Contribution to the
XVI International Conference
on High Energy Physics, 1972

July 1972

*Batavia, Ill.
Sept 6-13, 1972*

Recoil Proton Polarization in Neutral
Pion Photoproduction between 1000 and
1800 MeV[†]

N. Tanaka[†], M.M. Castro, R.H. Milburn, W.B. Richards^{††}
J.P. Rutherford[§], and B.F. Stearns[§]

Department of Physics, Tufts University, Medford, Mass. 02155

and

M. Deutsch, P.M. Patel^{§§} and K. Tsipis[‡]
Laboratory of Nuclear Science and Department of Physics,
M.I.T., Cambridge, Mass. 02139

ABSTRACT

Measurements are presented of the recoil proton polarization for π^0 production angles near 64° c.m.s.. The steep angular dependence observed by others at lower energies persists to at least 1500 MeV, and the polarization crosses through zero near 63° over the entire 900-1600 MeV energy interval. Summary fits are made to available recoil proton polarization data, 950-1250 MeV, and are found to require terms of order $\cos^3\theta$, but no higher.

NOTICE
This report was prepared as an account of work sponsored by the United States Government. Neither the United States nor the United States Atomic Energy Commission, nor any of their employees, nor any of their contractors, subcontractors, or their employees, makes any warranty, express or implied, or assumes any legal liability or responsibility for the accuracy, completeness or usefulness of any information, apparatus, product or process disclosed, or represents that its use would not infringe privately owned rights.

MASTER

DISCLAIMER

This report was prepared as an account of work sponsored by an agency of the United States Government. Neither the United States Government nor any agency Thereof, nor any of their employees, makes any warranty, express or implied, or assumes any legal liability or responsibility for the accuracy, completeness, or usefulness of any information, apparatus, product, or process disclosed, or represents that its use would not infringe privately owned rights. Reference herein to any specific commercial product, process, or service by trade name, trademark, manufacturer, or otherwise does not necessarily constitute or imply its endorsement, recommendation, or favoring by the United States Government or any agency thereof. The views and opinions of authors expressed herein do not necessarily state or reflect those of the United States Government or any agency thereof.

DISCLAIMER

Portions of this document may be illegible in electronic image products. Images are produced from the best available original document.

We have measured the polarization of the recoil proton in neutral pion photoproduction for incident photon energies between 1000 and 1800 MeV, at a mean pion production angle of 64.5° in the center of mass. The experiment was performed at the Cambridge Electron Accelerator.

Bremsstrahlung produced on an internal synchrotron target by an 1800 MeV electron beam passed through a collimator, sweeping magnets and a scraper before striking a 5.08 cm diameter liquid hydrogen target (Figure 1). Photons from the decay of the neutral pion passed through a permanent 700 gauss-cm field into a shower detector consisting of a tantalum plate spark chamber, a scintillation counter and a lead-glass Čerenkov counter hodoscope. Pulse heights from the scintillation counter and Čerenkov counters, together with hodoscope information, were recorded on film along with the shower chamber pictures. The recoil proton entered a spectrometer consisting of a scintillation counter and two thin-plate optical spark chambers at each end of a dipole magnet providing mean deflection of 15° . This proton arm subtended 2.7×10^{-3} ster at the target and provided momentum resolution $\Delta p/p = 0.02$. Time-of-flight between the two scintillation counters and pulse height information from the 2.5 cm thick downstream counter permitted

rejection of particles other than protons. The protons from the spectrometer entered a spark chamber built of aluminum-sheathed graphite plates, each 91.4 cm square and containing 1.27 cm of graphite, 0.05 cm of aluminum, and epoxy cement to total 1.40 cm. Sixty-one plates were mounted with 1.27 cm spacing in a gas tight enclosure filled with helium at slightly above atmospheric pressure. The chamber was photographed in 90°-stereo on 35 mm Linagraph Shellburst film through an optical system employing parabolic-cylindrical mirrors as field elements.

