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PREDICTION OF FISSION GAS RELEASE FROM UO₂ FUEL



NOVEMBER 1974

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PREDICTION OF FISSION GAS RELEASE FROM UO2 FUEL

bу

C. E. Beyer

C. R. Hann

On page 22 change the following equation

$$F = 0.050 X_1 + 0.141 X_2 + 0.807 X_3 + 1.68 (0.002112 + 0.0052 X_2^2 - 0.00269 X_2 X_3 + 0.00217 X_3^2$$

to read

$$F = 0.050 X_1 + 0.141 X_2 + 0.807 X_3 + 1.68 (0.002112 + 0.0052 X_2^2 - 0.00269 X_2 X_3 + 0.00217 X_3^2)^{1/2}$$

On page 26 the second line of the text reads "...shows that there is $\sim 50\%$ chance that D = 0 and K = 0 and thus indicates...", change $\sim 50\%$ to $\sim 30\%$.

PREDICTION OF FISSION GAS RELEASE FROM UO_2 FUEL

by

C. E. Beyer

and

C. R. Hann

November 1974

BATTELLE PACIFIC NORTHWEST LABORATORIES RICHLAND, WASHINGTON 99352

TABLE OF CONTENTS

1.0	INTRO	ODUCTION	١.		•			•	•	•		•	•		•	•	•	•	1
2.0	SUMM	ARY AND	CONCL	.USI	ONS								•		•				3
3.0	HIGH	TEMPERA	ATURE	GAS	RE	LEAS	SE M	ODE	_				•						4
	3.1	DATA SE	ELECT	ON															4
	3.2	DATA RE	EDUCTI	ON								•		•			•		10
	3.3	MODELS	REVIE	WED	F0	R H	[GH	TEM	PERA	TUR	E G	AS	REL	EAS	E				13
		3.3.1	Volum	ne A	ver	ageo	d Fu	e1 :	Гетр	era	tur	е	•						14
		3.3.2	Theor	eti	cal	Mod	de1	•											15
		3.3.3	Local	Те	mpe	ratı	ıre	Dis	trib	uti	on				•				16
		3.3.4	Effec	tiv	e D	iffu	ısio	n C	oeff	ici	ent	Мо	de1						16
	3.4	SELECT	lo no	HI	GH	TEM	PERA	TUR	E GA	S R	ELE.	ASE	МО	DEL					18
		3.4.1	Co1un	ınar	Gr	ain	Gro	wth	Reg	ion									18
		3.4.2	Equia	axed	Gr	ain	Gro	wth	Reg	ion									18
		3.4.3	Regio	on o	f N	o M	icro	str	uctu	ral	Ch	ang	e						19
		3.4.4	Desci	⁴ipt	ion	of	Mod	le1									•		19
	3.5	CORRELA	ATING	THE	MO	DEL	T0	THE	DAT	Ά									20
	3.6	EFFECT:	S OF [DENS	ITY	ANI) BL	IRNU	P										25
4.0	LOW :	TEMPERA	TURE (SAS	REL	EASE	E MO	DEL	•										27
	4.1	DEVELO	PMENT	0F	THE	MOI	DEL							•					27
5.0	LIMI	TATIONS	OF TI	HE G	AS	REL	EASE	MO	DELS	·			•			•	•	•	31
ACKN	OWLED	GEMENTS	•						•	•	•	•	•		•				32
REFE	RENCE	s.		•						•	•	•	•			•	•		33
APPE	NDIX	Α.								•	•		•	•		•	•	•	A-
APPF	NDTX	В.									•				•				B- ⁻

PREDICTION OF FISSION GAS RELEASE FROM UO2 FUEL

C. E. Beyer and C. R. Hann

1.0 INTRODUCTION

High temperature (>1200°C) gas release from UO_2 fuel is an important consideration in steady state reactor safety calculations because of its effect on the fuel-to-cladding gap conductance (and thus fuel temperatures) and fuel rod internal gas pressures. Conservative and best-estimate correlations for gas release are needed to initialize gap conductance and internal pressure in the rod before accident calculations can be performed. Several methods for calculating the high temperature fission gas release have been proposed but the results vary widely. However, most investigators agree that high temperature gas release is a nonlinear phenomenon which is dependent upon local conditions in the fuel, with fuel temperature being the primary controlling parameter. The large uncertainties that are inherent in estimating fuel temperatures often preclude a reliable correlation for gas release. These uncertainties in determining fuel temperatures, plus the inherent differences in the models themselves, account for the lack of agreement between previously proposed models.

Low temperature (<1200°C) gas release from fuel with burnups of less than 20,000 MWD/MTM is typically in the range of 2% or lower. The release from low temperature fuel is not as significant as the high temperature release because the gap conductance and internal rod pressures change very little when gas release is on the order of 2%. A low temperature release model will be used to extend gas release predictions below temperatures of 1200°C.

