





Investigation of Simple Daily Solar Radiation Models Suitable for Use in the Design of Solar Heating Systems

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SANFORD SILLMAN

AUGUST 1980

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FOREWORD

This document is based on research done by the author as a consultant to Gordon Tully of Massdesign Architects. It describes a simple procedure for modeling daily solar radiation that can be used in the design of solar heating systems. The data in this report provide support for projects in the Building Systems Development Branch of the Solar Energy Research Institute, including analysis of annual storage systems and development of design tools.

The author wishes to express appreciation to Frank Baylin and Michael Holtz, both of whom reviewed the completed document and provided valuable advice in its preparation, and to Gordon Tully, who collaborated in the development of the original concept.

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Building Systems Development Branch

Approved for:

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SUMMARY

Solar heating system simulations typically require the use of hourly weather data. While these simulations are highly accurate, they are only of use to designers who have access to a main-line computer. A simpler alternative would be to model daily system performance using daily rather than hourly weather data. This approach has been used in simulations such as TEANET which are designed for use on programmable calculators. Such programs are generally intended to simulate a day or week rather than a full year.

This paper investigates simulation of the annual performance of solar heating systems based on daily weather data. If accurate, such a simulation would require only 1460 data inputs for a year's run, instead of 10,000 inputs for an hourly simulation, and could be run easily on a microcomputer.

The simulations investigated here are all based on sinusoidal models for daily solar radiation. The most accurate radiation model requires as input data the maximum and total insolation for each day. The maximum and daily total insolation uniquely determine a sine curve, which is taken as the daily solar radiation pattern. The more common approach of modeling radiation by a sine curve with frequency based on day length is found to be inaccurate. Since maximum daily insolation is rarely tabulated, alternate models for daily radiation requiring only the total daily insolation as input are also investigated.

A theoretical comparison is made between daily radiation model results and hourly data for each day of the year in ten cities. In addition, performance of the daily radiation models in active solar heating system simulation is assessed. It is found that when an hourly step simulation is performed using daily weather data and a sinusoidal model for radiation in place of hourly data, the resulting error is always less than 1.5%. Use of a daily step simulation is found to be accurate for evacuated tube collector systems or for flat plate collector systems with large storage capacity (enough to meet the load of three days or more). For flat plate collector systems with smaller storage, daily step simulation underestimates annual system performance by up to 5%. Simulation results using daily weather data also compare favorably with f-chart and with designs for annual storage solar heating systems.

It is concluded that the use of daily weather data with a radiation model is of sufficient accuracy to be used in place of hourly weather data in the simulation of active solar heating systems. It is also concluded that efforts should be made to collect and tabulate daily total and maximum insolation data on which the daily radiation model is based.

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SECTION 1.0

INTRODUCTION

The design of solar heating systems is difficult because system operation typically varies from hour to hour, in response to insolation. As a result, design methods often are based on hour-by-hour simulation, requiring hourly weather data. While simulations such as TRNSYS are highly accurate, they are of limited usefulness to designers because they require access to a main line computer. The alternative to hourly simulation is a design code, such as f-chart, or solar load ratio for passive design. These codes are easy to use but are limited in applicability and often cannot reflect innovative designs.

This paper presents an investigation of sinusoidal models for daily solar radiation that could be used in a day-by-day simulation of solar heating systems. If accurate, this type of simulation would require only 1,000-1,500 data inputs for a complete year's run, and could be run on a microcomputer. Hourly simulations, by contrast, require over 10,000 data inputs for a year's run. Simple daily radiation models already have been used in simulations designed for programmable calculators, such as the TI-59. However, these simulations are aimed at modeling daily system performance rather than accurately reflecting annual performance. The accuracy of daily radiation models for annual runs will be the subject of this paper.

Accuracy of the daily radiation models wil be assessed in two ways. First, an hour-by-hour comparison will be made to Typical Meteorological Year weather data. Second, results of actual system simulations will be presented and compared to results of standard hourly simulations.





SECTION 2.0

SIMPLE SOLAR RADIATION MODELS

The simplest daily radiation model is a sinusoidal function of the form:

$$Q(t) = Q_k \cos \omega t \qquad (2-1)$$

where t is the time of day in hours with solar noon set at zero. The parameters \boldsymbol{Q}_{k} and $\boldsymbol{\omega}$ are to be set based on daily radiation data.

There are two independent ways of setting Q_k and ω . One method is to set ω (in radians) accurately based on day length (t_D) :

$$\omega = \pi/t_{D} \quad . \tag{2-2}$$

Calculation of the day length, t_D , will be presented in Appendix B. The other parameter, Q_k , is set so that the total radiation equals the actual total radiation from weather data. Thus,

$$Q_{k} = \frac{1}{2} \omega \cdot QTOT \qquad (2-3)$$

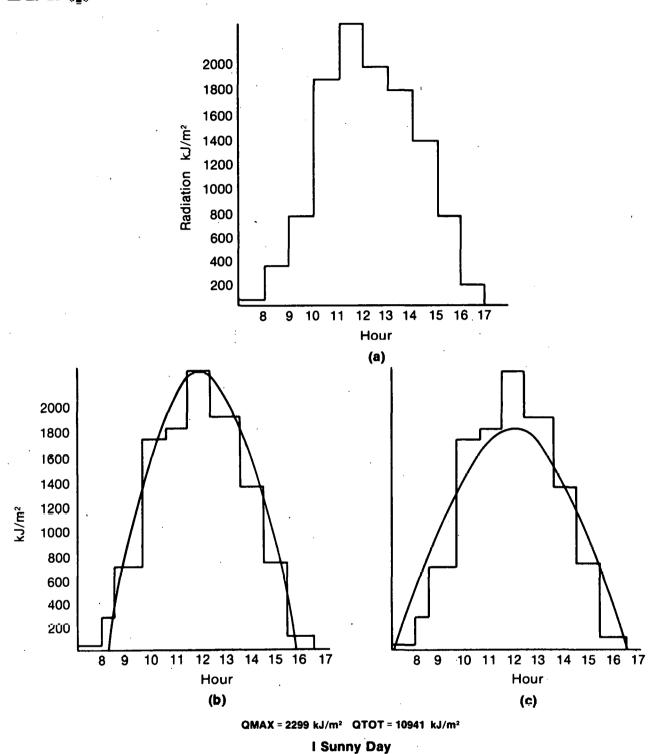
QTOT will be used henceforth for the actual daily total radiation from weather data.

The second method is to set Q_k to accurately reflect the actual daily maximum hourly insolation (henceforth known as QMAX). Maximum insolation is found from the hourly Typical Meteorological Year data, with the daily maximum (QMAX) set equal to the maximum hourly insolation during the day. In this method, Q_k is set equal to QMAX, and ω is calculated to assure that total daily radiation equals the actual total (QTOT). Thus,

$$Q_k = QMAX$$

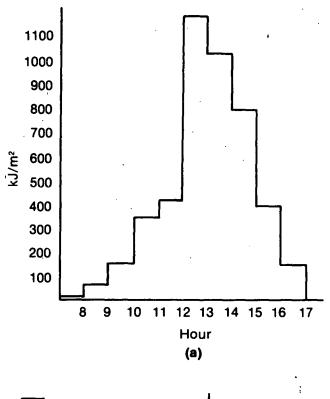
$$\omega = 2 QMAX/QTOT . \qquad (2-4)$$

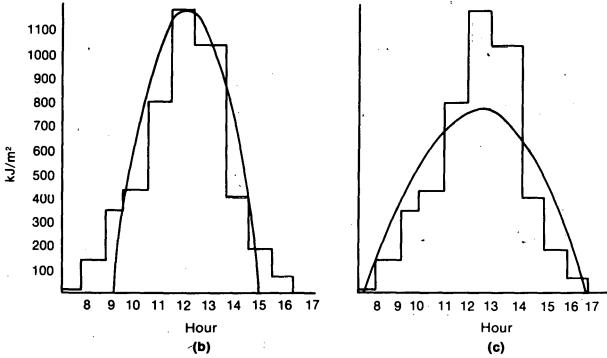
At first glance, approximation of daily radiation by a sine function appears accurate on clear days but may not adequately model the intermittent radiation pattern of cloudy days. Figure 2-1 indicates how the radiation models compare with weather data. The figures at the right in Figure 2-1 give the hour-by-hour insolation for four January days in Boulder, Colo. In the "b" and "c" figures at the left, hourly insolation is rearranged out of the proper time sequence, with the hour of maximum insolation presented at noontime and hours of successively smaller insolation plotted as progressively further from noon. Superimposed on the modified hourly insolation pattern are the calculated sinusoidal radiation functions. A comparison of Figure 2-la with Figures 2-l b and c shows how irregular radiation patterns may in truth be modeled accurately by a sinusoidal function.



The "a" figures (top) give hourly insolation data for each of four January days in Boulder, Colo. (from Duffie and Beckman, 1974). The "b" and "c" figures (bottom) give the hourly insolation pattern for the same four days rearranged with maximum hourly insolation at the center and minimum insolation at the edges. Superimposed on the insolation pattern are the functions for insolation generated by the QMAX daily model (Figure b) and by the day-length model (Figure c)

Figure 2-1. Daily Solar Radiation Patterns





QTOT = 4488 QMAX = 1185 kJ/m²

II Partly Sunny Day

Figure 2-1. Daily Solar Radiation Patterns (cont.)

