate constants cancel when comparing a series of related reactions. As a result Eq. 6 is obtained,

$$k_{ij} = (k_{ii} \cdot k_{jj} \cdot K_{ij} \cdot f_{ij})^{\frac{1}{2}} \quad (6)$$

$$\text{with } \ln f_{ij} = (\ln K_{ij})^2 / 4 \ln(k_{ii} \cdot k_{jj} / Z^2)$$

where k_{ij} is the rate constant for electron transfer, k_{ii} and k_{jj} are the corresponding electron exchange rate constants, and Z is the collision frequency of two uncharged molecules ($10^{11} \text{ M}^{-1} \text{ sec}^{-1}$). A number of electron transfer reactions have been shown (9-12) to satisfy Eq. 6. These studies have included a series of oxidation-reduction reactions involving iron complexes such as $\text{Fe}(\text{OH}_2)_6^{2+,3+}$, $\text{Fe}(\text{CN})_6^{4-,3-}$, $\text{Fe}(\text{phen})\text{-(CN)}_4^{2-,1-}$, $\text{Fe}(\text{phen})_2(\text{CN})_2^{0,1+}$, $\text{Fe}(\text{dipy})_3^{2+,3+}$, $\text{Fe}(\text{dipy})_2(\text{CN})_2^{0,1+}$, $\text{Fe}(\text{dipy})(\text{CN})_4^{2-,1-}$, and a series of substituted tris-1,10-phenanthroline iron complexes. It was of interest in this study to determine if Eq. 6 was also satisfied by the electron transfer reactions of ferrocene, and to see if Eq. 6 could then be used in a predictive sense to calculate as yet unmeasured rate constants. To provide a fair test of Eq. 6 for a series of related reactions the series should cover the widest range of k_{ij} and K_{ij} values possible.

(c) With the hope of learning about the detailed mechanism(s) for electron transfer in the ferrocene compounds several points were investigated. First, to learn if steric requirements were of importance various size substituents

were used; methyl, *n*-butyl, phenyl, etc. Second, to determine what effect the geometry of the cyclopentadiene rings play, two "pseudo-ferrocenes" prepared originally by Hawthorne et al. (13) were reacted, see Figure 1. Third, since it is known that ferricenium ion associated with anions such as triiodide (14) and chloride (15) in solution, and since it appears that association may stabilize ferricenium ion relative to ferrocene (16), some reactions were studied under conditions of added chloride. Also the possibility of a "bridging"¹ mechanism was investigated by including studies on iodoferrocene and chloromercuriferrocene.

¹This is not meant to imply a conventional halide ion inner-sphere type of bridge; but rather the possibility of a weak association between an electronegative substituent like I on one ferrocene with the positive charge associated with the iron atom on another ferricenium ion.

Figure 1. Structures of ferrocene (a) and two "pseudo-ferrocenes" π -cyclopentadienyl- π -(3)-1,2-dicarbollyliron(II) ion (b) and bis- π -(3)-1,2-dicarbollyliron(II) ion (c).

EXPERIMENTAL SECTION

Reagents

Ferrocene derivatives

All the compounds used in this study were previously known and were either purchased or prepared as described in the literature. Ferrocene, $\text{Fe}(\text{C}_5\text{H}_5)_2$, (Alfa Inorganics) was purified by vacuum sublimation. 1,1'-Dimethylferrocene, $\text{Fe}(\text{C}_5\text{H}_4\text{CH}_3)_2$, (Alfa Inorganics) was recrystallized twice from water-ethanol (1:1, v/v). 1,1'-Di-n-butylferrocene, $\text{Fe}(\text{C}_5\text{H}_4\text{C}_4\text{H}_9)_2$, and n-butylferrocene, $\text{Fe}(\text{C}_5\text{H}_5)(\text{C}_5\text{H}_4\text{C}_4\text{H}_9)$, (Alfa Inorganics) were used without further purification. Phenylferrocene, $\text{Fe}(\text{C}_5\text{H}_5)(\text{C}_5\text{H}_4\text{C}_6\text{H}_5)$, was prepared and purified by the method of Weinmayr (17). Iodoferrocene, $\text{Fe}(\text{C}_5\text{H}_5)(\text{C}_5\text{H}_4\text{I})$, was prepared and purified as described in the literature (18a). Chloromercuriferrocene, $\text{Fe}(\text{C}_5\text{H}_5)(\text{C}_5\text{H}_4\text{HgCl})$, (Research Organic Chemical) was recrystallized once from acetone. Hydroxymethylferrocene, $\text{Fe}(\text{C}_5\text{H}_5)(\text{C}_5\text{H}_4\text{CH}_2\text{OH})$, (Research Organic Chemical) was recrystallized twice from "Skelly B".

Characterization of ferrocene derivatives

The identity and purity of the ferrocene compounds were established by melting point (solids), or refractive index (liquids), and by visible-uv spectrophotometry in comparison

with literature values (17-27). In a few cases elemental analyses were also obtained. These results are summarized in Table 1. The NMR spectrum of each compound was also determined and in each case was in agreement with the assumed identity.

The uv-visible spectra of all of the ferrocene derivatives (28a), have been obtained and appear in Table 2; a complete spectrum is given for ferrocene in Figure 2. In addition each ferrocene derivative can be oxidized by iron(III) perchlorate to give the corresponding ferricenium ion (Eq. 4), whose spectrum can then be determined.

The uv-visible spectrum of each ferricenium ion derivative (28b) is also given in Table 3; a complete spectrum of ferricenium ion is shown in Figure 2.

All of the ferrocene derivatives, with the exception of iodoferrocene, are quantitatively oxidized by iron(III) in aqueous n-propanol and dilute perchloric acid (ca. 1×10^{-3} M). Hence, each ferrocene derivative can be analyzed by a spectrophotometric titration using a standard iron(III) solution at the appropriate wavelength in the 600-700 nm region. In this region only the ferricenium ions absorb; ferrocene, iron(III), and iron(II) have negligible absorbance. In every case the

Table 1. Characterization of ferrocene derivatives

#	Substituted ferrocene	Melting point (solids) or refractive index (liquids)			Elemental analysis	
		obsd.	lit.	ref.	obsd.	calcd.
1	1,1'-di-(CH ₃)	34-5°	34-5° 37-9°	-- ^a -- ^c	C: 66.64 ^b H: 6.52	67.32, 6.59
2	1,1'-di-(<u>n</u> -C ₄ H ₉)	$n_D^{20}=1.548$	1.5511	-- ^d		
3	<u>n</u> -C ₄ H ₉	$n_D^{20}=1.5755$	1.5701 1.5795	-- ^e -- ^f		

^aRef. (19).

^bAnalysis by Ames Lab Analytical Group I.

^cRef. (20).

^dRef. (23).

^eRef. (21).

^fRef. (22).

Table 1. (Continued)

#	Substituted ferrocene	Melting point (solids) or refractive index (liquids)			Elemental analysis	
		obsd.	lit.	ref.	obsd.	calcd.
4	Ferrocene	173-4°	174°	--g	C: 64.22 ^h H: 5.38	64.56, 5.42
5	HgCl	194-6°	194-6°	--i		
6	CH ₂ OH	79-80°	81-2°	--j	C: 60.95 ^h H: 5.52	61.15, 5.60
7	C ₆ H ₅	110-111°	109-110° 110-111°	--k --l	C: 73.29 ^h H: 5.46	73.31, 5.38
8	I	43-4°	44-5°	--m		

^gRef. (18b).

^hAverages of results from Chemalytics, Inc., Tempe, Arizona and Ames Lab
Analytical Group I, Iowa State University.

ⁱRef. (24).

^jRef. (25).

^kRef. (26).

^lRef. (17).

^mRef. (27).

Table 2. U.V.-visible spectra of the ferrocene derivatives

#		$\lambda_{\max} \text{nm} (\epsilon, \text{M}^{-1} \text{cm}^{-1})$	Ref.
1	1,1'-di-(CH ₃)	240 (4140) sh ^a 325 (80) 435 (104)	--b
2	1,1'-di-(<u>n</u> -C ₄ H ₉)	240 (4,400) sh ^a 325 (89) 435 (112)	--b
3	<u>n</u> -C ₄ H ₉	240 (3,600) sh ^a 325 (58) 450 (100)	--b
4	Ferrocene	240 (3,280) sh ^a 325 (52) 440 (96)	--b
5	HgCl	240 (6,840) sh ^c 448 (160)	--b
6	CH ₂ OH	240 (4,940) sh ^c 325 (100) sh 435 (100)	--b
7	C ₆ H ₅	238 (16,300) sh ^c 278 (10,400) 433 (344)	--b
		237 (16,100) 277 (9,900) 447 (322)	--d

^aSpectrum taken in 1:1 v/v water-ethanol.^bThis work.^cSpectrum taken in 1:1 v/v water-n-propanol.^dRef. (17).

Table 2. (Continued)

#	Substituted ferrocene	$\lambda_{\max} \text{nm}(\epsilon, \text{M}^{-1} \text{cm}^{-1})$	Ref.
7	C_6H_5	238 (17,600) 278 (10,600) 310 sh 447 (330)	-- ^e
8	I	240 (5,200)sh ^c 280 (2,300)sh 430 (188)	-- ^b

^eRef. (28a).

Table 3. U.V.-visible spectra of the ferricenium ion derivatives

#	Substituted ferricenium ion	$\lambda_{\max} \text{nm} (\epsilon, \text{M}^{-1} \text{cm}^{-1})$	Ref.
1	1,1'-di-CH ₃	257 (15,200) ^a 285 (10,600)sh 650 (332)	-- ^b
2	1,1'-di- <u>n</u> -C ₄ H ₉	258 (15,400) ^a 285 (11,200)sh 650 (380)	-- ^b
3	<u>n</u> -C ₄ H ₉	255 (15,400) ^a 280 (10,600)sh 625 (352)	-- ^b
4	Ferricenium ion	254 (16,500) ^a 280 (10,000)sh 380 (325)sh 618 (450) 255 (~17,000) 617 (420)	-- ^b -- ^c
5	HgCl	254 (15,900) ^d 280 (10,700)sh 623 (504)	-- ^b
6	CH ₂ OH	255 (15,200) ^d 285 (9,800)sh 627 (400)	-- ^b

^aSpectra taken in 1:1 v/v water-ethanol.^bThis work.^cRef. (28b).^dSpectra taken in 1:1 v/v water-n-propanol.

Table 3. (Continued)

#	Substituted ferricenium ion	$\lambda_{\max} \text{nm}(\epsilon, \text{M}^{-1} \text{cm}^{-1})$	Ref.
7	C_6H_5	235 (15,500) ^d	--b
		250 (14,200) ^{sh}	
		293 (11,400)	
		750 (521)	
8	I	244 (10,250) ^d	--b
		255 (11,400)	
		280 (9,000) ^{sh}	
		700 (?)

Figure 2. Spectrum for ferrocene (broken line) and ferricenium ion (solid line) in 1:1 v/v water-ethanol

spectrophotometric titration for ferrocene agreed within 1% of the weighed amount.

Stability of ferrocene and ferricenium solutions

Stock solutions of the ferrocene derivatives were prepared in several solvents (n-propanol, acetone, 95% ethanol) and in each case the solution was stable towards oxidation or decomposition over extended periods of time (up to 6 months). This is not a general property of ferrocene compounds, however, and is dependent on the derivative and solvent.

