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DEVELOPMENT OF HIGH-TEMPERATURE STRUCTURAL DESIGN METHODS
FOR LIQUID-METAL FAST-BREEDER REACTOR SYSTEM COMPONENTS*

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Abstract

A brief description of liquid-metal fast-breeder reactor systems will be given along with some attendant structural design problems associated with inelastic material behavior. Central features of the ORNL program to develop applicable structural design methods will be outlined, including considerations of material deformation and failure. Activities to develop constitutive equations applicable to elastic-plastic and creep behavior will be discussed and currently recommended methods described. Some basic features of inelastic behavior of pertinent materials (particularly type 304 stainless steel) will be illustrated, along with the role they play in the development of constitutive equations. A number of elevated temperature structural tests will be described, and selected comparisons of test results with analysis predictions will be presented.

* Research sponsored by the U.S. Atomic Energy Commission under contract with the Union Carbide Corporation.

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|--|----------|
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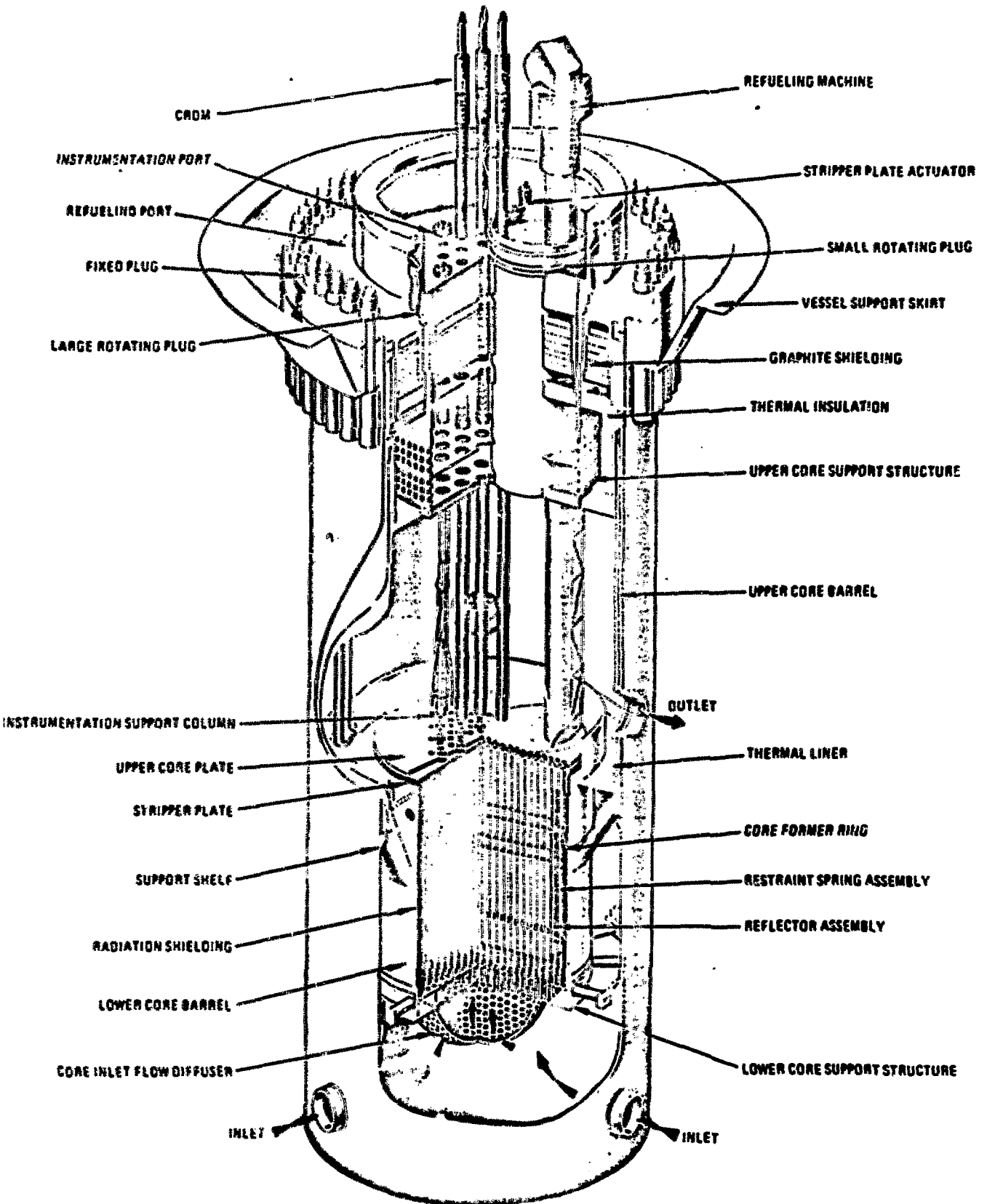
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- | | |
|----------------------------------|----------------------|
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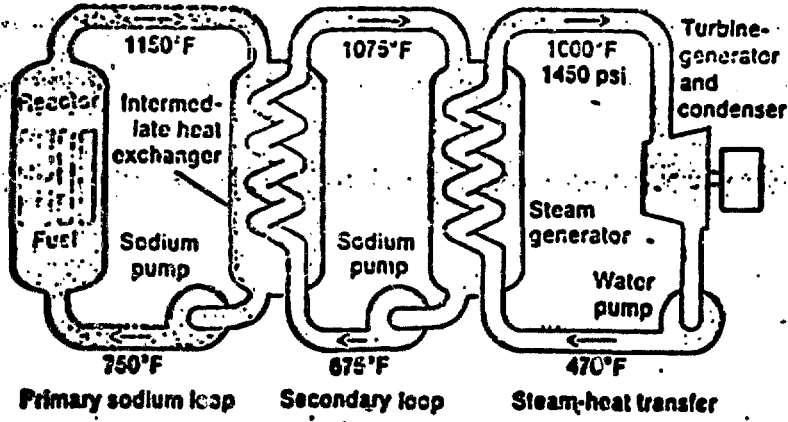
G. Conclusions: Constitutive equations currently in use are based on small deformation theory and the postulate that the total strain tensor can be decomposed into time-independent components and time-dependent components. On the basis of available data, these equations are capable of representing essential features of inelastic behaviors to be expected under service conditions. However, in-depth studies are needed of the inelastic behavior of materials under general nonradial loading programs, including possible creep-plasticity interactions. An integral tie must exist between experimentation and theory development.

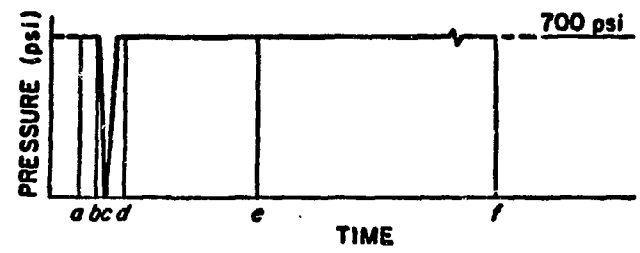
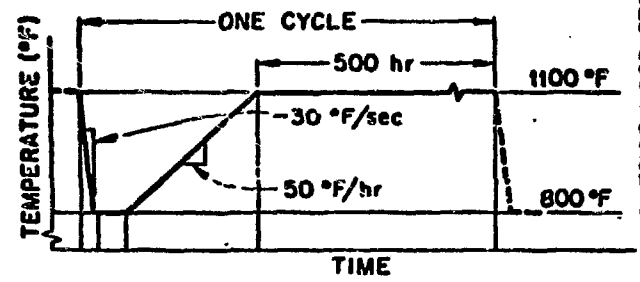
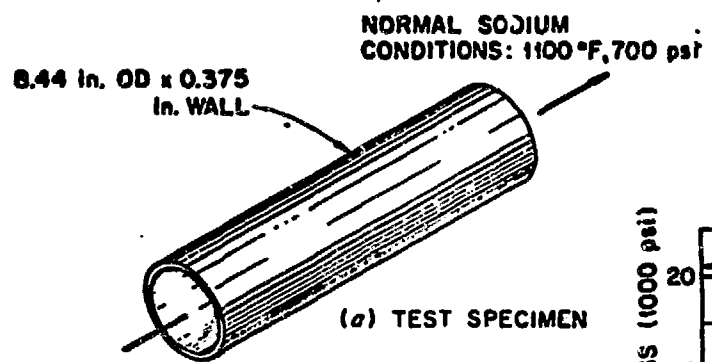


**REACTOR (UNDER-THE-PLUG REFUELING)
WESTINGHOUSE I.MFBR DEMONSTRATION PLANT**

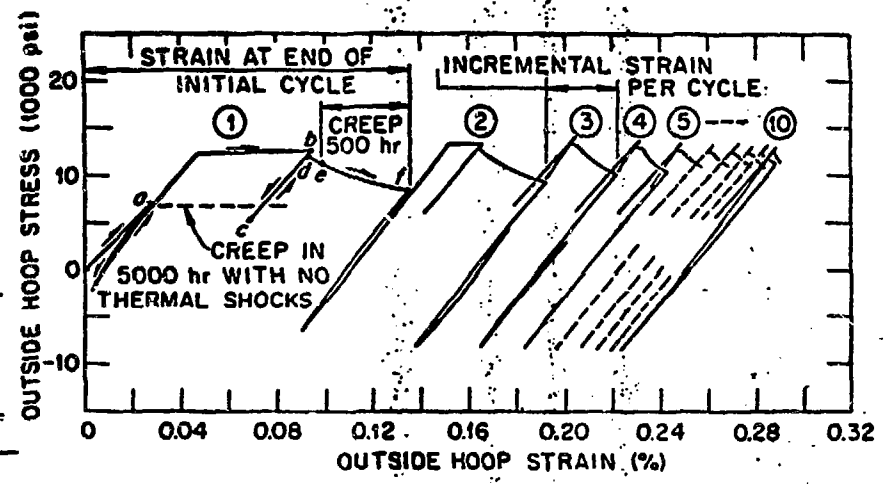
M+C
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THE LIQUID-METAL-COOLED FAST-BREEDER REACTOR