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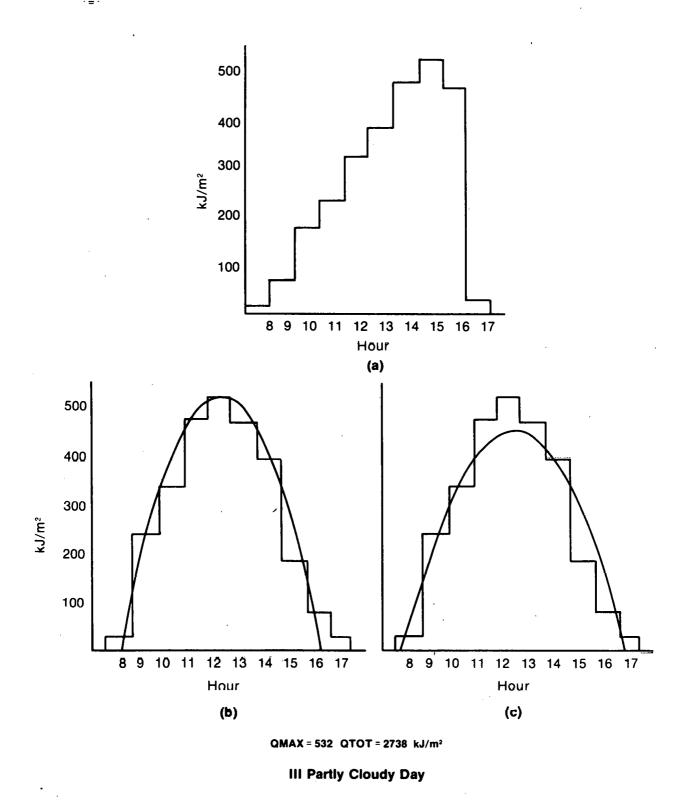


Figure 2-1. Daily Solar Radiation Patterns (cont.)



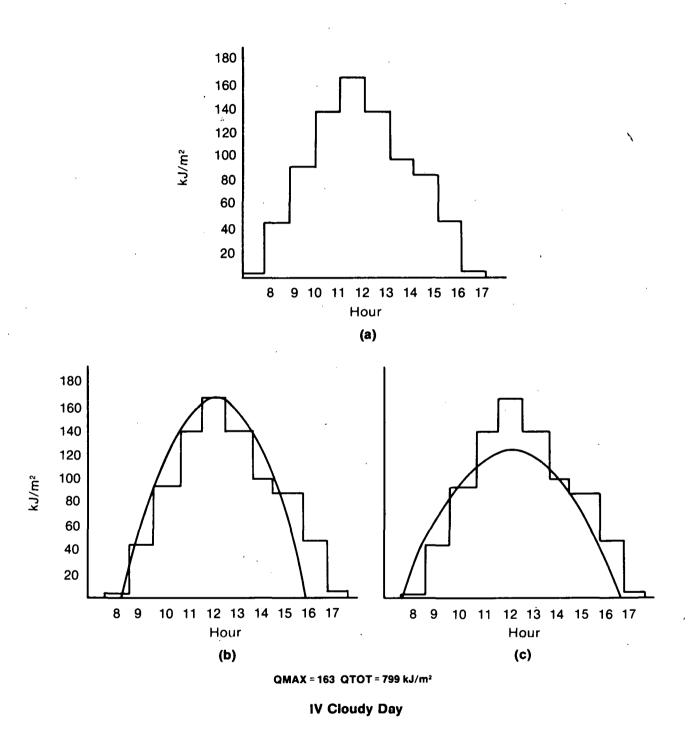


Figure 2-1. Daily Solar Radiation Patterns (concl.)



Figure 2-1 also provides a contrast between the two sinusoidal models—one based on day length and one based on maximum insolation. The day—length model is the most commonly used, and its usefulness in passive solar modeling has been documented (Barley 1979). However, the day—length model fails to accurately reflect maximum radiation intensity, particularly on partly sunny days. The maximum insolation is important in determining the collector turn—on time when collector losses are large. However, the maximum insolation model requires a new piece of daily radiation data, QMAX, which is not often compiled.

2.1 SIMULATIONS WITH THE RADIATION MODEL

The usefulness of the radiation models depends on their accuracy in modeling flat-plate collector performance.

The solar collector equation is (Duffie and Beckman 1974):

$$Q_{COL}(t) = F_r(\alpha \tau)[Q(t) - H_c], \qquad (2-5)$$

where $Q_{COL}(t)$ = instantaneous solar collection,

F_r = the collector heat exchange factor,

 $(\alpha\tau)$ = the transmission-absorption product,

Q(t) = the instantaneous insolation, and

H_c = the critical radiation level, determined from collector operating temperature, ambient temperature, and collector heat loss factor.

Total solar radiation is the integral of $Q_{COL}(t)$ over all time for which Q(t) exceeds H_c . Since $F_r(\alpha \tau)$ is constant, the collected energy is determined by the integral

$$Q_{u} = \int [Q(\tau) - H_{c}]d\tau \qquad (2-6)$$

where the integral is taken over all time for which solar collection occurs. This integral will be referred to as the utilizable insolation (Ω_u). Solar utilization (Φ) is defined as

$$\Phi = \frac{Q_u}{Q_t} \tag{2-7}$$

where Q_t is total insolation for the given time period. If solar utilization is known, the total solar heat (Q_c) collected for the given period of time may be calculated easily as:



$$Q_{c} = F_{r}(\alpha \tau) \Phi A_{c} Q_{t} \quad \text{or} \quad Q_{c} = F_{r}(\alpha \tau) A_{c} Q_{u} \qquad (2-8)$$

where Ac is the collector area.

Daily solar collector performance may be calculated from the hourly data by finding the hourly utilizable insolation:

$$Q_{u} = \begin{cases} Q_{h} - H_{c} & \text{if } Q_{h} - H_{c} > 0 \\ 0 & \text{if } Q_{h} - H_{c} \le 0 \end{cases}$$
 (2-9)

where Q_h is hourly insolation. Daily utilization may be found by summing the hourly utilizable insolation and dividing it by the total daily insolation (OTOT).

With the daily radiation model, daily utilizable insolation ($\mathbf{Q}_{\mathbf{u}}$) is found from the integral:

$$Q_{u} = \int_{t_{a}}^{t_{b}} (Q_{k} \cos \omega t - H_{c}) dt \qquad (2-10)$$

with the turn-on and turn-off times set to assure that insolation is greater than $\rm H_{c}$, for the period of collector operation. Turn-on and turn-off times were set according to the critical time, $\rm t_{x}$, at which radiation in the model equals $\rm H_{c}$. This time is given by:

$$t_{x} = \frac{1}{\omega} \arccos (H_{c}/Q_{k}) \qquad (2-11)$$

where t = 0 at solar noon.

The calculation based on hourly data introduces uncertainty over the turn-on and turn-off times. Consequently, daily model calculations for purposes of comparison with hourly calculations are performed with the turn-on and turn-off times being one-half hour smaller than the critical time.

The collector equation becomes:

$$Q_u = 2 \int_0^{t_x} (QMAX \cos wt - H_c) dt$$
 (2-12)



If H_c is assumed to be constant, then

$$Q_{11} = QTOT \sin[\omega(t_x - 1/2)] - 2(t_x - 1/2)H_{C}$$
 (2-13)

Utilization is found by dividing the result by QTOT.

Alternatively, the daily radiation model may be used to generate values for hourly insolation. Hourly insolation is found by integration to be:

$$Q_{h} = QTOT \sin(\omega t_{h}) - \sin[\omega(t_{h} - 1)] \qquad (2-14)$$

where t_h is the hour, t_h at noon being set to zero.* Utilization then may be calculated from hourly insolation in the manner described above. This method yields the same utilization values as those found by daily integration.

2.2 VALIDATION

Accuracy of the daily radiation models is assessed by comparing utilizations calculated with the daily model to utilization calculated from Typical Meteorological Year weather data. Independent comparisons were made each day of the year in 10 cities for seven different values of the critical level $\mathrm{H_{C}}$. The seven values of the critical level were set independently for each day as

$$H_{C} = QMAX(n/8) \tag{2-15}$$

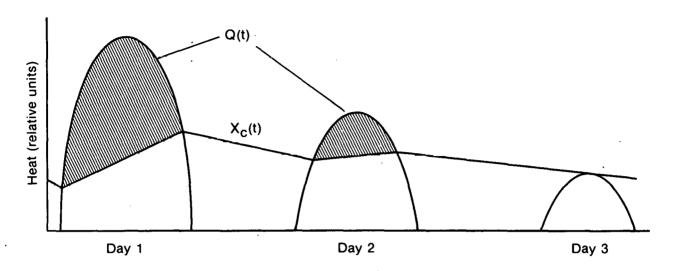
where QMAX is the daily maximum insolation and n is an integer varying from 1 to 7. The critical levels are treated as constants for each day. Thus, for each day considered, seven utilization values are obtained for the seven values of the critical level.

Figure 2-2 illustrates how the seven critical levels selected for each day typify all modes of flat-plate collector operation. As shown in Figure 2-2(a), the collector utilization varies from day to day; sunny days typically have high utilization and cloudy days have low or zero utilization. Utilization also is affected by the type of collector; evacuated tube collectors have high utilization values even on cloudy days. Consequently, it is important for the daily radiation models to be proven accurate at both high and low utilization levels. Figure 2-2(b) illustrates the selection of seven values of the critical level to be used in the comparison between the daily models and hourly data. As the figure shows, the different critical levels assure that high and low utilization levels are compared for each day.