Ferricenium ion derivative solutions are generally much less stable than the corresponding ferrocene compound (2,18b). In water-n-propanol, (1:1, v/v), $\mu = 0.050$ (maintained with barium perchlorate), however, all of the ferricenium ion derivatives studied here were stable (i.e., u.v.-visible spectra did not change by more than 3-5%) for at least 30 min. This is sufficient time to carry out any of the studies done here. Except for phenylferricenium and iodo-ferricenium ions, the ferricenium ion derivatives were stable for even longer periods of time. It was generally found that as the oxidation potential of the ferrocene derivative became more negative the stability of the ferricenium ion derivative decreased. Hence, 1,1' dimethylferricenium and ferricenium ions were found to be

more stable than phenylferricenium and iodoferricenium ion solutions. Many ferrocene derivatives (methylferrocenoate, $\text{Fe}(\text{C}_5\text{H}_5)(\text{C}_5\text{H}_4\text{COOCH}_3)$, ferrocenecarboxylic acid ($\text{Fe}(\text{C}_5\text{H}_5)(\text{C}_5\text{H}_4\text{COOH})$), ferrocenyl acetic acid, $\text{Fe}(\text{C}_5\text{H}_5)(\text{C}_5\text{H}_4\text{CH}_2\text{COOH})$, 1,1'-di-iodoferrocene, $\text{Fe}(\text{C}_5\text{H}_4\text{I})_2$, N,N-dimethylaminomethyl ferrocene, $\text{Fe}(\text{C}_5\text{H}_5)(\text{C}_5\text{H}_4\text{CH}_2\text{N}(\text{CH}_3)_2)$, benzolyferrocene, $\text{Fe}(\text{C}_5\text{H}_5)(\text{C}_5\text{H}_4\text{COC}_6\text{H}_5)$, and ferrocenecarboxaldehyde, $\text{Fe}(\text{C}_5\text{H}_5)(\text{C}_5\text{H}_4\text{CHO})$) were also found to be oxidized by iron(III) to the blue ferricenium ion derivatives. In each case the blue ferricenium ion solution then decomposed rapidly (3-300 sec for the compounds cited) making it unsuitable for the studies of interest here. All of the compounds having ferricenium ion solutions too unstable to study have oxidation potentials near or higher than iodoferrocene (29,30).

π -(3)-1,2-Dicarbollyliron(III) and iron(II) derivatives (31)

Bis- π -(3)-1,2-dicarbollyliron(III) and bis- π -(3)-1,2-dicarbollyliron(II) were prepared as their tetramethylammonium salts: $[(\text{CH}_3)_4\text{N}][\pi\text{-(3)-1,2-B}_9\text{C}_2\text{H}_{11}]_2\text{Fe}$ and $[(\text{CH}_3)_4\text{N}]_2[\pi\text{-(3)-1,2-B}_9\text{C}_2\text{H}_{11}]_2\text{Fe}$, and characterized by their uv-visible spectra as given by Hawthorne and co-workers (13).

Solvents

Water used in all rate studies, reagent purifications,

and stock solutions was the product of a double redistillation of laboratory distilled water from alkaline permanganate in a tin-lined Barnstead still. Specific conductance of the water was $\leq 1 \times 10^{-6} \text{ ohm}^{-1} \text{ cm}^{-1}$. Baker analyzed reagent grade n-propanol and acetone were used without further purification. Baker analyzed reagent grade tetrahydrofuran (THF) was freshly distilled from a Na-THF mixture which had refluxed for 6-12 hours. THF thus purified was collected and stored under an atmosphere of dry nitrogen, and was used within 6 hours of distillation.

Other reagents

Hydrated iron(III) perchlorate was prepared by fuming solutions of the chloride in perchloric acid. The chloride-free iron(III) perchlorate was then recrystallized twice from perchloric acid solution. The iron(III) perchlorate solutions were analyzed by reduction with stannous chloride followed by titration of the iron(II) produced with a standard cerium(IV) solution (32).

Solutions of iron(II) perchlorate were prepared by oxidation of electrolytic iron by perchloric acid under a nitrogen atmosphere.

Nitrogen gas was purified by passage through a series of

five gas-washing bottles. The first two bottles contained Cr^{2+} over amalgamated zinc, followed by one bottle containing dilute sodium hydroxide, one bottle containing distilled water, and one empty bottle. Where necessary, this nitrogen was dried by scrubbing with concentrated sulfuric acid followed by a calcium sulfate drying tube.

Hydrated lithium and barium perchlorate salts were crystallized from solutions prepared by dissolving the carbonate in perchloric acid. The products, twice recrystallized from water, were used to prepare stock solutions which were analyzed by a cation exchange method using Dowex 50W-X8 resin (50-100 mesh) in the hydrogen ion form.

Potassium dichromate, perchloric acid, and sodium chloride were obtained commercially and used without further purification.

Equipment

Kinetic measurements

Kinetic measurements were carried out using a Durrum-Gibson D-100 stopped-flow spectrophotometer equipped with a Kel-F mixing system. The output signal of the photomultiplier tube of the spectrophotometer was connected to a Tektronix storage oscilloscope. An oscilloscope trace was electron-

ically triggered by the spectrophotometer when freshly mixed solutions were in the observation cuvette. The oscilloscope trace was then photographed with a Polaroid camera. The experimental concentrations and wavelengths were adjusted so that the absorbance changes were less than 0.10 absorbance units (more typically 0.02-0.05 absorbance units). When the change in absorbance, D , is ≤ 0.10 absorbance units the absorbance and transmittance are related by the expression, $T \cong 1 - 2.303 D$. This expression is differentiated with respect to concentration, giving $\partial T / \partial C \cong -2.303 \partial D / \partial C$. Hence, the change in transmittance with respect to concentration is directly proportional to the change in absorbance with respect to concentration. Consequently the voltage display on the vertical axis of the oscilloscope screen is proportional to absorbance in this limit, and thus to concentration.

Formal electrode potential ($E^{\circ'}$) measurements

$E^{\circ'}$ measurements were made by potentiometric titration versus a saturated calomel electrode (SCE) using a Leeds and Northrup K-2 potentiometer and galvanometer.

Spectral measurements

UV-visible spectral measurements were made with a Cary 14 recording spectrophotometer. NMR measurements were made with a Perkin-Elmer R-20B spectrometer.

Methods, Procedures, and Data Treatment

Reaction media

Different solvents and electrolytes were used for each of the three main categories of reactions. Except as otherwise noted in the text, the following conditions apply to all measurements in the different systems:

Ferrocene-ferricenium ion electron transfer reactions: water-n-propanol (1:1 v/v; $Z_{\text{PrOH}} = 0.194$), 0.05 M ionic strength provided by barium perchlorate.

Ferrocene-iron(III) reactions: water-tetrahydrofuran (1:1 v/v; $Z_{\text{THF}} = 0.180$), 1.00 M ionic strength maintained with lithium perchlorate-perchloric acid, $[\text{H}^+] \geq 0.1\text{M}$.

Ferrocene-chromium(VI) reaction: water-acetone (1:1 v/v; $Z_{\text{Acetone}} = 0.195$), 1.00 M ionic strength maintained with lithium perchlorate-perchloric acid, $[\text{H}^+] \geq 0.01\text{M}$.

Formal electrode potential measurement

Several methods have been used in previous studies to determine the E^0 values of the ferrocene derivatives (29,30, 33,34). Potentiometric titration was one of these methods (33) and was used here.

A typical E^0 titration was done as follows. A ferrocene solution in the desired medium, typically $6 \times 10^{-4}\text{M}$ in ferro-

cene, was placed in the titration cell which was then equilibrated at the desired temperature. A standard iron(III) solution was then titrated into the cell, and the EMF measured potentiometrically.

The Nernst equation is

$$E = E_{\text{FeCp}_2^+/\text{FeCp}_2}^{\circ'} + RT/nF \ln \frac{[\text{FeCp}_2^+]}{[\text{FeCp}_2]} \quad (7)$$

where E is the measured electrode potential vs. SCE and FeCp_2 and FeCp_2^+ represent ferrocene and ferricenium ion respectively, for which $n = 1$. The following equation is obtained from it:

$$E = E_{\text{FeCp}_2^+/\text{FeCp}_2}^{\circ'} + RT/F \ln \left[\frac{V_t \times N_t}{V \times N - V_t \times N_t} \right] \quad (8)$$

where V_t and N_t are volume and normality of titrant respectively and V and N are the initial volume and concentration of ferrocene placed in the titration cell. A plot of E vs. $\ln[V_t \times N_t / V \times N - V_t \times N_t]$ is linear with a slope RT/F and has a value of $E_{\text{FeCp}_2^+/\text{FeCp}_2}^{\circ'}$ vs. SCE at the half equivalence point (i.e. when $[\text{FeCp}_2^+] = [\text{FeCp}_2]$). $E^{\circ'}$ titration data was treated in this manner.

For titrations of air sensitive compounds and for all titrations in THF-water mixtures, the side of the titration cell containing the ferrocene solution was purged with nitrogen

throughout the titration. In addition the titrant was purged with nitrogen and added with a syringe rather than with a buret.

Iodoferrocene has a potential too close to that of iron (III) to allow a potentiometric titration as above. To obtain E^0 for iodoferrocene a solution of iodoferrocenium ion was prepared by oxidizing with cerium(IV) perchlorate a small amount of a concentrated (0.010 M) solution of iodoferrocene in 3M perchloric acid. This solution was then diluted and added in known increments to an iodoferrocene solution.

Ferrocene-ferricenium ion rate studies

The Durrum-Gibson stopped flow spectrophotometer was used to follow these reactions. The reaction rates were very high and consequently measured under second-order conditions.

The rates of reaction were studied at wavelengths between 240 and 300 nm where the ferricenium species have large molar absorbtivities. The reaction is more conveniently studied at wavelengths slightly away from the wavelength maximum (for example at 240 nm for the ferricenium ion-1,1'dimethylferrocene reaction rather than 254 nm or 257 nm) since the spectrum of both species are changing more rapidly there than at the

peak. By doing this one observes a larger absorbance change and a smaller background absorbance. In all cases where more than one wavelength was used to study a reaction the reaction rate was independent of wavelength.

Ferrocene-iron(III) rate studies

These reactions were studied in water-THF rather than water-n-propanol to avoid formation of n-propanol complexes of iron(III) (35). To avoid formation of significant amounts of hydrolytic polymers of iron(III), all experiments were at hydrogen ion concentrations greater than 0.1 M.

A typical iron(III)-ferrocene oxidation-reduction reaction experiment was done as follows. Solutions of ferrocene and of iron(III) of the desired composition were prepared under nitrogen from freshly prepared THF. The perchloric acid was usually added to the iron(III) reactant solution, with the exception of experiments at high hydrogen ion concentration where perchloric acid was initially added to both solutions.

The ferrocene and iron(III) reactant solutions were then transferred under nitrogen, using glass syringes with Teflon needles, to the Durrum-Gibson stopped flow spectrophotometer. Since the peroxide formed in THF in the presence of oxygen was shown to react with ferrocene in acidic solution, oxygen was

excluded from all phases of the experiment and only freshly distilled solvent was used.

The iron(III)-ferrocene reactions were observed in the region 600-700 nm where only the various ferricenium ions absorb ($\epsilon_{\text{max}} = 300-600$). Experiments with lower reactant concentrations were observed in the region 300-340 nm where the molar absorptivities of the ferricenium species formed are much larger. In all cases the reaction rate was independent of wavelength.

The rate studies were carried out under pseudo-first-order conditions both with ferrocene in excess and with iron (III) in excess.

Ferrocene-chromium(VI) rate studies

The reaction of $\text{Fe}(\text{C}_5\text{H}_5)_2$ and $\text{Cr}(\text{VI})$ (Eq. 5) does not occur in the absence of added H^+ . The kinetic studies were carried out using the stopped-flow method. In all the experiments reported here, a solution containing both HCrO_4^- and $\text{Fe}(\text{C}_5\text{H}_5)_2$ was mixed with a solution of perchloric acid. In this manner, (a) the oxidation of acetone by HCrO_4^- was rendered unimportant and (b) the slow decomposition of $\text{Fe}(\text{C}_5\text{H}_5)_2$ in acidic acetone solution is avoided.

All experiments were done under pseudo-first-order

excesses of $\text{Fe}(\text{C}_5\text{H}_5)_2$. The experiments were done at four wavelengths; the molar absorptivities were determined at these wavelengths and appear in Table 4. No rate dependence on wavelength was found.

