# Production of $K^{+} K^{-}$and pp paira in Four-body reactiong at $13.1 \mathrm{GeV} / \mathrm{e}$.* 

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Abstract: Data in the channelg m+p }\mp@subsup{\pi}{0}{+}\mp@subsup{\pi}{}{+}P\mp@subsup{K}{}{+}\mp@subsup{K}{}{+
and #+p}->\mp@subsup{\boldsymbol{\pi}}{}{+
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## A. Introduction

We have extended an analysis of the four-constraint four-prong $\pi^{+}{ }_{p}$ Interactions at $13.1 \mathrm{GeV} / \mathrm{c}$ to include $\mathrm{K}^{+} \mathrm{K}^{-}$and Pp pairs. The data derives from a $\sim 9$ event/ $\mu \mathrm{b}$ equivalent exposure obtained in the SLAC $82^{\prime \prime}$ hydrogen bubble chamber. The r-f separated $\pi^{+}$beam had a momentum spread of $\sim 1.5 \%$ in the chamber; however, from the known dispersion, beam nomenta were correlated with chamber coordinates and determined to ${ }^{\circ} .5 \%$.

The $\mathrm{K}^{+} \mathrm{K}^{-}$and $\mathrm{P} \mathrm{\bar{P}}$ candidates were selected from some 70,000 events which failed the $\pi^{+} \mathrm{p}^{+} \pi^{+} \pi^{-}$hypothesis [1] and for which the unbalance of measured momenta was less than $2 \mathrm{GeV} / \mathrm{c}$. By varying the beam until momentum was conserved,
 was suggested and employed by Ehrlich et al. [2]. This procedure was complicated in most cases by the inability to uniquely identify $\pi^{+}, \mathrm{p}, \mathrm{K}^{+}$components of the three positive tracks produced; for these events, permutations of identity were included. The mass spectrum of the assumed particle-antiparticle paizs thus obtained, contained large contributions extending through the K and P mass values. Those combinations for which at least one permutation had $\mathrm{m}^{2}>\left(5 \mu_{\pi}\right)^{2}$ $\sim 13,500$ events, were processed in the usual manner by the SQUAW fitting routines with $\Pi^{+} \mathrm{pK}^{+} \mathrm{K}^{-}$and $\mathrm{T}^{+}{ }^{+}-\overline{p p}$ four-constraint hypotheses. Each of the 1,310 events passing SQUAW was examined on the scanning table to ascertain whether observed Lonizations were consistent with particle assignments of the fitted hypothesis; 560 events were acceptable. Finally a $P\left(X^{2}\right)<.1 \%$ cut was imposed, reducing the sample to 468 good events. The $m^{2}$ distribution of those combinationa which passed SQUAW is shown in Fig. 1; the solid sub-histogram cor* responds to the 468 good events. The ordinate label applys strictly only to the solid area in that there are from $1 \rightarrow 6$ combinations possible before applying the lortzation criterion. Evidently the $\overline{K K}$ and $\mathbf{P P}$ events are well separated in $\mathrm{mi}^{2}$. This selection yielded $343 \pi^{+} \mathrm{PK}^{+} \mathrm{K}^{-}$and $125 \pi^{+} \mathrm{p}$ $\overline{\mathrm{p}}$ events, corresponding to crosa sections of $39 \pm 8 \mu \mathrm{~b}$ and $14 \pm 5 \mu \mathrm{~b}$ respectively.

Each step in sifting the data preferentially reduced the number of event points outside of the $K$ and $p$ mass ranges in the $m^{2}$ plot, the final chisquared cut nearly eliminating values of $\mathrm{m}^{2}$ not in the desired peaks. It 2 is apparant that selecting only on narrou $m$ bands about the $K$ and $p$ masses in the original data sample would save much labor and generate little real event loss; our choice of $m^{2}>54 \pi^{2}$ was very conservative.