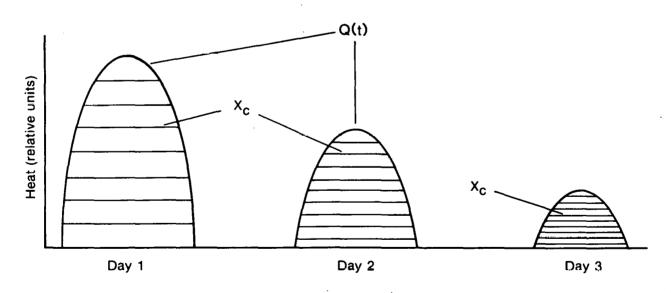
Results of the comparisons are tabulated in the following manner. For each critical level, the daily utilizations are averaged over all days having a given percentage of possible sunshine. Model accuracy is determined by how the average utilization values, obtained by using the daily model, compare to the values calculated from hourly data. The root mean square (rms) deviation

^{*}An adjustment to this formula must be made at hours near sunrise or sunset to avoid negative values of $sin(\omega t_h)$.





(a) Typical collector operation over a hypothetical three day period. The cross-hatched area gives the utilizable insolation ($Q_{\rm u}$) defined by equation 2-4.



(b) Seven values of the critical level $\rm X_{\rm C}$ for the three days above to be used in testing model accuracy. (See equation 2-7)

Figure 2-2. Illustration of Critical Levels and Solar Utilization



between the model utilization values and the hourly data values also is calculated. In addition to the tabulation by daily percentage of possible sunshine, the yearly average utilization and standard deviation are calculated, weighted by the daily insolation levels. The yearly average is weighted to assure that the error on days of high insolation counts more than the error on days of low insolation.

When tabulated by percentage of possible sunshine, results were found to be nearly identical for the 10 cities* and uniform throughout the year. Results for Madison, Wis. are presented in Appendix A. The QMAX model results, shown in Table 1 of Appendix A, show the model to be very accurate for sunny and partly sunny days. On cloudy or partly cloudy days, the QMAX model overestimates solar collection by 20% or more. Because cloudy days account for a relatively small percentage of yearly insolation, the cloudy day errors have a small impact on simulated annual performance. The weighted annual average utilization figures show, at most, a 6% overestimate of utilization, and often less. The standard deviation, typically 0.05 out of a utilization value of about 0.40, may be significant.

The results of the day-length model, presented in Table 2 of Appendix A, show a different pattern. The day-length model is very accurate for low values of the critical level $\rm H_{\rm C}$, and increasingly inaccurate for higher values of $\rm H_{\rm C}$. This model is also more accurate for sunny days than for cloudy ones, but the weighted yearly average utilizations are low by 15-25%. Yearly standard deviation ranges up to 0.08.

The results of Table 2 in Appendix A may be explained by considering the nature of the utilization function. When the critical level is low, the collector is in operation for nearly all the day, and modeling the proper day length is more important than daily maximum insolation when determining collector output. Thus, at low critical levels, the day-length model is more accurate than the QMAX model. At higher critical levels, the midday insolation pattern, near the time of maximum insolation, determines collector output. Consequently, the day-length model, which does not accurately model maximum insolation, becomes increasingly inaccurate.

^{*}Albuquerque, N. Mex.; Bismarck, N. Dak.; Boston, Mass.; Caribou, Maine; Dodge City, Kans.; Great Falls, Mont.; Madison, Wis.; Medford, Oreg.; Phoenix, Ariz.; and Santa Maria, Calif.



SECTION 3.0

MODIFIED DAILY RADIATION MODELS

In this section, three modifications of the sinusoidal daily radiation models are presented. The modifications have two goals: generate a more accurate model, and eliminate the dependence on hard-to-obtain maximum insolation data.

The possibility of obtaining a more accurate model is indicated by the nature of the error between the daily model and hourly data. Both the utilization values and the model errors are remarkably consistent for the 10 cities when tabulated by daily percentage of possible sunshine.

3.1 A COMBINED MODEL BASED ON BOTH QMAX AND DAY LENGTH

Results presented in Section 2.0 indicate that the QMAX model yields high utilization values, while the day-length model yields low values. The cause of these errors is the inaccurate estimation of day length in the QMAX model and inaccurate estimation of maximum insolation in the day-length model. By changing the parameters Q_k and ω in equation 2-1, it is possible to generate a sinusoidal function with values for maximum insolation and for day length that are midway between the values of the two previous models.

The combined model is of the same form as the two previous models, with the same basic equation:

$$Q(t) = Q_k \cos(\omega \tau) . \qquad (2-1)$$

In Section 2.0, the two models used the following values of the parameter $Q_{\bf k}$ (from equations 2-2, 2-3, and 2-4):

$$Q_k = \frac{1}{2} \pi QTOT/t_D$$
 (day-length model) (3-1)

$$Q_k = QMAX$$
 . (QMAX model)

In the combined model, the parameter $\boldsymbol{\textbf{Q}}_k$ is a linear combination of these two values:

$$Q_k = 0.6 \text{ QMAX} + 0.4 \left(\frac{1}{2} \pi \text{ QTOT/t}_D\right)$$
 (combined model) (3-2)

The frequency ω is set, as above, to ensure that the daily total insolation matches the actual daily total (QTOT):

$$\omega = 2 Q_k/QTOT . (3-3)$$

Results of the combined model, presented in Table 3 of Appendix A, indicate that it is more accurate than both the day-length and the QMAX model. Average



utilizations differ from the hourly data values by at most 0.02, and the annual rms deviations are less than 0.04. Also, the average utilization shows no tendency to be too high or too low.

3.2 A MODIFIED MODEL BASED ON MAXIMUM INSOLATION

A highly accurate daily model can be generated by regarding insolation as the sum of a constant term and a sinusoidal term. The constant term, reflecting perhaps the diffuse component of radiation, is set at 10% of the daily extraterrestrial radiation or one-half the daily total radiation, whichever is larger. The sinusoidal term is set to reflect maximum insolation. The resulting equations are:

$$Q(t) = Q_{con} + Q_{k} \cos \omega t$$

$$Q_{con} = \min \left\{ \begin{array}{l} 0.1 & (Q_{x}/t_{D}) \\ 0.5 & (QTOT/t_{D}) \end{array} \right.$$

$$Q_{k} = QMAX - Q_{con}$$

$$\omega = 2 Q_{k}/(QTOT - Q_{con}t_{D})$$
(3-4)

where t_D is day length and Q_x is extraterrestrial radiation. Extraterrestrial radiation may be found monthly from the average daily radiation and the ratio of average daily radiation to extraterrestrial radiation (K_T), both commonly available data (Jordan and Liu 1977). Figure 3-1 shows how this representation (referred to below as the modified QMAX model) compares with hourly weather data for the four days presented in Figure 2-1.

The integrated equation for utilization with this model, equivalent to equation 2-13, is

$$Q_u = (QTOT - Q_{con}t_D) \sin \omega(t_x - \frac{1}{2}) + 2(t_x - \frac{1}{2})(Q_{con} - H_c)$$
 (3-5)

Results of the modified QMAX model, presented in Table 4 of Appendix A, are accurate for all but the cloudiest days. The annual average utilizations are all very close to the values calculated from hourly data, within 0.01, and the largest rms deviation is 0.036. These results also were duplicated for the other cities used in this study. While further refinements could improve these results, this model demonstrates that a high degree of accuracy is possible when using a daily radiation algorithm. The combined model presented in the previous section may be more useful because it achieves a comparable level of accuracy while being simpler.

3.3 A MODIFIED MODEL BASED ON DAY LENGTH

While daily total radiation data are frequently tabulated, daily maximum insolation data are harder to find. Consequently, a modified daily radiation model, not dependent on maximum insolation, will be examined.

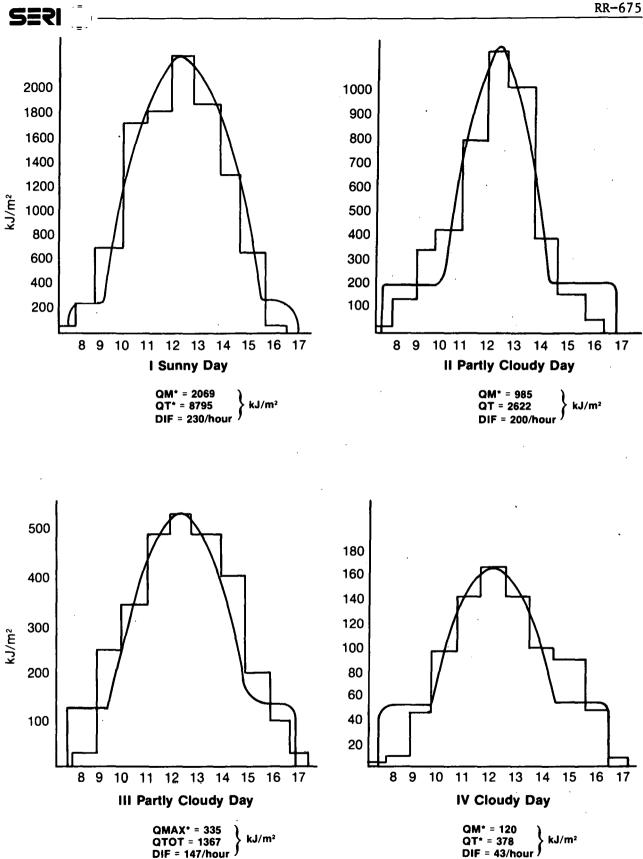


Figure 3-1. Daily Solar Radiation Patterns, From Modified Model

Daily insolation pattern calculated by the second daily model for four days. The superimposed hourly pattern is from the "b" graphs in Figure 2-1.