Table 4. Wavelengths and molar absorptivities of reactants and products in the ferrocene-chromium(VI) reaction

λ, nm	Molar absorptivities, $\text{cm}^{-1}\text{M}^{-1}$			
	FeCp_2	FeCp_2^+	HCrO_4^-	Cr^{3+}
618	0	450	0	~ 10
330	53	1280	1170	~ 8
350	19	588	1600	~ 10
370	17	380	1260	~ 12

Kinetic data

The pseudo-first-order kinetic data in terms of absorbance, D , for the $\text{Fe}(\text{III})$ oxidations, Eq. 4, were treated by the equation:

$$\ln(D_\infty - D_t) = \ln(D_\infty - D_0) - k_i [X]_{\text{ave}} t \quad (9)$$

where k_i is the second-order rate constant corresponds to the kinetic expression,

$$-d[\text{ferrocene}]/dt = k_i [\text{Fe}(\text{III})][\text{ferrocene}] \quad (10)$$

$[X]_{\text{ave}}$ is the average concentration of the reactant in excess, either $\text{Fe}(\text{III})$ or ferrocene, for that particular run, and the

subscripts refer to time. Plots of $\log (D_{\infty} - D_t)$ vs. time were linear, and from their slopes values of k were computed using the average concentration of X in each run.

A similar treatment of the kinetic data was applied to the reaction of $\text{Fe}(\text{C}_5\text{H}_5)_2$ by $\text{Cr}(\text{VI})$, for which a third-order rate constant is defined by the following rate equation:

$$-d[\text{Cr}(\text{VI})]/d\underline{t} = -\frac{1}{3} d[\text{Fe}(\text{C}_5\text{H}_5)_2]/d\underline{t} = k' [\text{Fe}(\text{C}_5\text{H}_5)_2] [\text{Cr}(\text{VI})] [\text{H}^+] \quad (11)$$

In this case the slope of the plot of $\ln(D_t - D_{\infty})$ vs. t is $k' [\text{Fe}(\text{C}_5\text{H}_5)_2]_{\text{ave}} [\text{H}^+]_{\text{ave}}$ permitting the calculation of k' .

The reactions between ferrocenes and ferricenium ions follow the kinetic pattern:

$$-d[\text{A}]/d\underline{t} = k[\text{A}][\text{B}^+] - k'[\text{A}^+][\text{B}] \quad (13)$$

the integrated rate expression for which has been derived by Frost and Pearson (36). The form of the equation used depended upon the conditions:

(a) with $[\text{B}^+]_0 \neq [\text{A}]_0$ and A^+ and B initially absent, the following expression applies

$$[(1 - K^{-1})Q]^{-1} \ln \left[\frac{X_e (A - A_e + Q)}{(A - A_e)(X_e + Q)} \right] = k\underline{t} \quad (14)$$

where the subscript e refers to equilibrium, $A = A_0 - X$, $X_e = A_0 - A_e$, and $X = X_e(D_0 - D_t)/(D_0 - D_e)$. The equilibrium concentration of A is given by

$$A_e = \frac{-b + (b^2 - 4ac)^{\frac{1}{2}}}{2a} \quad (15)$$

with $a = K - 1$, $b = 2A_0 + KB_0^+ - KA_0$, and $c = -A_0^2$. Q is given by Eq. 16.

$$Q = [1/(K - 1)][K^2(B_0^+ - A_0)^2 + 4A_0B_0^+K]^{\frac{1}{2}} \quad (16)$$

(b) with $[A]_0 = [B^+]_0$, $[A^+]_0 = [B]_0 = 0$, Eq. 14 simplifies to

$$\left[\frac{(K)^{\frac{1}{2}}}{2A_0} \right] \ln \left[\frac{X(A_0 - 2X_e) + A_0 \cdot X_e}{A_0(X_e - X)} \right] = kt \quad (17)$$

where A_e under these conditions is calculated from the expression $A_e = A_0/(\sqrt{K} + 1)$ and X and X_e have the same definition as above.

The fit of the individual kinetic data to the appropriate integrated rate expression, Eq. 14 or 17, was carried out using a CPS computer program.

The experiments on these reactions were of one of these two forms. In addition, the equilibrium in Eq. 12 may be approached from either side with the same result. Hence, similar equations can be written for experiments starting with

mixtures of A^+ and B, and no initial A and B^+ . For $[A^+]_0 \neq [B]_0$ Eq. 18 results; for $[A^+]_0 = [B]_0$ Eq. 19 is derived.

$$[Q(K^{-1} - 1)]^{-1} \ln \left[\frac{X_e(A^+ - A_e^+ + Q)}{(A^+ - A_e^+)(X_e + Q)} \right] = kt \quad (18)$$

where $Q = [(K^{-1} - 1)^{-1}[(K^{-1})^2(B_0 - A_0^+)^2 + 4A_0^+B_0K^{-1}]]^{\frac{1}{2}}$,

$A^+ = A_0^+ - X$, $X_e = A_0^+ - A_e^+$, $X = X_e(D_0 - D_t)/(D_0 - D_e)$, and

$A_e^+ = (-b + (b^2 - 4ac)^{\frac{1}{2}}/2a)$ with $a = K^{-1} - 1$, $b = 2A_0^+ + K^{-1}B_0 - K^{-1}A_0^+$, and $C = -(A_0^+)^2$.

$$\left[\frac{(K)^{\frac{1}{2}}}{2A_0^+} \right] \ln \left[\frac{X(A_0^+ - 2X_e) + A_0^+X_e}{A_0^+(X_e - X)} \right] = kt \quad (19)$$

where X_e , X are as defined for Eq. 18 and $A_e^+ = A_0^+ [K^{-\frac{1}{2}} + 1]^{-1}$.

A sample oscillogram for a typical ferrocene-ferricenium ion reaction, Eq. 2, is shown in Figure 3A, and for a typical iron(III)-ferrocene reaction, Eq. 4, in Figure 3B. To illustrate the treatment of these data, the data from Figure 3A have been treated in accord with the integrated equation for reversible second-order kinetics given by Eq. 17 and are shown on Figure 4. The data from Figure 3B have been treated in accord with Eq. 9, and are shown in Figure 5.

Figure 3. Typical stopped flow oscillograms

- A. $\text{Fe}(\text{C}_5\text{H}_5)(\text{C}_5\text{H}_4\text{C}_6\text{H}_5)^+$, $4 \times 10^{-6}\text{M}$, $\text{Fe}(\text{C}_5\text{H}_5)(\text{C}_5\text{H}_4\text{CH}_2\text{OH})$, $4 \times 10^{-6}\text{M}$, in H_2O - n -propanol (1:1 v/v), $\mu = 0.05$ maintained with $\text{Ba}(\text{ClO}_4)_2$ at 25°C , $\lambda = 278 \text{ nm}$
- B. Fe^{3+} , $3 \times 10^{-5}\text{M}$, $\text{Fe}(\text{C}_5\text{H}_5)(\text{C}_5\text{H}_4\text{C}_4\text{H}_9)$, $3 \times 10^{-4}\text{M}$, in H_2O -THF (1:1 v/v), $[\text{H}^+] = 0.50\text{M}$, $\mu = 1.00$ maintained with LiClO_4 at 25°C , $\lambda = 620 \text{ nm}$

Figure 4. A plot of the left-hand side of Eq. 17, here designated $f(A)$, vs time for oscillogram A in Figure 3

Figure 5. A plot of $-\ln(D_\infty - D_t) / (D_\infty - D_0)$ vs time for oscillogram B in Figure 3.

Stoichiometry studies

Ferricenium ion was determined to be the only product resulting from iron(III) oxidation of ferrocene by its characteristic uv-visible spectrum. The 1:1 stoichiometry of this oxidation was established by spectrophotometric titration of ferrocene with iron(III) at a wavelength where only ferricenium ion absorbs. In this titration the absorbance increased linearly as iron(III) was added until the equivalence point (determined by weighed amount of ferrocene and the analytical concentration of iron(III)). Iron(III) added in excess of the equivalent amount resulted in no further absorbance changes at this wavelength. This established that one mole of iron(III) reacts with one mole of ferrocene to produce one mole of ferricenium ion and that ferricenium ion does not react further with excess iron(III).

The stoichiometry of the chromium(VI)-ferrocene reaction was determined via a spectrophotometric titration (at $\lambda = 618$ nm) of ferrocene by chromium(VI) in a manner similar to that used for the iron(III)-ferrocene reaction. This titration, however, was carried out in 1:1 v/v water-acetone and the order of addition of reactants to each sample was: ferrocene followed by chromium(VI) followed by perchloric acid, with

vigorous stirring during the perchloric acid addition. Ferricenium ion was also established as being the only ferrocene product resulting from this reaction as long as ferrocene was present in three-fold molar excess over chromium(VI). However, when greater than 1/3 mole of chromium(VI) per mole of ferrocene was present the ferricenium ions produced by the initial oxidation were subsequently destroyed by a further slow reaction with chromium(VI). During the titration and up to the equivalence point of three moles of ferrocene to one mole of chromium(VI) the reaction does proceed with quantitative production of ferricenium ion. All kinetic studies were performed under conditions of excess ferrocene where this second slow reaction is not important. No kinetic or stoichiometric studies were carried out on the second slow reaction between chromium(VI) and ferricenium ion.

RESULTS

Formal Electrode Potential Measurements

Formal electrode potentials of the compounds used in this study were determined by potentiometric titration. The results, given in Table 5, were obtained under the same conditions as the kinetic studies. By combining the appropriate electrode potentials from Table 5, the equilibrium constants for the electron transfer reactions, Eq. 2, and the Fe(III) oxidation reactions, Eq. 4, were calculated. To check the equilibrium constants obtained in this manner, spectral studies for several ferrocene-ferricenium ion systems, Eq. 2, were carried out. Using the known molar absorptivities of the reactants and products, the equilibrium constant as determined above, and mass balance of the ferrocene and ferricenium ion reactants and products, spectra of the mixed ferrocene-ferricenium ion systems, Eq. 2, were calculated. The calculated spectra are within 2% of the observed spectra of the equilibrated solutions. For example, in the reaction described by Eq. 20,

Table 5. Formal electrode potentials^a of iron compounds studied

#	Compound	@25° E°', V ^b	@0° E°', V ^b	@25° E°', V ^c
Ferrocenes:				
1	1,1'-di-(CH ₃)	+0.1899 ± 0.0005	+0.1940 ± 0.0005	+0.167
2	1,1'-di-(<u>n</u> -C ₄ H ₉)	+0.2353 ± 0.0004	+0.2421 ± 0.0004	+0.184 ± 0.003
3	<u>n</u> -C ₄ H ₉	+0.2556 ± 0.0005	+0.2614 ± 0.0003	+0.2188 ± 0.001
4	Ferrocene	+0.2719 ± 0.0005	+0.2760 ± 0.0003	+0.2545 ± 0.002
5	HgCl	+0.2797 ± 0.0004	Not soluble	Decomposes in H ⁺
6	CH ₂ OH	+0.2806 ± 0.0005	+0.2861 ± 0.0003	+0.270
7	C ₆ H ₅	+0.3267 ± 0.0010	+0.3301 ± 0.0003	+0.3011 ± 0.001
8	I	~+0.427	~+0.444	---

^aE°' values versus SCE.

^bData refer to 1:1 v/v H₂O-n-propanol, μ = .05 M (Ba(ClO₄)₂).

^cData refer to μ = 1.00 M(LiClO₄), [H⁺] = 0.50 M, 1:1 v/v H₂O-THF.

Table 5. (Continued)

#	Compound	@ 25°	@ 0°	@ 25°
		E°', V ^b	E°', V ^b	E°', V ^c
	Fe(C ₅ H ₅)(π -C ₂ B ₉ H ₁₁) ⁻	-0.12 ^d	---	---
	Fe(π -C ₂ B ₉ H ₁₁) ₂ ⁼	--- ^e	---	---
	Fe ²⁺	+0.4960 $\pm$ 0.0003	+0.4613 $\pm$ 0.0006	+0.5248 $\pm$ 0.001

^dValue determined by Hawthorne et al. (13), in 1:1 acetone-H₂O, 0.1 N (Et)₄NC10₄ is -0.08 V.

