Modelling HIV Intervention among Most-at-Risk/Key Population: Case Study of FWSS in Nigeria

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Abstract

Using FWSS in Nigeria as a case study, this research develops a novel risk equation for estimating new infections among FWSS, their clients and communities. It uses a hybrid SUDT and SIT structural model. It considers number of contacts, number of protected and unprotected sexual acts, population and other existing values as base inputs. Simulation of the model was done using python programming. The model also estimates the impacts of these interventions on the clients of the sex workers, their female partners and the general population. The levels of the program implementation, needed on each scenario, to achieve the required number of averted new infections are also modelled. This model can be used to estimate the risk of a population set to a sexually transmitted disease. Public health workers can use the model to prepare a fit for- purpose intervention program for specific community members.

Keywords: FWSS; FSW; MARPs; Simulation; Mathematical modelling; Python programming

Introduction

Nigeria, with a population of 186 Million (2016 estimate), is the largest country in Africa. With over 3.5 million HIV positive persons, Nigeria has the second highest HIV burden globally. An estimated 60% of new HIV infections in Western and Central Africa in 2015 occurred in Nigeria [1]. Men who have Sex with Men (MSM), Female who Sell Sex (FWSS) and People who Injects Drugs (PWID) account for about 32% of new HIV infections in Nigeria and are the worst affected population sets by the epidemic. FWSS account for 20% of new infections in Nigeria. The country level prevalence for Brothel-Based Female who Sell Sex (BBFWSS) was 19.4% in 2014.

Using FWSS in Nigeria as a case study, this research develops a novel risk equation for estimating new infections among FWSS, their clients and communities. It uses a hybrid SUDT and SIT structural model. It considers number of contacts, number of protected and unprotected sexual acts, population and other existing values as base inputs. Simulation of the model was done using python programming. The model also estimates the impacts of these interventions on the clients of the sex workers, their female partners and the general population. The levels of the programme implementation, needed on each scenario, to achieve the required number of averted new infections are also modelled. This model can be used to estimate the risk of a population set to a sexually transmitted disease. Public health workers can use the model to prepare a fit-for-purpose intervention program for specific community members.

Objective

The objective of this research is to develop a mathematical model to estimate how many indirect HIV infections will be averted among FWSS, their clients and the general population, attributable to prevention programs targeting female sex works in Nigeria. The model also estimates the impacts of these interventions on the clients of the sex workers, their female partners and the general population. The model includes a risk ratio used to estimate the impact of the programme on each of the sub-population sets. The number of new infections averted on the sex workers and their clients, attributable to different scenarios and levels of the programme implementation is presented in this paper.

Methodology

A mathematical model was developed, using python programming language. A hybrid S-U-D-T and S-I-T structures were used in designing the model. The I group of FWSS was further divided into U and D while S-I-T was used for other population groups. A Susceptible (S) group includes all members of the population set; The Undiagnosed (U) group includes infected members of the population that are yet to be tested. The Diagnosed are the tested and confirmed members of the population set. The Infected (I) group includes both tested and yet-to-be tested infected persons (I=U+D); The Treatment group involves all persons on treatment and care [2].

The model considers various factors affecting the implementations of the program. Current values of the model variables, as shown in the Table 1 below, served as baseline inputs to the model [3]. The variables include initial prevalence of HIV among FWSS, their clients; proportion of sex acts that are protected; initial population of the target group; duration of the intervention; number of sexual contacts per FWSS, average number of sexual acts per week, etc. A specific risk equation was developed for the FSW, incorporating the current value of each variable [4]. Three Scenarios of the model was estimated over a period of five years. The first scenario entails putting all infected FWSS on treatment, irrespective of their CD4 or WHO staging and keeping other variables constant. The model considers the impact of this scenario on the clients of the sex workers. Putting only eligible FSWs on treatment and increasing condom distribution was the second scenario. Universal access to treatment for all FSWs and their clients was then modelled. An uncertainty analysis was also carried out as part of the model [5] (Figures 1-7).