As already noted, the day-length model is inaccurate because it generally underestimates maximum insolation. The discrepancy between the parameter Q_k calculated by equations 2-2 and 2-3 and the actual maximum insolation (QMAX) indicates a strong correlation to cloud cover. On cloudy days in Madison, Wis., this discrepancy averages 30%, while on sunny days the discrepancy is only 3%. The discrepancy also shows a consistently increasing trend as daily percentage of possible sunshine decreases. Insolation for Albuquerque, N. Mex., shows a similar pattern but the cloudy day discrepancy is only 21%.

The modified day-length model presented here begins with the same form:

$$Q(t) = Q_k \cos \omega t . \qquad (2-1)$$

The parameter $Q_{\mathbf{k}}$ is calculated based on day length and then increased by a factor which is a function of percentage of possible sunshine. The equations become:

$$Q_k = I_c(\frac{1}{2} QTOT/t_D)$$

$$I_c = 1 + 0.25(1 - QTOT/Q_V)$$
(3-6)

where $Q_{\mathbf{x}}$ is the daily extraterrestrial radiation. The fraction QTOT/ $Q_{\mathbf{x}}$ is the daily percentage of possible sunshine, varying from 0 to 1. As before, the parameter ω is calculated to make total radiation equal to the actual total:

$$\omega = 2Q_k/QTOT . (3-7)$$

Results from this model are presented in Table 5 of Appendix A. The annual average utilizations are all accurate to within 2%. However, the breakdown of the data by percentage of possible sunshine shows significant errors, most notable for 30-40% days. The annual rms deviations reach a maximum of 0.063. These results suggest that this model could be useful. A more thorough analysis to find the best values for the factor I_c should improve accuracy.



SECTION 4.0

RESULTS OF DAILY SIMULATIONS

The most direct way of estimating model accuracy is to simulate a known system and compare results. In this section, daily simulation results will be presented for three types of systems that have been the subject of more detailed study. The three comparisons that will be made are (1) a simulated active solar heating system with daily storage, to be compared with f-chart, (2) annual storage solar heating system compared with hourly simulations with the SOLANSIM computer code, and (3) a "two-tank" solar heating system with both a daily and a seasonal storage tank, compared to the original designs of Cha, Conner, and Mueller (1979).

Simulation of an active solar heating system with daily storage in Madison, Wis., was performed using hourly steps with hourly insolation data generated by the daily radiation models. Then, the same simulation was performed using hourly Typical Meteorological Year weather data. Figure 4-1 shows how the simulation with each of the daily radiation models compares to simulation with hourly weather data, for flat-plate collectors.

The QMAX model and the combined model simulations are the most accurate, with results consistently within 1.5% of the hourly data results. These models performed as well or better in simulations with evacuated tube collectors and in different locations. The day-length model is inaccurate, consistently underestimating system performance by 5%. The modified day length model, while not as accurate as the models based on QMAX, is still of sufficient accuracy to be useful. It consistently overestimates system performance, but only by 2-3%.

Simulations also were performed in Madison for an evacuated tube collector, and in Albuquerque, N. Mex., for both flat-plate and evacuated tube collectors. In each of these cases, performance of the day-length model improved significantly, underestimating performance by only 2%. The improved performance indicates that the day-length model may be useful in sunny locations or in systems with high utilization factors.

Figure 4-1 also shows the results of a simulation that used daily, rather than hourly, steps with the QMAX model. This simulation is accurate for systems supplying a large fraction of solar heat, but it decreases in accuracy for smaller systems. The inaccuracy introduced by the use of daily steps is, at most, 5% for flat-plate collector systems. For evacuated tube collector systems, the daily step model was accurate to within 1%.

A comparison is made in Figure 4-2 between the hourly simulation using hourly weather data and results from f-chart. This comparison shows significant discrepancies between the simulation and f-chart, occasionally as high as 5%. The discrepancies indicate that differing assumptions about system performance have a greater impact on results than inaccuracies in the daily radiation algorithm.

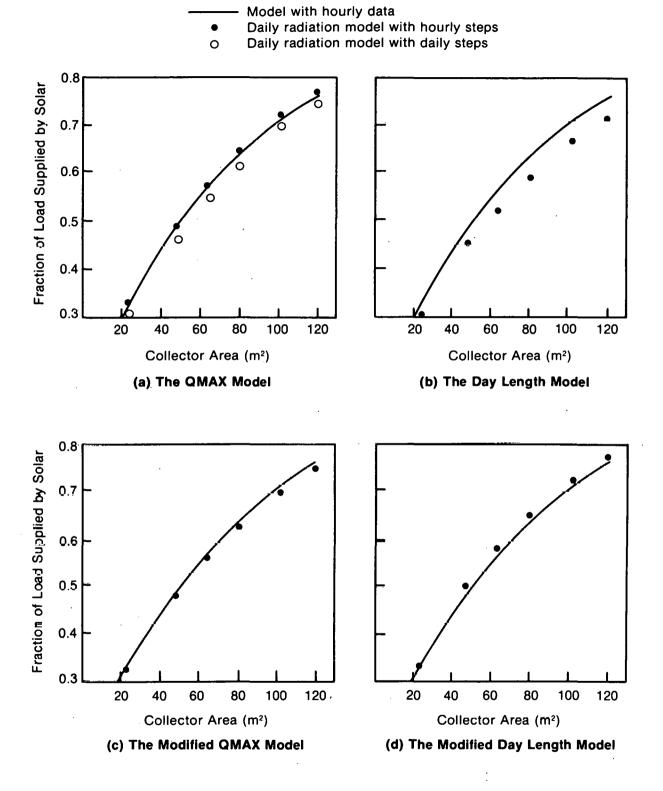


Figure 4-1. Results of Solar Heating System Simulations

Comparison of simulations using daily radiation models (discrete points) simulations using hourly weather data (solid lines), Flat-plate collector system, Madison, Wisconsin



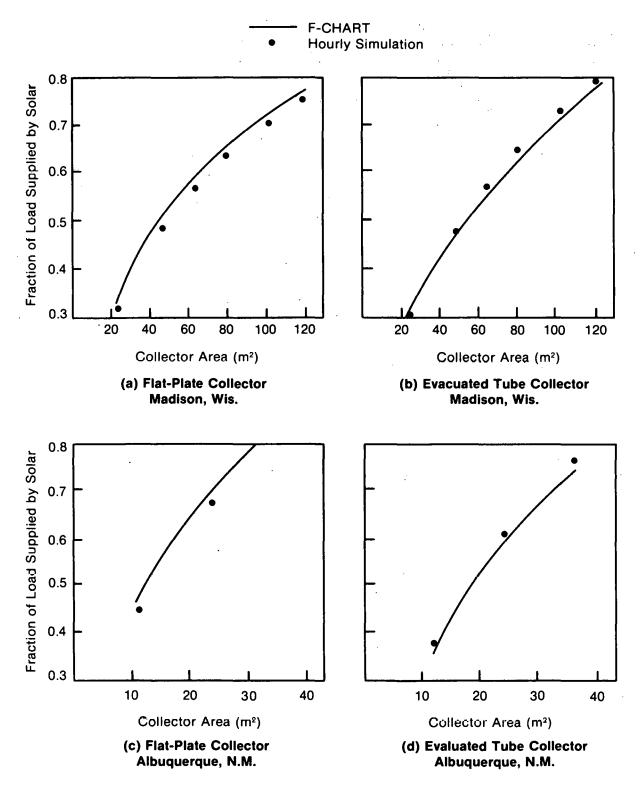


Figure 4-2. Comparison of Simulation Results from Figure 4-1 with F-CHART



Simulations of annual storage systems were performed with the daily radiation models, using daily steps, and compared to a detailed study of annual storage systems based on the SOLANSIM computer code (Baylin et al. 1980). In the study with SOLANSIM, the yearly swing in storage temperature is calculated, assuming that the system provides 100% of the space heating load so long as the storage temperature remains above 33°C. The key parameter in the comparison is, therefore, the end-of-year storage temperature. Results of the comparison, performed for all 10 cities, are as follows.