^eValue determined by Hawthorne et al. (13), in 1:1 acetone-H₂O, 0.1 N (Et)₄NC10₄ is -0.425 V.

the equilibrium constant determined from data in Table 5 is 1.89 and in the region 600 nm to 700 nm only the $\text{Fe}(\text{C}_5\text{H}_5)_2^+$ and $\text{Fe}(\text{C}_5\text{H}_5)(\text{C}_5\text{H}_4\underline{\text{n}}-\text{C}_4\text{H}_9)^+$ species absorb.

Based on the spectra of the two absorbing species ($\text{Fe}(\text{C}_5\text{H}_5)_2^+$ and $\text{Fe}(\text{C}_5\text{H}_5)(\text{C}_5\text{H}_4\underline{\text{n}}-\text{C}_4\text{H}_9)^+$), Figure 6, the spectrum of the reaction mixture, Eq. 20, was calculated. The observed and calculated spectra of this solution are given in Figure 7. The agreement between the observed and calculated spectra is not a strong confirmation of the value of K because the spectra are not a sensitive function of equilibrium constant. Consequently spectrophotometric determinations of the equilibrium constant are not reliable and were not attempted.

Data in Table 5 at 0°C and 25°C are combined to calculate equilibrium constants at other temperatures. In principle ΔS° and ΔH° for the electron transfer reactions, Eq. 2, also can be calculated from the data at 0°C and 25°C, however, this calculation is based on data for only two temperatures and a temperature range of only 25°C over which the measured E°' values do not change very much. Hence, ΔS° and ΔH° values calculated in this manner must be regarded as estimates.

The potentials in Table 5 are formal electrode potentials (E°') rather than standard electrode potentials (E°), since

Figure 6. Spectrum of ferricenium ion and n-butylferricenium ion in 1:1 v/v H₂O-n-propanol, $\mu = 0.05$ Ba(ClO₄)₂ at 25°C

Figure 7. Observed spectrum (solid line) and calculated spectrum (dots) for a mixture of ferrocene, ferrocenium ion, *n*-butylferrocene, and *n*-butylferrocenium ion, Eq. 20. Calculated concentrations are 1.43×10^{-4} , 1.3×10^{-4} , 1.03×10^{-4} and $1.70 \times 10^{-4} \text{ M}$ respectively. 1:1 v/v H_2O -*n*-propanol, $\mu = 0.05 \text{ M}$ maintained with $\text{Ba}(\text{ClO}_4)_2$ at 25°C

attempts were not made to extrapolate data to infinite dilution or to correct for junction potential. However, since all the ferrocene potentials were measured with the same experimental method and apparatus and by titration with the same titrant (Fe(III)) it is assumed that junction potentials and activity effects are identical for each of the ferrocene-ferricenium ion couples, which is especially so considering that each couple involves the same charge types and similar structures. Any differences between the experimental $E^{\circ'}$ s and the true E° 's would then cancel in the combination of a pair of $E^{\circ'}$ s to compute an equilibrium constant.

Iron(III)-Ferrocene Reactions

Kinetic studies were carried out on iron(III) oxidations of substituted ferrocenes, Eq. 4. The rate law, Eq. 10, was established by following the reactions under pseudo-first order excesses of either iron(III) or the ferrocene derivative. The second-order rate constants obtained were independent of the reagent in excess and were constant over a wide range of reactant concentration. The second-order rate constants were also independent of hydrogen ion concentration from 0.10 to 1.00 M.

The results of these experiments are given in Table 6.

Table 6. Rate data for the iron(III)-ferrocene reactions^a

Substituted ferrocene	[Fe ³⁺] <u>M</u> × 10 ³	[Ferrocene] <u>M</u> × 10 ³	[H ⁺] <u>M</u>	k _i , <u>M</u> ⁻¹ sec ⁻¹ × 10 ⁻⁴ ^b
Ferrocene	0.05	1.00	0.50	1.00 ± 0.03
	1.00	0.05	0.50	1.03 ± 0.03
	0.01	0.10	0.10	1.07 ± 0.05
	0.10	0.01	1.00	1.11 ± 0.05
	Ave. 1.05 ± 0.04			
	0.02	0.20	0.50	2.57 ± 0.13 ^c
	0.30	0.02	0.50	2.56 ± 0.12 ^c
	Ave. 2.56 ± 0.13 ^c			
	0.10	2.00	0.50	0.41 ± 0.01 ^d
	5.00	0.10	0.50	0.43 ± 0.01 ^d
	Ave. 0.42 ± 0.01 ^d			
1,1'-di-CH ₃	0.05	0.50	0.50	3.1 ± 0.15
	3.00	0.10	0.50	3.4 ± 0.10
	0.03	0.003	0.50	3.1 ± 0.15
	Ave. 3.2 ± 0.15			

^aExcept where noted all data pertain to 1:1 v/v H₂O-THF, $\mu = 1.00$ LiClO₄, 25°C.

^bThe indicated uncertainty in the individual rate constants represents the average deviation from the mean in three or four repetitive determinations using the same set of reagents. The uncertainty cited for the average rate constants is the average deviation from the unweighted mean of the individual values.

^cData obtained at 40°C.

^dData obtained at 10°C.

Table 6. (Continued)

Substituted ferrocene	[Fe ³⁺] <u>M</u> x10 ³	[Ferro- cene] <u>M</u> x10 ³	[H ⁺] <u>M</u>	k _i , <u>M</u> ⁻¹ sec ⁻¹ x10 ⁻⁴ ^b
C ₆ H ₅	0.05	0.50	0.50	0.52 ± 0.02
	2.00	0.10	0.50	0.48 ± 0.01
	0.10	0.01	0.50	0.49 ± 0.01
	0.50	1.00	0.50	0.47 ± 0.02
	0.80	0.08	0.25	0.54 ± 0.02
				Ave. 0.50 ± 0.02
CH ₂ OH	0.089	1.00	0.50	1.80 ± 0.07
	3.00	0.10	0.50	1.77 ± 0.05
	0.10	0.01	0.50	1.85 ± 0.05
	0.05	0.50	0.20	1.73 ± 0.10
				Ave. 1.79 ± 0.07
1,1'-di- <u>n</u> -C ₄ H ₉	0.08	1.00	0.50	1.39 ± 0.05
	0.03	0.30	0.50	1.31 ± 0.05
	3.00	0.10	0.50	1.43 ± 0.05
	0.10	0.01	0.50	1.59 ± 0.05
				Ave. 1.43 ± 0.10
<u>n</u> -C ₄ H ₉	0.30	0.03	0.50	1.50 ± 0.04
	0.03	0.30	0.50	1.47 ± 0.04
	0.10	1.00	0.50	1.55 ± 0.06
	3.00	0.10	0.50	1.49 ± 0.04
				Ave. 1.50 ± 0.05
Fe(C ₅ H ₅)(C ₂ B ₉ H ₁₁) ⁻	0.0025	0.025	0.50	480 ± 30
	0.025	0.0025	0.50	460 ± 30
	0.010	0.0015	0.50	530 ± 30
				Ave. 4.90 ± 30
Fe(C ₂ B ₉ H ₁₁) ₂ ²⁻	0.003	0.003	0.001	>1x10 ⁴

The oxidation of ferrocene by Fe^{3+} is the only member of the series for which rate constants were evaluated at temperatures other than 25° . From the experiments at 10° , 25° , and 40°C for the iron(III)-ferrocene reaction $\Delta S^\ddagger$ and $\Delta H^\ddagger$ are found to be -6.5 ± 0.7 eu and 10.0 ± 0.2 kcal mole $^{-1}$ respectively.

Data for the iron(III)-iodoferrocene reaction, Eq. 21, are not included in Table 6.

The oxidation potential for iodoferrocene is too close to that of Fe(III) for the oxidation of iodoferrocene by Fe(III) to be complete, hence Eq. 9 and 10 do not apply to this system. The rate law for the reaction described by Eq. 21 is given by Eq. 22.

$$\frac{d[\text{Fe}(\text{C}_5\text{H}_5)(\text{C}_5\text{H}_4\text{I}^+)]}{dt} = k_8[\text{Fe}^{3+}][\text{Fe}(\text{C}_5\text{H}_5)(\text{C}_5\text{H}_4\text{I})] - k_8'[\text{Fe}^{2+}][\text{Fe}(\text{C}_5\text{H}_5)(\text{C}_5\text{H}_4\text{I}^+)] \quad (22)$$

With pseudo-first-order excesses of Fe(III) and Fe(II), Eq. 21 and 22 lead to a pseudo-first-order observed rate constant given by Eq. 23.

$$k_{\text{obs}} = d \ln[\text{Fe}(\text{C}_5\text{H}_5)(\text{C}_5\text{H}_4\text{I}^+)]/dt = k_8[\text{Fe}^{3+}]_{\text{ave}} + k_8'[\text{Fe}^{2+}]_{\text{ave}} \quad (23)$$

A plot of $k_{\text{obs}}/[\text{Fe}^{3+}]_{\text{ave}}$ versus $[\text{Fe}^{2+}]_{\text{ave}}/[\text{Fe}^{3+}]_{\text{ave}}$ gives a straight line having an intercept, k_8 of $5.5 \times 10^2 \text{ M}^{-1}\text{sec}^{-1}$ and a slope, k_8' , of $19 \text{ M}^{-1}\text{sec}^{-1}$, Figure 8. All experiments for this system are given in Table 7. From k_8 and k_8' an equilibrium constant of 29 is obtained.

Table 7. Rate data for iron(III)-iodoferrocene system^a

$[\text{Fe}^{2+}]$, $\text{M} \times 10^3$	$[\text{Fe}^{3+}]$, $\text{M} \times 10^3$	$[\text{Fe}(\text{C}_5\text{H}_5)(\text{C}_5\text{H}_4\text{I})]$ $\text{M} \times 10^3$	k_{obs} , sec^{-1}
1.00	1.00	0.10	$0.55 \pm .015$
0.50	10.00	0.05	$5.61 \pm .15$
10.00	0.05	0.05	$0.44 \pm .03$
10.00	1.00	0.10	$0.64 \pm .01$
50.00	0.50	0.05	$1.31 \pm .02$
0.00	0.50	0.50	--- ^b
0.00	1.50	0.50	--- ^b
50.00	1.00	0.05	$1.42 \pm .05$

^aAll data at 1:1 v/v H₂O-THF, $\mu = 1.00 \text{ LiClO}_4$, $\text{H}^+ = 0.50 \text{ M}$ at 25°C.

^bThese two experiments were carried out under second-order conditions and were treated in the same manner as the ferrocene-ferricenium electron transfer reactions as described in the experimental section of this thesis. Hence, the rate constants are second order rate constants, the values being 510 ± 30 and $540 \pm 20 \text{ M}^{-1}\text{sec}^{-1}$ for these two experiments respectively. These correspond to a determination of k_8 , which is also the intercept on Figure 8.

Figure 8. A plot of kinetic data as suggested by Eq. 23 for the iron(III)-iodoferrocene reaction

Ferrocene-Ferricenium Electron Transfer Reactions

The ferrocene-ferricenium electron transfer reactions, Eq. 2, are much too fast to be followed under pseudo-first-order conditions. However, the reactions can be studied under reversible second-order conditions. The assumed rate law, Eq. 13, has several integrated forms, Eq. 14, 17, 18, 19, the form applicable depending on the concentration conditions of the experiment.

Kinetic studies have been carried out under conditions pertaining to each of the different forms of the integrated rate equation and over a range of concentrations within these limits. The constraints on which were based the lower and upper limits of concentrations studied for a given reaction were (a) the minimum amount of reactants necessary to produce a measurable absorbance change (about 0.01 absorbance unit) and (b) the maximum concentration of reactants that could be used without rendering the reaction immeasurably fast. For some reactions these limits were so restrictive that only a narrow range of concentration could be covered (e.g. ferrocene-iodoferricenium ion reaction).

All data obtained for these systems are in agreement with the assumed rate law, Eq. 13, and its related integrated

forms. The conditions and results of these experiments appear in Table 8.

The reactions between ferricenium ion and 1,1'-dimethylferrocene and between phenylferricenium ion and ferrocene have also been studied as a function of temperature. The activation parameters for these two reactions are given in Table 9.