The objectives of the work reported here were:

• to evaluate the open literature data and select those data that were well characterized with regard to high temperature gas release and fuel temperatures,

- to reduce the selected data to a useful form by employing a consistent and documented method,
- ullet to select a model (or models) which best describes these data and is consistant with known theory and phenomenology of gas release from light water reactor (LWR) UO₂ fuel, and
- to correlate the gas release model (or models) against these data.

2.0 SUMMARY AND CONCLUSIONS

High and low temperature gas release models were developed to provide an improved method for predicting gas release from $\rm UO_2$ fuel because of the important role of fission gas release in LWR safety calculations. The high temperature release model was fit to a consistent and well characterized set of 45 data points using a multiple linear regression code. The low temperature release model is a modification of one developed by Bellamy and Rich⁸ and is compatible with the high temperature model (i.e., extends gas release predictions to temperatures below 1200°C where the high temperature model is not applicable).

The conclusions reached as a result of this study are:

- 1. The high temperature gas release model fits the data well with a correlation coefficient of 0.980 and a standard deviation of 4.7 in percent release.
- 2. In the operating range of current design light water reactors, previously proposed high temperature release models are more conservative (i.e., predict larger gas release fractions) than the model developed here.
- 3. Power histories, large axial power gradients, and fuel temperature estimates seem to be the major factors which cause the large variance among gas release data. A definite reduction in the variance results if the above parameters are controlled.
- 4. Burnup and density have no detectable influence on high temperature gas release over the range 400 to 18,000 MWD/MTM and 91.3 to 98.0% theoretical density.
- 5. Experimental data indicate that low temperature gas release increases with increasing burnup for burnups greater than 20,000 MWD/MTM.

3.0 HIGH TEMPERATURE GAS RELEASE MODEL

3.1 DATA SELECTION

From the open literature 74 sources $^{1-74}$ for high temperature gas release information were examined. Some sources did not supply new data but did propose and discuss various models for gas release, while others provided data on gas release that were not applicable to light water reactor $\rm UO_2$ fuels. Table 1 is a list of the sources and the data used in correlating the high temperature model. Before discussing these data in detail we will provide some background on 1) the methods used to measure gas release, 2) the methods which provide data applicable to current commercial reactor fuels, and 3) the general rationale we have used to select data for the correlation.

Data from out-of-reactor tests were not used because out-of-reactor gas release data typically do not agree well with in-reactor release data. Out-of-reactor tests usually consist of postirradiation annealing studies wherein irradiated fuel is heated in the laboratory while simultaneously monitoring the release of gas. Results from these tests do not agree with in-reactor release because the fuel is subjected to different environments. Laboratory annealing tests involve isothermal heating of fuel, while in-reactor fuel is subjected to severe temperature gradients on the order of 4000°C/cm. Current theories 17,18 indicate that temperature gradients have a strong influence on gas release. Laboratory tests also do not subject the fuel to the continuing perturbations created by the fissioning process. These perturbations are thought to both impede and enhance gas movement. The gas is impeded by the creation of structural defects within the fuel matrix which can trap the gas either in the form of an atom or bubble. Fission spiking can enhance gas release by 1) enabling the gas atom to break away from these traps, or 2) if the gas is in bubble form it can promote resolution of the trapped bubble.

In-reactor tests for measuring gas release can be separated into two categories. The first employs a sweep gas technique while the second