- The QMAX model yields the most accurate results. For flat-plate collectors, the calculated end-of-year storage temperatures are consistently within 1°C of the SOLANSIM results. For evacuated tube collectors, the calculated temperatures are consistently higher than the SOLANSIM results, but the discrepancy is always less than 2°C.
- The day-length model yields consistently low results for flat-plate collectors. The discrepancy between the calculated end of year temperature and the SOLANSIM results is approximately 4°C, which in these systems is equivalent to 5% of the annual heat load. In contrast with the results of the f-chart comparison, this error persisted in sunny locations such as Albuquerque, N. Mex. For evacuated tube collectors, the day-length model again underestimated performance, but this time results were within 1.5°C of the SOLANSIM results. For evacuated tube collectors, this model is of sufficient accuracy to be used.
- According to the analysis presented in Sections 2.0 and 3.0, the combined model presented in Section 3.1 should be the most accurate daily radiation model. In the comparison with SOLANSIM, the combined model yields very accurate results for evacuated tube collectors, with calculated storage temperatures consistently within 1°C of the SOLANSIM results. For flat-plate collectors, the combined model underestimates system performance with end-of-year temperatures 2°C too low.
- The modified day-length model presented in Section 3.3 consistently yields final temperatures about 2°C above the SOLANSIM results for both flat-plate collectors and evacuated tube collectors.

Lastly, the QMAX model was used to simulate the performance of the "two-tank" system designed by Cha, Conner, and Mueller (1979). In this system, a solar collector operated with two storage tanks, one sized for storage on a daily basis and the other an annual storage tank. The collector operates to charge whichever tank is at the lower temperature, thus assuring the most efficient operation. Heat for the building load is drawn preferentially from the daily storage tank. The advantage of the two-tank system over single-tank annual storage lies in the efficient collection of low temperature solar heat during the early winter, when the fully charged annual storage tank is too hot to permit efficient collection.

A simulation for the two-tank system was constructed by using daily simulation intervals and the QMAX daily model. Figure 4-3 compares the simulation results with the designs of Cha, Conner, and Mueller (1979). The QMAX model results in virtually identical designs.



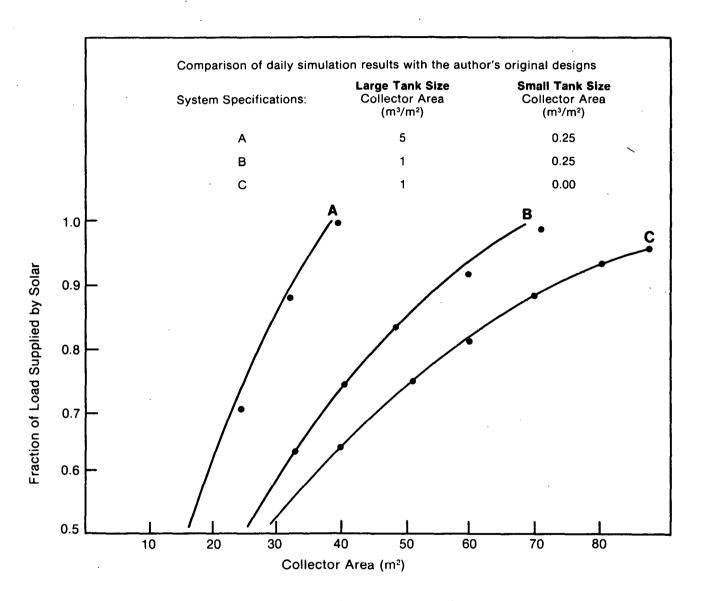


Figure 4-3. Design for Two-Tank System





SECTION 5.0

CONCLUSION

The results of this study show that daily radiation algorithms are accurate for use in solar system design, with errors limited to 2%. By contrast, differing assumptions about system performance can cause design errors of greater significance.

The accuracy of the daily radiation models is particularly impressive when the inaccuracies of existing radiation data, or the inherent variability of weather, are taken into account. The discrepancy between anisotropic (Hay 1979) and isotropic (Klein 1978) algorithms for calculating radiation on tilted surfaces, alone, amounts to 10%.

The following are specific conclusions and recommendations of this study.

- The QMAX sinusoidal function yields the most accurate results of the daily radiation models presented here.
- The day-length model is the most commonly used daily radiation algorithm. Although it yields accurate results for evacuated tube collectors, the model consistently results in design errors of 5% for flat-plate collectors. All of the modified daily models presented here are more accurate.
- Use of daily maximum insolation data permits significantly greater accuracy in a daily radiation model. Consequently, more of an effort should be made to collect and tabulate such data.
- If maximum daily insolation data are unavailable, the modified daylength model is of sufficient accuracy to be useful to designers. Also, it is likely that this model's accuracy could be improved by further study.
- Use of daily radiation algorithms for solar heating design could be particularly useful to designers with access to minicomputers. To facilitate this use, more of an effort should be made to tabulate insolation and temperature data on a daily basis rather than on an hourly basis. Formulas for generating the total and maximum daily insolation on a tilted surface directly from horizontal data also need to be developed.





SECTION 6.0

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Appendix A

COLLECTOR UTILIZATION FOR VARYING H_{C} LEVELS, TYPICAL METEOROLOGICAL YEAR, MADISON, WIS.

Five Tables



Table A-1. COLLECTOR UTILIZATION FOR VARYING H LEVELS TYPICAL METEOROLOGICAL YEAR, MADISON, WIS. THE $\underline{\text{QMAX}}$ MODEL

			Utili:	zations				
		H _C =0.125*QM	0.125*QM	0.2	5*QM	0.375*QM		
PPS	3	ND	H.	D .	H	D	H	D
0.0-	.1	35	.7527	.7856	.5526	.6138	.3916	.4585
.1-	.2	36	.7200	.7841	.5112	.6124	.3475	.4572
.2-	.3	28	.7437	.7896	.5392	.6176	.3785	.4622
.3-	.4	38	.7321	.7871	.5321	.6152	.3767	.4598
.4-	.5	34	.7553	.7932	.5646	.6211	.4050	.4654
.5-	.6	53	.7781	.7967	.5978	.6244	.4402	.4685
.6-	•7	73	.7878	.8004	.6123	.6279	.4575	.4719
.7-	.8	47	.7998	.7998	.6296	.6274	.4767	.4714
.8-	.9	19	.8133	.8005	.6399	.6281	.4875	.4720
.9-	1.0	2	.8314	.8033	.6698	.6308	.5171	.4746
ANNUA	L*	365	.7798	.7977	.5989	.6254	.4429	.4695

•	Utiliz	ations						
	Hc0.5#QM		0.625*QM		0.75*QH		0.875*QM	
PPS	H	D	Н.	D	H	D	H	D
0.01	.2634	.3207	.1615	.2017	.0869	.1036	.0343	.0311
.12	.2264	.3195	.1410	.2006	.0799	.1028	.0324	.0306
.23	.2503	.3241	.1520	.2046	.0820	.1060	.0329	.0328
.34	.2560	.3219	.1614	.2027	.0882	.1045	.0338	.0317
.4~ .5	.2777	.3270	.1720	.2071	.0914	.1081	.0345	.0341
.56	.3046	.3299	.1932	. 2097	.1037	.1101	.0380	.0355
.67	.3239	.3330	.2078	.2124	.1109	-1124	.0390	.0370
.78	.3410	.3325	.2205	.2120	.1213	.1120	.0441	.0367
.89	.3453	.3331	.2266	.2125	.1207	.1124	.0450	.0370
.9-1.0	.3673	.3354	.2460	.2146	.1359	.1142	.0536	.0382
ANNUAL*	.3097	.3307	.1976	.2104	.1063	.1108	.0389	.0359

PPS H _C =	.125	.250	.375	.500	.625	.750	.875	QM*
0.01	.0477	.0834	.0894	.0771	.0585	.0327	.0123	
.12	.0802	.1194	.1286	.1089	.0715	.0337	.0152	
.23	.0579	.0944	.1039	.0915	.0662	.0365	.0127	
.34	.0625	.0943	.0975	.0804	.0563	.0307	.0122	
.45	.0461	.0723	.0795	.0688	.0540	.0324	.0120	
.56	.0281	.0416	.0481	.0498	.0413	.0283	.0218	
.67	.0175	.0247	.0274	.0262	•ÓŽŽŽ	.0184	.0088	
.78	.0140	.0184	.0214	.0233	.0217	.0173	.0099	
.89	.0139	.0165	.0199	.0175	.0175	.0125	.0091	
.9-1.0	.0283	.0416	.0462	.0396	.0389	.0273	.0175	
ANNUAL#	.0337	.0509	.0555	.0497	.0382	.0239	.0105	

PPS = Daily percent of possible sunshine

ANNUAL* = Yearly average utilization and RMS deviation weighted by daily total insolation.