Several experiments were done under different salt and solvent conditions and are presented as the last seven entries in Table 8.

Chromium(VI)-Ferrocene Reaction

The oxidation of ferrocene by chromium(VI), Eq. 5, was found to obey the rate law given by Eq. 11 under conditions of pseudo-first-order excesses of ferrocene and hydrogen ion. Under these conditions the observed pseudo-first-order rate constant is given by Eq. 24.

$$k_{\text{obs}} = -d \ln[\text{Cr(VI)}]/d\underline{t} = k' [\text{H}^+]_{\text{ave}} [\text{Fe}(\text{C}_5\text{H}_5)_2]_{\text{ave}} \quad (24)$$

The results of kinetic experiments are given in Table 10 and also in Figure 9. The data in Table 10 indicate a slight but systematic decrease in k' with increasing $[\text{H}^+]$. This effect might be related to the following equilibrium:

Table 8. Rate and equilibrium data for the ferrocene-ferricenium electron transfer reactions^a

$$A + B^+ \xrightleftharpoons[k_{ij}]{k'_{ij}} A^+ + B; \quad K_{ij} = k'_{ij}/k_{ij}$$

Reaction ij	Substituted ferrocene system		Initial concentrations				$k_{ij} \times 10^{-6} \text{ M}^{-1} \text{ sec}^{-1}$
	A	B	[A]	$[B^+] \times 10^6, \text{ M}$	[A ⁺]	[B]	
24	1,1'-di- <u>n</u> -C ₄ H ₉	Ferrocene	6.0	6.0	0.0	0.0	15. $\pm$ 1.
			1.0	1.0	0.0	0.0	16. $\pm$ 2.
			8.0	8.0	0.0	0.0	15. $\pm$ 2.
			3.0	3.0	0.0	0.0	11.3 $\pm$ 2.
			4.0	8.0	0.0	0.0	13.8 $\pm$ 1.
			6.0	4.0	0.0	0.0	11.8 $\pm$ 1.3
			0.0	0.0	6.0	6.0	13. $\pm$ 1.2
			0.0	0.0	9.0	9.0	11.5 $\pm$ 1.
	(K = 4.17)						
							Ave. 12.8 $\pm$ 1.4
34	<u>n</u> -C ₄ H ₉	Ferrocene	6.0	6.0	0.0	0.0	7.1 $\pm$ 0.8
			3.0	3.0	0.0	0.0	6.5 $\pm$ 0.4
			8.0	3.0	0.0	0.0	8.0 $\pm$ 0.5
			4.5	8.0	0.0	0.0	7.9 $\pm$ 0.6
			0.0	0.0	6.0	6.0	7.8 $\pm$ 0.5
			0.0	0.0	8.0	8.0	6.7 $\pm$ 0.6
			0.0	0.0	8.0	4.5	7.1 $\pm$ 0.6
	(K = 1.89)						
							Ave. 7.3 $\pm$ 0.5

^aExcept where noted all data obtained at 25°C, $\mu = 0.05 \text{ Ba(ClO}_4)_2$, 1:1 v/v H₂O-n-propanol, also see note b in Table 6.

Table 8. (Continued)

Reaction ij	Substituted ferrocene system		Initial concentrations				$k_{ij} \times 10^{-6} \text{ M}^{-1} \text{ sec}^{-1}$
	A	B	[A]	$\times 10^6 \text{ M}$ [B ⁺]	[A ⁺]	[B]	
14	1,1'-di-CH ₃	Ferrocene	6.0	6.0	0.0	0.0	23. $\pm$ 3.
			3.0	3.0	0.0	0.0	27. $\pm$ 3.
			1.5	1.5	0.0	0.0	17.5 $\pm$ 3.
			4.5	4.5	0.0	0.0	28.3 $\pm$ 3.
			5.0	5.0	0.0	0.0	27. $\pm$ 3. ^b
			4.0	7.0	0.0	0.0	24. $\pm$ 5.
			6.0	6.0	0.0	0.0	20. $\pm$ 2.
			0.0	0.0	12.0	12.0	20. $\pm$ 1.5
			0.0	0.0	6.0	6.0	20. $\pm$ 1.5
			Ave. 23. $\pm$ 3.				
			6.0	6.0	0.0	0.0	26.5 $\pm$ 1.5 ^c
			4.0	4.0	0.0	0.0	27. $\pm$ 1. ^c
			Ave. 27. $\pm$ 1.5 ^c				
			6.0	6.0	0.0	0.0	15. $\pm$ 2.5 ^d
			4.0	4.0	0.0	0.0	14. $\pm$ 1. ^d
			Ave. 14.5 $\pm$ 2.5				

^bFerricenium prepared by oxidation of ferrocene with Cr(VI) rather than Fe(III).

^cData obtained at 40°C.

^dData obtained at 10°C.

Table 8. (Continued)

Reaction ij	Substituted ferrocene system		Initial concentrations				$k_{ij} \times 10^{-6} \text{ M}^{-1} \text{ sec}^{-1}$
	A	B	[A]	$[B^+] \times 10^{-6} \text{ M}$	$[A^+] \times 10^{-6} \text{ M}$	[B]	
45	Ferrocene (K = 1.36)	HgCl	6.0	6.0	0.0	0.0	7.0 ± 0.5
			10.0	10.0	0.0	0.0	9.7 ± 1.0
			4.0	4.0	0.0	0.0	7.5 ± 0.7
			0.0	0.0	10.0	10.0	8.6 ± 0.6
			0.0	0.0	6.0	6.0	8.2 ± 0.7
			Ave. 8.2 ± 0.8				
46	Ferrocene (K = 1.40)	CH ₂ OH	6.0	6.0	0.0	0.0	5.8 ± 0.3
			12.0	12.0	0.0	0.0	6.2 ± 0.3
			12.0	6.0	0.0	0.0	5.6 ± 0.5
			0.0	0.0	6.0	6.0	4.6 ± 0.4
			0.0	0.0	12.0	12.0	6.7 ± 0.3
			0.0	0.0	9.0	9.0	7.3 ± 0.6
Ave. 6.0 ± 0.7							
47	Ferrocene (K = 8.4)	C ₆ H ₅	6.0	6.0	0.0	0.0	$32. \pm 2.$
			3.0	3.0	0.0	0.0	$33. \pm 3.$
			6.0	2.0	0.0	0.0	$23. \pm 3.$
			0.0	0.0	6.0	6.0	$24. \pm 3.$
			Ave. $28. \pm 4.$				
			(K = 9.3)	4.0	4.0	0.0	0.0
2.0	2.0	0.0		0.0	20.1 ± 0.8^d		
Ave. $19.2 \pm 1. d$							

Table 8. (Continued)

Reaction ij	Substituted ferrocene system		Initial concentrations $\times 10^6 \underline{M}$				$k_{ij} \times 10^{-6} \underline{M}^{-1} \text{sec}^{-1}$
	A	B	[A]	[B ⁺]	[A ⁺]	[B]	
47	Ferrocene (K = 7.7)	C ₆ H ₅	4.0	4.0	0.0	0.0	33.8 $\pm$ 1.5 ^c
			2.0	2.0	0.0	0.0	36.8 $\pm$ 3. ^c
			Ave. 35.3 $\pm$ 2. ^c				
48	Ferrocene (K = 423.)	I	2.0	2.0	0.0	0.0	150. $\pm$ 30.
			2.0	2.0	0.0	0.0	140. $\pm$ 20.
			Ave. 145. $\pm$ 30.				
13	1,1'-di-CH ₃ (K = 12.9)	n-C ₄ H ₉	6.0	6.0	0.0	0.0	33. $\pm$ 4.
15	1,1'-di-CH ₃ (K = 33.2)	HgCl	4.0	4.0	0.0	0.0	26. $\pm$ 1.
16	1,1'-di-CH ₃ (K = 34.4)	CH ₂ OH	4.0	4.0	0.0	0.0	38. $\pm$ 2.
17	1,1'-di-CH ₃ (K = 207)	C ₆ H ₅	2.0	2.0	0.0	0.0	115. $\pm$ 15.
			2.0	2.0	0.0	0.0	98. $\pm$ 10.
			Ave. 107. $\pm$ 10.				
18	1,1'-di-CH ₃ (K = 1×10^4)	I	1.0	1.0	0.0	0.0	$\geq 150.$

Table 8. (Continued)

Reaction ij	Substituted ferrocene system		Initial concentrations $\times 10^6 \text{M}$				$k_{ij} \times 10^{-6} \text{M}^{-1} \text{sec}^{-1}$
	A	B	[A]	[B ⁺]	[A ⁺]	[B]	
23	1,1'-di- <u>n</u> -C ₄ H ₉ (K = 2.21)	<u>n</u> -C ₄ H ₉	8.0	8.0	0.0	0.0	8.9 $\pm$ 1.
25	1,1'-di- <u>n</u> -C ₄ H ₉ (K = 5.65)	HgCl	6.0 6.0	3.0 6.0	0.0 0.0	0.0 0.0	14.8 $\pm$ 1. 13.3 $\pm$ 1. Ave. 14. $\pm$ 1.
26	1,1'-di- <u>n</u> -C ₄ H ₉ (K = 5.85)	CH ₂ OH	6.0 8.0	6.0 8.0	0.0 0.0	0.0 0.0	12.2 $\pm$ 0.8 11.4 $\pm$ 0.8 Ave. 11.8 $\pm$ 0.8
27	1,1'-di- <u>n</u> -C ₄ H ₉ (K = 35.3)	C ₆ H ₅	2.0 1.0	2.0 1.0	0.0 0.0	0.0 0.0	66. $\pm$ 5. 68. $\pm$ 4. Ave. 67. $\pm$ 5.
35	<u>n</u> -C ₄ H ₉ (K = 2.56)	HgCl	6.0	6.0	0.0	0.0	8.3 $\pm$ 0.5
37	<u>n</u> -C ₄ H ₉ (K = 16.0)	C ₆ H ₅	2.0 4.0 0.0	2.0 4.0 0.0	0.0 0.0 10.0	0.0 0.0 10.0	39. $\pm$ 3. 40. $\pm$ 2. 38. $\pm$ 3. Ave. 39. $\pm$ 3.

Table 8. (Continued)

Reaction ij	Substituted ferrocene system		Initial concentrations $\times 10^6 \underline{M}$				$k_{ij} \times 10^{-6} \underline{M}^{-1} \text{sec}^{-1}$
	A	B	[A]	[B ⁺]	[A ⁺]	[B]	
56	HgCl (K = 1.03)	CH ₂ OH	8.55	8.55	0.0	0.0	4.2 ± 0.3
57	HgCl (K = 6.25)	C ₆ H ₅	6.0 2.0	6.0 2.0	0.0 0.0	0.0 0.0	29.5 ± 1. 28.5 ± 2. Ave. 29. ± 2.
67	CH ₂ OH (K = 6.04)	C ₆ H ₅	4.0 2.0	4.0 2.0	0.0 0.0	0.0 0.0	20.5 ± 2. 20. ± 1. Ave. 20. ± 2.
68	CH ₂ OH (K = 302.)	I	2.0	2.0	0.0	0.0	95. ± 10.
78	C ₆ H ₅ (K = 50.0)	I	2.0 2.0	2.0 2.0	0.0 0.0	0.0 0.0	88. ± 15. 130. ± 15. Ave. 109. ± 15.
	Fe(C ₅ H ₅)(C ₂ B ₉ H ₁₁) (K = 6 × 10 ⁹)	Ferrocene	6.5	6.0	0.0	0.0	≥ 100.
	Fe(C ₂ B ₉ H ₁₁) ₂ (K = 4 × 10 ⁵)	Ferrocene	3.0	3.0	0.0	0.0	≥ 200.