During the experimental runs about 160,000 events were photographed, after a coarse electronic selection based upon pulse heights in the Čerenkov and scintillation counters and time of flight in the spectrometer. The proton spectrometer and gamma-spark chamber pictures were scanned and measured automatically on the M.I.T. "SPASS" system¹. About 25 percent of the events passed rigid requirements set to define neutral pion photoproduction. Included in these events is a background of proton Compton scatterings estimated to be less than 7 percent over the photon energy range of interest. Also included are possible multi-pion productions. A Monte-Carlo estimate placed this background at less than 3 percent of the accepted events.² Carbon chamber photographs of the events

selected by "SPAS'S" were then scanned and measured automatically by an early version of the "SPAS" system, then at Harvard³, and the various measurement data were merged onto a common set of computer tapes.

Polarization determinations are extraordinarily sensitive to small systematic errors in angular measurements. To assist in the reduction of the proton-carbon scattering data a set of grid lines intersecting on a 20 cm lattice were ruled on both carbon-plate spark chamber windows and were photographed at the beginning and end of each roll of film. Separate photographs were made of wires stretched 61 cm in front of each of the windows to permit determination of the effective camera locations, in the two views, as a function of the chamber gap number, to allow for certain optical system distortions. Using averaged measurements of the photographed grids as made on a Vanguard film-plane digitizer, an optimized 22-coefficient function was calculated to map from the film plane onto the window grid of each view. Separate functions were determined for each 20 cm x 20 cm square cell of the chamber window, and then the individual mappings were assembled into a continuous weighted average to eliminate discontinuities at the cell boundaries. The aim was to obtain a mapping that was conformal

not only over large areas but also over the 15-20 cm regions that are critical for the determination of projected scattering angles of individual protons. The individual events as measured by the "SPASM" system were first mapped onto the film plane to correct for lens and CRT distortions, then onto the planes of the spark chamber window grids and then into real space, using a smoothed representation of the effective camera locations for each view. It is believed that this overall procedure effectively compensated for both the intrinsic pin-cushion distortion of the parabolic field mirror system and the smaller scale distortions associated with the incidental bending of the large flat mirrors required to fit the optics onto the accelerator floor. The gross mapping fitted the 20 cm-cell vertices on the windows to ± 0.06 cm, at worst. A check on a smaller geometrical scale was carried out using actual proton tracks as mapped by the above procedure.

Measurements of two successive spark locations were used to predict the location of the spark preceeding the pair for comparison with actual measurements of that spark. The precision of transverse measurement of individual spark positions was found to be ± 0.1 cm in the top view and $\pm .13$ cm in the side view. The mean extrapolated spark location did not deviate from

the expected straight line more than 0.010 cm in the top view and 0.015 cm in the side view.

For each event so measured and mapped scatterings were detected by dividing the spark trail into two portions and fitting a straight line in space to each portion, weighting the individual sparks to account for multiple Coulomb scattering appropriate to the scattering energy as inferred from the known incident energy and range of the particle. Such fits were obtained for all possible subdivisions of the track having at least two sparks in each of the two branches. The mean points of closest approach of the two fitted lines were determined and acceptable fits were required to have this point lie between the two assumed track segments. The closest approach distance, which was distributed with standard deviation 0.064 cm, was required to be less than 0.152 cm. A goodness-of-fit parameter was also calculated and, in case of ambiguities, the scattering was assumed to occur in the plate giving the best goodness of fit. For the selected fit the angles of scattering, proton energy at scatter, and inelasticity were calculated. This procedure yields "scatterings" down to angles of about 2° below which the algorithm becomes progressively unreliable. Proton-carbon analyzing powers and an estimated uncertainty thereof were determined for the

conditions of each scattering event using an extension of tables and a program prepared at the California Institute of Technology⁴. Data summary tapes were prepared and used to calculate the proton polarization and other results for a variety of cuts and conditions⁵. All data were subjected to cuts correlating a proton's trajectory in the spectrometer with its initial path in the carbon chamber in order to minimize spurious events.