The ratios $\Pi^{+} \mathrm{P} \mathrm{K}^{+} \mathrm{K}^{-} / \pi^{+} \mathrm{PH}^{+} \pi^{-\quad}$ and $\pi^{+}{ }_{\mathrm{PPP}}^{-} / \pi^{+} \mathrm{p}^{+} \pi^{-}$are $\sim 1 / 30$ and $\sim 1 / 85$ respectively at $13.1 \mathrm{GeV} / \mathrm{c}$. If we define $\mathrm{r}(\mathrm{a})$ as the ratio of cross sections for $\pi^{+} p \rightarrow \pi^{+} p$ aa production at $8 \mathrm{GeV} / \mathrm{c}^{[3]}$ to that at $13.1 \mathrm{GeV} / \mathrm{c}$. The data yields $\mathrm{t}\left(\mathbb{1}^{+}\right)$; $\mathrm{r}\left(\mathrm{K}^{+}\right): \mathrm{r}(\mathrm{p})=1.61$ 1.8: 1.1 witch can be compared with $\left(\mathrm{P}_{1 \mathrm{ab}}=8.0 / \mathrm{P}_{1 \mathrm{ab}}=13.1\right)^{-.5}=1.3$. B. $\boldsymbol{T}^{+} \mathrm{P}^{+} \mathrm{K}^{-}$

A scatterplot of $\mathrm{M}\left(\mathrm{K}^{-} \mathrm{T}^{+}\right)$vs $\mathrm{M}_{\left(\mathrm{T}^{+} \mathrm{p}\right.}$ ) is given in fig, 2 , with a projection on the $M\left(\Pi^{+}+\right.$axis showing a conspicuous $\Delta^{++}$signal of $\sim 99$ events within the mass band $M(\Delta)=1.24 \pm .1$ Gev. Events in the $K^{*}(890)-\Delta^{++}$overlap region were divided between the $\Delta$ and $K^{*}$ in ratio to the poptilation of their respective non-overlapping adfacent side bands. The projection on the M(K $\mathrm{H}^{+}$) axis is given in fig. 3(a), where the shaded portion corresponds to removal of $A^{++}$events. There are $\sim 106$ points in the $K^{*}$ ( 890 ) region defined as $M\left(K^{*}\right)=0.89 \pm .1 \mathrm{GeV}$, and in addition there is some indication of $a \mathrm{~K}^{*}(1420)$ signal. Removing the $K^{*}(890)$ bend yields the shaded area in the M( $\left.\mathrm{r}^{+} \mathrm{p}\right)$ distribution of fig. 2. The marginal enhancenent at ditrip) $\sim 1.6$ Gev is also observed in the $\pi^{+} \mathrm{pr}^{+} \Pi^{-}$data where again it is more suggestive than indicative. Within the present data, the $A^{+4}$ decay is described by ( $1+3 \cos ^{2} \theta_{J}$ ) where $\theta_{J}$ is the usual Jackson angle; the $M\left(T^{+}{ }^{+}\right) \sim 1.6$ Gev region is flat in $\cos \theta_{j}$, and beyond $\mathrm{M}\left(\mathrm{TH}^{+} \mathrm{P}\right) \sim 1.7 \mathrm{GeV}$, the eventa are almost wholiy within $\cos \theta_{3}>.8$.

The $M\left(K^{+}{ }^{-}\right)$spectrum is given in fig. 3-b where the hatched area indicates removal of $\mathrm{K}^{*}$ ( 890 ) events and the double hatched portion shows the $\mathrm{M}\left(\mathrm{K}^{+} \mathrm{K}^{-}\right.$) distribution produced with the $\Delta$. There is, perhaps, an indication of a shoulder in the or $S^{*}$ band and a modest $f^{\circ}$ and/or $A_{2}{ }^{0}$ signal. Selecting on the $A$ does not sharpen the $f^{0} / A_{2}$ signal, a result evidently different from the 8 Gev data. ${ }^{[3]}$ A preliminary sample of $\sim 50$ events in the $\pi^{+}{ }^{+} K^{0}{ }^{0}$ channel also shows no signal, and comparably modest $F^{\circ} / A_{2}{ }^{\circ}$ production. $[4]$ The M(K $p$ ) spectrum suggesta no clear resonance fonmation.

A lownasg_enhancenent is evident in the $M\left(K^{+} K^{\prime \prime} \boldsymbol{T}^{+}\right)$distribution in fig. 4 . The hatched area remains after removed of $\Delta^{++}$events and the double-hatched part is left following the further substraction of $\mathrm{K}^{*}(890)$ events. A possible explanation of the $M\left(K^{*} K\right)$ threshold enhancement will be given in the following section.
C. $K^{*} K P$