Table 8. (Continued)

Reaction ij	Substituted ferrocene system		Initial concentrations				$k_{ij} \times 10^{-6} \text{ M}^{-1} \text{ sec}^{-1}$
	A	B	[A]	[B ⁺]	$\times 10^6 \text{ M}$ [A ⁺]	[B]	
	$\text{Fe}(\text{C}_2\text{B}_9\text{H}_{11})_2^-$ (K = 7×10^5)	$\text{Fe}(\text{C}_5\text{H}_5)(\text{C}_2\text{B}_9\text{H}_{11})^-$	2.0	2.0	0.0	0.0	$\geq 200.$
14	1,1'-di-CH ₃	Ferrocene	6.0 6.0	6.0 6.0	0.0 0.0	0.0 0.0	$21.6 \pm 1.^e$ $16. \pm 2.^f$
34	1,1'-di-n-C ₄ H ₉	Ferrocene	6.0 6.0 6.0	6.0 6.0 6.0	0.0 0.0 0.0	0.0 0.0 0.0	7.4 ± 0.5^g $21. \pm 1.^h$ 3.85 ± 0.2^i

^eChloride ion as NaCl added at 0.01 M.

^fChloride ion as NaCl added at 0.50 M, $\mu = 0.50$.

^gNo salt added to maintain ionic strength; $\mu \approx 0.0007$ from HClO₄, Fe²⁺, and ferricenium ion.

^hIonic strength maintained at 0.50 with LiClO₄.

ⁱ1:1 v/v THF-H₂O, $\mu = 0.05 \text{ M}$ Ba(ClO₄)₂ at 25°C.

Table 8. (Continued)

Reaction ij	Substituted ferrocene system		Initial concentrations $\times 10^6 \underline{M}$				$k_{ij} \times 10^{-6} \underline{M}^{-1} \text{sec}^{-1}$
	A	B	[A]	[B ⁺]	[A ⁺]]	[B]	
34			6.0	6.0	0.0	0.0	$10. \pm 1.^j$
			6.0	6.0	0.0	0.0	$24. \pm 2.^k$
14	1,1'-di-CH ₃	Ferrocene	4.0	4.0	0.0	0.0	$120. \pm 10.^l$

^j1:1 v/v THF-H₂O, $\mu = 1.00 \text{ LiClO}_4$, $[\text{Cl}^-] = 0.50 \underline{M}$.

^k1:1 v/v THF-H₂O $\mu = 1.00 \text{ LiClO}_4$, $[\text{H}^+] = 0.50 \underline{M}$.

^lNeat methanol, $\text{HClO}_4 \approx 1 \times 10^{-3} \underline{M}$, no added salt; $\mu \approx 1 \times 10^{-3}$ from HClO_4 .

Table 9. Activation and thermodynamic parameters for ferrocene-ferricenium ion electron transfer reactions

$A + B^+ \rightleftharpoons A^+ + B$						
Reaction	Substituted ferrocene		$\Delta H^\ddagger$, kcal mole ⁻¹	$\Delta S^\ddagger$, eu	ΔH° , kcal mole ⁻¹	ΔS° , eu
	A	B				
14	1,1-di-CH ₃	Ferrocene	+3.0 $\pm$ 1.0	-15.0 $\pm$ 3.0	-1.91	-0.05
47	Ferrocene	C ₆ H ₅	+3.0 $\pm$.64	-14.4 $\pm$ 2.1	-1.08	+0.61

Table 10. Rate data for the oxidation of ferrocene by chromium(VI)^a

[Ferrocene], $\times 10^3, \underline{M}$	Cr(VI), $\times 10^5, \underline{M}$	$[H^+]$, $\underline{M}$	k_{obs} , sec^{-1}	$\underline{M}^{-2} k'$ $sec^{-1} \times 10^{-4}$
1.01	3.34	0.050	$0.47 \pm .01$	0.98
2.06	3.0	0.050	$0.98 \pm .03$	0.97
0.12	0.4	0.050	$0.059 \pm .004$	1.04
0.60	2.0	0.050	$0.28 \pm .01$	0.98
1.65	2.0	0.100	$1.38 \pm .03$	0.85
1.03	2.0	0.100	$0.85 \pm .02$	0.85
0.206	0.686	0.100	$0.168 \pm .01$	0.86
0.237	0.79	0.100	$0.23 \pm .01^b$	1.02
1.85	2.0	0.300	$4.28 \pm .10$	0.78
0.82	2.0	0.300	$1.88 \pm .03$	0.79
0.83	2.0	0.300	$2.16 \pm .17^b$	0.90
1.24	2.0	0.300	$2.66 \pm .05$	0.73
0.515	1.72	0.300	$1.13 \pm .05$	0.77
1.24	2.0	0.300	$4.19 \pm .1^c$	
0.82	2.0	0.300	$2.13 \pm .06^d$	
				Ave. $0.89 \pm 10\%$

^aAll work done at $\mu = 1.00$ maintained with added $LiClO_4$, 25°C.

^bFerricenium present initially at 1×10^{-3} , and 2×10^{-4} for these experiments at $0.100 \underline{M}[H^+]$ and $0.300 \underline{M}[H^+]$ respectively.

^cTemperature held at 35°C for this experiment.

^dSolvent ratio held at 55:45 v/v H_2O -acetone, all others at a solvent ratio of 1:1 v/v H_2O -acetone.

Figure 9. A plot of kinetic data in accord with Eq. 24 for the ferrocene-chromium(VI) reaction. The legend refers to different $[\text{H}^+]$: 0.05 (solid circles), 0.10 (solid squares), and 0.30 M (open circles)

To obtain a rate expression in terms of the predominant species of Cr(VI), rather than in terms of the total Cr(VI) concentration as in Eq. 24, the substitution $[\text{HCrO}_4^-] = [\text{Cr(VI)}]K_a/([\text{H}^+] + K_a)$ is made, leading to the equation

$$\frac{-d[\text{Cr(VI)}]}{dt} = k[\text{HCrO}_4^-][\text{H}^+][\text{Fe}(\text{C}_5\text{H}_5)_2] \quad (26)$$

with $k' = k K_a/([\text{H}^+] + K_a)$. While K_a has been determined in strictly aqueous medium ($K_a \sim 5.0 \text{ M}$ at $\mu = 1.00 \text{ M}$, 25°) (37), its value is not known in water-acetone. Judging by this value of K_a , the correction for reaction 25 is likely to be a relatively small one.

An alternative approach is to fit the data in Table 10 numerically, treating both k and K_a as unknowns. A least squares calculation gives the result $k = 1.01 \pm 0.04 \times 10^4 \text{ M}^{-2} \text{ sec}^{-1}$ and $K_a = 1.06 \pm 0.25 \text{ M}$. While this cannot be taken as an accurate determination of K_a , it does show that the K_a necessary to account for the observed trend in k' with hydrogen ion concentration is not an unreasonable one.

To compare the results of the two parameter treatment (K_a , k) to that of the single parameter treatment (where

formation of H_2CrO_4 was ignored), the deviations between the observed and calculated values of k_{obs} can be cited:

	<u>Ave. deviation, %</u>	<u>Max. deviation, %</u>
2 parameter treatment	4	10
1 parameter treatment	10	18

While it is not surprising that the addition of a parameter improves the fit of the data, it is important to note that this treatment does remove the systematic trend of k' with hydrogen ion concentration and does so without invoking an unreasonable K_a . Consequently, it is concluded that over the range of hydrogen ion concentration and reactant concentration studied that only one transition state, $(\text{Fe}(\text{C}_5\text{H}_5)_2 \cdot \text{H} \cdot \text{HCrO}_4)^\ddagger$ is important.

In studies with excess chromium(VI) it was found that the stoichiometry is no longer given by Eq. 5. The ferricenium ion produced by the initial oxidation step is subsequently destroyed in a slower reaction by excess chromium(VI). In addition, to interpret data with chromium(VI) in excess successfully, the equilibrium constant and relaxation time for the reaction below (38), Eq. 27, must be known.

Attempts to measure this relaxation, Eq. 27, in 1:1 v/v H₂O-acetone were unsuccessful since the relaxation is complicated by the attack of chromium(VI) on the solvent at a rate comparable to that of Eq. 27.

INTERPRETATION AND DISCUSSION

Ferrocene-Ferricenium Ion Reactions

The 22 electron transfer reactions, as described by Eq. 2, have rate constants which are related to their respective equilibrium constants. Figure 10 shows a plot of $\log k_{ij}$ vs $\log K_{ij}$. The plot is approximately linear with the slope of the line shown being 0.55. The linearity and slope of this line are predicted by the Marcus cross-relation, Eq. 6, provided the exchange rates, k_{ii} and k_{jj} , remain approximately constant and provided that f_{ij} , Eq. 6, remains close to unity. Since f_{ij} is a function of K_{ij} one expects some curvature in a plot of this form, the extent of curvature being dependent on how significantly f_{ij} deviates from unity as well as on the assumed equality of all the exchange rates. For the data presented in Figure 10 the experimental error in k_{ij} in addition to these effects could disguise such curvature.

While Figure 10 then appears to be in reasonable agreement with the Marcus cross-relation a more rigorous test is possible, removing the assumption that all the exchange rates are identical. The method can be simply illustrated by considering only three ferrocene compounds. Three cross-reactions are possible between them, the resulting experimental

Figure 10. A plot of the log of the observed rate constant, k_{ij} , for the ferrocene-ferricenium ion electron transfer reactions, Eq. 2, vs the log of the respective equilibrium constants, K_{ij}

rate constants, say k_{12} , k_{13} , and k_{23} can be expressed in terms of their known equilibrium constants K_{12} , K_{13} , and K_{23} and unknown exchange rates k_{11} , k_{22} , and k_{33} as given by Eq. 6. The result is three equations and three unknowns.¹

Solving these three equations gives k_{11} , k_{22} , and k_{33} under the assumption that the Marcus relation is correct.

To apply this method more generally so as to utilize all the data in computing a "best" value for each exchange rate, a general solution for the separation of variables in the Marcus cross-relation was used. The relation is

$$\ln k_{ii} + \ln k_{jj} = A_{ij} \quad (28)$$

where $A_{ij} = (\ln k_{ij} - \frac{1}{2} \ln K_{ij} + \ln Z) - [(\ln Z - \ln k_{ij})^2 + \ln K_{ij}(\ln Z - \ln k_{ij})]^{\frac{1}{2}}$. Note that A_{ij} is a function only of the collision frequency Z ($\simeq 10^{11} \text{ M}^{-1} \text{ sec}^{-1}$) and of the experimentally determined cross-reaction rate k_{ij} and equilibrium constant K_{ij} . With more than three related reactions it becomes useful to fit Eq. 28 for the "best" k_{ii} , k_{jj} values. The 22 cross reactions and hence 22 equations such as Eq. 28 were fit for the best eight exchange rates k_{11} through k_{88} . The results of this compilation are given in Table 11.

¹The solution to these three equations for the three unknown exchange rates is given in the appendix of this thesis.