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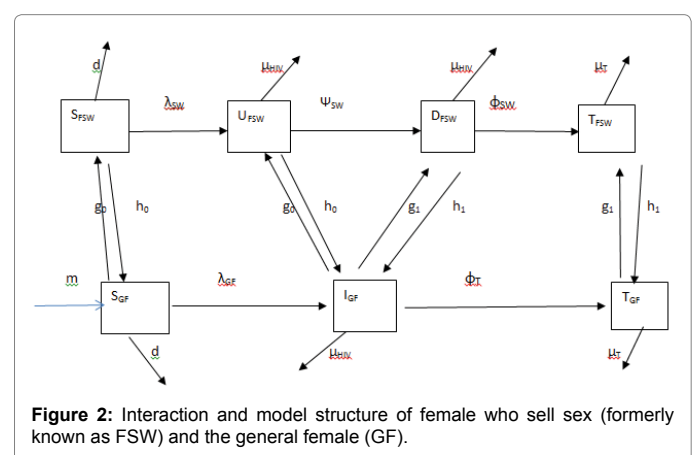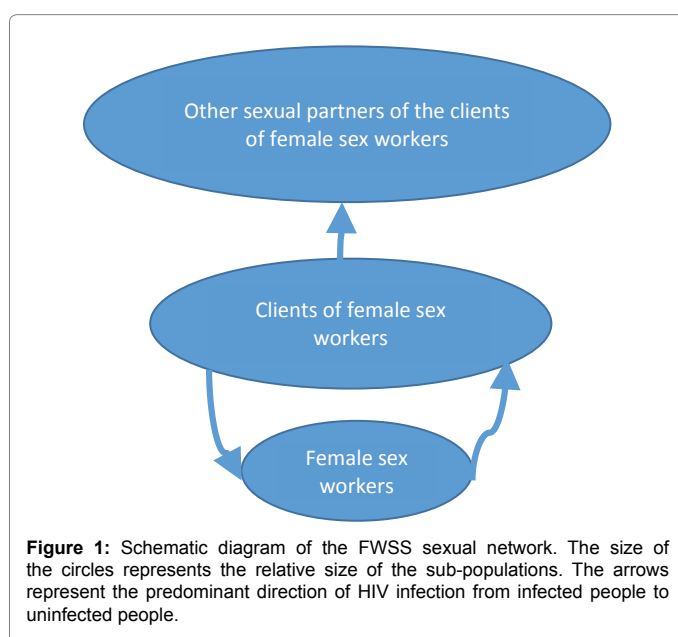
Parameters	Description	Symbol	Value
(FWSS)	Proportion of FWSS that are infected	p_{SW}	19.5
Initial prevalence in GF	Proportion of Gen Female that are infected	p_{GF}	4.1
Initial prevalence in GM	Proportion of Gen Male that are infected	p_{GM}	3.2
Efficacy of condom	Efficacy of condom	ε	0.95
Proportion of FWSS that are infected with STI	Proportion of FWSS that are infected with STI	p_{sti}	28.5
Maturity rate	Rate of maturity into adulthood for gen population	m	15
No of acts 1	Number of acts in FWSS-Clients	n_1	200
No of acts 2	Number of acts in Gen Population	n_2	80
No of contacts 1	Number of contacts of the FWSS	c1	432
No of contacts 2	Number of contacts of the Clients	c2	50
No of contacts 3	Number of contacts of the GF, GM	c3	2
Beta	Rate of transmission (general unprotected sex)	ß	0.01
Initial Population of GM	Initial male population size	NGM	39,208,214
Initial Population of FSW	Initial FSW population size	NSW	308340
Initial Population of Clients	Initial Clients population size	NCL	18500400
Initial Population of GF	Initial Female population size	NGF	38942286
Death rate among susceptible	Natural death rate among susceptible FWSS, GF, CL & GM	d	0.014
Death rate among infected	Death rate among infected FWSS, GF, CL & GM	µHIV	0.12
Death rate among those treatment	Death rate among FWSS, GF, CL & GM on treatment	µT	0.03
Tethar FSW	Rate of migration from Undiagnosed to Diagnosed FWSS	Ψsw	0.6
Tethar Treatment FSW	Rate of migration from diagnosed to treatment FSW	ΦSW	0.05
Tethar Treatment	Rate of migration from infected to treatment	ΦT	0.33
Rate of migration/upwards zero	Rate of migration from SGF to SFSW; and IGF to UFSW	go	1
Rate of migration/downwards zero	Rate of migration from SFSW and UFSW to SGF & IGF	ho	1
Rate of migration/upwards one	Rate of migration from IGF & TGF to DFSW and TFSW	g1	1
Rate of migration/downwards one	Rate of migration from DFSW and TFSW to IGF & TGF	h1	1
Rate of migration (Gen Male)	Rate of migration from GM to Clients	g2	1
Rate of migration (Gen Male)	Rate of migration from Clients to GM	h2	1
Rate of migration/upwards zero	Rate of migration from SGF to SFSW; and IGF to UFSW	go	1
Rate of migration/downwards zero	Rate of migration from SFSW and UFSW to SGF & IGF	ho	1
Rate of migration/upwards one	Rate of migration from IGF & TGF to DFSW and TFSW	g1	1
Rate of migration/downwards one	Rate of migration from DFSW and TFSW to IGF & TGF	h1	1
Rate of migration (Gen Male)	Rate of migration from GM to Clients	g2	1
Rate of migration (Gen Male)	Rate of migration from Clients to GM	h2	1