The $\mathrm{K}^{*}$ Kp subsampie of the data is characterized by low four-momentum trangers $t\left(\Pi K^{*}\right), t(\Pi K)$ and $t(p p)$ and consequently a tendancy towards Iow values of $M\left(K^{*} K\right)$; these features are reniniscent of the (户, 1 ) behaviour through the $A_{1}$ enhancement region and suggest that a similar interpretation in terns of double-exchange peripheral amplitude may be appropriate [1]. By requiring $-t\left(\pi K^{*}\right)$ and $-t(\Pi K)<2.0(G e V / c)^{2}$ and $-t(p p)<0.5$ (GeV/c) ${ }^{2}$ a peripheral set of 60 events is obtained with the t-distributions shown in fig. 5; also pictured is the double-Regge diagran assumed. The amplitude was taken as
with the usual Reggeized $K^{*}$-exchange propogator $R\left(K^{*}\right)^{\dagger}$ and a linear trojectary $\alpha_{K}^{*}=1-\alpha^{\prime \prime}(0)_{K}{ }_{K}\left[M_{K} *^{2}=t\right]$. The values $\alpha^{\prime}(0)_{K}^{*}=1(G e V / c)^{2}$ and $S_{0}=1(G e V / c)^{2}$ are used throughout. Pomeranchuk exchange is described by $0_{\text {Pom }}=1$ and an expanential residue determined from elastic scattering. The predictions are normalized to the dsta and comparisons to the t-spectra and mass distributions are shown in fig. 5 and fig. 6 respectively. Evidently there is no necessity
to include a diggram involving $K$-exchange ( $K$ *and $K$ positions interchanged). Dualicy arguments would suggest that the observed $M\left(\mathrm{~K}^{*} \mathrm{~K}\right)$ threshold enhancement corresponds to the existence of a resonance in the $K{ }^{*}$, system at a low mass value; in addition to the $A_{3}(1640)^{\dagger}$, there is a reported abnormal (spin-parity) state decaying into the $\mathrm{KK}^{*}$ channel with a mass of 1.54 GeV , 1isted as the $\mathrm{F}_{1}$. ${ }^{\text {[5] }}$
D. $\mathrm{K}^{+} \mathrm{K}^{-} \mathrm{A}^{++}$

A description of the $K^{+} K^{-} \Delta$ channel is given in terms of che doubleexchange diagram shown in fig.7. There are 49 events within the kinematical region defined by $-t\left(\pi K^{+}\right)<1.0(\mathrm{GeV} / \mathrm{c})^{2}$ and $-t(\mathrm{pA})<0.5(\mathrm{GeV} / \mathrm{c})^{2}$. The couble-Regge amplitude assumed to describe this data is teken as:

$$
A\left(K^{*} \pi\right)=R\left(K^{*}\right)\left(S_{K^{+}} K^{-/ S_{0}}\right)^{\alpha_{K} K^{*}} \cdot R(\pi)\left(S_{K_{p}}^{-} / S_{0}\right)^{\alpha}
$$

with $\alpha_{\pi}=-\left(\mu_{j T}^{2}-t(p A)\right)$ and $R\left(K^{*}\right)$ as in section $C$. The $t$ distributions and mass spectra are given in fig. 7 and fig. 8 respectively along with curves representing the predictions of $A\left(\mathrm{~K}^{*} \pi\right)$. Although sparse, the dsta are well described by the double-exchange mechanism.
E. $\Pi^{+}{ }^{+} \overline{P P P}$

Both combinations of $M\left(\pi^{+} p\right)$ are shown in fig, $\theta$-a where $\Delta$ production is clearly evident, with approximately $30 \%$ of the reaction involving a 0 . The curve in fig. 9-a is the prediction of phase space. There is no suggestion of a resonant atace at 3.755 GeV in the $M$ (ppp) distribution shown in fig. 9-b; the only deviation from phase space is the high rass peaking which reflects $\Delta$ formation in $M\left(\pi^{+} p\right)$. ${ }^{[3]}$ The $M(\overline{p p})$ spectrum is given in Eig. 10; the two small enhancements in the low masa range may correspond to production of $N \bar{N}(2190)$ and $\rho$ (2290) respectively. [6]
P. Conalusion