TABLE 1. High Temperature Gas Release Data

							GRAIN G	ROWTH	_	
	SPECIMEN	ENRICHMENT	PELLET DIAMETER	FUEL LENGTH	HEAT RATING	BURNUP	EQUIAXED	COLUMNAR	PELLET	GAS RELEASE
<u>REFERENCE</u>	NUMBER	(WT % 235U)	OD/ID (IN.)	(IN.)	(KW/FT)	(MWD/MTM)	(R/R ₀)	(R/R_0)	(%TD)	(PERCENT)
CYRANO-(9, 10)* EXP.	CYRANO-II CYRANO-III	4.0 DID NOT US	0.433/0 <mark>.0472</mark> SE BECAUSE POWER	3.94 R HISTORY	13.9 VARIED	940 ~20%)69 ⁰ C**	96.4	15.0
	CYRANO-VIII	4.0	0.512/0.0472	3.94	11.5	1282	1890/19	969°C * *	94.8	13.0
HPR-129 (11) *	116-1		SE BECAUSE THERM				DEARLY IN LIFE			
	116-5 117-1	6.0 6.0	0.541/0.126 0.5451/0.126	19.0 19.0	22.8 21.0	4223 7148	2070/23	374°C * * 329°C * *	91.3 96.9	27.5 25.4
	117-5 117-6	DID NOT US	SE BECAUSE OF THE SE BECAUSE OF LAR	RMOCOUP	LE FAILUR	RE EARLY IN LII	FE	<i>2</i> .7 C	70.7	27.4
BELGONUCLEATRE (12)							O INC PIN			
AND CEA	EPL-3 EPL-4	2.4	SE BECAUSE POWER 0.2921 -	39.37	12.3	~ 10% 11, 100	0,5256	_	93.9	9.9
· · · · · · · · · · · · · · · · · · ·	EPL-5	2.4	0.2921 -	39.37	13.5	3990	0.4582	-	93.9	4.4
	EPL-6	2.4	0.2921 -	39.37	15.1	14,400	0.6873	.5445	93.9	21.3
	EPL-7 EPL-8		SE BECAUSE POWER SE BECAUSE POWER							
	EPL-9	2.4	0,2921 -	39.37	14.9	18,300	0,6119	.4582	93,9	23.2
	EPL-10	2.4	0.2921 -	39.37	14.9	9940	0.6280	.4906	93.9	18.3
	EPL-11		SE BECAUSE POWER							
	EPL-12	2.4	0.2921 -	39.37	13.3	8,440	0.6388	.4232	93.9	17.8
AECL-2662 (13)	LFL	2.40	0.7638	9.57	18.0	2230	0.375	-	98.0	5.7
	LFF	2.40	0.7638	9.57	17.8	2230	0.582	-	95.7	17.3
	LFB	2.40	0.7638	9.57	17.3	2230	0.642	0.497	93.4	23.4
	LFS LFW	2.40 2.40	0.7638 0.7638	9.57 9.57	24.5 25.0	3120 3290	0.697 0.640	0,631 0.575	98.0 98.0	37.9 24.8
	LFT	2.40	0.7638	9.57	24.1	3290	0.735	0.659	93.4	49.6
	LFX	2.40	0.7638	9.57	24.9	3290	0.715	0.646	95.7	36.8
	LFK	2.40	0.7638	9.57	24.3	3120	0.712	0.633	-	-
	LFM	2.40	0.7638	9.57	22.7	3030	0.609	0.536	98.0	15.5
	LFH	2.40	0.7638	9.57	22.1	3030	0.702	0.602	95.7	31.1
	LFD	2.40	0.7638	9.57	22.1	3030	0.743	0.679	93.4	45.8
AECL-2230 (14)	CBN	4.5	0.6429	6.02	17.1	2650	0.51	0,31	97.9	12.3
(TEST X-501)	CBO CBB	4.5 4.5	0.6425 0.6425	6.02	17.3	2670	0.52 0.50	0,37 0.33	97.8	14.9
	CBP CBR	4.5 4.5	0.642	6.02 6.02	16.8 17.4	2610 2710	0.56	0.33	97.2 97.1	14.1 15.7
i	CBT	4.5	0.6425	6.02	16.6	2620	0.52	0.43	96.2	15.3
•	CBV	4.5	0.6425	6.02	17.5	2760	0.54	0.45	95.9	16.5
	CBY	4.5	0.6425	6.02	16.55	2630	0.55	0.47	95.0	16.8
	CBX	4.5	0.6425	6.02	17.1	2720	0.57	0,51	95.2	18.8
AECL-1676 (15)	DFE	4.34	0.748	6.26	35.8	794	-	0.74	96.6	40.1
(TEST X-211)	DFH	4.34	0.748	6.26	29.5	648	-	0.67	96.6	32.6
	DFD	4.34	0.748 Se because power	6.26	29.05	658	**	0.70	96.6	33.0
	DFJ DFB	4.34	0.748	6.26	24.0	~ 17 % 528	_	0.597	96.6	17.9
	DFA	4.34	0.748	6.26	17.7	386	-	0.460	96.6	4.95
CEA-R-3358 (16)	4110-AE1	2.98	0,5094	4.84	18.1	6416	0,6934	_	96.0	21.6
	-AE2	2.98	0.5094	4.84	17.6	6243	0.6549	-	96.0	22.1
	-BE1	2.98	0.5094	4.84	15.1	5222	0.5639	-	96.0	13.9
	-BE2	2.98	0.5094	4.84	17.8	6566	0.6009	-	96.0	15.9
	4111-AE1		SE BECAUSE POWER		-					
	-AE2 -BE 1		SE BECAUSE POWER SE BECAUSE POWER							
	-BE2		SE BECAUSE POWER	-						
	4112-AE1	2.98	0.5111	4.84	19.5	3453	0.6225	0.431	95.0	12.6
	-AE2	2.98	0.5110	4.84	17.7	3230	0.6133	0.421	95.0	11.2
	-BE1	2.98	0.5111	4.84	15.4	2796	0.4330	- 0.070	95.0	7.9
	-BE2	2.98 2.98	0.5110 0.5138	4.84	16.6	3015	0.5794 0.7627	0,279 0:644	95.0 05.0	12.6
	4113-AE1 -AE2	2.98 2.98	0.5138	4.84 4.84	17.1 15.6	3110 2836	0.7627	0.564	95.0 95 . 0	26.7 28.0
	-BE1	2.98	0.5138	4.84	16.0	2843	0.5794	0.411	95.0	17.0
	-BE2	2.98	0.5138	4.84	15.9	2895	0.7190	0.548	95.0	21.0