Table 1: Parameters, description, symbol and values used.

Figure 1: Schematic diagram of the FWSS sexual network. The size of the circles represents the relative size of the sub-populations. The arrows represent the predominant direction of HIV infection from infected people to uninfected people.

Figure 2: Interaction and model structure of female who sell sex (formerly known as FSW) and the general female (GF).

Assumptions

- Net rate of migration from SFWSS group to SGF is the same as SGF>>SFWSS, (go/ho), UFSW and different from IGF to DFSW and TFSW

- There are different rate of migration for each of the sub-groups

- There are different death rate for Susc, Und, Diag, Infected and Treatment group

- No significant sexual contact between FSW and GF

- Individuals in the infected population, not on ART, lives for extra 10 to 15years

- Maturity rate of 15 years

- Only GF within the age range of 15-49 are considered

Modelling Equations

Equations for FSW

$$S(t+1) = S_{FSW}(t) + g_o S_{GF}(t) - \lambda_{sw} S_{FSW}(t) - d S_{FSW}(t) - h_o S_{FSW}(t)$$

$$U(t+1) = U(t) + \lambda_{sw}.S(t) - \mu_{HIV} U(t) - \Psi_{fsw} U(t) + g_o I_{GF}(t) - h_o U(t)$$

$$D(t+1) = D(t) + \Psi_{fsw} U(t) - \mu_{HIV} D(t) - \phi_{fsw} D(t) + g_1 I_{GF}(t) - h_1 D(t)$$

$$T(t+1) = T_{fsw}(t) + \phi_{fsw} D(t) - \mu_T T_{fsw}(t) + g_1 T_{GF}(t) - h_1 T_{fsw}(t)$$

Risk equation for FSW

$$\lambda_{SW} = [C_1 * \frac{I_{CL}}{N_{CL}} * (1-P_{Su}) * \{(1-(1-\beta)^{n(1-p)}\} \{(1-((1-\varepsilon)\beta)^{np}\}] + [C_1 * I_{CL}/N_{CL} * Psti *$$

$$\left\{(1-(e_{sti}\beta)^{n(1-p)}\right\} \{(1-((1-\varepsilon)e_{sti}\beta)^{np}\}] + [c_1 * \frac{T_{CL}}{N_{CL}} * (1-p_{sti})$$

$$* \{(1-\left(\left(1-\varepsilon_T\right)\beta\right)^{n(1-p)}\} \{(1-((1-\varepsilon_T)(1-\varepsilon)\beta)^{np}\}] +$$

$$[C_1 * P_{sti} * T_{CL}/N_{CL} * \{(1-(1-$$

$$(1-\varepsilon_T)e_{sti}\beta)^{n(1-p)}\} * \{(1-(1-\varepsilon_T)(1-\varepsilon)e_{sti}\beta)^{np}\}]$$