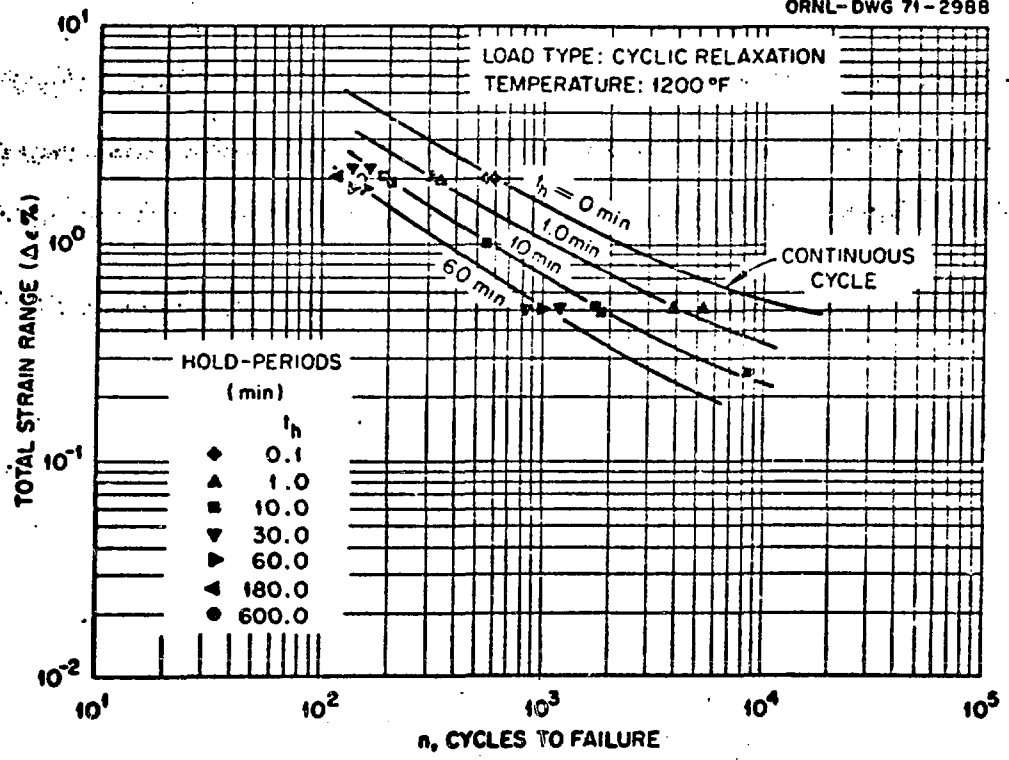


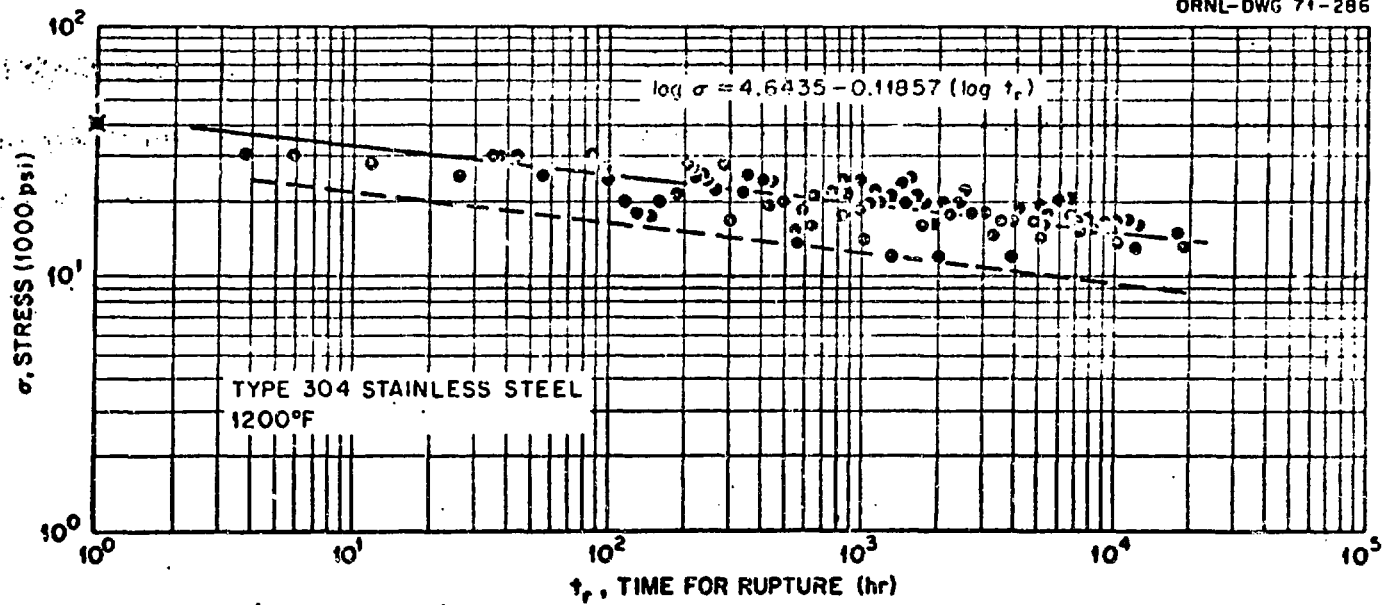
(b) TEMPERATURE-PRESSURE HISTOGRAMS

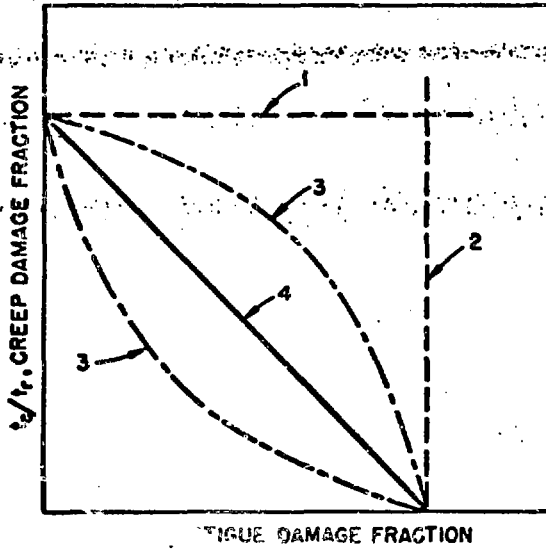


(c) PREDICTED RATCHETTING BEHAVIOR

Pipe Thermal Ratchetting Tests



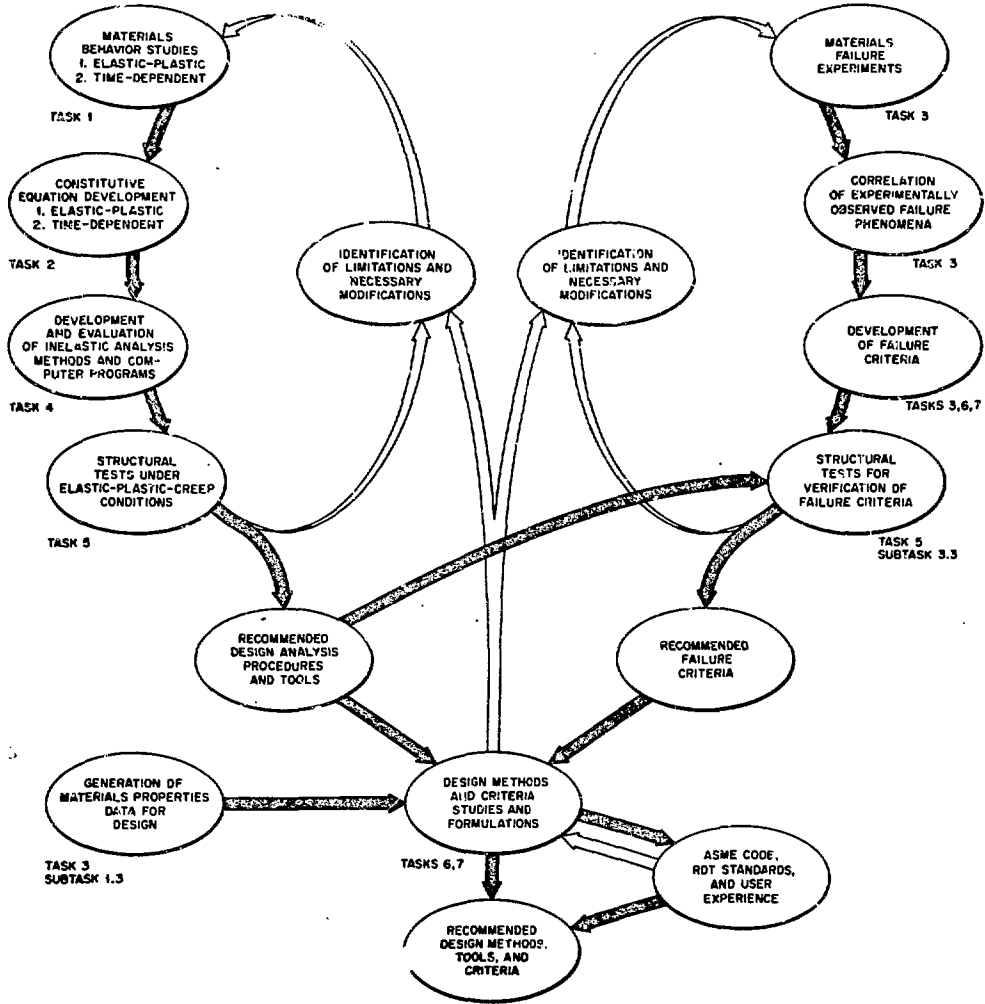


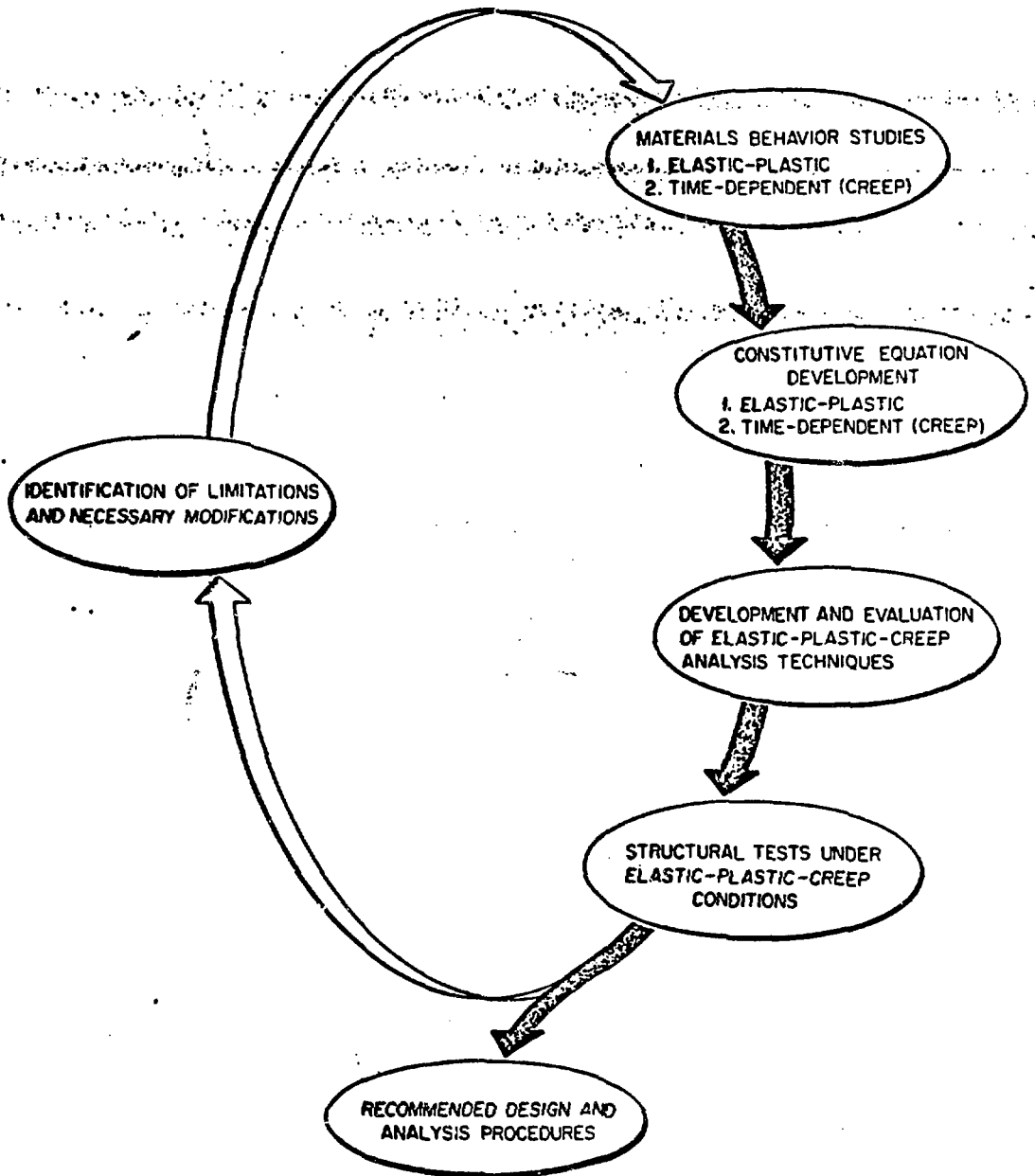


ONLY, $\alpha=0$
ONLY, $\beta=0$
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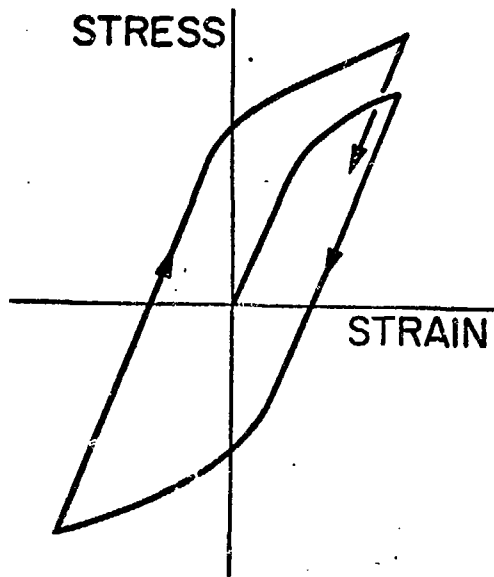
DEVELOPMENT AND EVALUATION OF ANALYSIS METHODS FOR PREDICTING INELASTIC STRUCTURAL BEHAVIOR

DEVELOPMENT AND EVALUATION OF FAILURE CRITERIA FOR MATERIALS





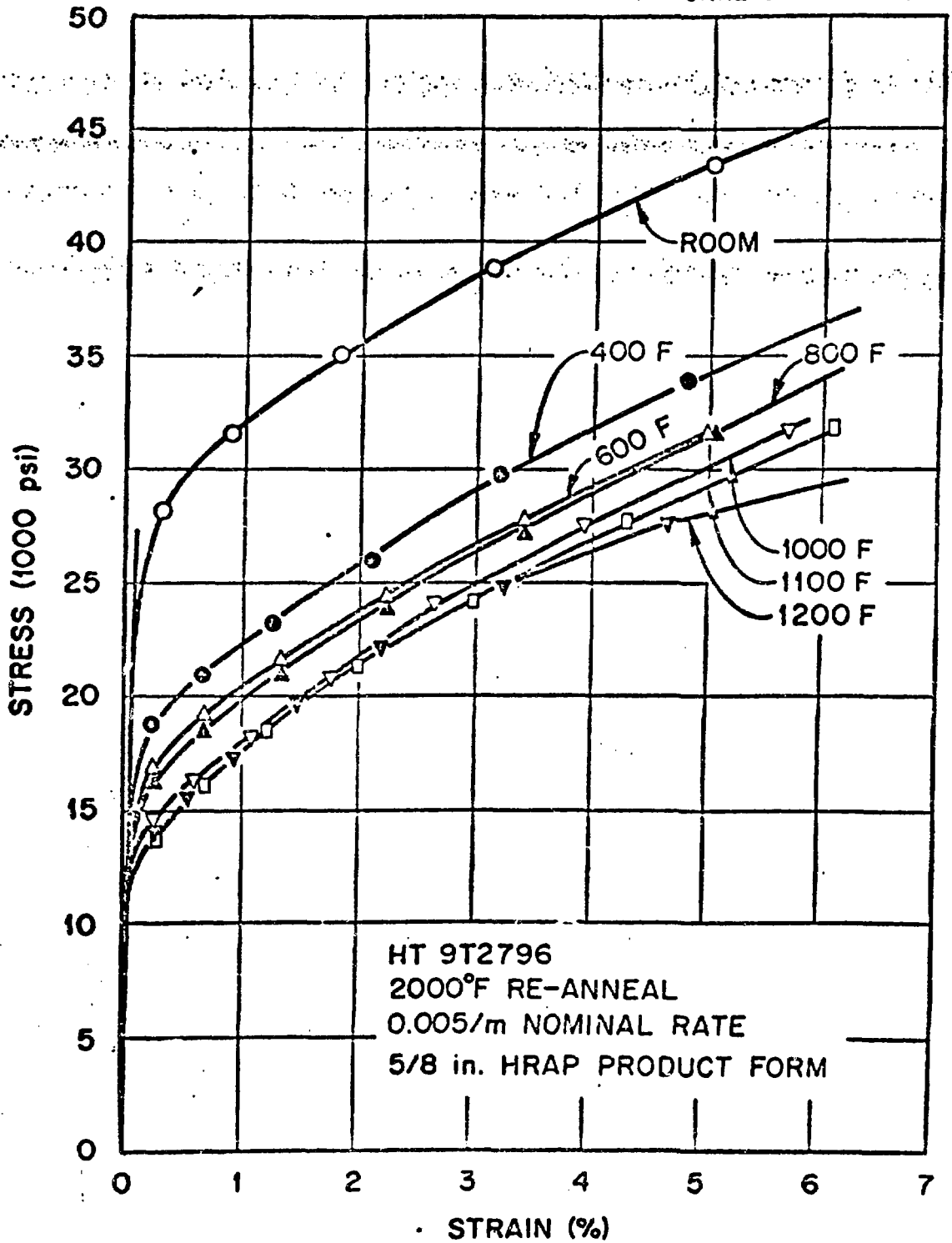
Coordinated Effort to Develop and Evaluate Analytical Methods.



TO DESCRIBE TIME-INDEPENDENT
ELASTIC-PLASTIC BEHAVIOR REQUIRES:

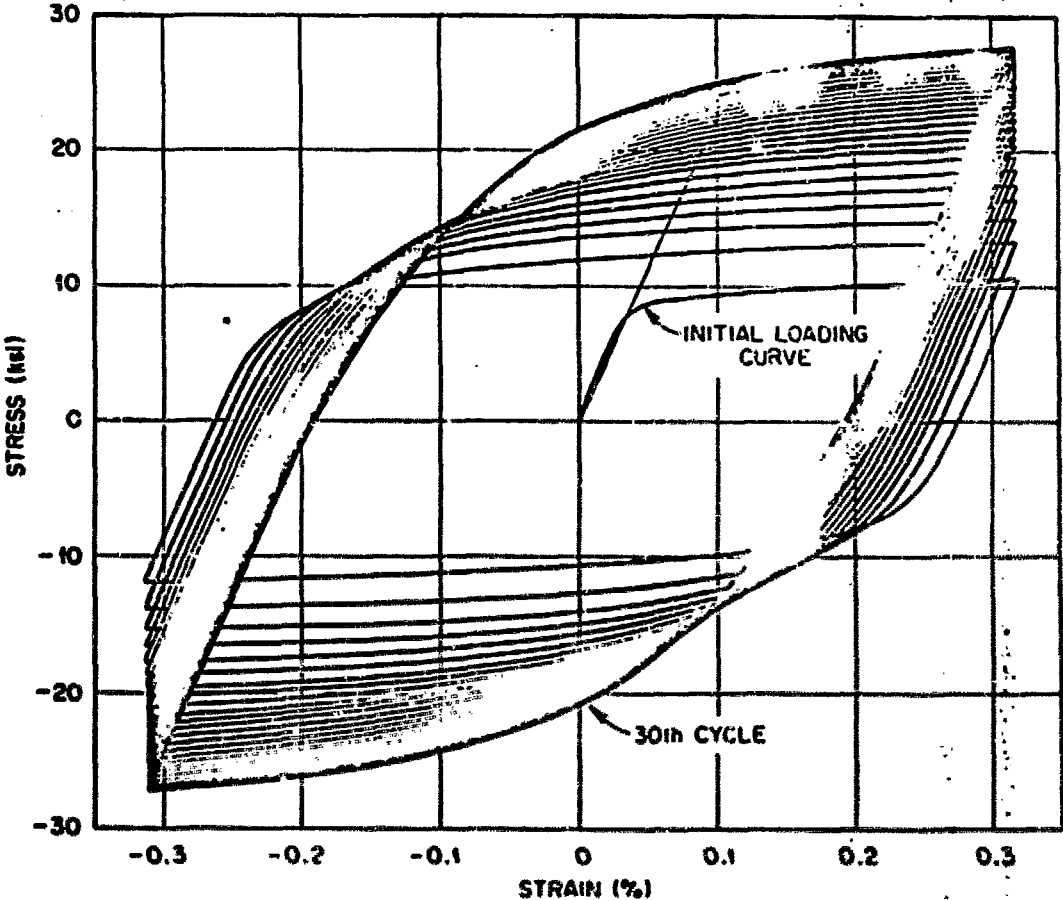
1. YIELD CRITERIA
2. FLOW RULE
3. HARDENING LAW

UNIAXIAL CYCLIC STRESS-
STRAIN CURVE FOR A WORK
HARDENING MATERIAL



TYPE 304 STAINLESS STEEL, ANNEALED
(HEAT 9T2796)

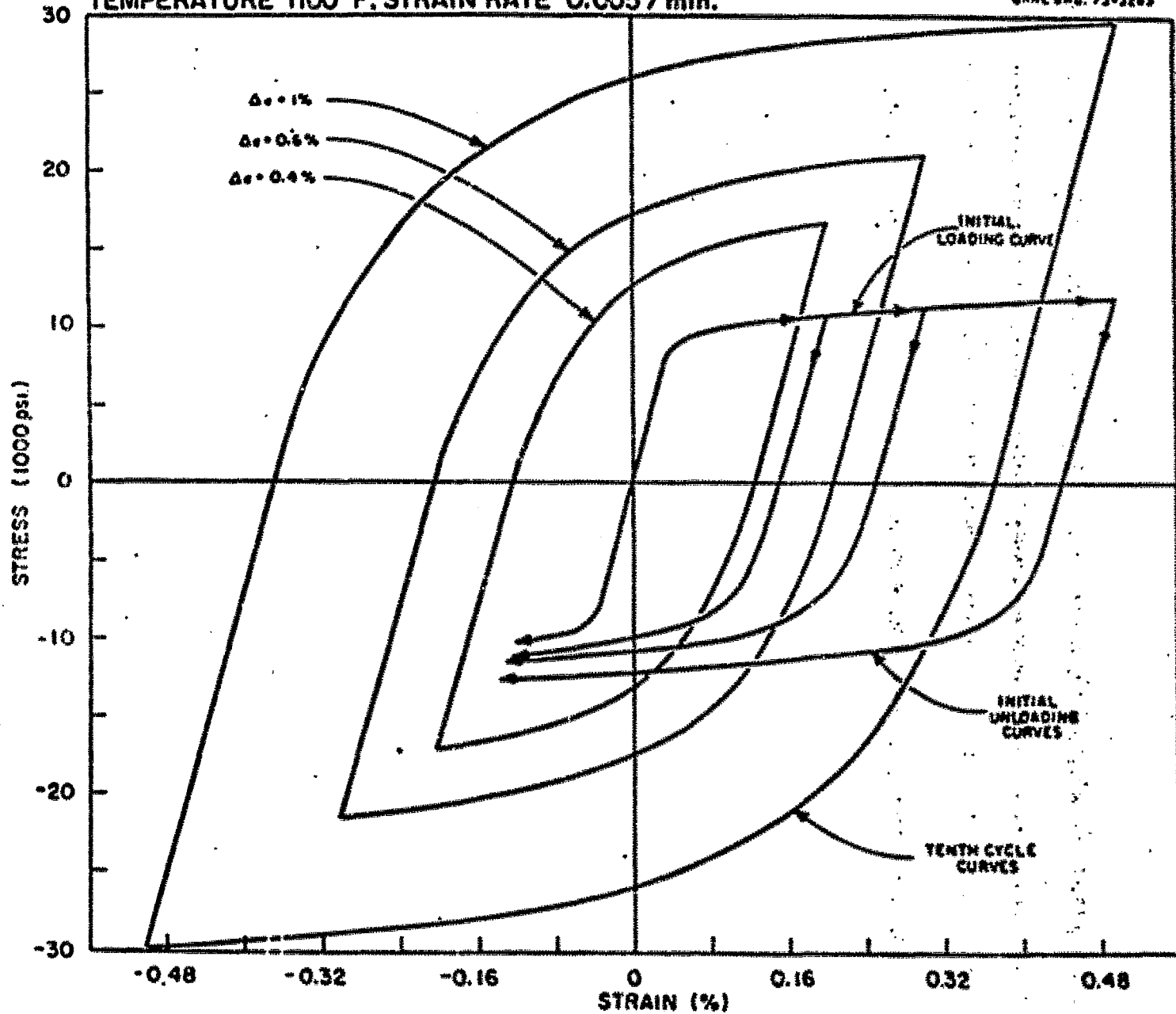
TEMPERATURE: 1100°F
STRAIN RATE: 0.005/min



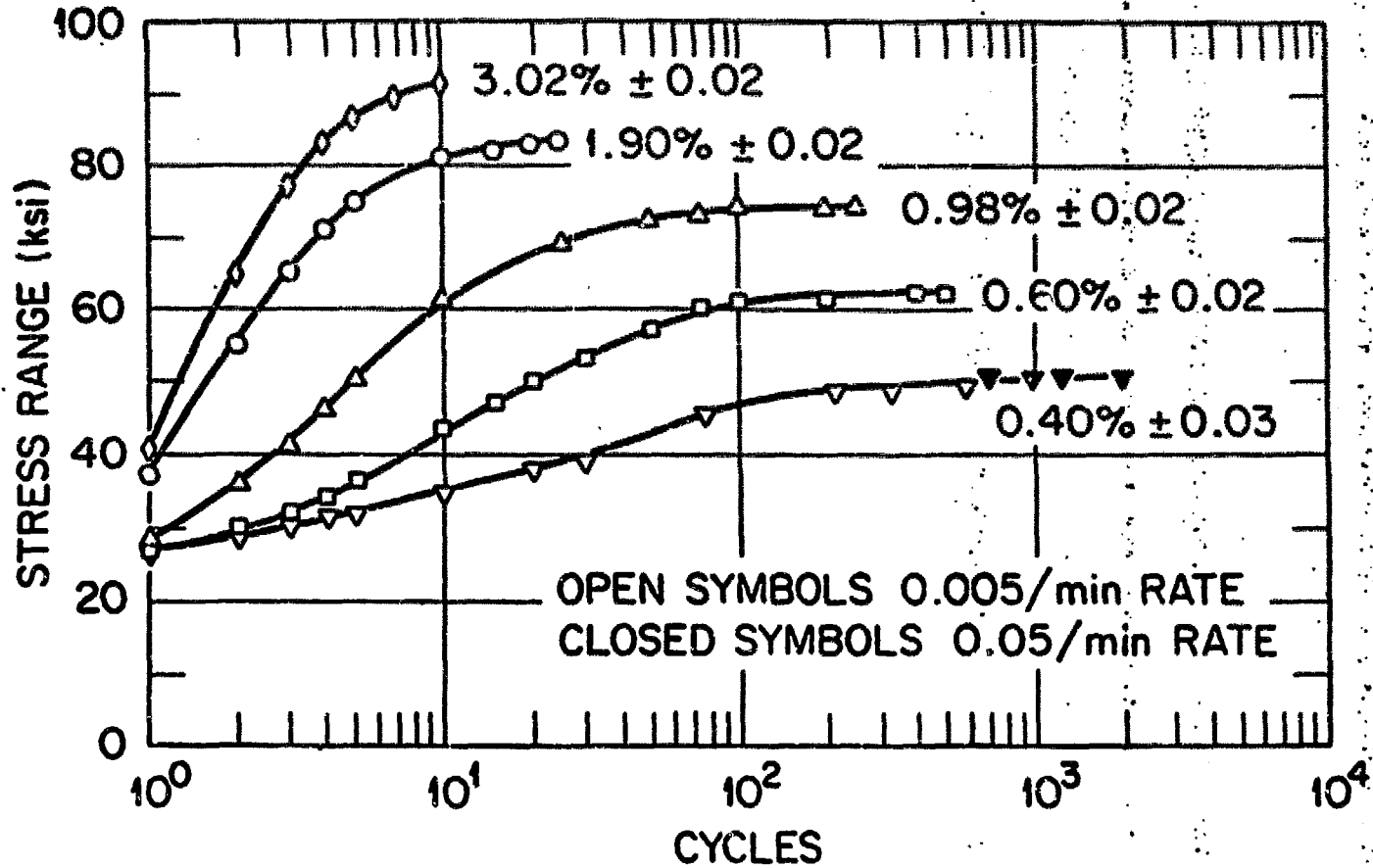
TYPE 304 STAINLESS STEEL, ANNEALED
(HEAT 9T2796)