Table 11. Calculated exchange rates for the ferrocene-ferricenium ion reactions

	Substituted ferrocene	$k_{ij} \times 10^{-6} \text{M}^{-1} \text{sec}^{-1}$
1	1,1'-di-CH ₃	6.6
2	1,1'-di- <u>n</u> -C ₄ H ₉	6.7
3	<u>n</u> -C ₄ H ₉	6.5
4	Ferrocene	5.7
5	HgCl	5.3
6	CH ₂ OH	4.2
7	C ₆ H ₅	18.0
8	I	13.7

A more complete comparison of experiment and theory is shown in Figure 11 where $\log k_{ij}$ experimental is plotted vs $\log k_{ij}$ calculated. The latter values were computed assuming the Marcus equation, and using the eight "best" k_{ij} values resulting from the computational procedure. The mean deviation of observed and calculated k_{ij} values is 13%. The fit of experiment to theory is quite satisfactory and should be useful in a predictive sense. The k_{ij} values given in Table 11 do not vary greatly ($\sim$ a factor of four) for a rather wide range of compounds and it seems reasonable that other ferrocenes not too greatly different from the ones here should

Figure 11. A plot of $\log k_{ij}$ observed vs $\log k_{ij}$ calculated for the ferrocene-ferricenium ion electron transfer reactions, Eq. 2. The values of k_{ij} calculated were determined using Eq. 6, the exchange rates in Table 11, and the equilibrium constants in Table 8

have similar exchange rates. Consequently, the calculation of related ferrocene-ferricenium ion electron transfer rates would be straightforward. Obviously the direct measurement of some of the above calculated exchange rates by isotopic labeling or some other method would be useful in checking the validity of this model and these calculations. However, as mentioned in the introduction, the methods available for electron exchange studies are limited by the fact that no net chemical change occurs for exchange reactions. Stranks (3) has measured the ferrocene-ferricenium ion exchange rate, Eq. 1, determining the exchange rate constant, k_{44} , to be $1.7 \pm 0.4 \times 10^6 \text{ M}^{-1} \text{ sec}^{-1}$ at -70°C in methanol. While work at -75°C and -65°C was also done in that study, the narrow temperature range covered and the large experimental error associated with the method make quantitative extrapolation of the data to 25°C unrealistic. In the same publication Stranks compared several theoretical models to the observed rates. The model that best fit the observed rates was one derived by Marcus (8e,f) which allows the calculation of the exchange rate provided an estimate of the molecular radius, a , is available. Maximum and minimum values for a of $4.10 \text{ \AA}$ and $3.54 \text{ \AA}$ respectively were tried in the calculation since these were felt to

be the maximum and minimum radius of either ferrocene or ferricenium ion. The calculation using $a = 3.54 \text{ \AA}$ gave results in good agreement with the experimental rate constants measured at -70°C . From this model a value of $\sim 3 \times 10^8 \text{ M}^{-1} \text{ sec}^{-1}$ was calculated for the ferrocene-ferricenium ion exchange rate at 25°C . Since data obtained in this study at 25° 1:1 v/v H_2O - n -propanol cannot be directly compared to this value because of the difference in solvent, one experiment (last experiment given in Table 10) has been done in neat MeOH for the 1,1'-dimethylferrocene-ferricenium ion reaction. By comparing the value ($1.2 \times 10^8 \text{ M}^{-1} \text{ sec}^{-1}$) obtained from this experiment with the average value for this same reaction in 1:1 v/v H_2O - n -propanol of $0.23 \times 10^8 \text{ M}^{-1} \text{ sec}^{-1}$ it can be seen the rate increased a factor of five in going from 1:1 v/v H_2O - n -propanol to MeOH solvent. If this same factor is applied to our computed exchange rate we might then predict an exchange rate of $\sim 0.3 \times 10^8 \text{ M}^{-1} \text{ sec}^{-1}$ in MeOH at 25° for the ferrocene-ferricenium ion exchange. While this is somewhat lower than the value of $\sim 3 \times 10^8 \text{ M}^{-1} \text{ sec}^{-1}$ computed by Stranks, the difference may not be meaningful when the large errors associated with Stranks' calculation and our experi-

ment¹ and subsequent extrapolation is considered.

An alternate interpretation of the ferrocene-ferricenium ion electron transfer reactions is embodied in the Hammett equation (39), Eq. 29.

$$\log k_{ij} = \log k_{ii} + \rho_i \sigma_j \quad (29)$$

Where k_{ij} and k_{ii} are as defined earlier, ρ_i , a constant, is a function of the reaction but not the substituent, and σ_j , a constant, is a function only of substituent. For example, a plot of $\log k_{4j}$ (k_{4j} being the rate constant for the reaction of ferrocene with the other substituted ferrocenes) versus σ_j (Hammett parameter for j th substituent) should yield a slope of ρ_i and an intercept of k_{44} . However, since Eq. 29 was originally used to correlate reactions of substituted benzoic acids, the σ values available apply to either meta or para

¹Only one experiment was carried out in methanol for several reasons; (a) all E^0 data were obtained in other solvents, the use of these E^0 values to obtain an equilibrium constant necessary to treat the data obtained in methanol is at best an approximation, (b) the reaction rates were very fast in methanol and hence the error associated with their measurement is greater than the error for rates measured in 1:1 v/v H₂O-*n*-propanol, (c) the method of preparing ferricenium ion by iron(III) oxidation was not successful in neat methanol, hence ferricenium ion prepared for methanol experiments was prepared by Cl₂ oxidation of ferrocene in dilute H⁺ in methanol, the concentration of ferricenium ion prepared in this manner is less precisely known.

substituted benzoic acids. Use of these values for ferrocene reactions is not justified. Hall and Russell (30) have shown, however, that a linear combination ($\sigma_j = (\sigma_m + 2\sigma_p)/3$) of the meta and para σ values correlated the oxidation potentials of substituted ferrocenes quite well. (Presumably these σ_j values should now be usable for any ferrocene reaction since σ_j is not a function of the reaction). Using the potentials obtained in this study approximate values of σ_j can be obtained from Hall and Russell's plot of electrode potential vs σ_j . A plot of $\log k_{4j}$ vs σ_j is shown in Figure 12. This plot is in reasonable agreement with Eq. 29 and yields a k_{44} value of $5.9 \times 10^6 \text{ M}^{-1} \text{ sec}^{-1}$, which compares well with the value of $5.7 \times 10^6 \text{ M}^{-1} \text{ sec}^{-1}$ (Table 11) obtained from the Marcus treatment, and gives ρ_4 of +5.0. Similar plots have been made for the other ferrocenes where sufficient data are available and in general give similar ρ values, (as they should since ρ is a function only of the reaction) and give k_{ii} values close to those found in the Marcus treatment.

As can be seen from the above arguments, the rate of the electron-transfer reactions, Eq. 2, can be understood quite well in terms of only the free energy for reaction. This is to say that substituent effects, other than their electronic

Figure 12. A plot of the log of the observed rate constant for the oxidation of ferrocene by substituted ferricenium ions vs the substituent constant, σ_j . The σ_j values were obtained by interpolation of data given in reference (30). Values for points 41, 42, and 43 were calculated from the reverse rate constants and equilibrium constants given in Table 8.

effects on the ferrocene oxidation potential, are not important for the types of substituents and degree of substitution studied here. There do not appear to be steric requirements depending on the size or geometry of the substituents nor does "bridging" from ferrocene to ferricenium ion via substituents appear to be important in forming the transition state. This is not to say, however, that a more drastic change in the structure of the ferrocene would not produce a noticeable effect. For example, it was of interest to determine if π -cyclopentadienyl- π -(3)-1,2-dicarbollyl iron(II) and (III) and bis- π -(3)-1,2-dicarbollyl iron(II) and (III) (See Figure 1) would have reaction rates significantly different than those predicted from the ferrocene results. It was felt that one possible detailed mechanism might involve electron transfer through the cyclopentadiene rings of two ferrocenes "sitting-on-top" of one another. If this is the correct mechanism the boron cage in the carbollyl compounds would serve to lengthen the iron-iron distance in the transition state and also block off the ring coordinated to the iron atoms and, as a result, might slow the rate of electron-transfer. From the potentials for the carbollyl compounds (Table 4), if no rate retarding effect were realized, the rate of reaction of

any of the ferrocenes with either of the carbollyl compounds, or the rate of reaction between the two carbollyl compounds would be predicted to be too fast to observe. As can be seen from data in Table 10 these reactions were too fast to observe in this study. While observing a large rate retardation effect for the carbollyl compounds might have lent some support to the "sitting-on-top" mechanism the lack of such an effect does not rule out such a mechanism for the ferrocene-ferricenium ion reactions. Studies on a ferrocene with all carbons in the π -cyclopentadienyl rings having substituents on them (such as decamethylferrocene) would also be of interest with regard to this possible mechanism. Such studies have not yet been done.

Another plausible geometry of the transition state for these reactions might involve ferrocenes "side-by-side". To elucidate the role of this type of mechanism studies on ferrocenes having substituents which bridge from one cyclopentadiene ring to the other ring on the same ferrocene would be of interest (e.g. 1,1',3,3'-bis(trimethylene)ferrocene), since in compounds of this type the bridging substituent chains might hinder "side-by-side" approach.

A brief solvent and salt dependence was carried out and is given in Table 10. Goals of this study were two fold:

(a) it has previously been reported (3) that salts in general and chloride ion in particular catalyze the ferrocene-ferricenium ion exchange rate, Eq. 1, it was of interest to determine if this was also the case in this study; (b) in order to compare the ferrocene-ferricenium ion electron transfer studies with the iron(III)-ferrocene oxidation studies it was necessary to determine the effect of changing medium composition from H₂O-n-propanol (1:1 v/v) $\mu = 0.050$ maintained with Ba(ClO₄)₂ to H₂O-THF (1:1 v/v) $\mu = 1.00$ maintained with LiClO₄. From the data in Table 10 it can be seen that chloride ion, in concentrations up to 0.50 M, did not catalyze the ferrocene-ferricenium ion electron transfer reactions studied here. With regard to salt dependence the last few experiments in Table 10 show the rate constant, k_{24} , of the di-n-butylferrocene-ferricenium ion reaction in H₂O-n-propanol (1:1 v/v) to be 7.4 ± 0.5 , 12.8 ± 1.4 , and $21. \pm 1.0 \times 10^6 \text{ M}^{-1} \text{ sec}^{-1}$ in experiments with no added salt ($\mu = 0.0007$), $\mu = 0.05$ maintained with Ba(ClO₄)₂, and $\mu = 0.50$ maintained with LiClO₄ respectively. While the rate does increase with increasing salt concentration, the increase is not as large as the effect observed by Stranks where the rate became immeasurably fast at salt concentrations greater than $1 \times 10^{-3} \text{ M}$ (3).

In going from H₂O-n-propanol (1:1 v/v) to H₂O-THF (1:1 v/v) both with $\mu = 0.05$ Ba(ClO₄)₂ the rate decreases from 12.8 ± 1.4 to $3.85 \pm 0.2 \times 10^6 \text{M}^{-1} \text{sec}^{-1}$. However, on increasing the ionic strength to $\mu = 1.00$ maintained with LiClO₄ and HClO₄ in H₂O-THF (1:1 v/v) the rate increases to $24. \pm 2.0 \times 10^6 \text{M}^{-1} \text{sec}^{-1}$. Hence, the net effect on going from H₂O-n-propanol (1:1 v/v) $\mu = 0.05$ maintained with Ba(ClO₄)₂ (the conditions under which the ferrocene-ferricenium ion reactions were observed) to H₂O-THF (1:1 v/v) $\mu = 1.00$ maintained with LiClO₄ and HClO₄ (the conditions under which the iron(III)-ferrocene reactions were observed) is to increase the electron transfer rates by about a factor of 2 from 12.8 ± 1.4 to $24. \pm 2. \times 10^6 \text{M}^{-1} \text{sec}^{-1}$. This result will be used in the discussion of the iron(III)-ferrocene reactions.

Iron(III)-Ferrocene Reactions

The rates of oxidation of the substituted ferrocenes by iron(III) for seven of the ferrocenes (chloromercuriferrocene decomposes rapidly in acid solution) and one of the carbollyl compounds (π -cyclopentadienyl- π -(3)-1,2-dicarbollyliron(II)) were measured and found to be a function of their respective equilibrium constants, Figure 13. From Figure 13 it can be seen that the rate of the iron(III)- π -cyclopentadienyl- π -(3)-

1,2-dicarbollyiron(II) anion reaction falls on the same line with the ferrocene derivatives. In terms of the Marcus cross-relation this kind of behavior would suggest a similar exchange rate for the π -cyclopentadienyl- π -(3)-1,2-dicarbolly iron(II)-iron(III) reaction as for the ferrocene-ferricenium ion exchange rates. The slope of the line shown in Figure 13 is $\simeq 0.44$. It is difficult to compare directly Figure 13 with what is predicted from the Marcus equation since for these reactions the f_i values represent a significant and varying contribution to the predicted rate. However, since estimates of the ferrocene-ferricenium ion exchange rates are available (which have been shown not to change greatly, $\sim$ factor of 2, in going to this reaction medium) and since the iron(II)-iron(III) exchange rate has been measured in various solvents (40) a direct comparison between observed and predicted rate can be made. Using an iron(II)-iron(III)¹ exchange rate of $4 \text{ M}^{-1}\text{sec}^{-1}$ and multiplying each value in Table 11 by two for the ferrocene-ferricenium ion exchange rates the plot shown

¹It was shown in reference (40) that the Fe(II)-Fe(III) exchange rate was in the range of 1 to $8 \text{ M}^{-1}\text{sec}^{-1}$ for various mole fractions of methanol, ethanol, or *n*-propanol. The value of $8.22 \text{ M}^{-1}\text{sec}^{-1}$ was obtained for 0.50M aqueous perchloric acid.