Equation for general female

$$S(t+1) = S_{GF}(t) + M_1 S_{GF}(t) - g_o S_{GF}(t) + h_o S_{FSW}(t) - \lambda_{GF}(t) S_{GF}(t) - d S_{GF}(t)$$

$$I(t+1) = I_{GF}(t) + \lambda_{GF} S_{GF}(t) + h_o U(t) - g_o I_{GF}(t) - g_1 I_{GF}(t) + h_1 D(t) - \phi_T I_{GF}(t) - \mu_{HIV} I_{GF}(t)$$

$$T(t+1) = T_{GF}(t) + \phi_T I_{GF}(t) - g_1 T_{GF}(t) + h_1 T_{fsw}(t) - \mu_T T_{GF}(t)$$
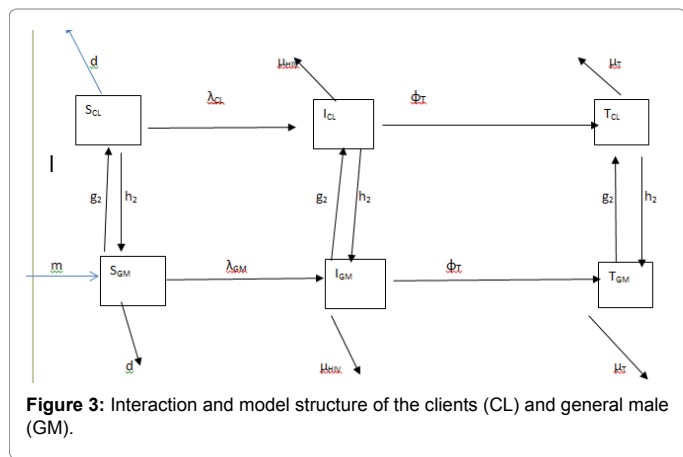

Figure 3: Interaction and model structure of the clients (CL) and general male (GM).
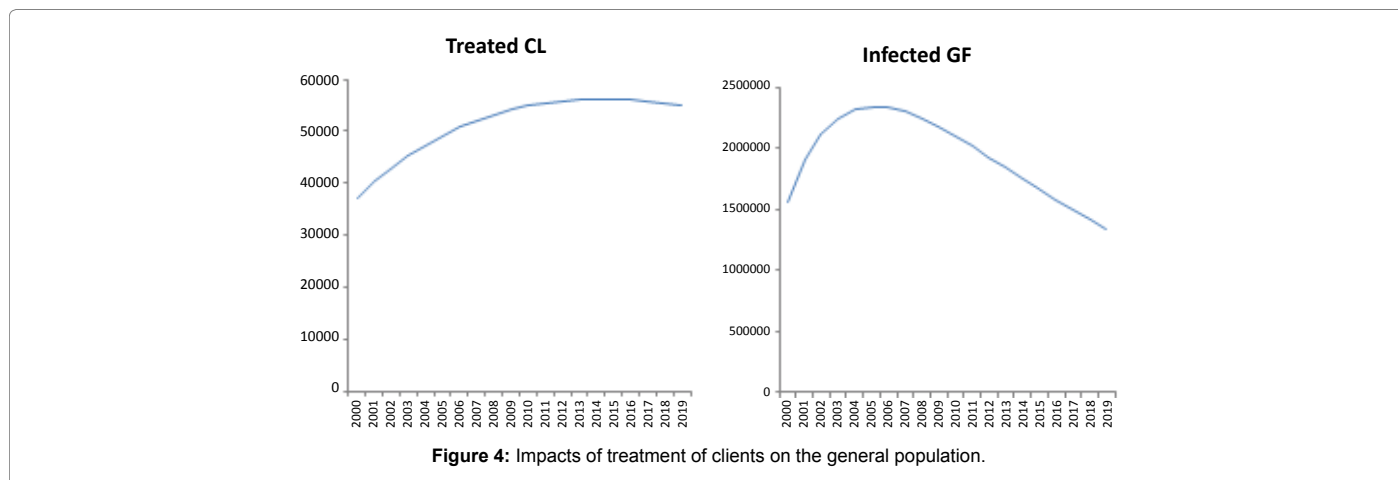