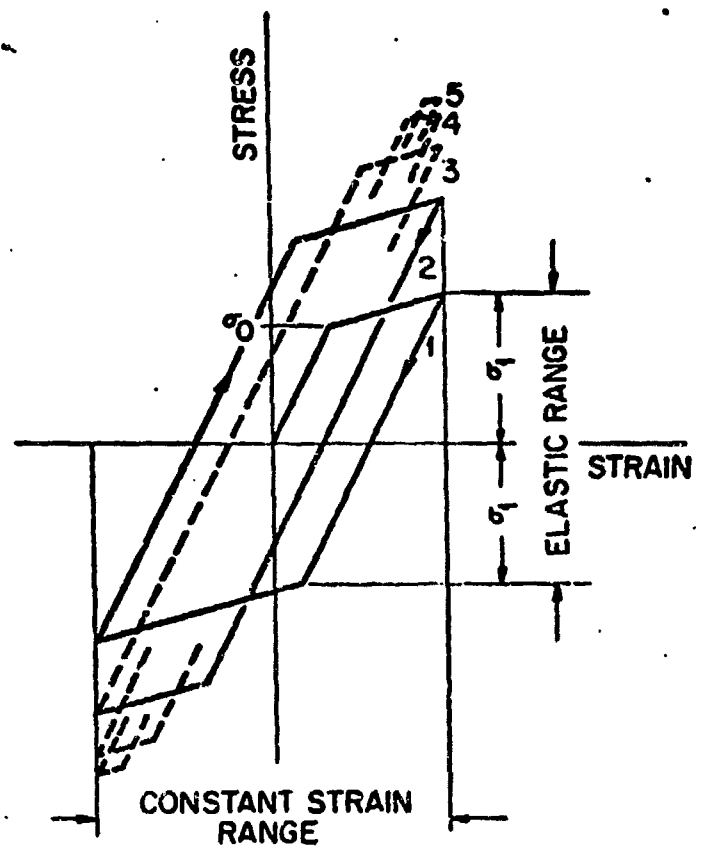
TEMPERATURE 1100°F. STRAIN RATE 0.005 / min.

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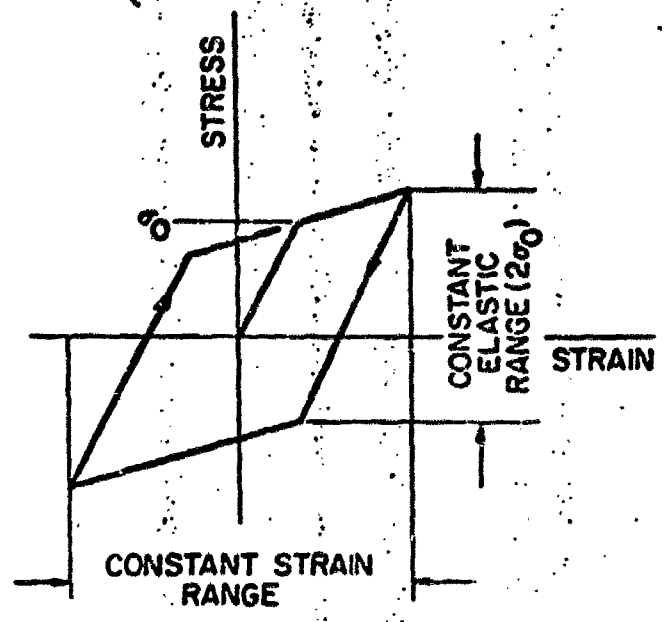


TYPE 304 STAINLESS STEEL
ANNEALED 1/2 hr AT 2000°F
(HEAT 9T2796)
TEMPERATURE: 1100°F



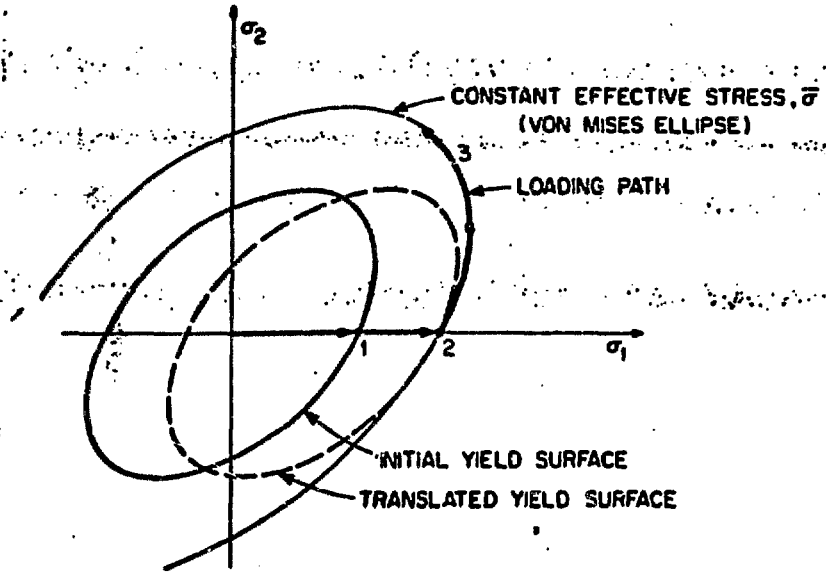


ISOTROPIC HARDENING

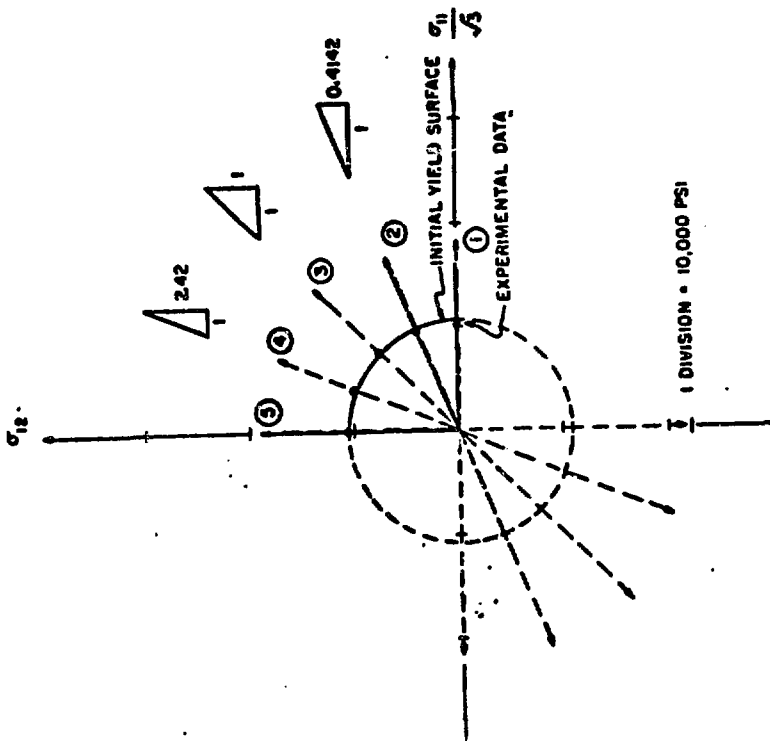
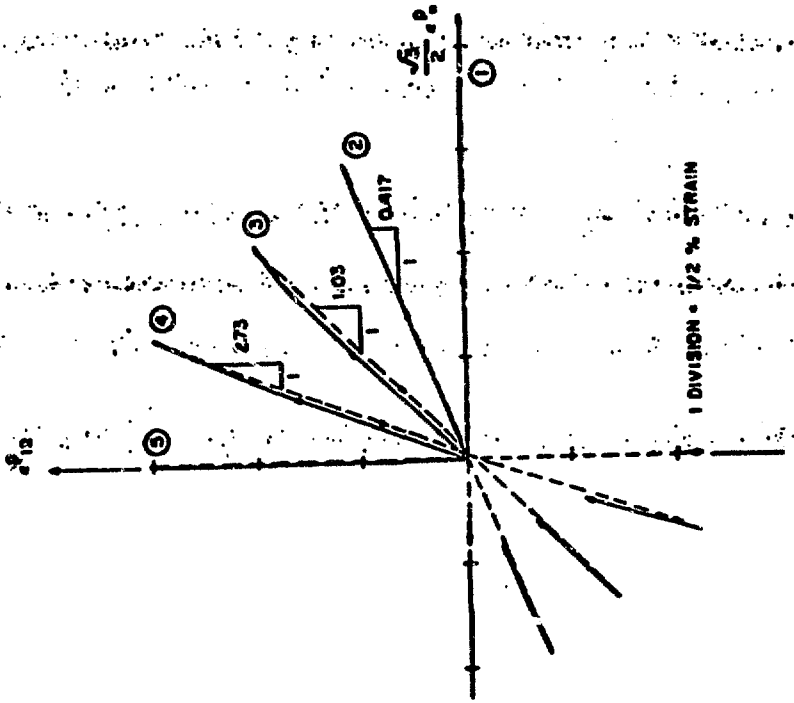


KINEMATIC HARDENING

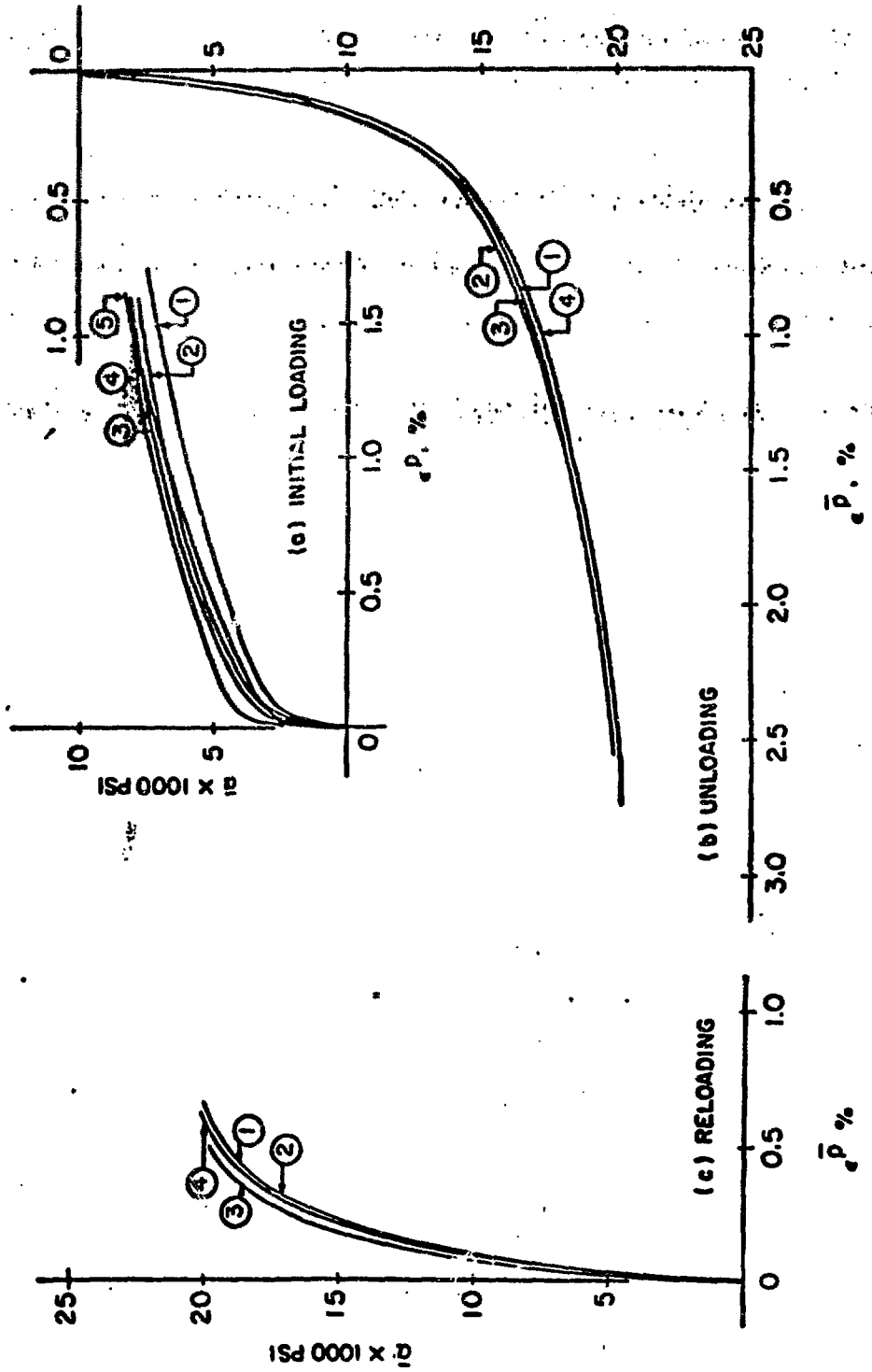
Uniaxial Elastic-Plastic Stress-Strain Behavior Predicted by Hardening Laws (Bilinear Representation Used for Simplicity).