Since it was known that a systematic angular error of as much as a few tenths of a degree could seriously affect the computed polarizations, an additional normalization procedure was carried out. For this, all events scattering at 2° or more, among which small-angle and other events of negligible analyzing power are vastly predominant, were assigned an analyzing power of 1.0 and the resulting spurious proton "polarization" was calculated for scatterings in each of the spark chamber plates. For each plate an empirical redirection of the polar axis of scattering was effected to minimize a smoothed representation of these spurious "polarizations". For the chamber view relevant to experiment -the top view- the spurious polarizations were approximately a constant 0.05° and were compensated by projected shifts of about 0.05° in the effective forward direction.

The scattering angles for each event as renormalized in this way, together with the corresponding analyzing powers, were also recorded on the data summary tapes. A comparison of results calculated both from the original data and from this renormalization of them provides a measure of the residual systematic uncertainties in this experiment.

To confirm that the track fitting routines selected legitimate p-carbon scatterings all data with measured inelasticity of scattering less than +10 MeV (within the measurement resolution) were distributed in 1° laboratory scattering angle bins between 6° and 20° , and in 20-MeV energy bins from 90 to 210 MeV, plus one bin extending to 300 MeV. For each bin an average elastic differential cross section was estimated from an interpolation of existing data⁴. The elastic scattering angle distribution was predicted for each energy range and normalized to the number of scatterings in that range. The results were summed over the whole (90-300 MeV) energy range, to obtain adequate statistics, and the predicted occupancy of each 1° angular bin was compared with the observed numbers. Including all angles ($7-20^\circ$) the observed numbers fitted to give a combined $\chi^2=4.35$ for 6 degrees of freedom, with a corresponding probability of 0.6.

Between 6° and 7° an excess of events was observed, especially below 150 MeV. These are interpreted as coming from the tail of the multiple scattering distribution. An additional comparison was made between the observed energy distribution and the suitably integrated cross section estimates. Again, for $(7-20^\circ)$ and $(90-300 \text{ MeV})$, the correspondence was satisfactory in terms of the known number of incident protons and with an estimated inelastic contribution of about 10 percent. The energy and angular range used in these tests contains the predominant contributors to the effective proton-carbon analyzing power, and the above checks give us additional confidence that our procedures properly select and measure bona-fide proton-carbon scattering events.

Our results are summarized in Figure 2 in which proton polarizations as calculated from the renormalized angles are plotted against incident photon energy. Polarization +1 corresponds to a proton spin in the direction of $\vec{k}_\gamma \times \vec{q}_{\text{pro}}$. Mean pion production angles are indicated. The error bars are statistical. The data include all p-carbon scattering angles above the angle: $\text{Max} [7^\circ, 10.9^\circ - 0.0289 T]$, where T is the laboratory kinetic energy at scattering, in MeV. This arbitrary cut-off eliminates potential dilution

from multiple-scattering events but does not seriously affect the statistical accuracy of the polarization estimate. To illustrate the sensitivity of the data to various assumptions, there are marked against each error bar points corresponding to the following alternatives: a) the use of all scattering angles greater than 3° ; b) the use of the original unnormalized scattering angles greater than 3° ; c) data in which an estimated uncertainty of the analyzing power data has been added to, or d) subtracted from, that analyzing power, for all renormalized scattering angles greater than 3° . It is seen that the results are remarkably insensitive to these variations. One may infer the the dominant contribution to the asymmetry comes from the larger scattering angles where the analyzing power is both large and well known and in which the angular normalization is not critical. Dilution resulting from multiple Coulomb scattering does not appear to be significant, even in the data cut off at 3° .