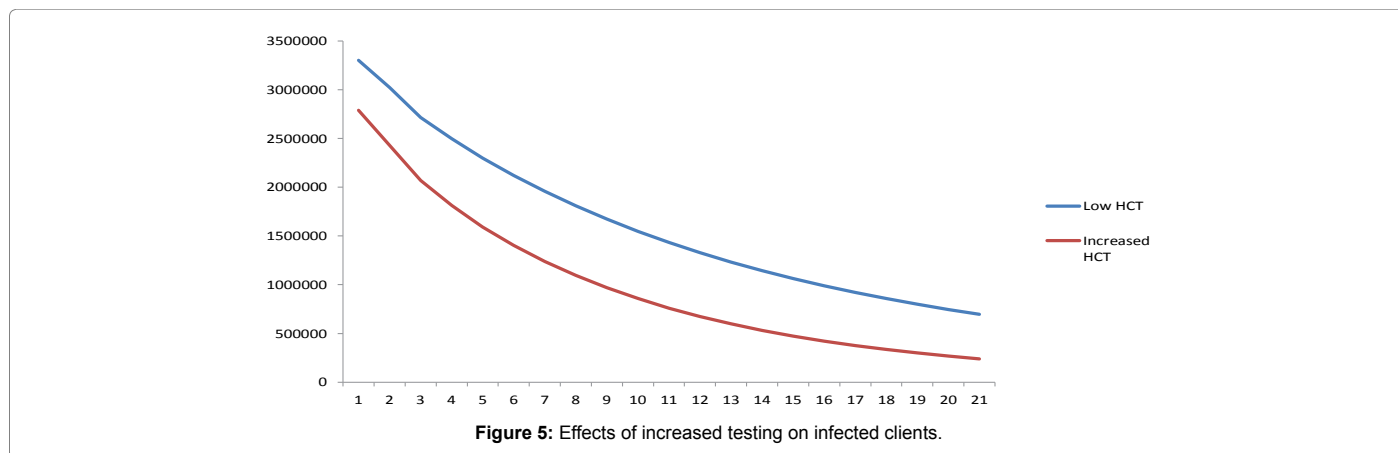**Figure 4:** Impacts of treatment of clients on the general population.