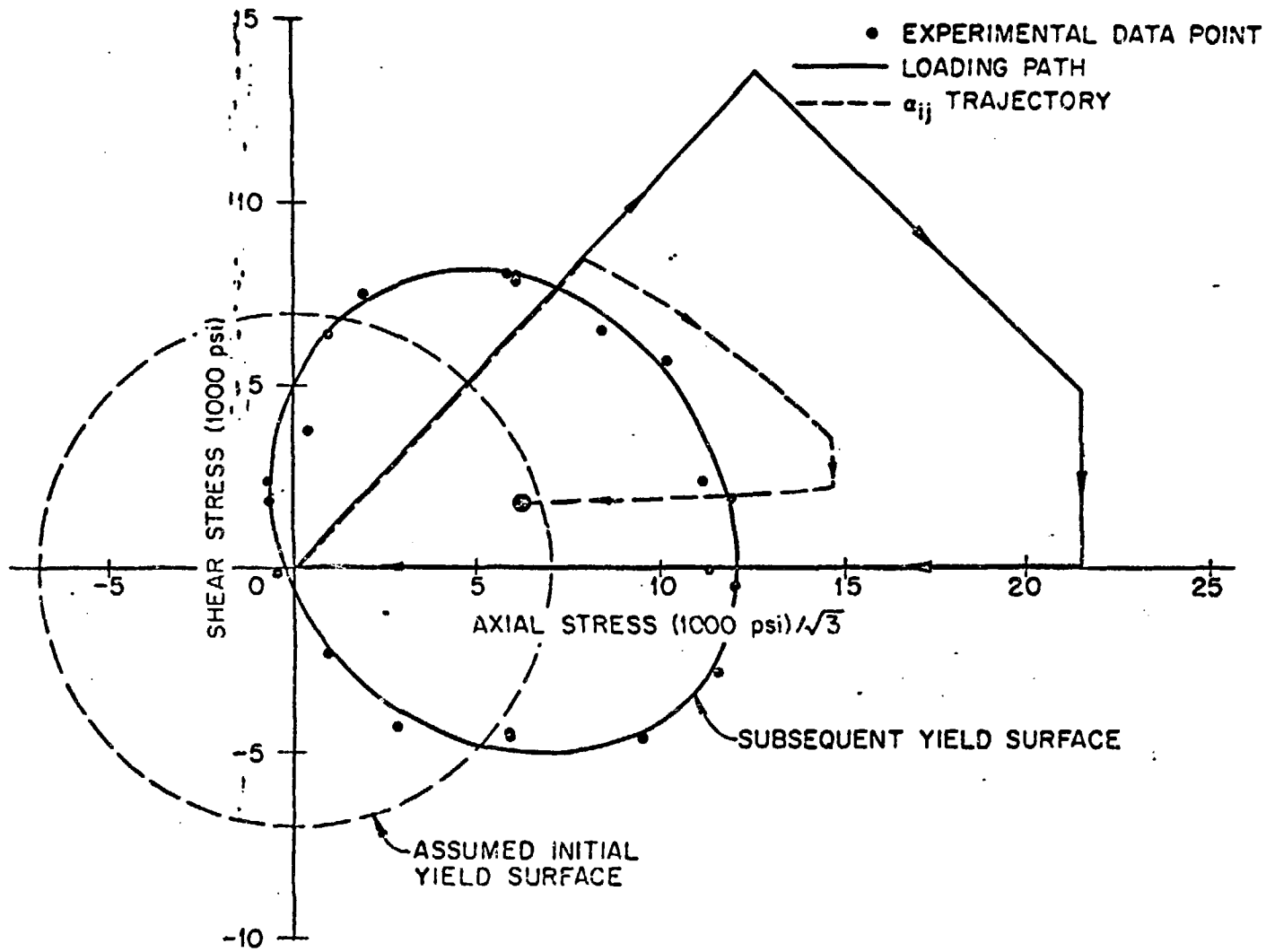


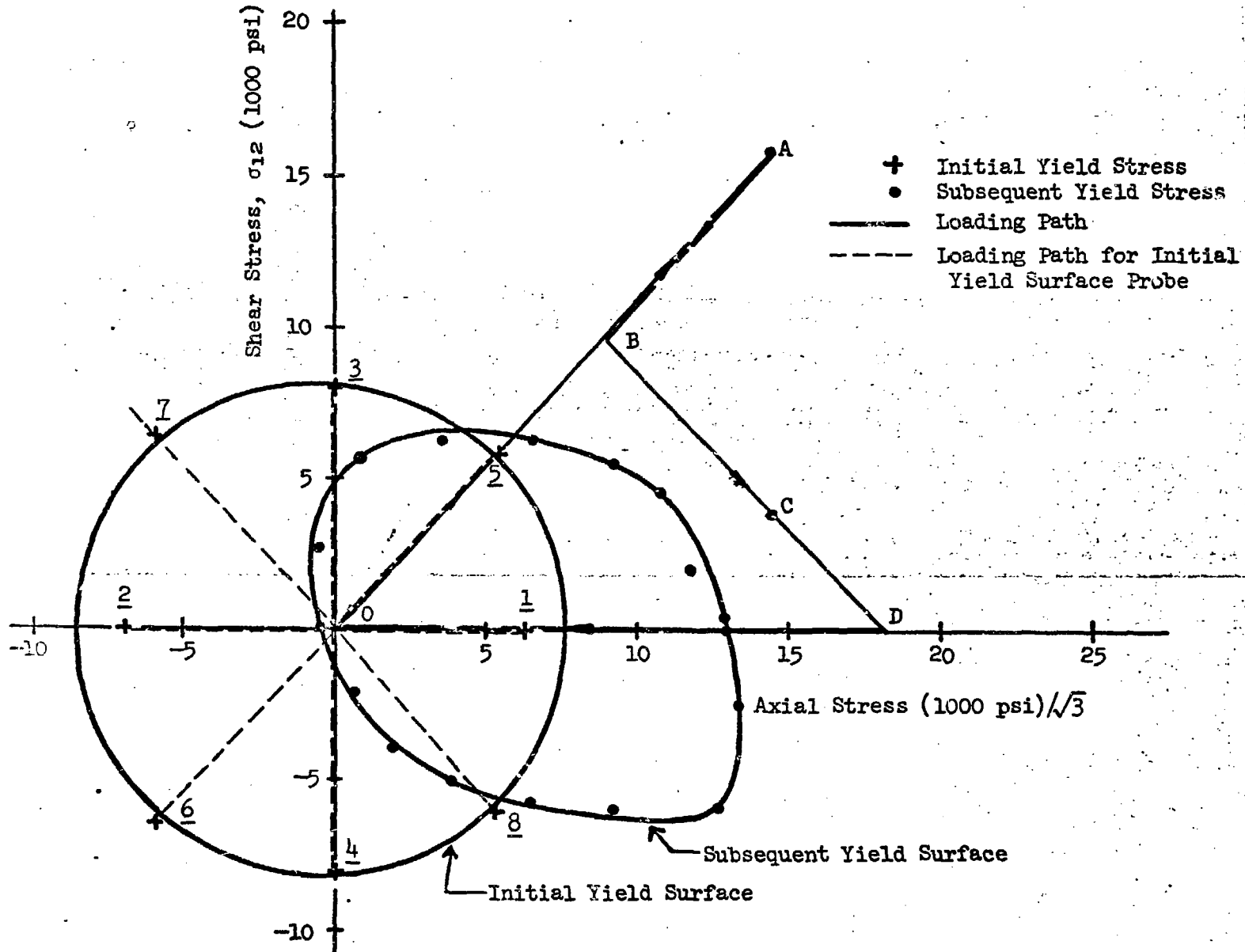
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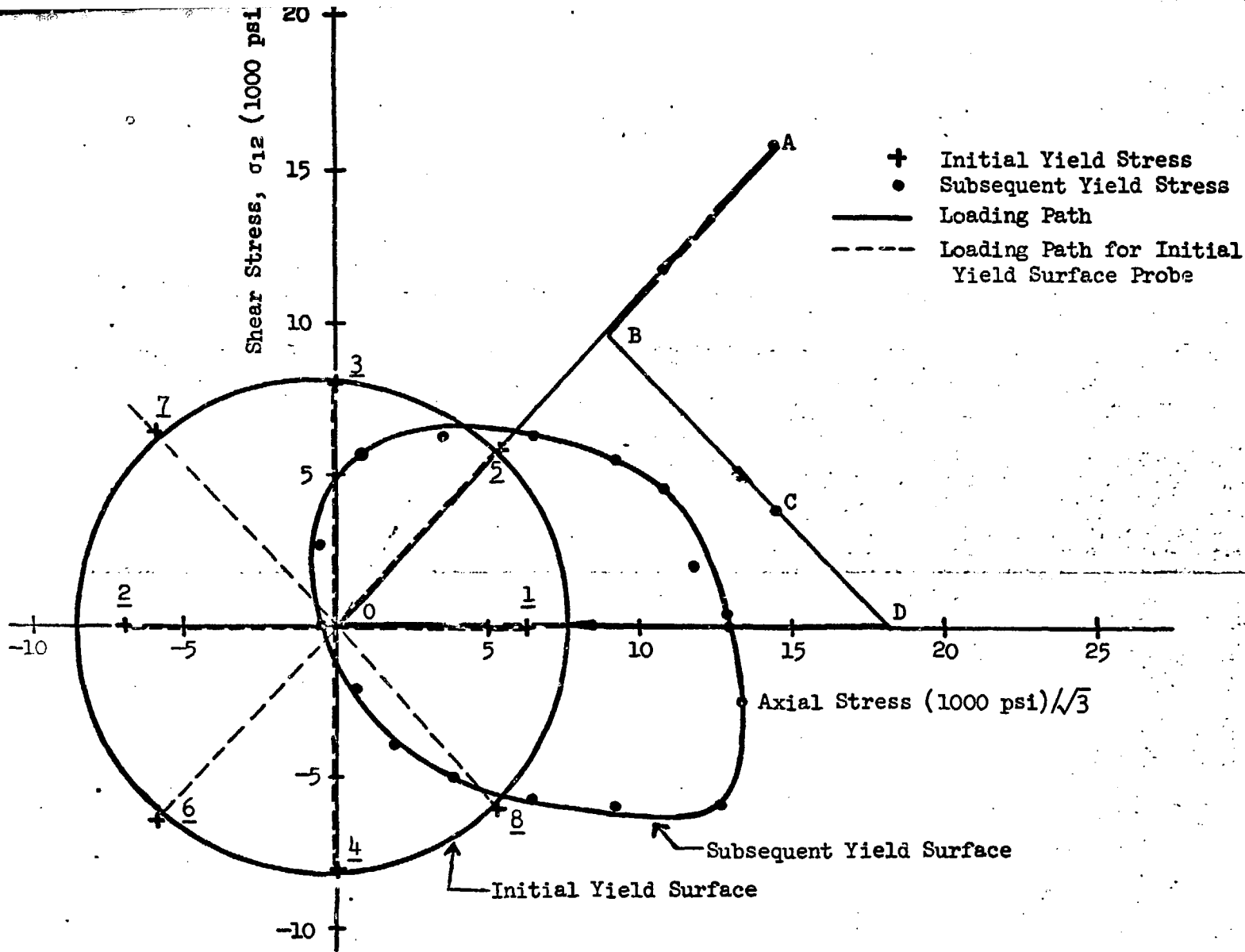


1 DIVISION = 10,000 PSI







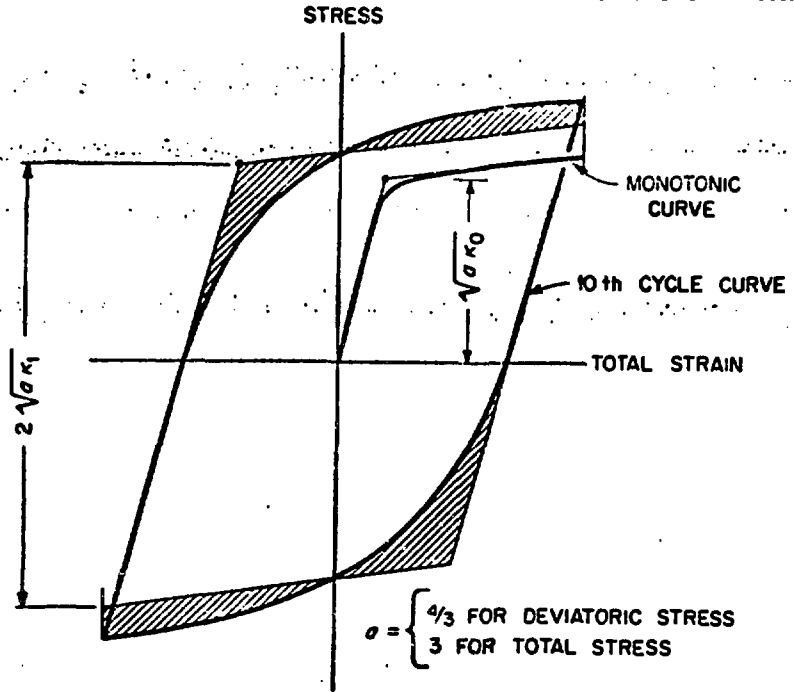


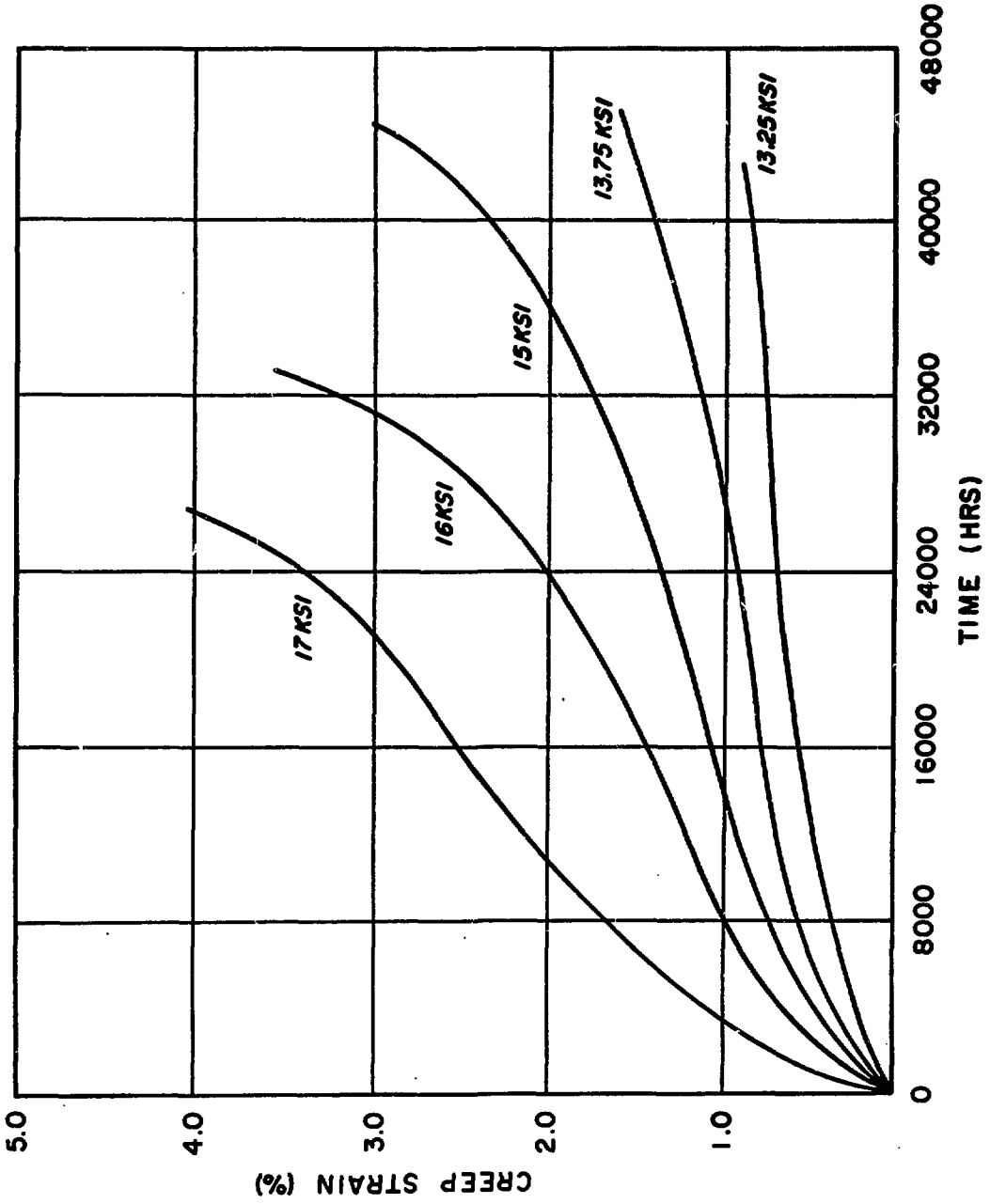
red to 8" - 74% of way

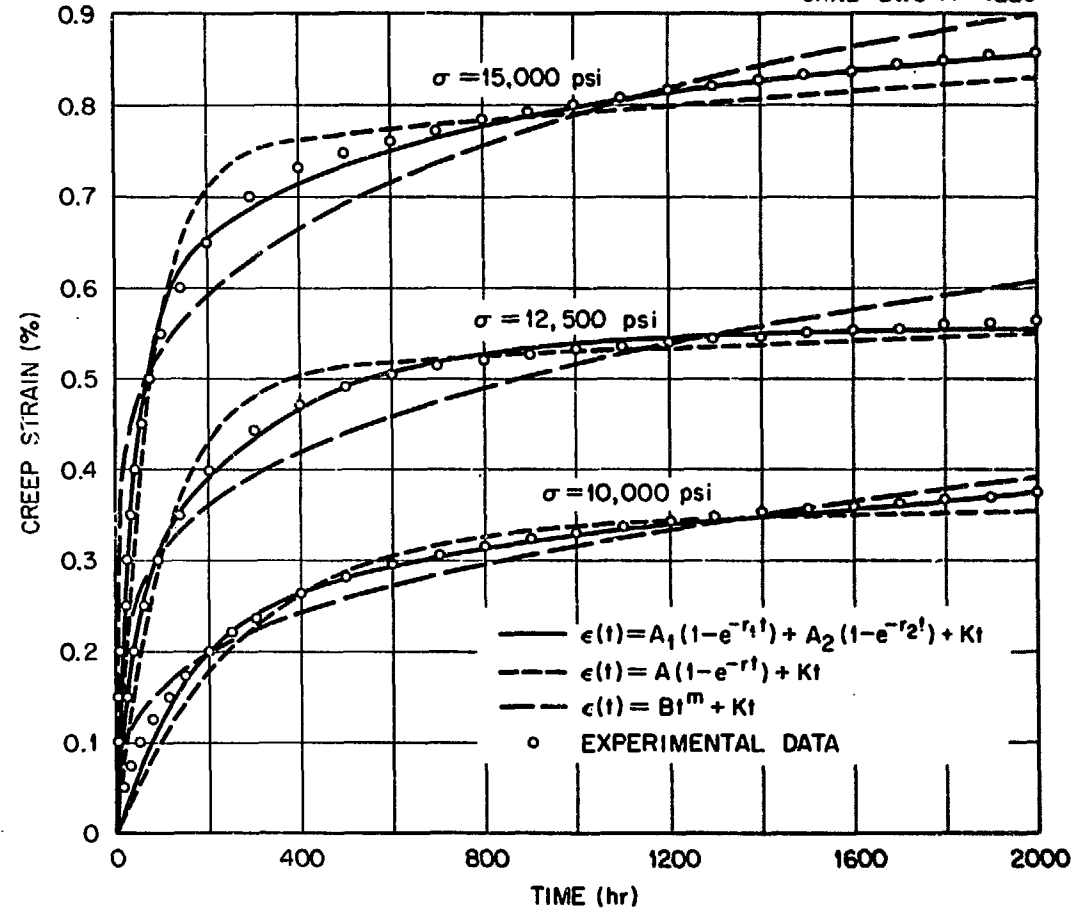
Inelastic Analysis Guidelines

Time-Independent Elastic-Plastic Behavior

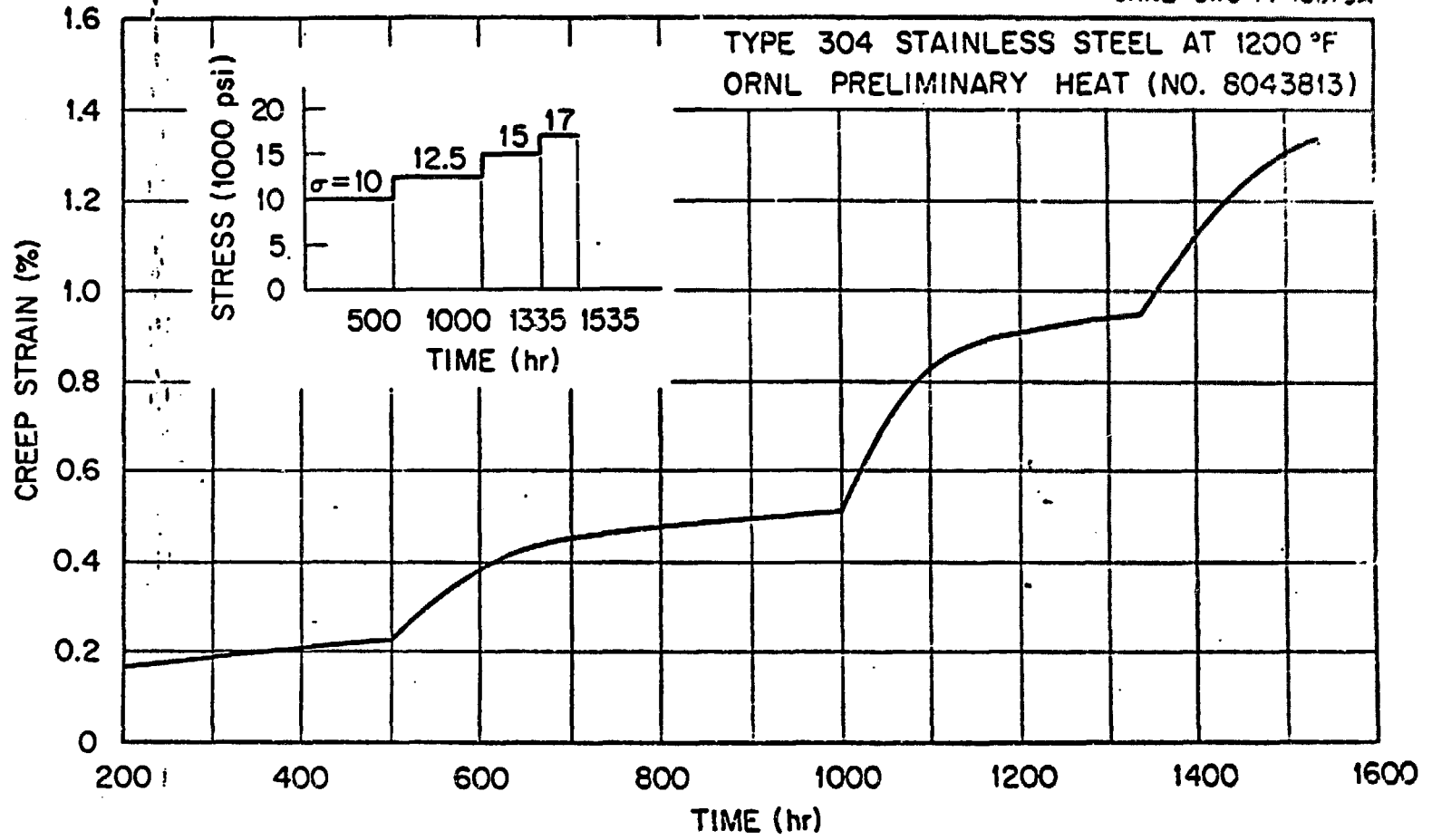
1. Yield Criterion: Von Mises or Tresca,
 $f(\sigma, \epsilon^P, H) = \kappa(T)$
2. Flow Rule: Von Mises Associated
Flow Law,
$$d\epsilon^P \sim \frac{\partial f}{\partial \sigma}$$
3. Hardening Rule: Nonisothermal Kinematic
Hardening
4. Stress-Strain Relation: Bilinear Relation
Required for Nonradial Loadings, with
Specific Rules Provided for Determining
the Equivalent Bilinear Curves from Actual
Uniaxial Stress-Strain Curves
Nonlinear Relation Acceptable for Radial
Loadings
5. Effects of Hardening Due to Cycling and to
Prior Creep Approximately Accounted for
by Changing from Initial Stress-Strain Curve
to Cyclic Stress-Strain Curve