For the purposes of further analysis and comparison with other experiments we shall take as our final results the polarizations calculated from the normalized scattering angles and all data having a p-carbon scattering angle above $\max [7^\circ, 10.9^\circ - 0.0289T]$. These results are presented in Table I, separated

according to whether the pion production angle was larger or smaller than 64.5° in the center-of-mass system. Also given in Table I are the corresponding results from two different experiments at the California Institute of Technology covering overlapping energy and angular regions^{6,7}. In this table our errors as presented are the statistical estimates which include, however, the range of likely systematic uncertainties. The errors for the other experiments are as quoted by the respective authors^{6,7}.

The polarizations in Table I show strong angular dependence. To compare these data it is convenient to plot them, for each 100-MeV energy bin, against the mean center-of-mass pion production angle. This is done in Figure 3. Also shown are minimum- χ^2 straight-line fits made under the assumptions that all the data are statistically compatible and that the variation over the 10° range is approximately linear.

Fitting the proton polarization to a function

$$P = a + b(\theta - 62^\circ) \quad , \quad \text{the coefficients}$$

a and b are also entered in Table I. These coefficients in effect summarize current experimental knowledge of the recoil proton polarization from π^0 photoproduction near 60° from 900-1600 MeV.

Most significant is the indication that the recoil proton polarization passes through zero at about 63° center-of-mass pion angle over the entire 900-1600 MeV photon energy interval. At this angle the momentum transfer, t , varies from $-.32 \text{ (GeV/c)}^2$ at 950 MeV to $-.60 \text{ (GeV/c)}^2$ at 1550 MeV, and the center-of-mass energy ranges between the D_{15} and F_{15} resonances near 1680 MeV and the F_{37} resonance at 1950 MeV. At 1250 MeV there is a suggestion in the a -coefficient (Table I) of a 2-3 standard deviation peak in the energy dependence of the polarization at 62° , corresponding to a momentum transfer of $-.45 \text{ (GeV/c)}^2$. However, there is no clear evidence of any structure in polarization as a function of t extending above or below this particular s -channel energy of 1.8 GeV. Further, experiments at higher energy where t -channel processes are presumed to dominate, show large negative polarizations in this t -range, in contrast to the zero crossing found here⁸.

In view of the steep angular dependence of the polarization near 62° it is interesting to compare these results with data at larger pion production angles. Information is now available from Daresbury⁹ and Bonn¹⁰ up to proton energies of 1250 MeV. For purposes of comparison and interpretation it is

convenient to calculate from all polarization data, the reduced cross section

$$P' = [k P(\theta) \sigma(\theta)] / [q \sin \theta] \quad (1)$$

where $\sigma(\theta)$ is the differential production cross section at angle θ , and k and q are the photon and pion center-of-mass momenta, respectively.

The reduced cross section is equal to the interference term in the helicity amplitudes,

$\text{Im} (H_1 H_3^* + H_2 H_4^*)$, divided by the ubiquitous factor $\sin \theta$ ¹¹. Differential cross sections were interpolated where available from recent Daresbury work¹².

Reduced cross sections are plotted in Figure 4 which summarizes currently available data above 900 MeV.

At 62° a composite point is entered representing a straight line fit to the reduced cross sections obtained from the data of the present experiment and from the 60-degree Caltech experiments. The individual data points are plotted without error bars.

Also indicated by dashed lines are the uncertainty ranges of the slopes of the straight-line fits

associated with the 62° composite point. We have

fitted these reduced cross sections to polynomials

in $\cos \theta$, $P' = A + B \cos \theta + C \cos^2 \theta + D \cos^3 \theta$,

which are also plotted in Figure 4., using coefficients

given in Table II. The third degree term is indispensable for fitting the data near 60° , but higher terms are unnecessary. It is to be observed that the slope of the fitted curve at 62° lies within the uncertainty limits of the slope associated with the fit to the 60-degree data alone. The latter slope as measured in the present experiment remains approximately constant at $dP'/d\theta = (-0.067 \pm .012)$ $\mu\text{b}/\text{ster}/^\circ$ between 900 and 1500 MeV and is consistent with this same value up to 1600 MeV photon energy.