ND = Number of days with given PPS

 $[\]rm H_{\rm C}$ = Critical radiation level set each day as a fixed percentage of QM, the daily maximum insolation

H = Hourly calculation

D = Daily radiation model



Table A-2. COLLECTOR UTILIZATION FOR VARYING H_C LEVELS TYPICAL METEOROLOGICAL YEAR, MADISON, WIS. DAY LENGTH MODEL

			Utili:	zations				
			H _C =	.0.125*QM	0.2	:5*QM	0.375*QM	
PPS	3	ND	Н	D	н	Ď	H	D
0.0-	.1	35	.7527	.7344	.5526	.5136	.3916	.3265
.1-	.2	36	.7200	.7078	.5112	.4682	.3475	.2763
.2-	.3	28	.7437	.7346	.5392	.5122	.3785	.3247
.3-	.4	38	.7321	.7146	.5321	4773	.3767	.2805
.4-	.5	34	.7553	.7472	.5646	.5328	.4050	.3480
.5-	.6	53	.7781	.7669	.5978	.5672	.4402	.3915
.6-	.7	73	.7878	.7865	.6123	.6014	.4575	.4360
.7-	.8	47	.7998	.7925	.6296	.6134	.4767	.4523
.8-	.9	19	.8133	.7994	.6399	.6261	.4875	.4694
.9-	1.0	2	.8314	.8319	.6698	.6878	.5171	.5530
ANNUA	L*	365	.7798	.7737	.5989	.5795	.4429	.4088

		Üt	ilizatio	ns	•			
	H _C =	0.5*QM	0.62	.5*QM	0.7	5*QM 0.	875*QM	
PPS	н С	D	. н	D	н.	D	н	D
0.01	.2634	.1793	.1615	.0813	.0869	.0285	.0343	.0054
.12	.2264	.1347	.1410	.0522	.0799	.0179	.0324	.0053
.23	.2503	.1796	.1520	.0822	.0820	.0326	.0329	.0104
.34	.2560	.1333	.1614	.0491	.0882	.0156	.0338	.0055
.45	.2777	.1960	.1720	.0859	.0914	.0270	.0345	.0066
.56	.3046	.2418	.1932	.1223	.1037	.0411	.0380	.0061
.67	.3239	.2916	.2078	.1703	.1109	.0768	.0390	.0190
.78	.3410	.3102	. 2205	.1886	.1213	.0906	.0441	.0234
.89	.3453	.3301	.2266	.2095	.1207	.1099	.0450	.0360
.9-1.0	.3673	.4304	. 2460	.3197	.1359	.2217	.0536	.1377
ANNUAL*	.3097	.2637	.1976	.1484	.1063	.0660	.0389	.0177
RMS Devia	ıtion							
PPS H _C =	.125	. 250	.375	•500	.625	.750	.875	QM*
0.01	.0288	.0562	.0908	.1332	.1023	.0688	.0312	
.12	.0351	.0846	.1128	.1249	.1106	.0748	.0339	
.23	.0282	.0622	.0984	.1089	.0932	.0636	.0304	
.34	.0320	.0787	.1270	.1495	.1296	.0844	.0376	
.45	.0265	.0610	.0928	.1182	.1141	.0799	.0363	
.56	.0267	.0529	.0757	.0919	.0954	.0767	.0370	
.67	.0179	.0330	.0489	.0607	.0642	.0531	.0271	
	4.76		0000			0101		

PPS = Daily percent of possible sunshine

.0290

.0196

.0191

.0439

.0393

.0272

.0385

.0659

.0454

.0270

.0650

.0796

.0460

.0274

.0767

.0774

.0426

.0249

.0910

.0595

.0266

.0194

.0922

.0311

.7- .8 .8- .9

.9-1.0

ANNUAL*

.0176

.0149

.0081

.0214

ND = Number of days with given PPS

 $^{{\}rm H_{C}}$ - Critical radiation level set each day as a fixed percentage of QM, the daily maximum insolation

H = Hourly calculation

D = Daily radiation model

ANNUAL* = Yearly average utilization and RMS deviation weighted by daily total insolation.



Table A-3. COLLECTOR UTILIZATION FOR VARYING H_C LEVELS TYPICAL METEOROLOGICAL YEAR, MADISON, WIS. COMBINED MODEL

			Utili	zations				
			H _C =0.125		0.2	5*QM	0.375*QM	
PPS		ИĎ	Я	D	Н	D	Н	D
0.0-	.1	35	.7527	.7719	.5526	.5842	.3916	.4171
.1	2	36	.7200	.7657	.5112	.5728	.3475	.4020
.2	3	28	.7437	.7751	.5392	.5870	.3785	.4196
.3	.4	38	.7321	.7681	.5321	•5755	.3767	.4048
.4	.5	34	.7553	.7793	. 5646	.5930	.4050	.4267
.5	6	53	.7781	.7868	.5978	.6048	.4402	.4415
.6	.7	73	.7878	.7956	.6123	.6185	.4575	.4590
.7	.8	47	.7998	.7971	.6296	.6222	.4767	.4642
.8	9	19	.8133	.8002	.6399	.6274	.4875	.4712
.9- 1.	.0	2	.8314	.8167	.6698	.6565	.5171	.5101
ANNUAL*	•	365	.7798	.7904	.5989	.6107	.4429	.4493

		ַ	tilizatio	ns				
		H _C =	0.5*QM0.62	.5*QM	0.7			
PPS	н	D	н	מ	H	D	н	D
0.01	.2634	.2720	.1615	.1511	.0869	.0593	.0343	.0098
.12	.2264	. 2549	.1410	.1343	.0799	.0467	.0324	.0064
.23	.2503	.2741	.1520	.1530	.0820	.0611	.0329	.0114
.34	.2560	.2575	.1614	.1363	.0882	.0469	.0338	.0059
.45	.2777	.2815	.1720	.1597	.0914	.0653	.0345	.0101
.56	.3046	.2981	.1932	.1762	.1037	.0792	.0380	.0151
.67	.3239	.3177	.2078	.1963	.1109	.0973	.0390	.0265
.78	.3410	.3240	.2205	.2029	.1213	.1035	.0441	.0303
.89	.3453	.3321	.2266	.2114	.1207	.1115	.0450	.0364
.9-1.0	.3673	.3780	.2460	.2609	.1359	.1603	.0536	.0785
ANNUAL*	.3097	.3077	.1976	.1857	.1063	.0884	.0389	.0228

RMS Devia	.125	. 250	.375	.500	.625	.750	.875	QM≖
0.01	.0346	.0531	.0500	.0422	.0449	.0449	.0286	
.12	.0621	.0797	.0773	.0599	.0488	.0509	.0319	
.23	.0421	.0609	.0620	.0501	.0376	.0400	.0264	
.34	.0428	.0548	.0511	.0441	.0499	.0542	.0328	
.45	.0326	.0482	.0520	.0498	.0490	.0463	.0307	
.56	.0219	.0316	.0389	.0452	.0460	.0421	.0284	
.67	.0143	.0196	.0247	.0286	.0307	.0280	.0182	
.78	.0144	.0202	.0255	.028/	.0280	.0251	.0170	
.89	.0138	.0164	.0210	.0187	.0184	.0146	.0112	
.9-1.0	.0149	.0136	.0073	.0116	•01.50	.0248	.0272	
ANNUAL*	.0252	.0344	.0370	.0359	.0351	.0333	.0224	

PPS = Daily percent of possible sunshine

ANNUAL* = Yearly average utilization and RMS deviation weighted by daily total insolation.

ND = Number of days with given PPS

 $[\]rm H_{\rm C}$ = Critical radiation level set each day as a fixed percentage of QM, the daily maximum insolation

H = Hourly calculation

D = Daily radiation model



Table A-4. COLLECTOR UTILIZATION FOR VARYING H_C LEVELS TYPICAL METEOROLOGICAL YEAR, MADISON, WIS. THE MODIFIED OMAX MODEL

		Utilizati	ons_					
		H _C =0.1	25*QM 0.2	5*QM	0.37	75*QM		
PPS	3	ND	H	D	H	D	H	D
0.0-	.1	35	.7527	.7321	.5526	.4820	.3916	.3436
.1-	.2	36	.7200	.6978	.5112	.4362	.3475	. 3099
.2-	.3	28	.7437	.7256	.5392	.5168	.3785	.3815
.3-	.4	38	.7321	.7038	.5321	.5369	.3767	.3994
.4-	.5	34	.7553	.7421	.5646	.5766	.4050	.4309
.5-	.6	53	.7781	.7660	.5978	.5993	.4402	.4490
.6-	.7	73	.7878	.7858	.6123	.6157	.4575	.4621
.7-	.8	47	.7998	.7913	.6296	.6200	. 47 67	.4653
.8-	.9	19	.8133	.7973	.6399	.6249	.4875	.4692
.9-	1.0	2	.8314	.8211	.6698	.6442	.5171	. 4843
ANNUA	L*	365	.7798	.7708	.5989	.5962	.4429	.4461

	Utiliz	ations						
	H _C =О.5*QM Н D		0.625*QM		0.75*QM		0.875*QM	
PPS	ъ.	D	Ħ	D	н	D	н	D
0.01	.2634	.2366	.1615	.1453	.0869	.0715	.0343	.0186
.12	.2264	.2109	.1410	.1280	.0799	.0614	.0324	.0146
.23	.2503	.2651	.1520	.1652	.0820	.0836	.0329	.0241
.34	.2560	.2779	.1614	.1734	.0882	.0878	.0338	.0253
.45	.2777	.3018	.1720	.1904	.0914	.0986	.0345	.0304
.56	.3046	.3155	.1932	. 2001	.1037	.1047	.0380	.0334
.67	.3239	.3256	.2078	.2074	.1109	.1095	.0390	.0359
.78	.3410	.3279	. 2205	.2088	.1213	.1102	.0441	.0360
.89	.3453	.3308	.2266	.2109	.1207	.1115	.0450	.0366
.9-1.0	.3673	.3421	.2460	.2187	.1359	.1163	.0536	.0390
ANNUAL*	.3097	.3135	.1976	.1989	.1063	.1042	.0389	.0334

	viation bet -= .125	ween hour	ly calcul	ation and .500	daily ra	diation .750	model .875	QM*
0.0-	.0323	.0836	.0626	.0502	•0447	.0340	.0216	
.12	•	-0983	40723	.0589	-0473	.0376	.0262	
2-		.0465	.0496	.0500	.0402	.0294	.0173	
.34		.0317	.0482	.0477	.0392	.0265	.0159	
.4	.0294	.0405	.0538	.0524	.0449	.0295	.0134	
.56	.0255	.0311	.0389	.0438	.0387	.0279	.0137	
.6	0147	.0185	.0231	.0243	.0224	.0184	.0090	
.78	.0170	.0207	.0238	.0253	.0230	.0183	.0105	
.89	.0167	.0184	.0220	.0189	.0186	.0131	.0094	
.9-1.0	.0114	.0268	.0353	.0322	.0342	.0248	.0166	
ANNIJAL.	.0235	.0313	,0355	.0357	.0309	.0222	.0119	

PPS - Daily percent of possible sunshine

ANNUAL* = Yearly average utilization and RMS deviation weighted by daily total insolution.