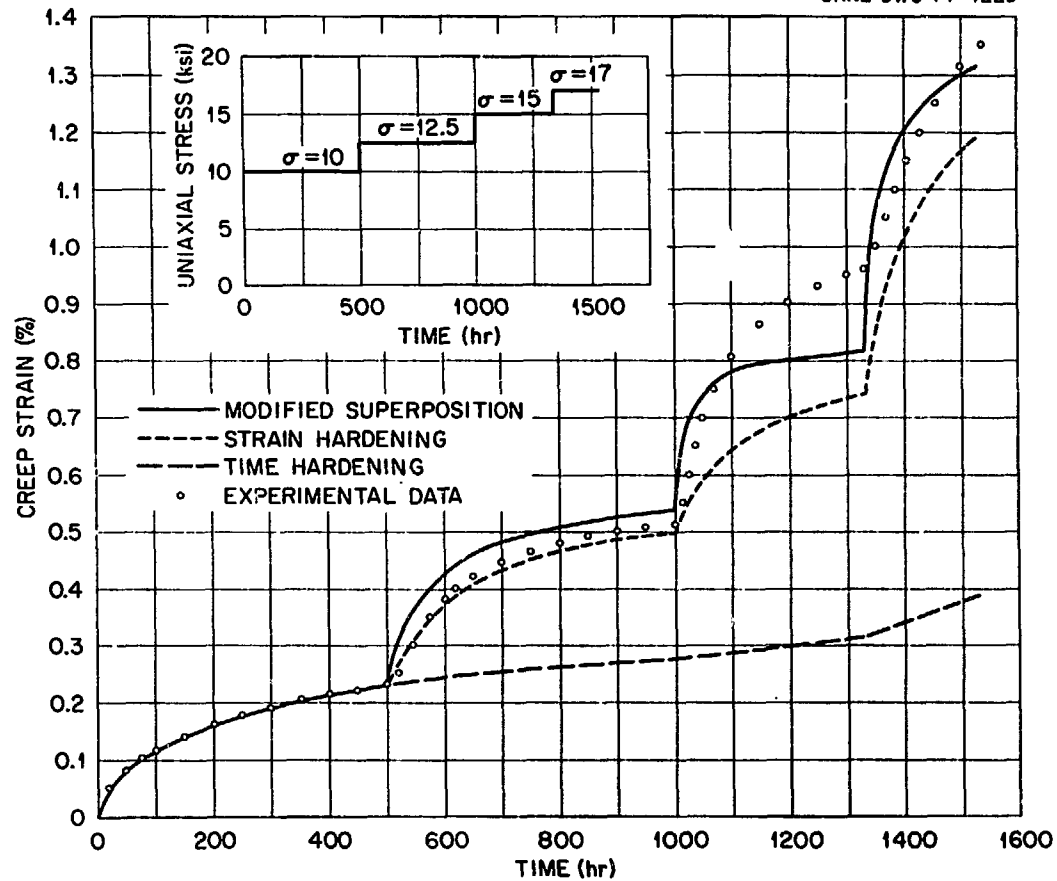




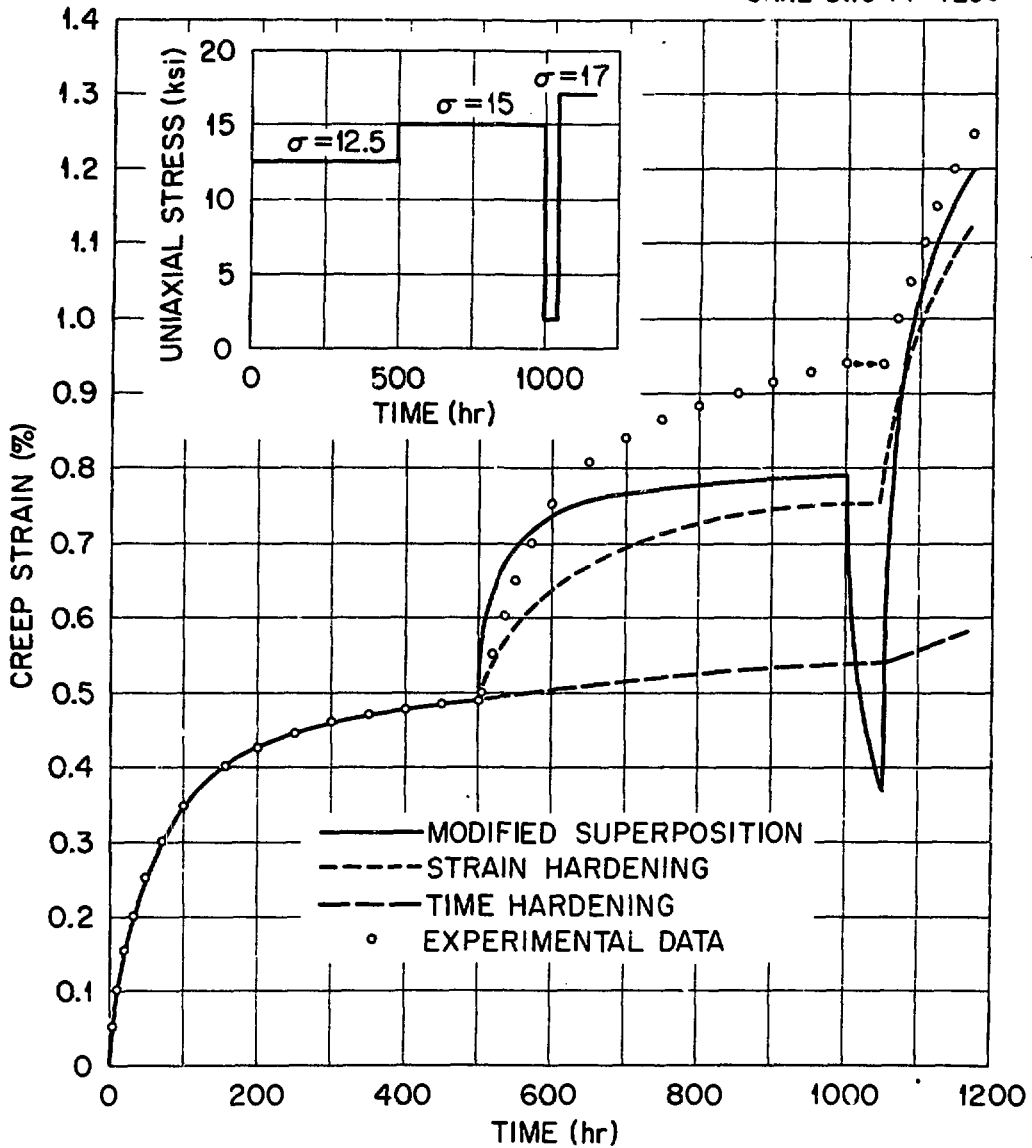


Least Squares Fit to Constant-Load Creep Curves for 304 Stainless Steel (Heat 8043813) at 1200°F.





Comparisons of Experimental Creep Response to Stepwise Varying Uniaxial Load with Predictions From Various Constitutive Formulations. 304 Stainless Steel (Heat 8043813); Temperature = 1200°F.



Comparisons of Experimental Creep Response to Stepwise Varying Uniaxial Load with Predictions From Various Constitutive Formulations. 304 Stainless Steel (Heat 8043813); Temperature = 1200°F.

ORNL DWG. 72-12771

**INGREDIENTS OF EQUATION-OF-STATE
CREEP REPRESENTATIONS**

1. Uniaxial Creep Relation
2. Multiaxial Flow Rule
3. Hardening Law for Variable Load Conditions

TIME-DEPENDENT (CREEP) BEHAVIOR

1. Constant-uniaxial-stress creep equation:

$$\epsilon^c(\sigma, T, t) = \epsilon_t(\sigma, T) \left[1 - e^{-r(\sigma, T)t} \right] + \dot{\epsilon}_m(\sigma, T)t.$$

2. Multiaxial constitutive equations:

$$\dot{\epsilon}_{ij}^c = \lambda \sigma'_{ij}.$$

Define

$$\bar{\sigma}^2 = 3J_2' = \frac{3}{2} \sigma'_{ij} \sigma'_{ij},$$

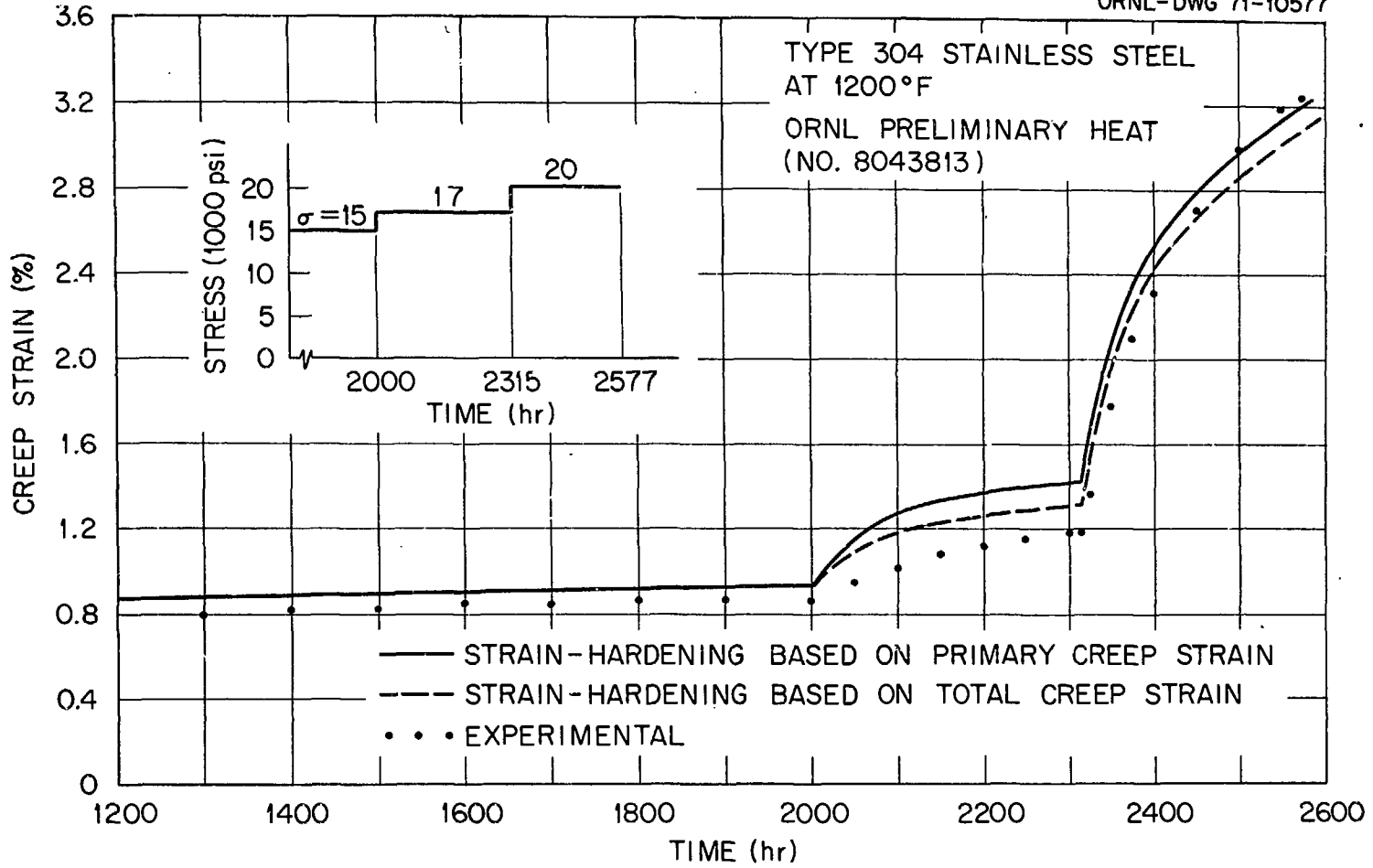
$$\bar{\epsilon}^2 = \frac{4}{3} I_2 = \frac{2}{3} \epsilon_{ij}^c \epsilon_{ij}^c.$$

Write:

$$\dot{\epsilon}_{ij}^c = \frac{3}{2} \frac{\dot{\bar{\epsilon}}(\bar{\sigma}, t, T)}{\bar{\sigma}} \sigma'_{ij}.$$

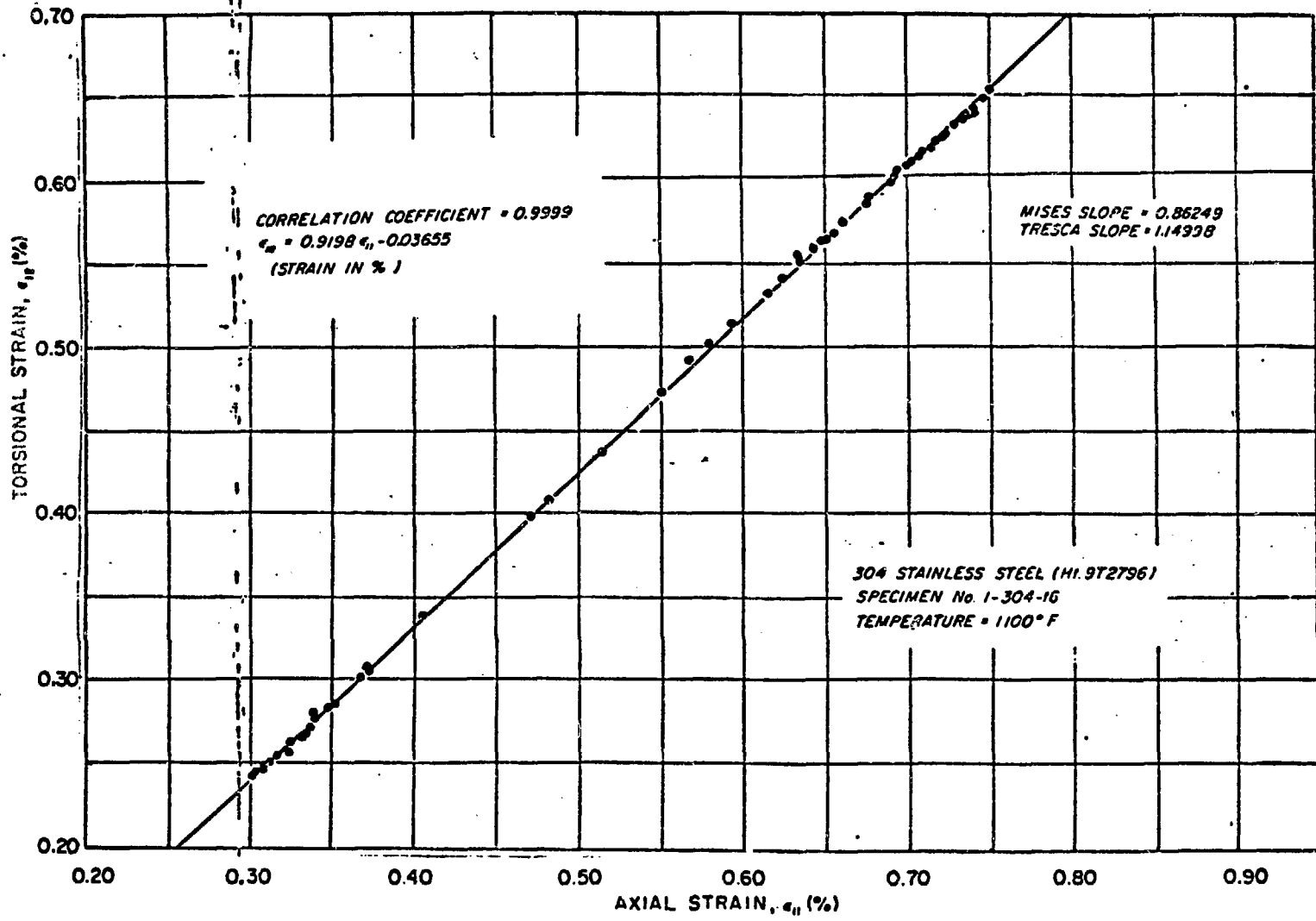
3. For strain-hardening law:

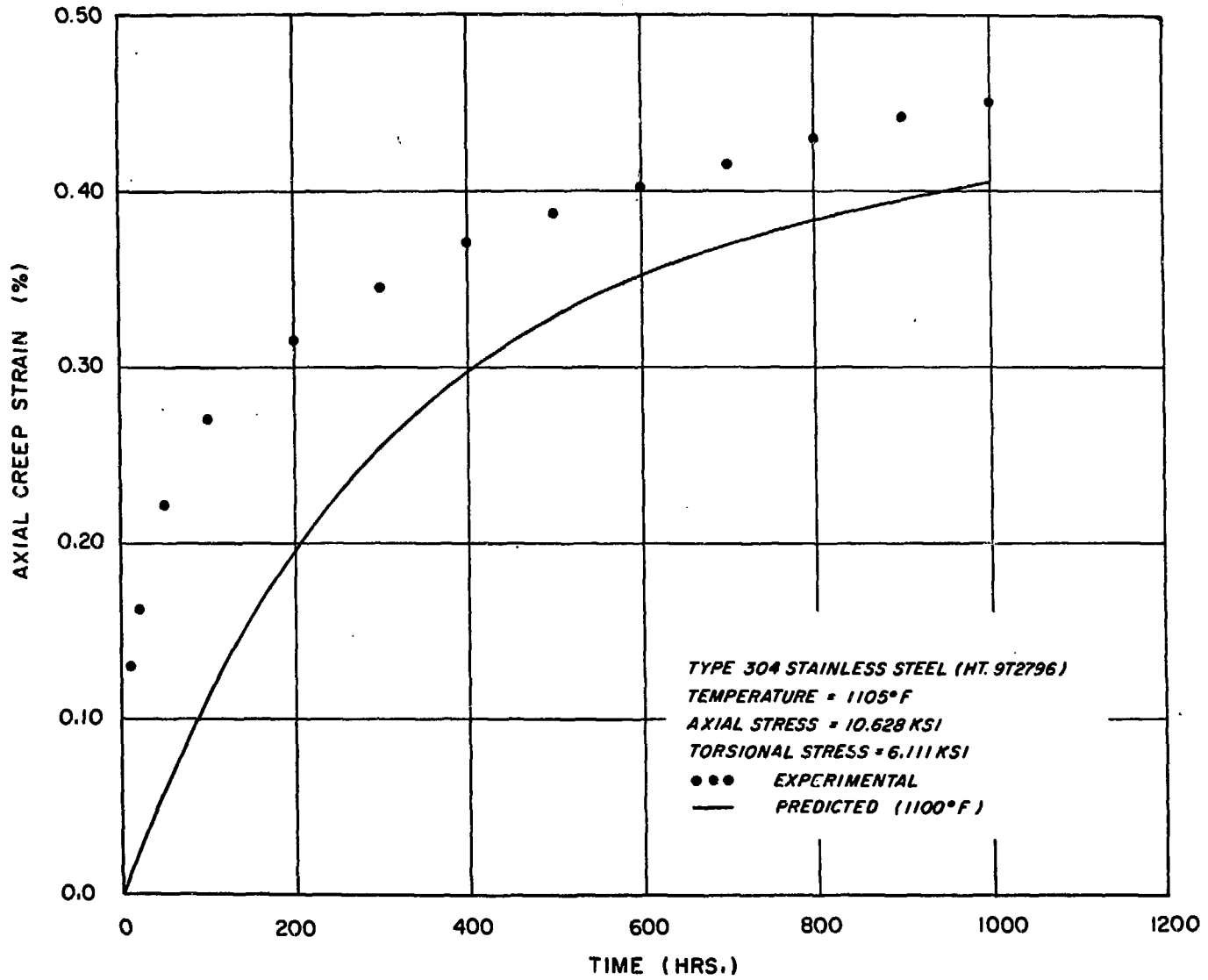
$$\dot{\epsilon}_{ij}^c = \frac{3}{2} \frac{\dot{\bar{\epsilon}}(\bar{\sigma}, \bar{\epsilon}, T)}{\bar{\sigma}} \sigma'_{ij}.$$

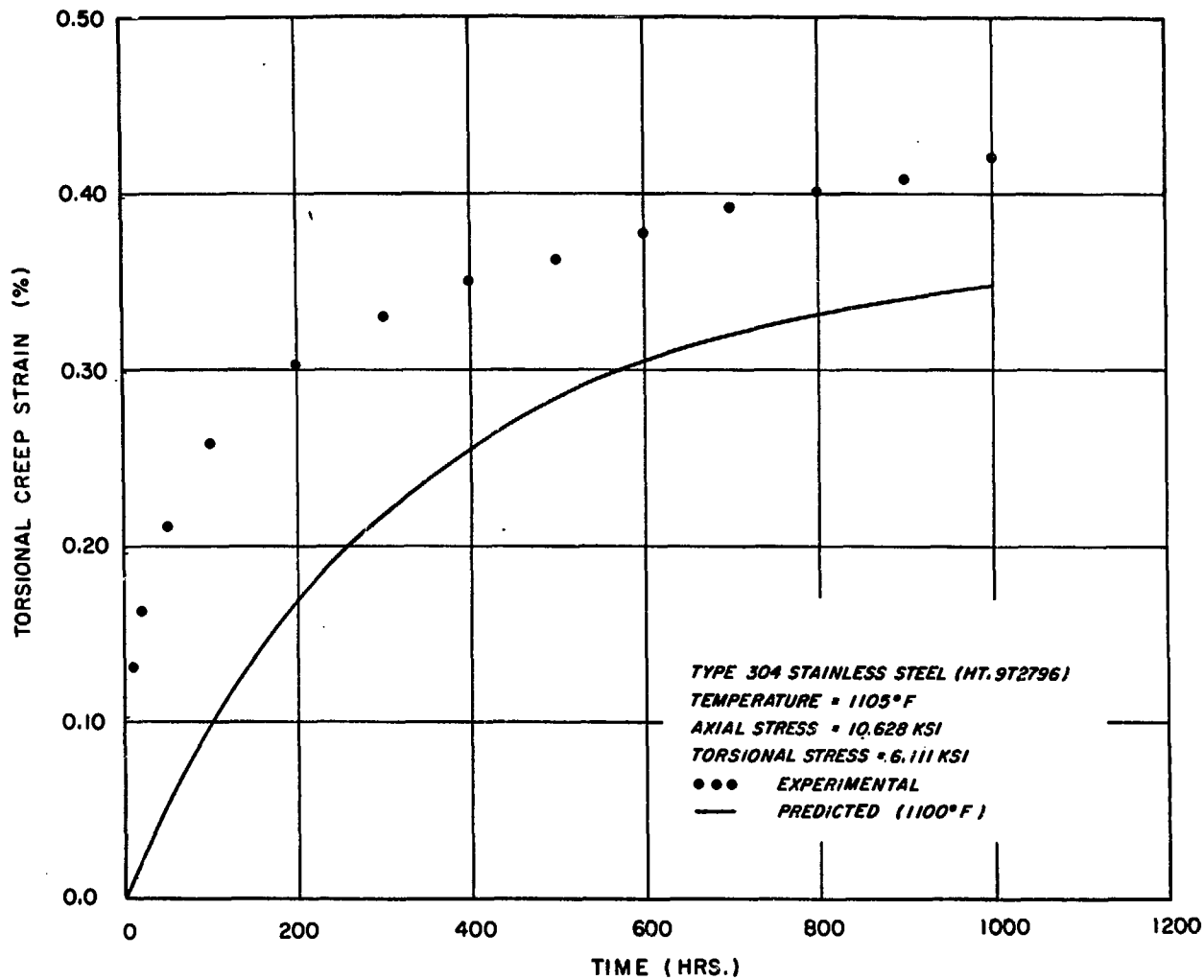


**Creep Strain Ratios for Combined Tension-Torsion
Loadings – Type 304 Stainless Steel (Ht. 9T2796), 1100°F**

Test No.	Axial Stress, σ (ksi)	Torsional Stress, τ (ksi)	Effective Stress, $\bar{\sigma}$ (ksi)	Stress Ratio, τ/σ	Creep Strain Ratio: Torsion/Axial $\epsilon_{12}/\epsilon_{11}$	
					Observed	Predicted
1	10.628	6.111	15.00	0.575	0.92	0.862
2	13.975	3.407	15.17	0.244	0.37	0.366
3	5.570	7.934	14.83	1.424	2.18	2.137



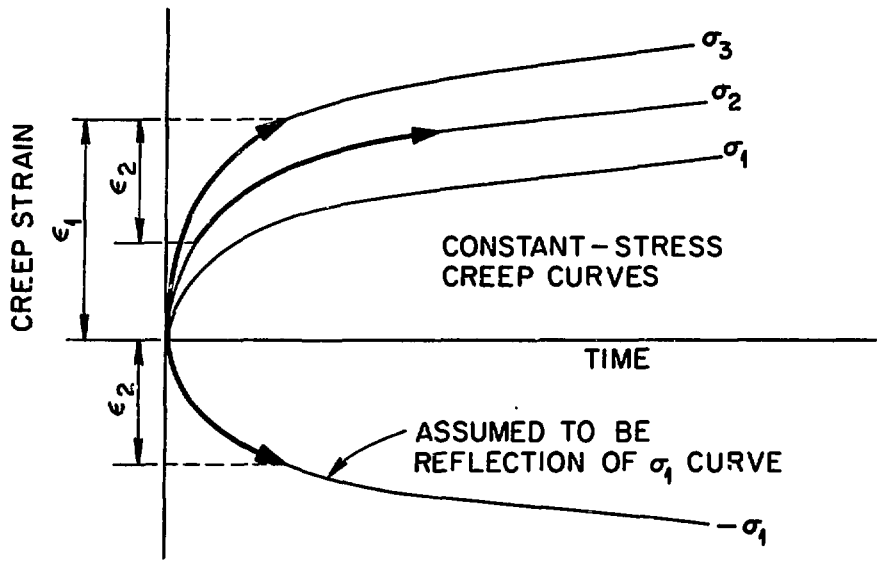
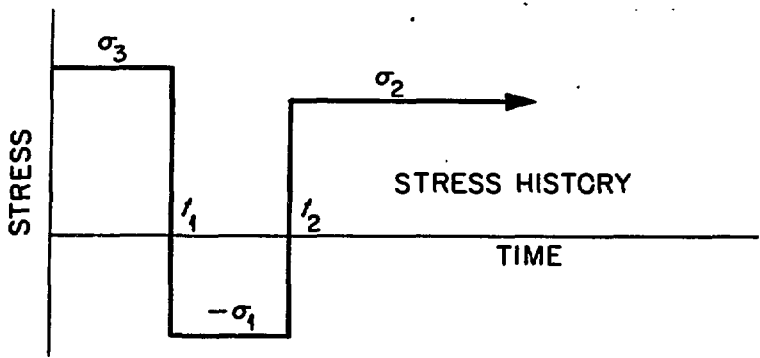




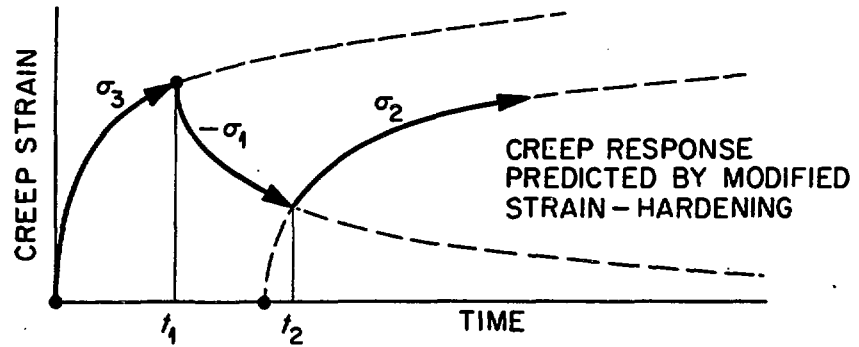
(50)