^{*} FUEL TEMPERATURES DETERMINED WITH THERMOCOUPLES

^{**} TEMPERATURE MEASUREMENT BY A THERMOCOUPLE AT FUEL CENTERLINE/CORRECTED CENTERLINE TEMPERATURES FOR THAT PORTION OF THE FUEL WITHOUT AN ANNULAR HOLE AND THERMOCOUPLE

utilizes sealed capsule irradiations. Sweep gas experiments are based on continually collecting and monitoring the gas given off during irradiation. The amount of gas released in sealed capsule experiments is determined by destructive examination after the fuel has been irradiated for a specified period of time. The data generated by the sweep gas technique are generally obtained from fuel operating at low heat ratings and thus temperature gradients within the fuel are small. Consequently, sweep gas experiments may yield atypical results because temperature gradients are believed to have a substantial effect on gas release in commercial fuel. A comparison of sealed capsule data at heat ratings >5 kW/ft with sweep gas data^{19,20} obtained at lower heat ratings but with similar fuel temperatures (1700-2000°C) shows significant differences (e.g., sweep gas release data are often more than an order of magnitude lower). Consequently, sweep gas tests using low heat ratings were not considered for our correlation. Data from the CYRANO experiments $^{9;10}$ which used the sweep gas technique were used in our correlation; however, these experiments operated with heat ratings large enough (10-15 kW/ft) to have a substantial thermal gradient (>2500°C/cm) and thus provide relevant data. The remaining data in Table 1 come from sealed capsule experiments wherein gas release was determined by destructive postirradiation examination.

To reduce the amount of variability in the gas release data, we have identified four factors (listed in Table 2) that might enhance this variability and used them as data selection criteria. These are:

- 1. Stoichiometry
- 2. Variable power operation
- 3. Variable axial power generation
- 4. Imprecise fuel temperature determinations

It has been shown that hyper-stoichiometric $U0_2$ has significantly higher fission gas release than stoichiometric $U0_2$.²¹ This is not unexpected since Xe and Kr have higher diffusion rates in hyper-stoichiometric $U0_2$.²²,²³

Soulhier and Notley 24 have shown that variable power histories can have a significant effect on gas release; this also may be expected since variation in power is reflected by a temperature variation.

TABLE 2. Rationale for Establishing Criteria for Data Selection

Fac	tors That Enhance the Variability of Gas Release	Criteria for the Selection of Data						
1.	Stoichiometry	1.	Only stoichiometric $U0_2$ (0/M 2.00 ± 0.005) data were selected					
2.	Variable power operation	2.	Only those data with a relatively constant power operating history were considered. The maximum power (Pmax) over the life of a fuel pin cannot be more than 15% greater than the time averaged power (P time avg)					
			$(i.e., \frac{Pmax}{P_{time avg}} \leq 1.15)$					
3.	Variable axial power generation	3.	Only those experiments with short fuel columns and relatively flat axial power distributions were selected					
			(<u>Peak Power</u>) ≤ 1.15)					
4.	Imprecise fuel temperature determinations	4.	Only those experiments where fuel temperatures were either measured at a particular point in the fuel or could be inferred from a microstructural change were considered					

A large variation in the axial power profile will result in a large axial variation in fuel temperature, changing the gas release fractions along the length of the fuel. Correlating the total release of such a fuel rod with the average temperature of the fuel rod can lead to errors because gas release along the length of the rod is not linearly dependent on temperature.

Finally, the uncertainties in estimating fuel temperatures contribute significantly to the variability of gas release data. Past methods have resulted in significant uncertainties because fuel temperatures were seldom

measured by thermocouples or inferred from temperature indicators such as grain growth radii. Temperatures were usually estimated through more indirect methods, such as making some assumption about the value for gap conductance. Furthermore, different values for thermal conductivity, 'grain growth temperatures, and flux depressions were used by previous investigators.