The reaction $\pi^{+} p \rightarrow \pi^{+} \mathrm{pK}^{+} \mathrm{K}^{-}$occurs with a frequency of $1 / 30$ th of that of the $\pi^{+} p \pi^{+} \pi^{-}$chanel; whereas the latcer is dominsted by $p, f^{0}$ and $d^{++}$production,
the former consists mostly of the $K^{*}(890)$ and $\Delta^{++}$states, each of which constitutes $\sim 30 \%$ of the resction; there is some evidence for a $\chi^{*}(1420)$. The significant difference is the lack of two-particle final states in the $\mathrm{K}^{+} \mathrm{K}^{-}$ case, no evidence for a strong (e.g.) is observed. The d\&ta are consistent with the predictions of double-Regge exchange; $\mathrm{K}^{*} /$ Pomeranchuk exchanges in the $\mathrm{K}^{+} \mathrm{K}^{-} \mathrm{p}$ state and $\mathrm{K}^{*} / \pi$ exchanges in the $\Delta^{++} \mathrm{K}^{+} \mathrm{K}^{-}$channel. The $\Pi^{+}{ }_{\mathrm{P}} \rightarrow \pi^{+}{ }_{\mathrm{p} P \mathrm{p}}^{-}$ reaction is 2.8 times less frequent than the $\pi^{+} \mathrm{pK}^{+} \mathrm{K}^{*}$ state. Formation of $\Delta^{+\boldsymbol{+}}$ occurs in $\sim 30 \%$ of these events with the remainder evidently following phase spare. At resonance at $M(\overline{p p D})=3.755 \mathrm{GeV}$, reported by Ehrlich et al. [2], was not obaerved.
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M. Aguilar-Benitez et al., Phys. Letters 29B (1969) 379.
(6) Reviews of Particle Properties, Phys. Letters 338 (1970).

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\because, t R(i)=\frac{\left[1+\tau_{i} e^{-i n \alpha_{i}}\right]}{\Gamma\left(1+\alpha_{i}\right) \sin \left(\pi \alpha_{i}\right)}
$$

it The possibility that the low masa $\mathrm{KK}^{*}$ enhanceant ia a decay made of the diffractively produced $A_{3}$ (1640) 1: under investigation.

Fig. 1. Distribution $i n m^{2}$ for the reaction $\pi^{+}{ }_{p} \rightarrow \pi^{+}{ }_{p n+}{ }^{+} m^{-}$at $\mathrm{GeV} / \mathrm{c}$ of those event combinations for which a fit was obtained with $m=M_{K}$ or $K_{p}$. The solid area indicates the $m^{2}$ distribution of the final good event $s$ smple.
Fig. 2. Scatterplot of $M\left(K^{-} n^{*}\right)$ va, $M\left(\pi^{+} p\right)$ axi日. An event with $\left|M\left(\pi^{*} p\right)=1.236\right|<0.1$ GeV was accepted as a $\Delta^{+4}$; the solid area corresponds to the removal of $K^{*}(890)$ points.

Fig. 3. (a) Distribation in $N\left(K^{-} \pi^{+}\right)$; the hatched portion remains after $\Delta^{+\dagger}$ Sube craction.
(b) Distribution in $M\left(K_{.}^{+} K^{-}\right)$; removal of $X^{*}(890)$ eventa yielda the hatched area and aelecting on the ${S^{+}}^{+}+i^{+}$ives the crosa-hatched spectrum.
Fig. 4. Distịibution in $M\left(K^{+} K^{-} n^{+}\right)$; removing $\Delta^{+\dagger}$ evente gives the hatched spectrum; further removal of $\mathrm{K}^{*}(890)$ data yielde the cross-hatched area.

Fig. 5. Four-momentum transfer distributione in the procese $\pi^{+} p \rightarrow p X^{+} X^{*}(890)$; the curves represent the prediction of the doubleexchange diagram shown.
Fig. 6. Invariant mase distributiona in the reaction $\pi^{\dagger} p \rightarrow p K^{+} \mathrm{K}^{*}(890)$; the curves are from the double-Regge model.

Fig. 7. Fourmmontum tranafer diatribucions in the process $\pi^{+} p \rightarrow \Delta^{++} K^{+} K^{-}$; the curves repreaent the predictions of the double-exchange diagram shown.

Yig. B. Invariant mase distributions in the reaction $\pi^{+} p \rightarrow d^{++} K^{+} X^{-}$; the curves are from the double-Regge model,

Fig. 9. (a) Dietribution in $M\left(\pi^{+} p\right.$ ) of the reaction $\pi^{+} p \rightarrow \pi^{+} p p p$ at $13.1 \mathrm{GeV} / \mathrm{c}$.
(b) Diatribution in $M\left(p p_{p}\right)$ of the reaction $\pi^{+} p \rightarrow \pi^{\dagger} p p p$ at 13.1 cev/e.







EVENTS / O.1 GeV



## EVENTS / 0.15 GeV

EVENTS / 0.10 GeV


EVENTS / O.I GeV


EVENTS / 0.05 GeV




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