80%

ORNL-DWG 71-10680



6 1/3

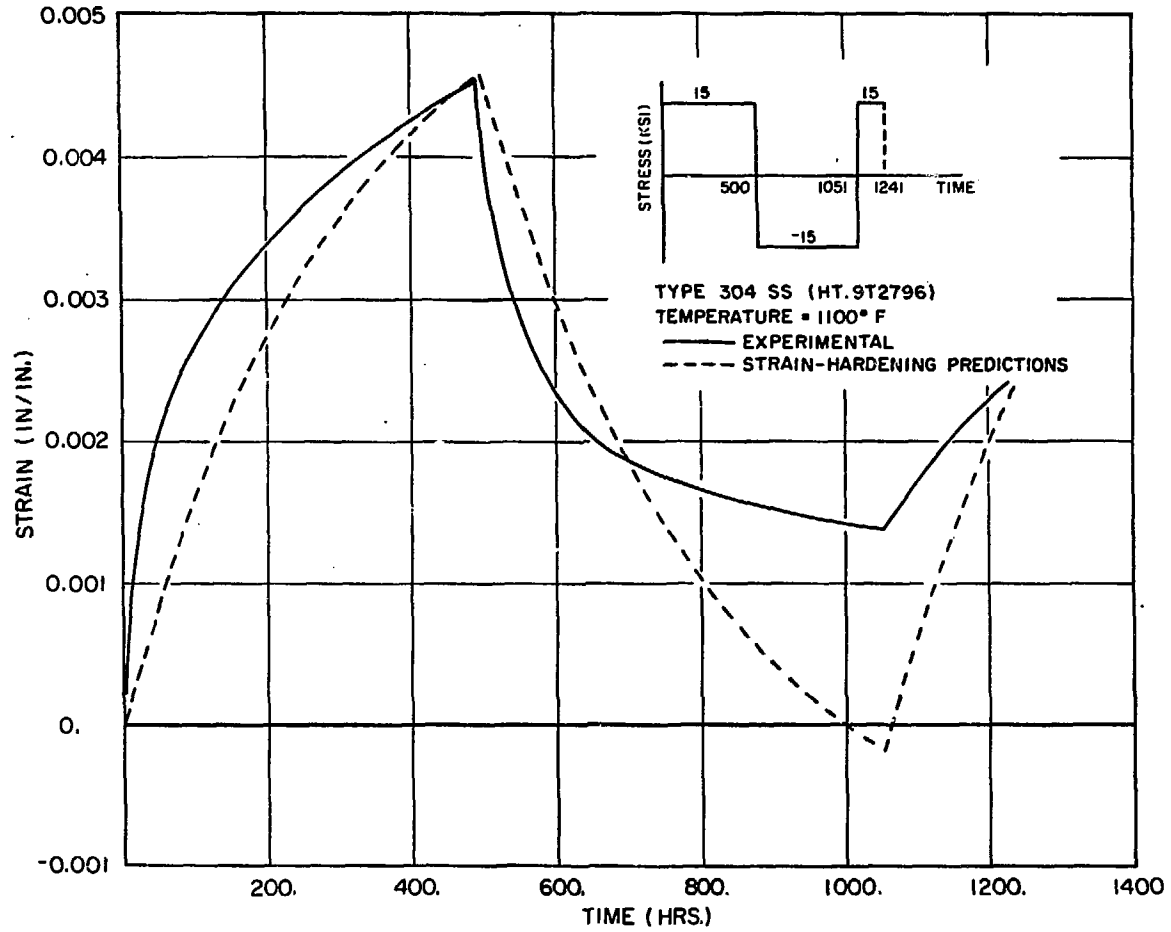


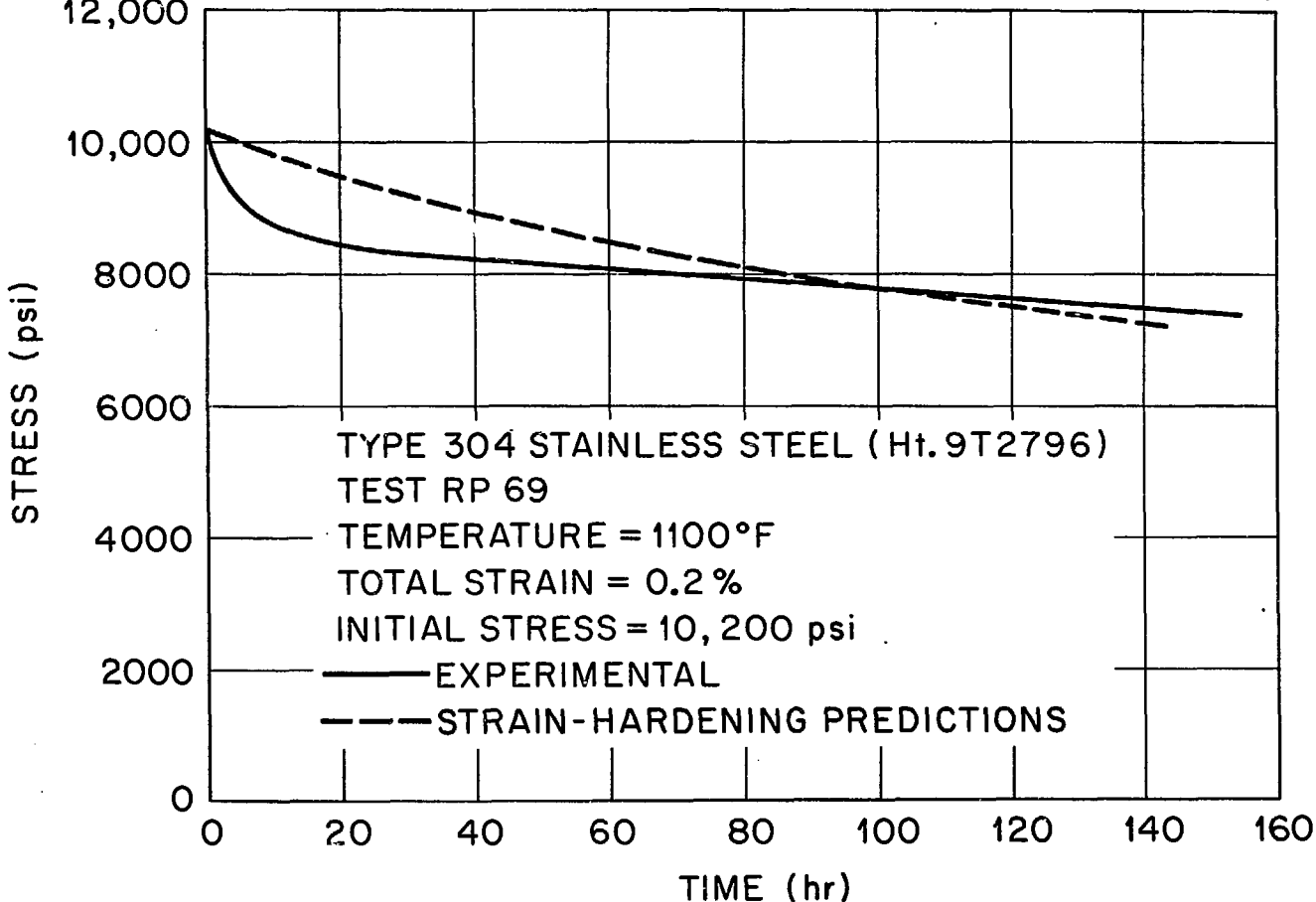
SLIDE 34

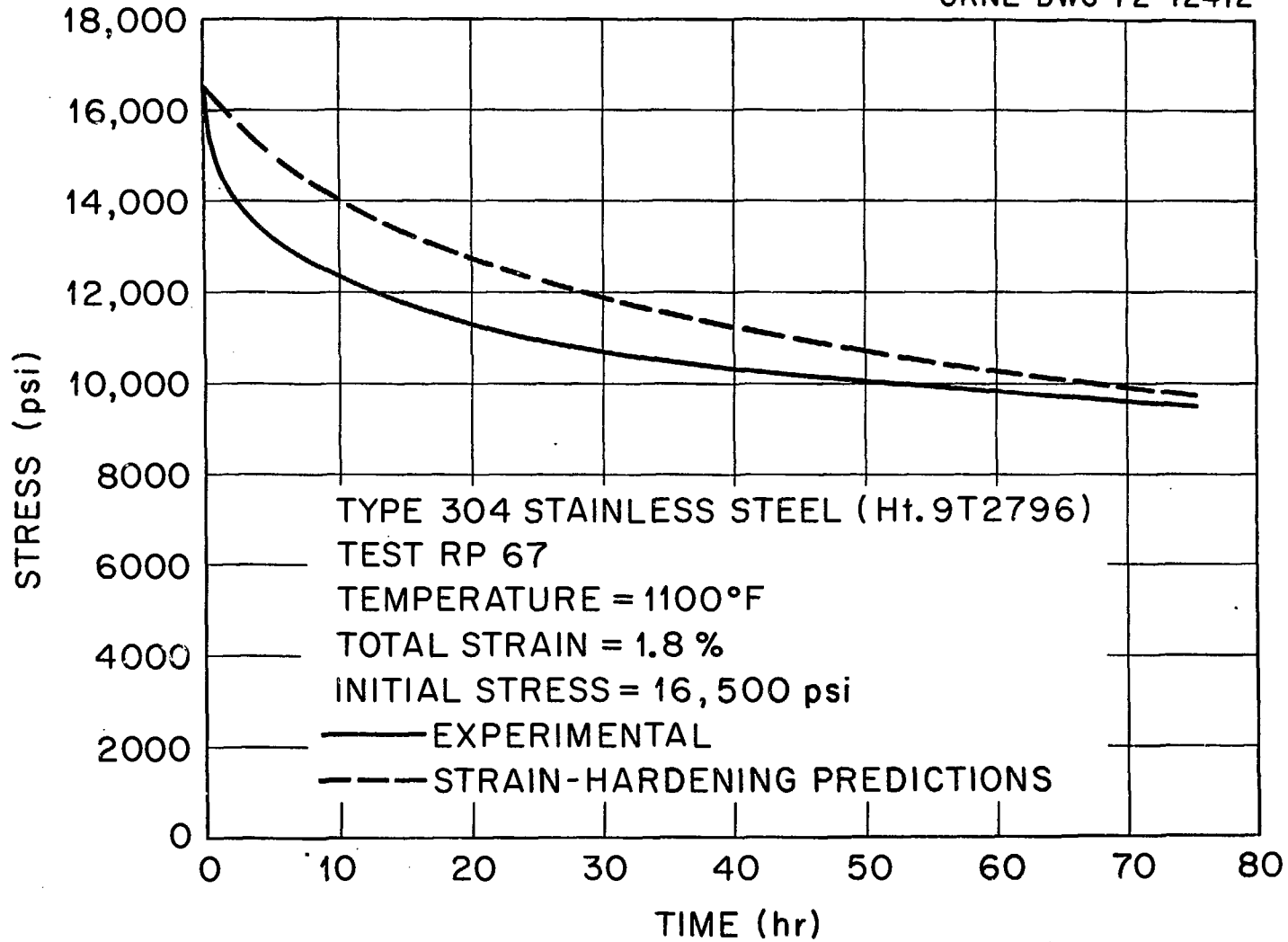
4

80%

Fig. 4.0

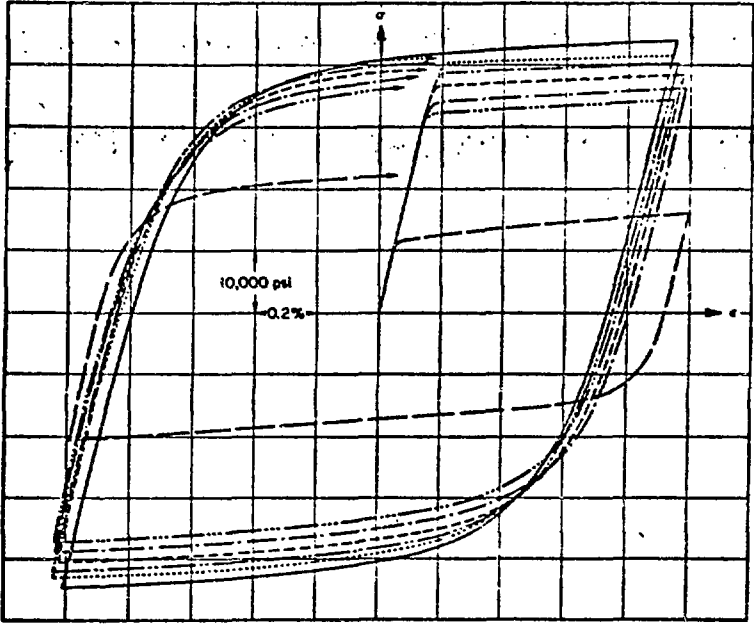




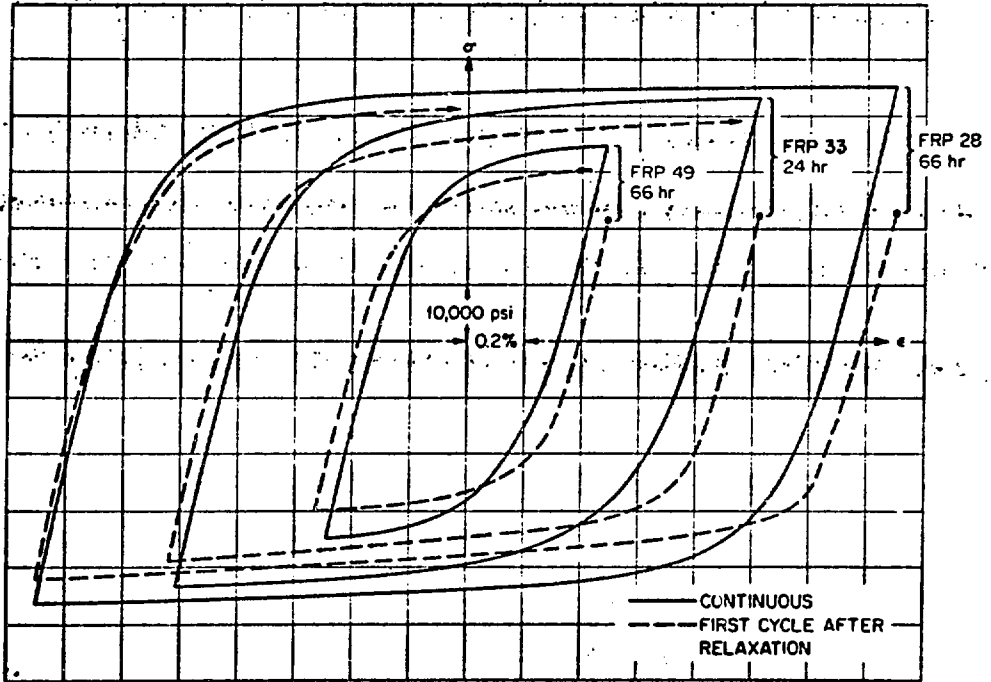


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——— FIRST CYCLE (SPECIMEN FRP 30) AT 0.005 min⁻¹
 ——— CONTINUOUS CYCLE (SPECIMEN FRP 33) AT 0.05 min⁻¹
 ······ AFTER 0.25 hr SOAK
 ——— AFTER 1 hr SOAK
 - - - - AFTER 4 hr SOAK
 ——— AFTER 16 hr SOAK
 ——— AFTER 66 hr SOAK

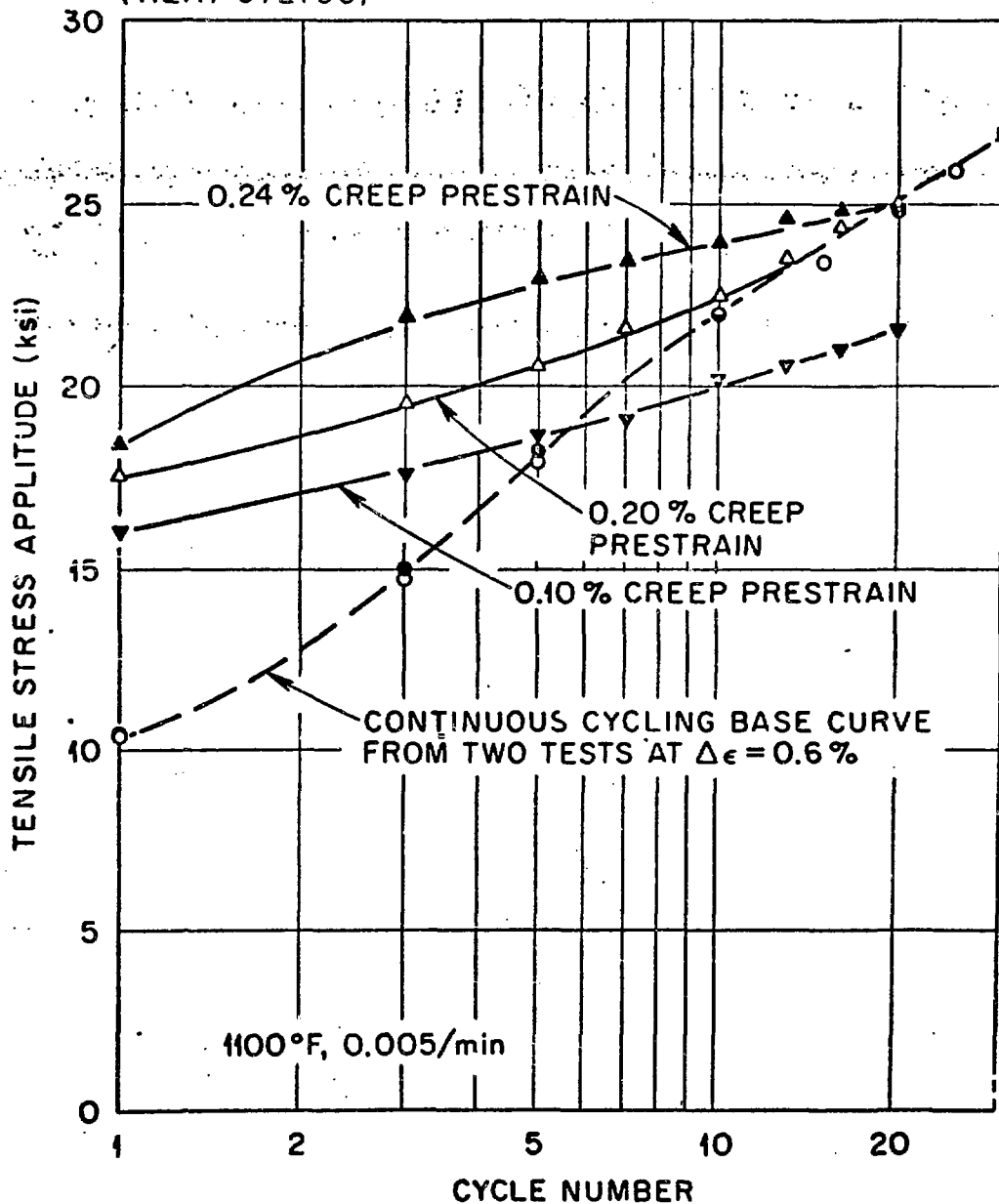


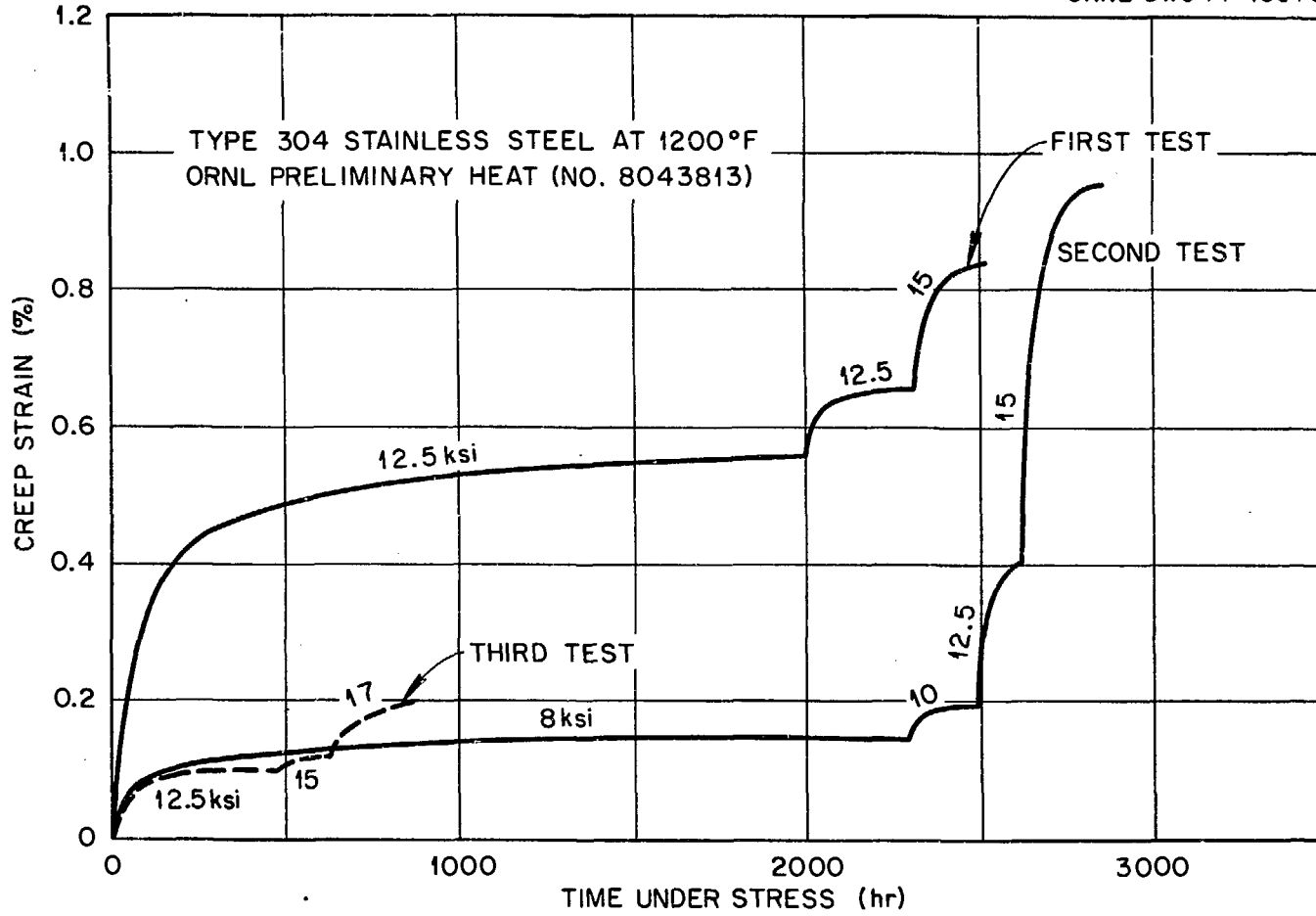
Effect of Soaking at Zero Stress and Strain on the Subsequent Cyclic Curve at 1100°F and 2% Strain Range. Type 304 Stainless Steel Heat 9T2796 (Re-annealed at 2000°F for 1/2 hr).

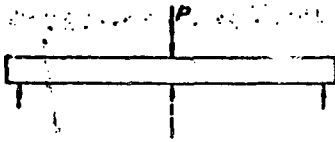


Effect of Relaxation at the Tensile Strain Limit on the Subsequent Cyclic Curve at 1100°F and Three Cyclic Strain Ranges. Type 304 Stainless Steel Heat 9T2796 (Re-annealed at 2000°F for 1/2 hr).

TYPE 304 STAINLESS STEEL, ANNEALED
(HEAT 9T2796)



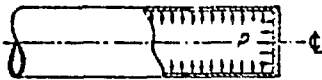




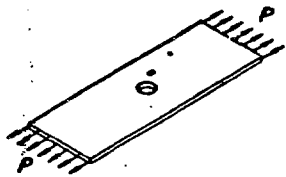
(1) SIMPLY-SUPPORTED BEAMS



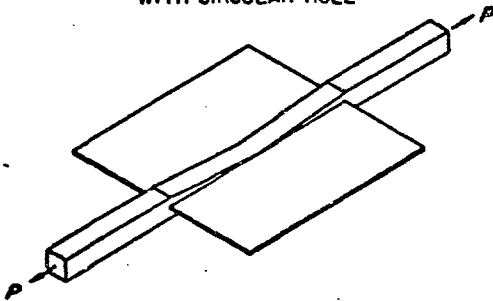
(2) SIMPLY-SUPPORTED FLAT CIRCULAR PLATES



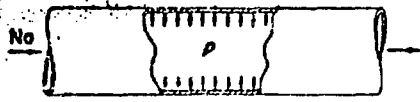
(3) CAPPED CIRCULAR-CYLINDRICAL SHELLS



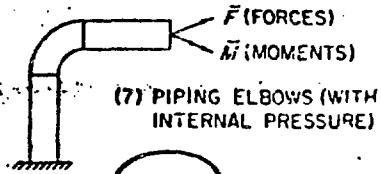
(4) FINITE-WIDTH FLAT PLATE WITH CIRCULAR HOLE



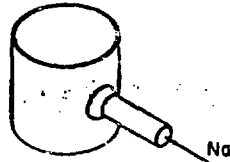
(5) STIFFENED SHEAR LAG PANEL



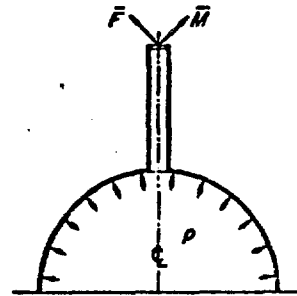
(6) PIPE THERMAL RATCHETTING



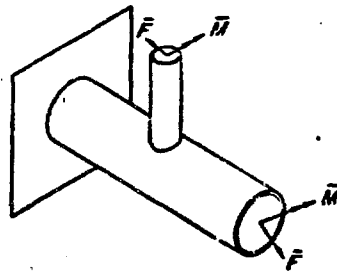
(7) PIPING ELBOWS (WITH INTERNAL PRESSURE)



(8) NOZZLE ATTACHMENT THERMAL RATCHETTING (WITH INTERNAL PRESSURE)