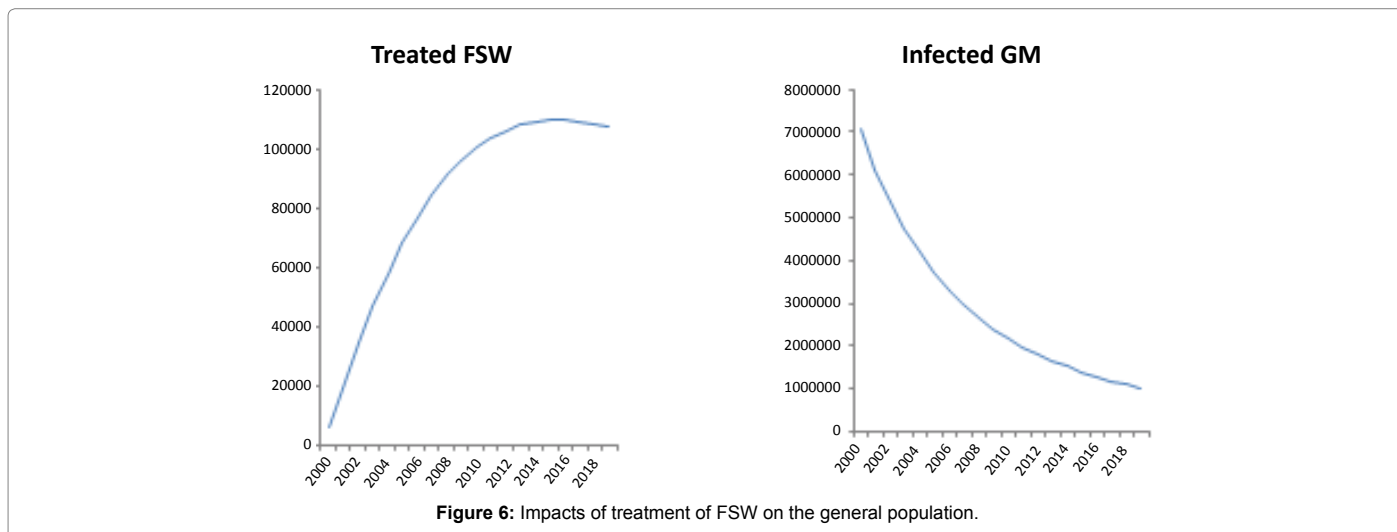**Figure 5:** Effects of increased testing on infected clients.

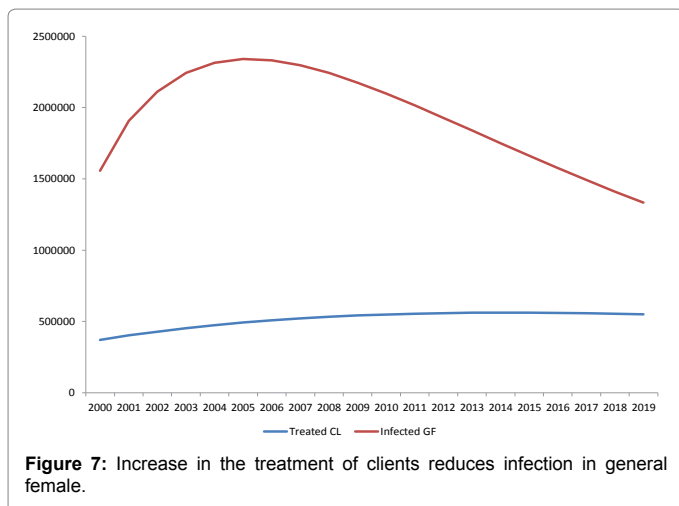**Figure 6:** Impacts of treatment of FSW on the general population.

Figure 7: Increase in the treatment of clients reduces infection in general female.

Risk equation for general female

$$\lambda_{GF} = \left[C_2 \ast \frac{I_{CL}}{N_{CL}} \ast \{(1-(1-\beta)^{n.(1-p)}\} \ (1-(1-\varepsilon)\beta^{np} \ )\right] + \left[C_2 \ast T_{CL} / N_{CL}\right.$$
$$\ast \left(1-(1-(1-\varepsilon_T)\beta)^{n(1-p)}\right)\left(1-(1-\varepsilon_T)(1-\varepsilon)\beta^{np}\right)] +$$
$$\left[C_2 \ast I_{GM} / N_{GM} \ast \left(1-(1-\beta)^{n(1-p)}\right)\left(1-(1-\varepsilon)\beta^{np}\right) \right] +$$
$$[C_2 \ast T_{GM} / N_{GM} \ast$$
$$(1-(1-(1-\varepsilon_T)\beta)^{n(1-p)})(1-(1-\varepsilon_T)(1-\varepsilon)\beta^{np} \ )]$$

Client equation

$$S(t+1) = S_{CL}(t) - dS_{CL}(t) - \lambda_{CL}(t).S_{CL}(t) - h_2 S_{CL}(t) + g_2 S_{GM}(t)$$
$$I_{(t+1)} = I_{CL}(t) + \lambda_{CL}(t) S_{CL}(t) - \mu_{HIV} I_{CL}(t) - \phi_T I_{CL} + g_2 I_{GM}(t) - h_2 I_{CL}(t)$$
$$T_{(t+1)} = T_{CL}(t) + \phi_T I_{CL}(t) - \mu_T T_{CL}(t) + g_2 T_{CL}(t) - h_2 T_{fsw}(t)$$