Assuming a gap conductance can lead to substantial errors in fuel temperatures because gap conductance has been shown to be a very difficult parameter to estimate without previous knowledge of fuel temperatures. For example, a fuel rod with a heat rating of 11 kW/ft with the hot fuel-to-clad gap open can easily have a gas conductance of 600 Btu/hr-ft²-°F with a fuel centerline temperature of 1615° C. However, if the hot fuel-to-clad gap were closed in this same fuel rod a gap conductance of ≈ 5000 Btu/hr-ft²-°F would not be unreasonable which would result in a centerline temperature of 1180° C.

Our evaluation of the gas release data indicates that the last three factors (variable power operation, variable axial powers, and imprecise temperature estimates) contributed the most to the large amount of variance among gas release data. Nonstoichiometric fuel was a problem in early irradiation tests; 21 however, stoichiometry was well controlled in later tests. The criteria used for the data selection is an attempt to reduce the variability of these four factors and thus the variability of the data. Of the 74 literature sources evaluated, 18 were selected which supplied gas release data applicable to LWR UO_2 fuel. Further evaluation of these 18 sources to determine whether they met the requirements listed in Table 2 resulted in rejection of experimental data from 11 of them. These data are listed in Table 3 along with the specific reasons for their rejection. The rejection of these particular experiments does not mean that they were not well characterized or executed, because the main objective of most of these experiments was not to evaluate gas release but other fuel performance parameters.

Not all data from the experiments selected (listed in Table 1) were used because some of the data did not meet the criteria listed in Table 2.

TABLE 3. References Rejected Which Contained Data Applicable to LWRs

Reference

- M.G. Balfour, "CVTR Fission Gas Release," WCAP-3850-5.
- W.A. Bezella, "Analysis of the Fission Gases Released Within Spent Yankee Fuel Rods," WCAP-6087.
- F.A. Brandt, et al., "Irrad. Results, N.S. Savannah Core II Prototype Fuel Assemb. (Assemb. SAV-II-2 & SAV-II-3)," GEAP-3559.
- J.P. Hoffman, et al., "The Release of Fission Gases from Uranium Dioxide Pellet Fuel at High Temperatures," GEAP-4596.
- C. Lepsky, et al., "Experimental Investigation of In-Reactor Molten Fuel Performance," Nucl. Tech. Vol. 16.
- R.D. MacDonald, et al., "10,000 MWD/Tonne from U02 Clad in This Zircaloy," Trans. Am. Nucl. Soc., 7, 449-450.
- R.D. Page, "Engineering and Performance of Canada's UO₂ Fuel Assemblies for Heavy Water Power Reactors," IAEA Symp. on Heavy Water Reactors, Vienna (1967).
- R. Soulhier, et.al., "Effect of Power Changes on Fission Product Gas Release from UO₂ Fuel," Nucl. Appl. Vol. 5.
- 9. C.N. Spalaris, et.al., "Residual and Fission Gas Release from UO2," GEAP-4314.
- W.J. Zielenbach, et.al., "Irradiation Behavior of Oxide Fuels at High Temperatures," BMI-1925.
- D.L. Zimmerman, "Irradiation and Postirradiation Examination of N.S. Savannah Test Fuel Element S1-A," GEAP-3342.

Reason for Rejection

- 1. No data given from which temperatures could be determined. Temperature gradients in the axial direction were too large (axial $\frac{Peak}{avg}$ power > 1.15).
- 2. No temperature data given. Power history varied too much $\left(\frac{P_{max}}{P_{time \ avg.}}\right) > 1.15$
- 3. Power history varied too much $\left(\frac{P_{max}}{P_{time avg}} > 1.15\right)$ Axial $\frac{P_{eak}}{avg}$ power > 1.15.
- 4. No temperature data given. Axial $\frac{\text{Peak}}{\text{avg.}}$ power > 1.15.
- 5. Axial $\frac{\text{Peak}}{\text{avg.}}$ power > 1.15. Vipac fuel, 85% T.D.
- 6. No temperature data given. Power history varied too $\operatorname{much}\left(\frac{\operatorname{Pmax}}{\operatorname{Ptime avg}}\right) > 1.15$
- 7. No temperature data given. O/M ratios > 2.005.
- 8. No temperature data given.
- 9. No temperature data given. Axial $\frac{\text{Peak}}{\text{avg.}}$ power > 1.15.
- 10. No temperature data given.
- 11. No temperature data given Power history varied too much $\left(\frac{Pmax}{Ptime}\right)$ > 1.15 . Axial $\frac{Peak}{avg}$ power > 1.15.

while others experienced thermocouple failures early in life. The specific reasons for the rejections of these data are included in Table 1. This table also shows the relatively small number of experiments that have concurrently used thermocouples to measure fuel temperatures while measuring the amount of gas release.