Figure 13. A plot of $\log k_i$, Eq. 4, vs $\log K_i$, the equilibrium constant for the reaction described by Eq. 4

in Figure 14 is obtained. As can be seen from Figure 14 the observed rates are in very poor agreement with calculated rates and are from 25-200 times lower than predicted. The lack of agreement of theory and experiment for the iron(III)-ferrocene reactions is not particularly surprising. In the derivation of Eq. 6 the assumption is made that the work terms associated with bringing reactants and products together cancel or are negligible, however, it has been pointed out by Marcus (8b) that this assumption is likely to break down when the work terms of the two exchange reactions and the cross-reaction are not quite similar. For example, for an electron transfer reaction between two substituted trisphenanthrolineiron complexes the assumption should be valid because the work terms of the two exchange reactions and the corresponding electron transfer reaction will be very similar. Alternatively if the cross-reaction was between two pairs of aquo ions where only charge is transferred again the work terms should cancel. However, for the reaction between an aquo ion, say iron(III), and trisphenanthrolineiron(II) Marcus argues that there is no reason to expect the work terms of the two exchange reactions and the electron transfer reaction to be equal. Similarly in the iron(III)-ferrocene reactions

Figure 14. A plot of $\log k_i$, Eq. 4, observed vs $\log k_i$ calculated. The solid line represents the predicted line from the Marcus equation and the dashed line is a line drawn through the observed points. The k_i calculated values were obtained by assuming Eq. 6 and using a value of $4\text{M}^{-1}\text{sec}^{-1}$ for the iron(II)-iron(III) exchange and twice the values given in Table 11 for the ferrocene-ferricenium ion exchange rates, Eq. 3

there is no reason to expect the work terms for hexaaquairon (II)-(III) exchange and the ferrocene-ferricenium ion exchange to be similar, or to be equal to the cross-reaction work terms.

When the work terms fail to cancel Marcus claims two deductions may be made (8b): (1) the observed rates will be lower than the predicted rates due to an unaccounted for contribution to the free energy of activation from the work terms, (2) if ratios of related reactions k_{12}/k_{13} are considered the work terms should again cancel. In looking at Figure 14 point (1) is evident. The comparison suggested by point (2) has been attempted and while in principle it should be a useful comparison the large error associated with the experimental rate constants greatly reduces its usefulness (24). Sutin (12) has observed that the experimental electron-transfer rates between substituted trisphenanthrolineiron(III) and iron(II) and between substituted trisphenanthrolineiron (II) complexes and Ce(IV), Mn(III), and Co(III) are lower than corresponding calculated rates from Eq. 6. In all but the Co(III)-trisphenanthrolineiron(II) reactions it was suggested that the discrepancy in observed and calculated rates resulted from non-cancellation of work terms as described

above, point (1).

Ferrocene-Chromium(VI) Reaction

The chromium(VI)-ferrocene reaction is of particular interest since the mechanisms of chromium(VI)-transition metal complex reactions have been extensively studied (41). The oxidation of ferrocene by chromium(VI) is consistent with a mechanism involving three one-equivalent steps, Eq. 30.

Mechanisms involving two-equivalent steps are disfavored since oxidation of ferricenium ion results in irreversible decomposition of the metallocene and it is known that the ferrocene-chromium(VI) reaction gives the stoichiometric amount of ferricenium ion. Furthermore it is known (42) that the chronopotentiometric oxidation of ferrocene is a one-equivalent reversible oxidation to ferricenium ion. Increasing the voltage to as high as +1.4 V versus SCE did not produce another oxidation wave for the ferrocene-ferricenium ion solutions. Hence, it does not seem possible that Cr(VI) could be involved

in a two-equivalent oxidation of ferrocene. This is not a surprising result since most chromium(VI) oxidations of transition metal complexes are thought to proceed via the one-equivalent mechanism (41).

The fact that only one transition state, $[\text{Fe}(\text{C}_5\text{H}_5)_2 \cdot \text{H} \cdot \text{HCrO}_4]^\ddagger$, is found for this reaction and that $\text{Fe}(\text{C}_5\text{H}_5)_2^+$ ion was not found to retard the rate indicate that (if mechanism 30 is the correct mechanism) step k_5 corresponds to the rate determining step and that k_4 and k_3 are rapid. In general for chromium(VI) oxidations where the one equivalent mechanism has been invoked the first step has been found rate determining in substitution inert complexes, such as $\text{Fe}(\text{CN})_6^{4-}$, $\text{Fe}(\text{CN})_4(\text{bipy})^{2-}$, $\text{Fe}(\text{CN})_4(\text{bipy})_2^{2-}$, $\text{Fe}(\text{CN})_2(\text{bipy})_2$, $\text{Fe}(\text{phen})_3^{2+}$, $\text{Fe}(\text{bipy})_3^{2+}$ and the second step has been found rate determining with labile transition metal complexes (41) ($\text{Fe}(\text{OH}_2)_6^{2+}$, VO_2^+). The results of the ferrocene-chromium(VI) reaction are also in agreement with this general point.

The hydrogen ion dependence of the chromium(VI)-ferrocene reaction can be interpreted in several ways: (a) a third-order reaction between H^+ , HCrO_4^- and ferrocene, (b) a second-order reaction between H_2CrO_4 and ferrocene, or (c) a second-order reaction between a protonated ferrocene cation, $\text{Fe}(\text{C}_5\text{H}_5)_2 \cdot \text{H}^+$ and HCrO_4^- (in addition to any other mechanism

which produces the correct composition of the transition state). All of these mechanisms are of course kinetically indistinguishable. A preference for mechanisms (b) and (c) can be expressed since they involve only bimolecular processes while mechanism (a) is a third-order process. A choice between mechanisms (b) and (c) is more difficult since both species $\text{Fe}(\text{C}_5\text{H}_5)_2 \cdot \text{H}^+$ (43) and H_2CrO_4 are known to be present in acidic solution.

APPENDIX

Exchange Rate Solution to the Marcus Equation

The Marcus cross-relation is:

$$k_{ij} = (k_{ii} \cdot k_{jj} \cdot K_{ij} \cdot f_{ij})^{\frac{1}{2}} \quad (1A)$$

where

$$\ln f_{ij} = (\ln K_{ij})^2 / 4 \ln(k_{ii} \cdot k_{jj} / Z^2)$$

Taking the natural logarithm of (1) and rearranging gives:

$$-\frac{1}{2}(\ln k_{ii})^2 + \ln k_{ii}(\ln k_{ij} - \ln k_{jj} - \frac{1}{2}\ln K_{ij} + \ln Z) + \quad (2A)$$

$$(\ln k_{jj} - 2\ln Z)(\ln k_{ij} - \frac{1}{2}\ln k_{jj} - \frac{1}{2}\ln K_{ij}) - \frac{1}{8}(\ln K_{ij})^2 = 0$$

Equation 2A is of the form $ax^2 + bx + c = 0$, where;

$$a = -\frac{1}{2}$$

$$b = (\ln k_{ij} - \ln k_{jj} - \frac{1}{2}\ln K_{ij} + \ln Z)$$

$$c = (\ln k_{jj} - 2\ln Z)(\ln k_{ij} - \frac{1}{2}\ln k_{jj} - \frac{1}{2}\ln K_{ij}) - \frac{1}{8}(\ln K_{ij})^2$$

$$x = \ln k_{ii}$$

The solution to this quadratic equation after algebraic rearrangement is:

$$\ln k_{ii} + \ln k_{jj} = A_{ij} \quad (3A)$$

$$A_{ij} = [(\ln Z - \ln k_{ij})^2 + \ln K_{ij}(\ln Z - \ln k_{ij})]^{\frac{1}{2}}$$

Given 3 equations of the form of Eq. 3A,

$$\ln k_{11} + \ln k_{22} = A_{12}$$

$$\ln k_{11} + \ln k_{33} = A_{13}$$

$$\ln k_{22} + \ln k_{33} = A_{23}$$

the following solutions for k_{11} , k_{22} , and k_{33} are obtained:

$$k_{11} = \exp[(A_{12} + A_{13} - A_{23})/2]$$

$$k_{22} = \exp[(A_{12} + A_{23} - A_{13})/2]$$

$$k_{33} = \exp[(A_{13} + A_{23} - A_{12})/2]$$

For more than three related equations the solutions are over-determined and are best obtained by a computer fit of Eq. 3A. A program to do this has been written¹ and is listed here.

¹This program was written by the Ames Lab computer service group, Iowa State University, Ames, Iowa.


```

DIMENSION A(28,8),Y(28),AT(8,28),DK(8),CK(28),X(8)
M=22
N=8
READ (1,900) ((A(I,J),J=1,N),I=1,M)
READ (1,930) (Y(I),I=1,M)
930 FORMAT (8F10.7)
IRANK=8
EPS=.1E-05
DO 5 I=1,M
5 WRITE (3,920) (A(I,J),J=1,N)
WRITE (3,920) (Y(I),I=1,M)
S=0
DO 10 I=1,M
10 S=S+A(I,1)**2
S=1./S
DO 20 I=1,M
20 AT(1,I)=S*A(I,1)
DO 200 K=2,N
KK=K-1
DO 40 I=1,KK
S=0.
DO 30 J=1,M
30 S=S+AT(1,J)*A(J,K)
40 DK(I)=S
SUM=0
DO 60 I=1,M
S=0
DO 50 J=1,KK
50 S=S+A(I,J)*DK(J)
CK(I)=A(I,K)-S
60 SUM=SUM+ABS(CK(I))
SUM=SUM/M
IF (SUM.GT.EPS) GO TO 90
IRANK=IRANK-1
S=1
DO 70 I=1,KK
70 S=S+DK(I)**2

```

```

      Q=1./S
      DO 80 I=1,M
      S=0
      DO 75 J=1,KK
75    S=S+DK(J)*AT(J,I)
80    AT(K,I)=Q*S
      GO TO 100
90    S=0
      DO 95 I=1,M
95    S=S+CK(I)**2
      S=1./S
      DO 98 I=1,M
98    AT(K,I)=S*CK(I)
100   DO 120 I=1,KK
      DO 110 J=1,M
110   AT(I,J)=AT(I,J)-DK(I)*AT(K,J)
120   CONTINUE
200   CONTINUE
      WRITE (3,910) IRANK
910   FORMAT (I4)
      DO 220 I=1,N
      S=0
      DO 210 J=1,M
210   S=S+AT(I,J)*Y(J)
220   X(I)=S
      WRITE (3,920) (X(I),I=1,N)
920   FORMAT (8F15.7)
900   FORMAT (8F5.2)
      ERR=0
      DO 240 I=1,M
      E1=0
      DO 230 J=1,N
230   E1=E1+A(I,J)*X(J)
      ERR=ERR+(Y(I)-E1)**2
240   CONTINUE
      WRITE (3,920) ERR
      STOP
      END

```

For this program M is the number of equations like Eq. 3A to be fit and N is the highest value of i and j.

A data deck consists of M cards block loaded in NF 5.2 format. Each card contains the coefficient either 1 or 0 for the N i and j in the N columns. These M cards are followed by the M A_{ij} values loaded in 8F10.7 format.

For example, for $M = 22$, and $N = 8$ if the first equation like Eq. 3A is: $\ln k_{11} + \ln k_{22} = 10.0$ the first card in the data deck would contain a 1 in columns one and six and a decimal in columns two and seven. Card 23 would have 1, 0, and a decimal in columns one, two, and three respectively. If the 22nd equation is: $\ln k_{55} + \ln k_{88} = 30.0$; then the 22nd card in the data deck would contain a 1 in columns 21 and 36 and a decimal in columns 22 and 37. The last value on the last card would then contain 30.0 in 8F10.7 format.

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