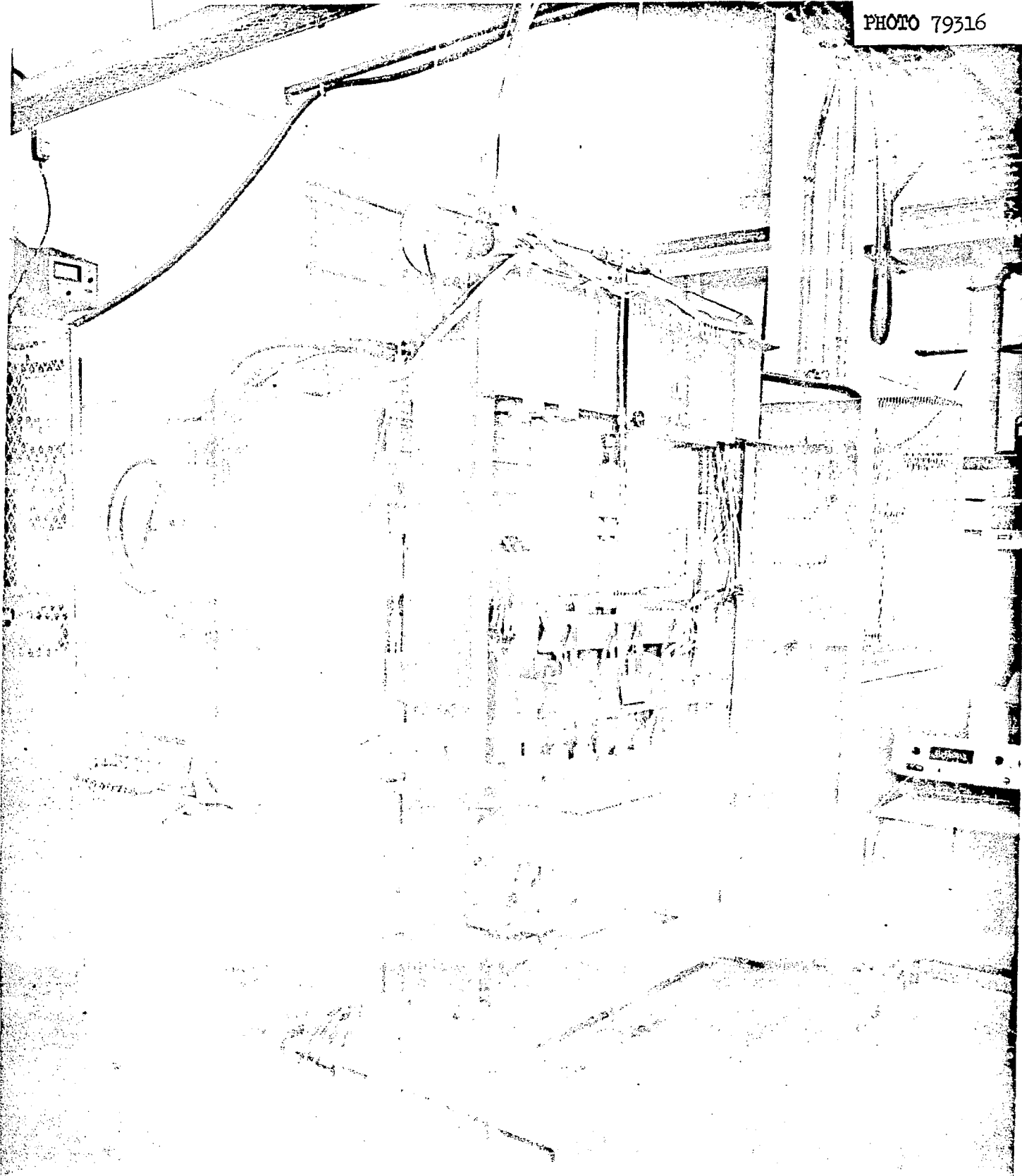


(9) NOZZLE-TO-SPHERE ATTACHMENTS



(10) INTERSECTING CYLINDRICAL SHELLS (WITH INTERNAL PRESSURE)

PHOTO 79316



SLIDE 43

5.9

PHOTO 79316

75

80%

7%

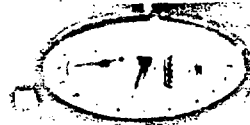
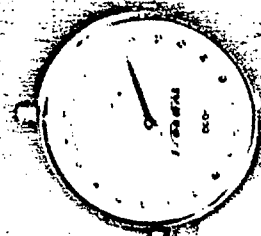


SLIDE 43

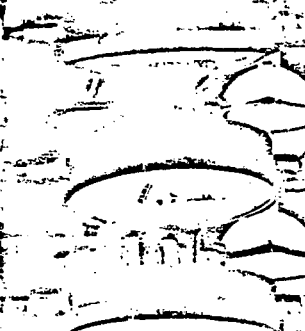
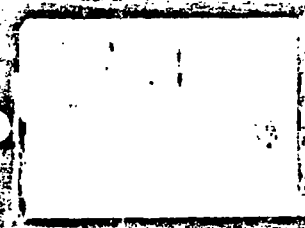
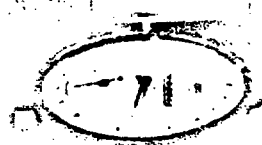
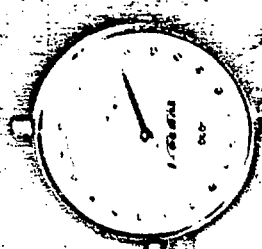
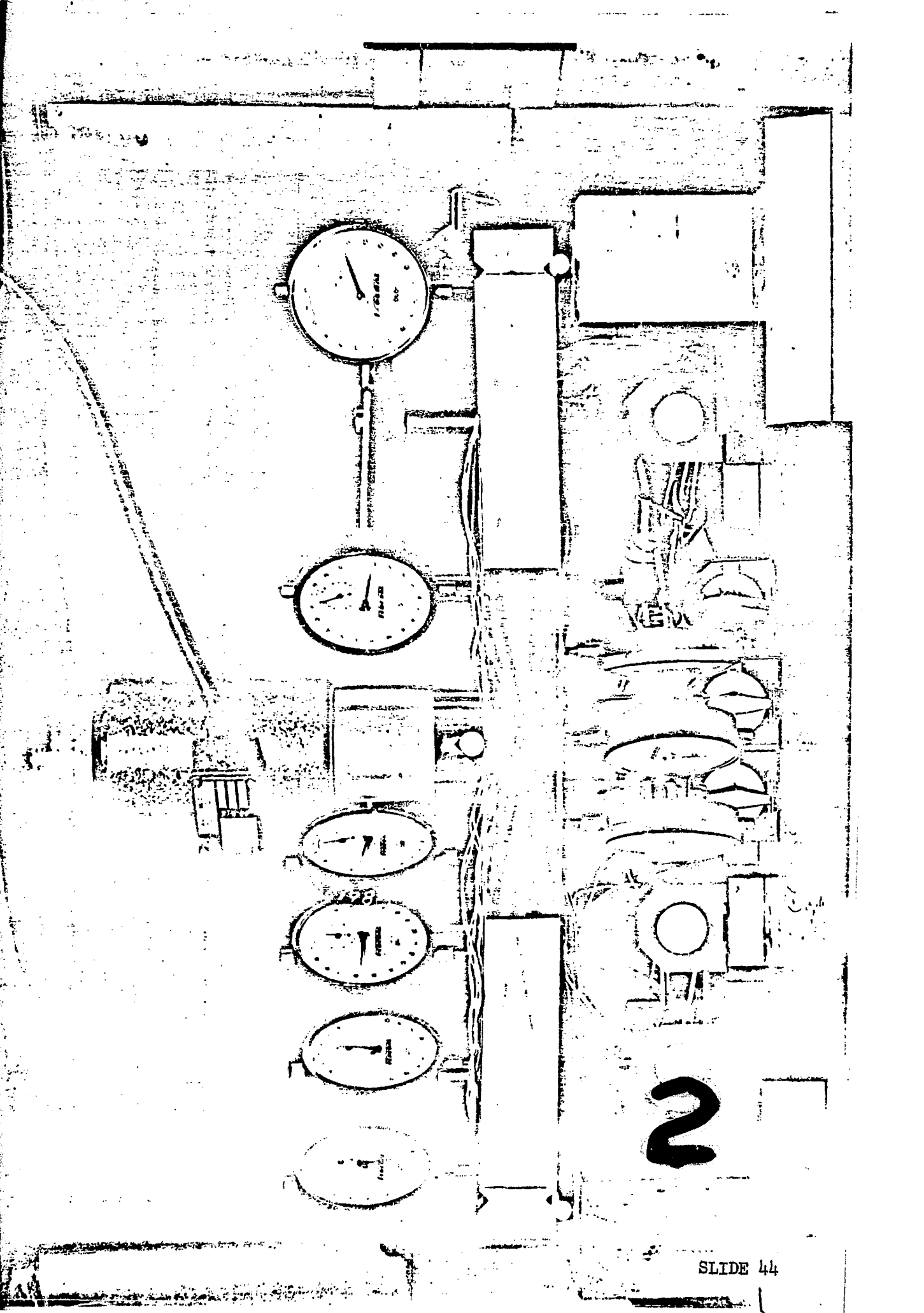
2

5.9

PHOTO 78124

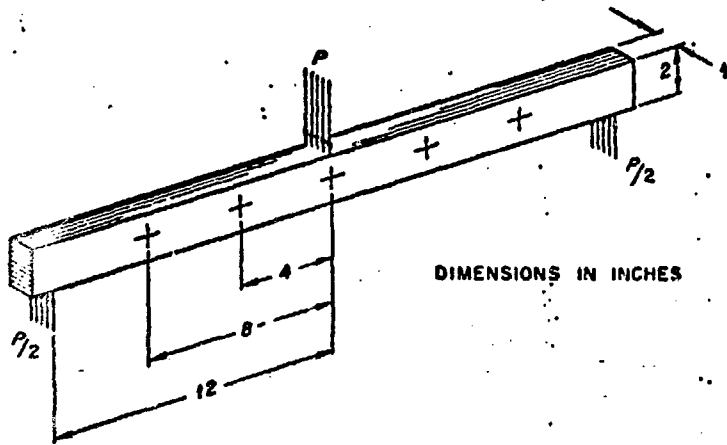


SLIDE 44



2

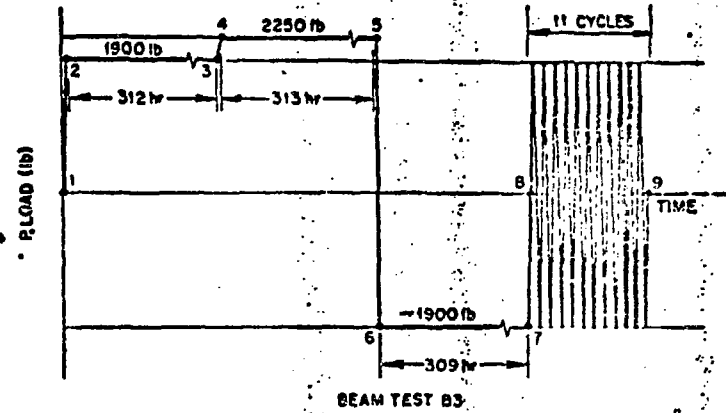
TEST TEMPERATURE 1200 °F



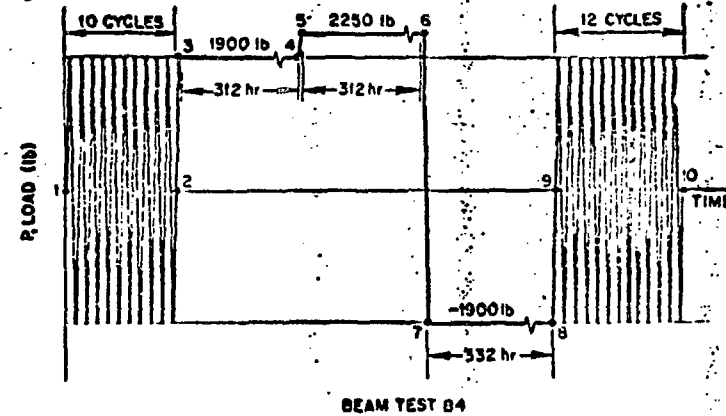
DIMENSIONS IN INCHES

(a) TEST SPECIMEN

ORNL-OWB 72-12415



BEAM TEST B3

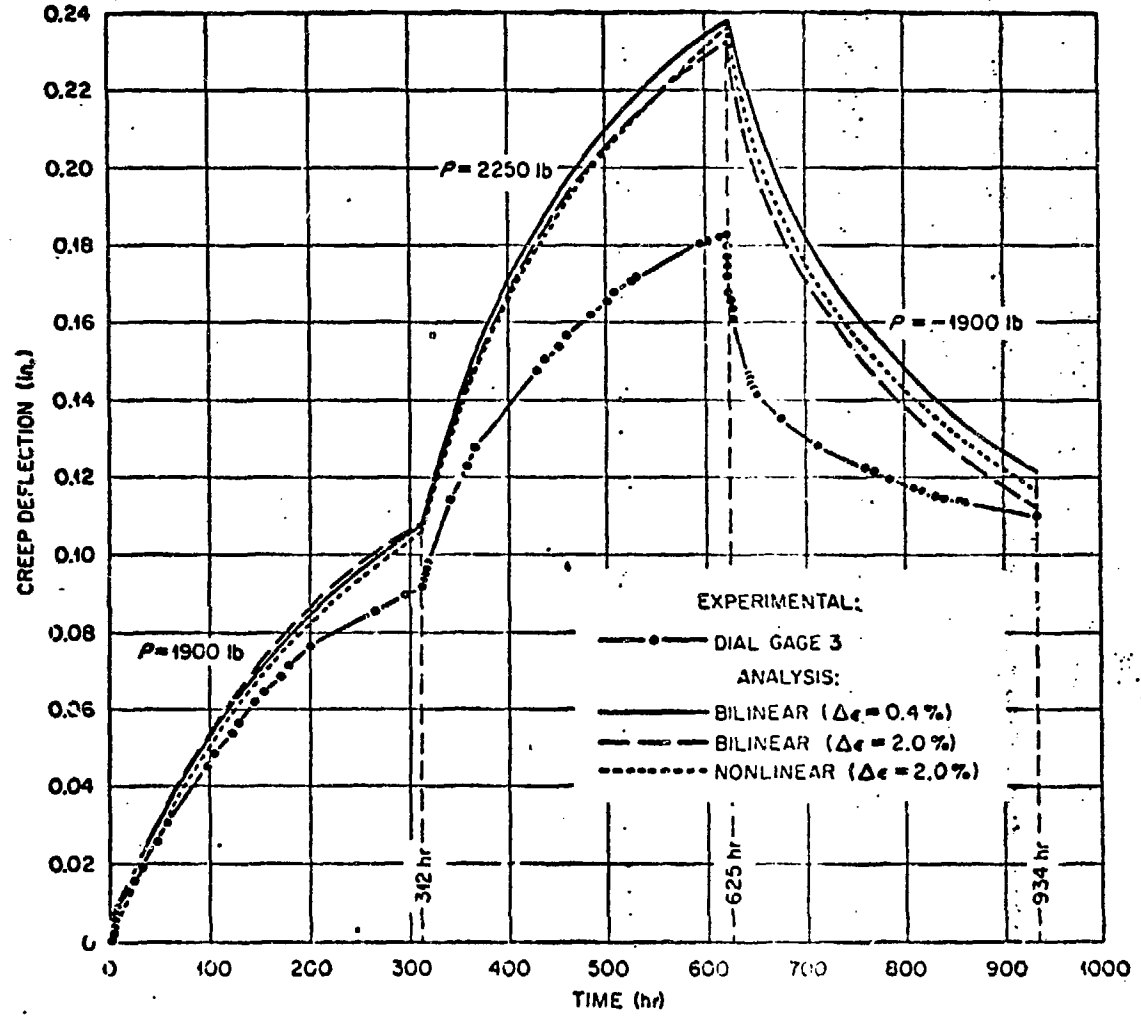


BEAM TEST B4

(b) LOADING HISTORIES

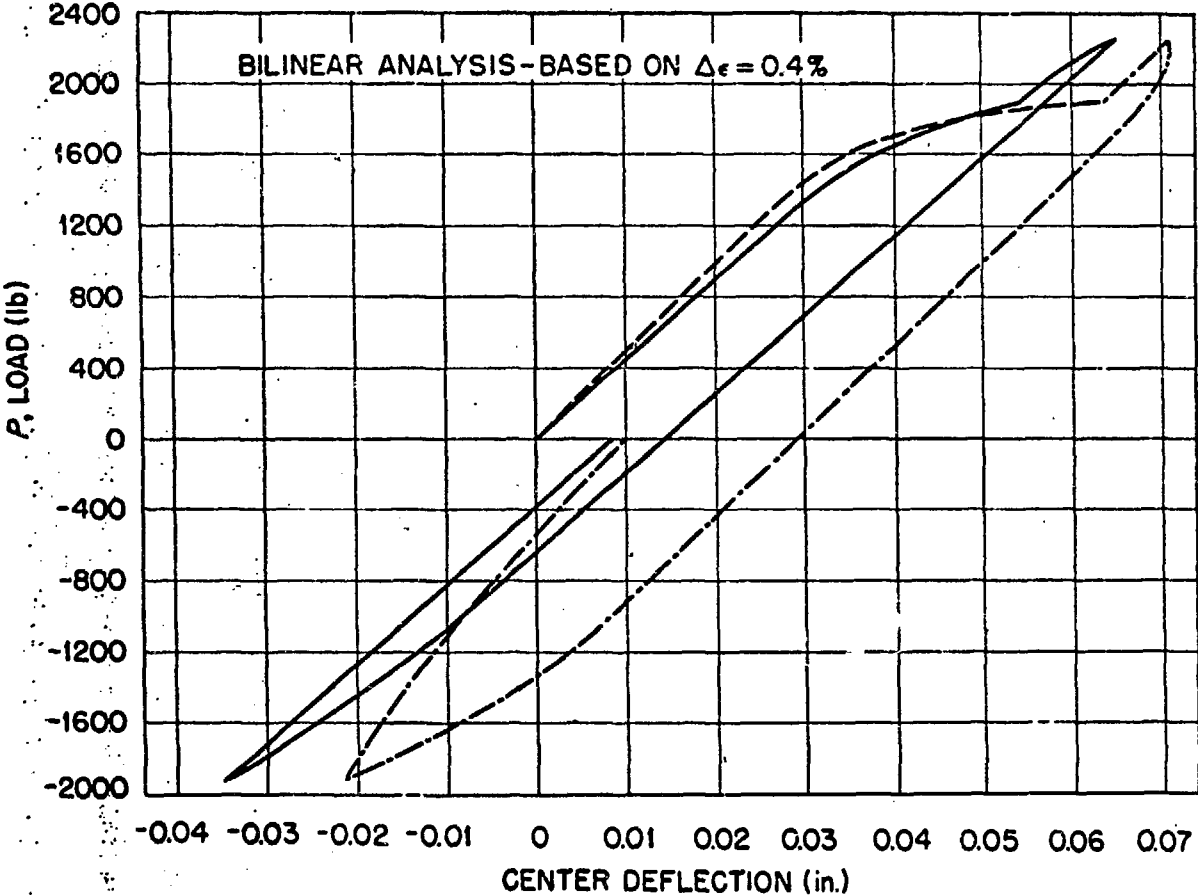
Elevated-Temperature Beam Tests.

BEAM B3
1200°F



SLIDE 46

BEAM B3
1200°F



Areas Requiring Research and Development

MATERIAL BEHAVIOR

- **Representation of Multiaxial Behavior for General Load Histories**
 - **Plasticity**
 - **Creep**
 - **Plasticity-Creep Interaction**
- **Creep-Fatigue**
- **Strain Limits**
- **Environmental Effects**
- **Fracture Mechanics**

ANALYSIS METHODS

- **Development of Efficient General Procedures for Treating Inelastic Behavior**

STRUCTURAL TESTING

- **High-Temperature Instrumentation**
- **Basic High-Temperature Tests – Deformation and Failure**