3.2 DATA REDUCTION

The data from the selected experiments have been reduced to obtain a radial fuel temperature profile for each data point using consistent values for $\rm UO_2$ thermal conductivity and grain growth temperatures. The reduced data in terms of fuel centerline and surface temperatures are supplied in a table in Appendix B. One dimensional heat transfer with one axial node was used in calculating fuel temperatures (which is consistent with the relatively flat axial power distribution and the short fuel lengths).

Calculating the radial temperature profile of a cylindrical fuel column requires the following information:

- operating power of the fuel rod,
- thermal conductivity of the fuel,
- flux depression across the fuel radius, and
- fuel temperature at a known position.

A computer code, MAIN, was used to calculate radial temperature profiles. A listing and description of the code is provided in Appendix A.

The time-averaged power output of the fuel was used in these calculations and we selected only data in which the power histories varied less than 15% from the time-averaged power. The thermal conductivity equation derived by Lyons, et al., 76,77 for 95% TD UO₂ was used, along with the Maxwell-Euken^{78,79} relationship to account for effects of porosity on UO₂ thermal conductivity. Flux depressions for fuel with enrichments less than 4 wt% U-235 were estimated by use of a flux depression subroutine from the GAPON-THERMAL-1 code.⁸⁰ For enrichments greater than 4 wt% U-235, we have used a method proposed by Robertson.⁸¹ Good agreement is obtained in comparing these two methods for calculating flux depressions

with a more sophisticated neutronics code, THERMOS.⁸² One of the criteria set down in Table 2 for the selection of gas release data was that fuel temperatures must be obtained by the use of thermocouples or from the observation of microstructural changes in the fuel such as equiaxed and columnar grain growth. The temperatures associated with equiaxed and columnar grain growth boundaries are somewhat uncertain with the following temperature ranges having been proposed in the past:¹⁰,¹⁶,⁸³⁻⁸⁵

- 1300 1500°C for equiaxed grain growth
- 1600 1800°C for columnar grain growth

Grain growth has been reported for higher temperatures than those listed above; however, the time-temperature relationship for grain growth at short times can be used to explain the differences. Hausner 6,67 has reported out-of-reactor equiaxed grain growth results for pellets fabricated by 5 different procedures. These results were obtained from tests performed at temperatures between 1900-2300°C and times of 100 hours or less. Due to the different grain growth characteristics of pellets from each fabrication method, Hausner used the data to develop a time-temperature relationship for each of the 5 groups. An extrapolation of these relationships to lower temperatures and longer times indicates that grain growth is possible at 1400-1500°C for times between 10 and 500 hours.

Ainscough, et al. 83 have indicated that equiaxed grain growth asymptotes to a limiting grain size for a specific temperature at relatively long times (200-700 hours) and that while out-of-reactor grain growth results agree qualitatively with in-reactor results, the latter will have smaller limiting grain sizes due to the retarding effect of fission products with increasing burnup. Ainscough presents in-reactor data that show for temperatures of 1300° C, 1400° C and 1500° C the limiting grain sizes are 7.8μ , 11.5μ and 16.5μ respectively. Thus an initial grain size between $6-8\mu$ would require a temperature of $1350-1400^{\circ}$ C for the onset of grain growth to be observed. Similarly, an initial grain size of $12-14\mu$ would require a temperature of $1450-1500^{\circ}$ C. It should be pointed out, however, that the assumptions used

by Ainscough to obtain in-reactor fuel temperatures were not available, making it impossible to estimate the uncertainties in these temperatures.

The initial grain sizes for 24 of the 45 selected data points were obtained. They vary between 4 to 37μ with a mean of 13μ . If a dependency existed between initial grain size and equiaxed grain growth temperature we would expect to over-predict temperatures and gas release for a small grained fuel and under-predict temperatures and gas release for a large grained fuel by choosing a 1400°C temperature for equiaxed grain growth (as we have done below). However, we have not observed such an effect over the range of the data. This does not mean that no such dependency exists because other sources of error may be obscuring this effect. It should also be pointed out that we do not have initial grain sizes for nearly half of the data points.

Recommendations by other investigators^{10,16,84} for an equiaxed grain growth temperature, irrespective of initial grain size, indicates that a value between 1400 and 1500°C is the most consistent.

Christensen⁸⁵ has presented the most reliable in-reactor measurements for a columnar grain growth temperature providing a mean temperature of $1648^{\circ}\text{C} \pm 62^{\circ}\text{C}$ (2σ) for 40 hours irradiation. These data were obtained from three capsules irradiated with three thermocouples each. The thermocouples were located at various radii on the fuel mid-plane, providing an accurate means of temperature measurement for grain growth.

For further insight into the selection of temperatures for grain growth, an analysis was performed to determine the temperature difference between the columnar and equiaxed boundaries. Equiaxed and columnar grain growth measurements from CEA-R-3358 16 and CVNA-142 84 capsule experiments were used in the analysis. The mean of these data gave a temperature difference of 300°C with a 1σ uncertainty of 80°C.