A full interpretation of all these data can, of course, only be made in the context of an overall analysis of pion photoproduction phenomena such as that of Walker¹¹. On the other hand, it is difficult to imagine how our principal result - the apparent zero in the recoil proton polarization at $62-63^\circ$ all the way from 900 to 1600 MeV-could arise from a complicated conspiracy of many contributing and resonating amplitudes. Neither would such a zero appear to be a reflection of a simple t-channel process since θ_s , rather than t, determines its location over the whole range of s. The simplest a priori interpretation would be in terms of a weakly energy dependent and real background amplitude which vanishes near 63° and against which imaginary resonant amplitudes

interfere to produce the energy dependent polarizations at larger angles. Presently available cross section data are insufficient to resolve these speculations, although there appears to be a broad minimum in the differential cross section in the region $70-90^\circ$ c.m.s. and 900-1300 MeV, which suggests the vanishing of a significantly contributing amplitude.

We wish to thank C. Bemporad, J.R. Sauer, C.K. Sinclair, K. Sisterson and the staff and Director of the Cambridge Electron Accelerator for their important assistance during various phases of this experiment.

Footnotes

*Research supported by the U.S. Atomic Energy Commission under Contract No. AT(11-1)3023.

[†]Present Address: Los Alamos Scientific Laboratory, Los Alamos, N.M. 87544.

^{††}Present Address: Dept. of Physics, Oberlin College, Oberlin, Ohio 44074.

[§]Present Address: Dept. of Physics, Hobart and William Smith College, Geneva, N.Y. 14456.

^{§§}Present Address: Dept. of Physics, McGill University Montreal, Quebec.

^{††}Present Address: Dept. of Biophysics, Mass. Institute of Technology, Cambridge, Mass. 02139.

¹M. Deutsch, IEEE Trans. on Nuclear Science, Vol. NS-12, 69 (1965).

²N. Tanaka, Ph.D. Thesis, Tufts University (1969) p. 131, unpublished.

³C.A. Bordner Jr., A.E. Brenner and P. deBruyne, Radio Electronic Engineer 33, 171 (1967); A.E. Brenner, IEEE Trans. on Nuclear Science NS-12, 241 (1965).

⁴C.S. Kretschmar, M.S. Thesis, Tufts University (1969), unpublished; W.A. McNeely, California Inst. of Technology Internal Report 30 (1967), unpublished.

⁵Polarizations were obtained by maximizing the

likelihood function $\mathcal{L}(P) = \prod_i [1 + A(T_i, \theta_i, \Delta T_i) P \cos \psi_i]$,

and where φ_1 is the azimuthal p-carbon scattering angle for each event and A is the corresponding analyzing power as a function of energy, polar angle and inelasticity.

⁶E.D. Bloom, C.A. Heusch, C.Y. Prescott, and L.S. Rochester, Phys. Rev. Letters 19, 671 (1967); E.D. Bloom, Ph.D. Thesis, California Institute of Technology, 1967 (unpublished), Table IV, p. 39.

⁷S. Cheng, Ph.D. Thesis, California Institute of Technology, 1970 (unpublished), Table 4.3, p. 69.

⁸M. Deutsch, P. Kijewski, L. Golub, D. Potter, D. Quinn, J. Rutherford, private communication, (to be published).

⁹M.N. Prentice et al, Daresbury Nuclear Physics Laboratory Preprint DNPL/P-103, (1972).

¹⁰P. Blüm et al, Universität Bonn Physikalisches Institut Report PI-1-105, (1970).

¹¹R.L. Walker, Phys. Rev. 182, 1729 (1969). (For definitions of $H_1 \dots H_7$)

¹²P.S.L. Booth et al, Daresbury Nuclear Physics Laboratory Preprint DNPL/P-95, (1971); also P. Spillantini and V. Valente, CERN Report # CERN-HERA 70-1, (1970).

¹³D.E. Lundquist et al, Phys. Rev. 168, 1527 (1968).