ND = Number of days with given PPS

 $^{{\}rm H}_{\rm C}$ = Critical radiation level set each day as a fixed percentage of QM, the daily maximum insolation

H - Hourly calculation

D = Daily radiation model



Table A-5. COLLECTOR UTILIZATION FOR VARYING H_C LEVELS TYPICAL METEOROLOGICAL YEAR, MADISON, WIS. MODIFIED DAY LENGTH MODEL

			Utili:	ations				
			H_=	0.125*QM	0.2	5*QM	0.3	75*QM
PPS.		ND	H	D	H	D	H	D
0.0-	.1	35	.7527	.7732	.5526	.5873	.3916	.4228
.1	. 2	36	.7200	.7490	.5112	.5424	.3475	.3662
	.3	28	.7437	.7684	.5392	.5746	.3785	.4049
.3	.4	38	.7321	.7474	.5321	.5365	.3767	.3549
.4	.5	34	.7553	.7724	.5646	.5800	.4050	.4100
	6	53	.7781	.7856	.5978	.6025	.4402	.4388
.6	.7	73	.7878	.8006	.6123	.6282	.4575	.4725
.7-	8 .	47	.7998	.8026	.6296	.6330	.4767	.4792
.8-	9	19	.8133	.8054	.6399	.6377	.4875	.4854
.9- 1.	.0	2	.8314	.8336	.6698	.6903	.5171	1.5577
ANNUAL*	k .	365	.7798	.7911 [.]	.5989	.6123	.4429	.4522

		U	tilipatio	no				
		H _C =O.5*QM			0.625*QM		0.75*QM	0.875*QM
PPS	н	ď.	Н.	D	H	D	н	D
0.01	.2634	.2818	.1615	.1688	.0869	.0889	.0343	.0397
.12	.2264	.2548	.1410	.1181	.0799	.0535	.0324	.0223
.23	.2503	.2620	.1520	.1524	.0820	.0766	.0329	.0354
.34	.2560	.2062	.1614	.0997	.0882	.0401	.0338	.0151
.45	2777	.2641	.1720	.1458	.0914	.0646	.0345	.0222
.56	.3046	.2957	.1932	.1754	.1037	.0827	.0380	.0240
.67	.3239	.3341	.2078	.2147	.1109	.1170	.0390	.0459
.78	.3410	.3419	.2205	.2224	.1213	.1227	.0441	.0469
.89	.3453	.3491	.2266	.2299	.1207	.1297	.0450	.0520
.9-1.0	.3673	.4361	.2460	.3260	.1359	.2281	.0536	.1438
ANNUAL*	.3097	.3120	.1976	.1942	.1063	.1023	.0389	.0392

RMC Device	.125	.250	.375	.500	.625	.750	. 875	QM*
0.01	.0290	.0484	.0640	.0813	.0891	.0722	.0492	
.12	.0415	.0722	.0929	.0967	.0950	.0784	.0498	
.23	.0342	.0601	.0817	.0930	.0842	.0726	.0511	
.34	.0280	.0507	.0821	.1056	.1050	.0798	.0472	
.45	.0294	.0516	.0704	.0866	.0904	.0733	.0433	
.56	.0269	.0413	.0558	.0669	.0702	.0588	-0343	
.67	.0212	.0336	.0449	.0515	.0541	.0470	.0307	
.78	.0165	.0243	.0309	.0336	.0340	.0316	.0233	
.89	.0093	.0132	.0187	-0207	.0197	.0229	.0187	
.9-1.0	.0068	.0211	.0416	.0695	.0814	.0953	.0956	
ANNUAL*	.0235	.0387	.0522	.0612	.0625	.0530	.0351	

PPS = Daily percent of possible sunshine

ND = Number of days with given PPS

 $^{{\}rm H}_{\rm C}$ = Critical radiation level set each day as a fixed percentage of QM, the daily maximum insolation

H - Hourly calculation

D - Daily radiation model

ANNUAL* = Yearly average utilization and RMS deviation weighted by daily total insolation.

APPENDIX B

SOLAR HEATING DESIGN WITH THE DAILY ALGORITHMS

In this appendix, detailed simulation methods using the daily algorithms will be described. The daily radiation model is assumed to be of the standard sinusoidal form

$$Q(t) = Q_k \cos \omega t . \qquad (2-1)$$

The parameters Q_k and ω are set as described in the text. System simulation may be done in either daily or hourly intervals. For the given interval, the simulation consists of five steps.

- (1) Solar heat collection is calculated based on a collector algorithm.
- (2) Building heat and hot water load is either calculated or input as data.
- (3) Amount of solar heat supplied to the load is calculated using a storage-to-load heat exchanger effectiveness formula.
- (4) Storage losses are calculated based on storage temperature, ground temperature, and overall storage U-value.
- (5) End-of-period storage temperature is found by summing the heat flows to and from storage--collected solar heat, heat supplied to load, and storage losses--and dividing by the storage heat capacity.

Each of these steps will be described separately. A model based on hourly steps will be described initially because it is conceptually simpler than a model using daily steps.

B.1 COLLECTOR ALGORITHM USING HOURLY STEPS

From equation 2-5, the hourly solar heat collection may be found as follows:

$$Q_{col} = F_r(\alpha \tau) (Q_h - H_c)$$
 (B-1)

$$H_{c} = \frac{F_{r}U_{1}}{F_{r}(\alpha\tau)} \left(T_{o} - T_{a}\right) . \qquad (B-2)$$

In this equation, U_1 is the collector heat loss factor, in joules/hr·m²°C. The quantities $F_r(\alpha\tau)$ and F_rU_1 are typical collector performance parameters which must be input as data. The operating temperature T_0 is taken as equal to the storage temperature at the beginning of the period.

Lastly, T_a is the average daytime ambient temperature. If only a daily average ambient temperature is available, T_a may be set by adding 1.5°C to the daily average.



This leaves the hourly radiation $\mathbf{Q_h}$ to be calculated according to the daily radiation model. The simplest method is to select insolation from the midpoint of the interval as average hourly insolation. Thus:

$$Q_{h} = Q_{k} \cos \omega \left(t_{h} - \frac{1}{2}\right) \tag{B-3}$$

where t_h is the hour time at the end of the interval. This method results in a 2% overestimate of solar radiation compared to integration over the time interval. Integration would yield:

$$Q_{h} = \frac{Q_{k}}{\omega} \left(\sin \omega t_{b} - \sin \omega t_{a} \right)$$
 (B-4)

where t_a and t_b are the beginning and end of period times, respectively, in hourly units and with solar noon set at zero. This hourly formula must be modified when the collector turn-on time and turn-off time falls within the interval in question. The following correction is added:

if
$$t_a \stackrel{>}{=} t_x$$
, then t_a is set equal to t_x
if $t_b \stackrel{>}{=} t_x$, then t_b is set equal to t_x

where t_x is the turn-on time calculated from Equation 2-11.

B.2 BUILDING LOAD

If building space heat load is not input as data, it may be calculated using the degree day method. This method uses the following equation:

$$I.OAD = II_b (T_b - T_a)$$
 (R-5)

where T_h is a base temperature, usually 18°C. The building heat loss coefficient, U_b , is typically one million joules/hour°C for a single family house but would drop substantially for an energy efficient house.

The degree day method becomes increasingly inaccurate for energy-conserving houses, especially when passive solar gain is significant. Hot water load is typically 50 million joules daily for a single family residence, a figure which also could drop with increased energy efficiency.

B.3 SOLAR HEAT SUPPLIED TO LOAD

The solar heat supplied to load, calculated from the initial storage temperature, must be figured separately for space heat and hot water load. For space heat, the fraction of the load which is supplied by solar energy is equal to



$$f_{SH} = x_h \frac{T_s - T_r}{T_r - T_a}$$
 (B-6)

where T_s is storage temperature, T_r is room temperature, and X_h is a heat exchange coefficient. This coefficient, typically of value 2, is determined by the ratio of maximum heat exchange capacity per degree temperature difference to the building heat loss coefficient (U_h) .

The fraction of hot water which is supplied by solar is given by a similar formula:

$$f_{HW} = c_x \frac{T_s - T_c}{T_h - T_c}$$
 (B-7)

where T_h and T_c are hot and cold water temperatures and c_x is the heat exchange effectiveness from storage to load, usually 80-95%.