Considering the above facts,

- the most consistent values quoted for equiaxed grain growth are between 1400-1500°C.
- a best estimate for columnar grain growth is ∿1650°C, and

BNWL-1875

• the temperature difference between columnar and equiaxed grain growth temperatures is $\sim 300^{\circ}\text{C}$.

We have selected 1400°C and 1700°C as the temperature boundaries for equiaxed and columnar grain growth, respectively.

As will be discussed later in Correlating the Model to the Data, gas release data from experiments wherein thermouples were used to measure fuel temperatures agree quite well with gas release data wherein grain growth boundaries were used to infer fuel temperatures. The good agreement indicates that the above estimates of grain growth temperatures are satisfactory.

As stated before, earlier attempts at calculating a radial temperature profile for gas release data were based on assumptions as to the gap conductance of the operating fuel rod. However, the uncertainties in estimating gap conductance can lead to errors as large as 500°C in centerline temperatures, while the errors associated with microstructural and thermocouple measurements can lead to errors (1σ) in centerline temperatures of ~ 120 °C and ~ 80 °C respectively (power and 100002 thermal conductivity uncertainties are also included in these 1σ 00 estimates). Because of the large error associated with assumed gap conductances, the latter two methods (microstructure and thermocouple measurements) were used to determine fuel temperatures rather than the less precise method of estimating gap conductance.

3.3 MODELS REVIEWED FOR HIGH TEMPERATURE GAS RELEASE

Existing models for gas release can be arranged into four categories:

- those that correlate gas release against rod <u>averaged</u> conditions (either average heat rating or average temperature);
- 2. those that describe the movement of fission gas within the fuel solely on theoretical considerations;
- those that correlate gas release against <u>local</u> operating conditions of the fuel;
- 4. and those that use an effective <u>diffusion parameter</u>, D; to correlate gas release against a fuel temperature and time.

3.3.1 <u>Volume Averaged Fuel Temperature</u>

Models⁵ based on rod volume-averaged fuel temperatures are undesirable because actual gas release is dependent on local conditions and is a nonlinear function of temperature. Since temperatures vary both axially and radially within a cylindrical fuel column, gas release will also vary in the axial and radial directions.

If axial temperatures are held relatively constant (as was done with the selected data) and gas release is correlated against a local volumeaveraged temperature in the radial direction, errors can still exist because the volume-average temperature is strongly weighted by the outer surface of the fuel, where temperatures are between 400 - 1200°C. It has been shown that gas release below 1200°C is negligible, 8,25 while gas release from fuel in the columnar grain growth region (1700°C and above) has been shown^{9,10,22} to range from 70 - 95%. The central portion of the fuel, however, will have less influence on volume-average temperature. Gas release can be correlated against volume-average temperature with some degree of success because fuel surface temperatures for the majority of gas release data are in a narrow temperature range between 350 - 700°C, and for similar fuel capsule designs an increase in fuel surface temperature will correspond to a similar increase in the center temperature. It is still possible, however, that such a model can lead to significant errors in the prediction of gas release because the variable that is correlated against gas release, volume-average temperature, is strongly influenced by a temperature region which has negligible gas release. For example, it is possible to use a fuel capsule design which would provide a fuel surface temperature of 400°C and a centerline temperature of 2000°C, resulting in a volume-average temperature of 1113°C. Correspondingly, a capsule with the same volume-average temperature, but a lower heat rating, could have surface and centerline temperatures of 750 and 1515°C, respectively. The former capsule design will release a larger amount of gas because it has a substantial portion of fuel in the temperature region, 1700°C and above, while the latter design with a centerline of 1515°C has essentially no fuel in this high gas release zone.

An experiment performed by W. J. Zielenbach, et al., 27 illustrates the high gas release rates exhibited in the temperature region of 1700°C and above. In this experiment several $\rm UO_2$ capsules were irradiated with extremely high fuel surface temperatures (1200-1900°C). Capsules with fuel surface temperatures between 1700 - 1800°C and centerline temperatures between 1900 - 2100°C released 70 - 95% of their gas. The volume-average temperatures of these capsules were approximately 1900°C. Using the volume-average temperature model of Hoffman and Coplin, 5 one would estimate that these capsules should release around 40% of their gas. This example points out the errors that can be encountered in applying the volume-average temperature model to a fuel design that is not typical of the data used to develop the model.

The models based on rod average heat rating⁶ have some obvious short-comings in that fuel temperatures can vary significantly for different fuel rod designs at the same heat ratings. Data from different fuel rod designs correlated in this manner almost always have a large amount of variability. These models also have the same problems as volume-average temperature models, in that gas release is nonlinearly dependent on local conditions of the fuel, making a correlation based on averaged conditions subject to additional errors.