Client risk equation

$$\lambda_{CL} = \left[C_2 \ast I_{GF} / N_{GF} \ast (1-(1-\beta)^{n(1-p)})\ (1-((1-\varepsilon)\beta)^{np}]+\right.$$
$$[C_2 \ast T_{GF} / N_{GF} \ast (1-((1-(1-\varepsilon_T)\beta)^{n(1-p)})(1-(1-\varepsilon_T)(1-\varepsilon)\beta^{np})]$$
$$+ [C_1 \ast I_{FSW} / N_{FSW} \ast (1-(1-\beta)^{n(1-p)} (1-(1-\varepsilon)\beta)^{np})]$$
$$+ [C_1 \ast T_{FSW} / N_{FSW} \ast (1-(1-(1-\varepsilon_T)\beta)^{n(1-p)} (1-(1-\varepsilon_T)(1-\varepsilon)\beta)^{np}]$$

General male equation

$$S(t+1) = S_{GM}(t) + M_1 S_{GM}(t) - g_2 S_{GM}(t) + h_2 S_{CL}(t) - \lambda_{GM}(t) S_{GM}(t) - dS_{GM}(t)$$
$$I_{(t+1)} = I_{GM}(t) + \lambda_{GM}(t).S_{GM}(t) + h_2 I_{CL}(t) - g_2 I_{GM}(t) - \phi_T I_{GM}(t) - \mu_{HIV} I_{GM}(t)$$
$$T_{(t+1)} = T_{GM}(t) + \phi_T I_{GM}(t) - g_2 T_{GM}(t) + h_2 T_{CL}(t) - \mu_T T_{GM}(t)$$

General male risk equation

$$\lambda_{GM} = [C_2 \ast I_{GF} / N_{GF} \ast (1-(1-\beta)^{n(1-p)} \left((1-(1-\varepsilon)\beta)^{np}\right)] +$$
$$[C_2 \ast T_{GF} / N_{GF} \ast \left(1-(1-(1-\varepsilon_T)\beta)^{n(1-p)}\right) (1-((1-\varepsilon_T)(1-\varepsilon)\beta)^{np}]$$

Results and Discussion

It was observed that if the status quo (37% of eligible positive FSW on treatment) is maintained, the new infection rate will gradually increase by 3.6% in five years' time. Putting 80% of eligible positive FSWs on treatment will avert 2789 new infections in the same duration and reduce the current rate of new infections to 0.7. A slight decrease of 0.3% would be experienced in the general female population. Putting all FSWs on treatment returns a 89.7% reduction on the number of new infections among clients of FSW.

Conclusion and Recommendations

The simulation model reveals the efficiency of treatment in reducing the rate of new infections among FSWs, their clients and general female. The models reveal the importance of the investing in the FSW intervention programs now, rather in the future. The model outputs can be used to calculate the Quality Adjusted Life Years (QALY) to be gained during the intervention. A slight contribution of the total number of condom distributed to a reduction in new infection rate was also noticed. Further modelling scenarios are required to effectively infer on the efficiency of the intervention programs.

References

1. Global Information and Education on HIV and AIDS (2016) Avert Publications, Nigeria.

2. Hernandez-Vargasa EA, Middleton RH (2013) Modelling the three stages in HIV infection. J Theor Biol 320: 33-40.

3. Perelson AS, Ribeiro RM (2013) Modelling the within-host dynamics of HIV infection. BMC Biol 11: 96.

4. Wodars D, Cassels S (2012) Mathematical models of HIV pathogenesis and treatment. Harvard Publications.

5. Alizon S, Magnus C (2012) Modelling the course of an HIV infection: Insights from ecology and evolution. Viruses 4: 1984-2013.