B.4 CHANGE IN STORAGE TEMPERATURE

The heat flow into the storage tank during the interval is calculated by

$$\Delta Q_s = Q_{col}$$
 - solar load - storage loss . (B-8)

The solar load and $Q_{\mbox{col}}$ have been found as described above. Storage loss is an additional term, found using an overall storage U-factor:

storage loss =
$$U_s(6V_s^{2/3})$$
 (B-9)

The term in parentheses approximates the storage surface area, in square meters, based on storage volume (V_s) in m^3 . The storage U-factor, U_s , is typically equal to 360 joules/ m^2 °C for a buried tank.

Change in storage temperature for the period is found by

$$\Delta T_3 = \Delta Q_5 / V_6 C_3$$

where C_s , the storage heat capacity, is 4.178×10^6 joules/m³°C.

The new storage temperature becomes the input to the calculation for the next interval. A flowchart for the simulation method with hourly steps is presented in Figure B-1.

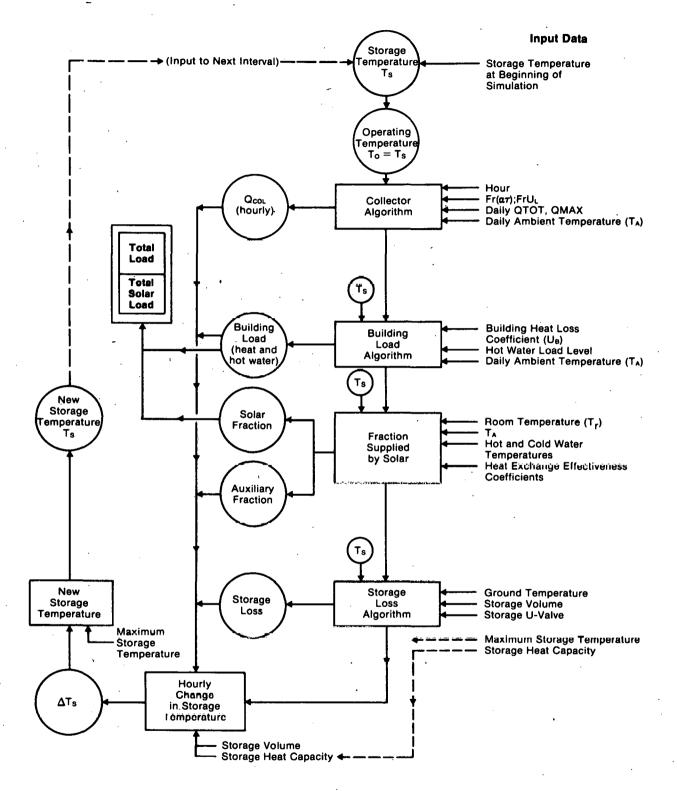


Figure B-1. Flowchart of Simulation with Hourly Intervals

Conventions: Boxes indicate calculations. Circles indicate calculated parameters, which may appear as input to a calculation (arrow leading away from parameter) or as the result of a calculation (arrow leading from calculation to parameter). Uncircled parameters, listed at the far right, are data inputs. The double box is the final result.



B.5 SIMULATION METHOD FOR SEASONAL STORAGE SYSTEMS

For seasonal storage systems, the daily change in storage temperature is, at most, a few degrees so that hourly change in storage temperature may be safely ignored. Simulation may proceed with a daily time step as outlined in Sections B.1 through B.4. The collector algorithm for the entire day is based on Equation 2-13 with the critical level held constant:

$$Q_{col} = F_r(\alpha \tau) (QTOT \sin \omega t_x - 2t_x H_c)$$
 (B-10)

with the turn-on time calculated according to Equation 2-11. All other steps remain the same, except that load and storage losses are calculated for a day rather than for an hour.

B.6 SIMULATION METHOD WITH DAILY STEPS FOR SMALL STORAGE TANKS

When the storage tank is small, storage temperature changes too fast to permit a direct simulation with daily steps. A daily step simulation may be performed using an iteration as follows.

- (1) Collector gain and daytime load are calculated, assuming that operating temperature remains equal to the initial storage temperature all day. Equation B-10 is used, with H_C assumed constant. The end-of-day storage temperature is calculated as in Section B.4, and average daytime storage temperature assumed midway between the beginning and end of day storage temperatures.
- (2) Collector gain and daytime load are recalculated, assuming that storage temperature changes through the day as found in step 1. Collector turn-on time (t_1) is the same as in step 1, but a new turn-off time (t_2) is found using equation 2-11 with the final storage temperature from step 1. The new algorithm is:

$$Q_{col} = F_r(\alpha \tau) \frac{QTOT}{2} \left(\sin \omega t_1 + \sin \omega t_2 \right) - \left(t_1 + t_2 \right) H_c \quad . \quad (B-11)$$

The critical level $H_{\rm C}$ in Equation B-ll is calculated as in Equation B-5 with the operating temperature ($T_{\rm O}$) set equal to the average daytime storage temperature calculated in step 1. The fraction of solar heat supplied to load is also calculated, assuming storage temperature is equal to the average daytime temperature from step 1. Final daytime storage temperature is again found as in Section B.4.

(3) Nighttime system performance is calculated by using the same two-step iteration to estimate the fraction of the load supplied by solar heat. The procedure is the same as in step 1 and 2 with collector gain set equal to zero.

A flowchart of this method is presented in Figure B-2.



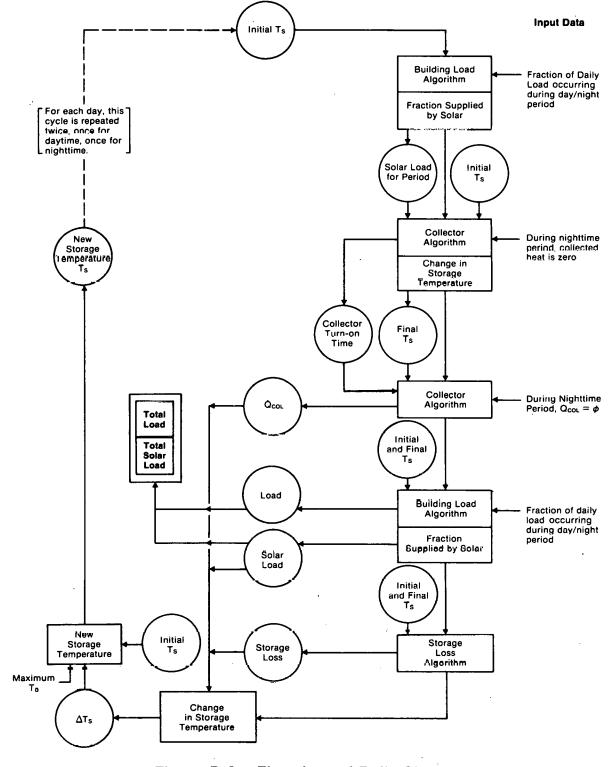


Figure B-2. Flowchart of Daily Simulation

Conventions are the same as in Figure B-1. Data inputs which are identical to those in Figure B-1 have been omitted in this flowchart. All calculations in this flowchart require the same data inputs as shown in Figure B-1.

This simulation runs twice for each day for the daytime and nighttime periods. Collector algorithm is bypassed for the nighttime period.



B.7 SIMULATION OF THE "TWO TANK" SYSTEM

The simulation of the "two tank" system is similar to the method outlined in Section B.6, with the following differences.

- Steps 1 and 2 are performed for the small storage tank. However, the final operating temperature calculated in step 1 and used in step 2 is constrained to be no greater than the temperature of the seasonal storage tank. The average daytime temperature for the small tank is calculated with the constraint that the storage temperature does not exceed the temperature of the seasonal tank.
- At the end of step 2, the end-of-day storage temperature is found differently. The net flow of heat into storage is added to the small storage tank, but this tank is again constrained to remain below the temperature of the seasonal storage tank. If the net heat flow into storage is too large to be added to the small tank, the remainder of the collected solar heat is added to both the small tank and the seasonal tank in proportion to their volumes. This assures that the temperature of the small tank never exceeds the temperature of the seasonal storage tank.
- In steps 2 and 3, the capacity of the small storage tank to meet the load is assessed as described in Section B.6. If the small storage tank is unable to meet the entire load, the remainder of the load is supplied by the seasonal storage tank. The system design assumes a separate heat exchanger for each storage tank. Consequently, if the two tanks together are insufficient to meet the load, the percentage supplied by solar energy is found by adding the percentage supplied by each tank separately.

B.8 CALCULATION OF THE DAY LENGTH

The following is a method for calculating the day length (t_D) used in the daily radiation algorithm (Duffie and Beckman 1974).

Necessary inputs are the latitude ϕ , collector slope s, and the declination δ . It is assumed that the collector faces due south.

Declination is calculated from

$$\delta = 0.4095 \sin 2\pi \frac{284 + n}{365}$$
 (B-12)

where n is the number of the day of the year, January 1 being equal to 1, and all angles are in radians. The day length is given by

$$t_D = \frac{12}{\pi} \arccos (-\tan \phi \tan \delta)$$
 (B-13)



A south-facing collector will, however, be shaded for large parts of the morning and late afternoon during the summer when the sun is in the northern half of the sky. This shading reduces the effective day length of a south facing collector. The effective day length is constrained by

$$t_{D} = \frac{12}{\pi} \arccos \left[-\tan(\phi - s) \tan \delta \right]$$
 (B-14)

Effective day length is, thus, the minimum of the values of Equations B-13 and B-14. With a collector tilt equal to the latitude, this means that the day length can never exceed 12 hours.

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