¹⁴Ref. 7 page 69.

FIGURE CAPTIONS

- FIG. 1. Arrangement of experimental equipment.
- FIG. 2. Recoil proton polarization near 64° pion production angle: results of this experiment. Points with indicated errors use renormalized p-carbon scattering angles cut off near 7° (see text). Also indicated are polarizations with scattering angles cut off at 3° using renormalized angles (symbol "3"); using unnormalized angles (symbol "u"); using renormalized angles and analyzing power data to which an uncertainty has been added (symbol "4") or from which it has been subtracted (symbol "-"). Actual mean production angles are shown.
- FIG. 3. Recoil proton polarization dependence on pion production angle for different photon energies: data from this experiment and from earlier Caltech work near 60° (refs. 6 and 7).
- FIG. 4. Reduced cross section (cf. Eq. 1) versus pion center-of-mass production angle for incident photon energies 950-1250 MeV: a summary of available data. The composite point at 62° ,

and slope (dashed lines) are fitted to data from this experiment and from Caltech (refs. 6 and 7). The solid curves are fits to the indicated points by the function $P' = A + B \cos \theta + C \cos^2 \theta + D \cos^3 \theta$ using the coefficients of Table II.

TABLE I. Recoil proton polarization in direction $\vec{P}_n \times \vec{q}$ ^{20.}

Photon Energy ^a (MeV)	This Expt.		Caltech ^b		Caltech ^c		$P=a+b(\theta-62^\circ)$ ^d	
	62.6°	66.5°	57°	62°	60.7°	65.3°	a	b
950			0.17 (±.21)	-.15 (±.18)	0.66 (±.33)	-.08 (±.15)	0.040 (±.096)	-.043 (±.031)
1050	0.42 (±.28)	-.21 (±.22)	0.26 (±.14)	-.32 (±.13)	0.05 (±.12)	0.03 (±.10)	0.018 (±.057)	-.029 (±.019)
1150	-.08 (±.23)	-.56 (±.21)	0.04 (±.15)	-.14 (±.15)	0.42 (±.10)	-.04 (±.13)	0.067 (±.059)	-.055 (±.021)
1250	0.51 (±.22)	-.01 (±.21)	0.58 (±.17)	0.01 (±.18)	0.29 (±.18)	0.32 (±.33)	0.264 (±.083)	-.052 (±.027)
1350	0.22 (±.25)	-.40 (±.29)	0.70 (±.24)	0.08 (±.27)			0.15 (±.13)	-.113 (±.039)
1450	0.24 (±.31)	-.96 (±.41)	0.76 (±.43)				0.08 (±.22)	-.189 (±.066)
1550	-.03 (±.42)	-.67 (±.54)					-.01 (±.43)	-.16 (±.17)

^aGeometrical center of 100 MeV bin.

^bFrom Bloom et al (Ref. 6).

^cFrom Cheng (Ref. 7).

^dStraight-line fits based on mean pion production angle for each datum.

TABLE II. Expansion coefficients for the reduced cross section
 (Eq. 1) in the form $P = A + B \cos \theta + C \cos^2 \theta + D \cos^3 \theta$,
 where θ is the pion production angle in the center of mass.

E (MeV)	A ($\mu\text{b/ster}$)	B ($\mu\text{b/ster}$)	C ($\mu\text{b/ster}$)	D ($\mu\text{b/ster}$)
950	$-.397 \pm .063$	$-.03 \pm .44$	$0.42 \pm .53$	2.4 ± 2.0
1050	$-.629 \pm .077$	$-1.36 \pm .57$	$1.67 \pm .66$	9.2 ± 2.8
1150	$-.361 \pm .053$	$-1.86 \pm .39$	$0.72 \pm .46$	11.8 ± 1.9
1250	$-.269 \pm .038$	$-1.42 \pm .27$	$2.25 \pm .34$	6.6 ± 1.3

Figure 1

Figure 2

Figure 3

Figure 4