3.3.2 Theoretical Models

Using a theoretical model⁷ to describe the movement of fission gas within the fuel would be an ideal way to predict gas release; however, gas release on a theoretical basis has proven to be an extremely complex subject with many controlling parameters (both material and operating). This approach requires a rather large computer program just to simulate gas release and knowledge of a large number of physical parameters, which currently makes it impractical for a wide range of fuel designs. Also, it still remains to be proved that such a model can be used with a high degree of confidence and without any compensating assumptions to bring the model into agreement with the data.

3.3.3 Local Temperature Distribution

Empirical models¹ based on the local temperature distribution within the fuel are usually correlated against two different types of experiments: those experiments that measure local fission gas concentrations within the fuel by drilling small cores of fuel and measuring the retained gas, and those that measure the gas released from irradiated fuel capsules. The local temperature model can be semiquantitatively checked against the former type of experimental data; however, there is a large degree of variability within the retained gas data so that the accuracy of a model based entirely upon these data is questionable. A major source of variability in both types of data is in the estimate of the fuel temperatures and the variability of temperatures over the in-reactor irradiation history.

3.3.4 Effective Diffusion Coefficient Model

The use of an effective diffusion parameter, D', to empirically fit a diffusion model against gas release was first used by Booth² and has subsequently been used by other investigators^{3,4} to describe both in-reactor and out-of-reactor gas release. Out-of-reactor data were not used in the present study; consequently, further discussions in this section are directed toward in-reactor data. Booth's derivation of this simple diffusion model from Fick's equations for volume diffusion depended on the assumption that an equivalent sphere can be used to approximate the boundary conditions for gas release. The approximate solution of Booth's model for small release fractions (F < 0.2) is:

$$F = 4\sqrt{\frac{D't}{\pi}}$$

In this expression F is the fractional release of stable fission gas, t is the irradiation time and

$$D' = \frac{D}{a^2}$$

where a is the radius of the equivalent sphere and D is the diffusion coeffecient used by classical diffusion theory. From diffusion theory

$$D = D_0 e^{-Q/RT}$$

where D $_0$ is a constant, Q is the activation energy, R is the gas constant and T is temperature. When D' is correlated against temperature the a 2 term is usually included in the D $_0$ term.

From this simple diffusion model it is predicted that gas release is a function of both temperature and time; however, as discussed in the section on Effects of Density and Burnup, the data that met our criteria show no burnup dependence (i.e., no time dependence). Disregarding the time dependence of a diffusion model still leaves the question as to what fuel temperature should be used to obtain the effective diffusion coefficient. The most logical approach would be a volume averaged temperature, but as discussed in the section on Volume Averaged Temperature errors can be introduced when fuel temperatures are volume averaged and correlated against gas release.

A local temperature model could be used wherein release fractions have been determined for specific temperature regions. From these fractions a D' could be determined for each temperature region. This method would be helpful in determining what diffusion mechanisms are controlling gas release and this should be pursued further to obtain a better mechanistic understanding of the process. It would be expected that different mechanisms will dominate within the various temperature regions.

Other approaches using the diffusion model are based on a separate determination of a^2 which is assumed to be a function of the surface-to-volume ratio which is in turn a function of fuel density. The gas release data used in this study did not show any dependence on fuel density.

Many of the models discussed above have been correlated against a substantial amount of data, but because a large amount of variability is associated with the data the uncertainties in the models are quite large. As stated earlier, the variability is often the result of poorly characterized data (e.g., with regard to temperatures, powers, 0/M ratios, etc.).

3.4 SELECTION OF HIGH TEMPERATURE GAS RELEASE MODEL

The model chosen to describe the selected gas release data is based on local temperatures. We have selected the following regions within the fuel to describe high temperature gas release:

- columnar grain growth region, 1700°C and above
- equiaxed grain growth region, 1400 to 1700°C
- no microstructural change, 1200 to 1400°C

The form of our model is based on both experimental data and current theories for high temperature gas release. Gas release below 1200°C is described by the low temperature gas release model.

3.4.1 Columnar Grain Growth Region

Measurements of the fission gas concentrations within the columnar grain growth region indicate that between 70 to 95% of the gas produced in this region is released. 9,22 Several investigators 17,18 have proposed that the columnar grain growth region is a region of high mobility for pores containing gas, i.e., porosity from the fabrication process or that created by the accumulation of gas. These investigators suggest that the gas-filled pores become lenticular in shape and move up the temperature gradient toward the central void. Whatever the explanation for gas release in this region, it is apparent that the physical conditions within the region of columnar grain growth enhance gas release, as evidenced by the large fraction of gas released in the region.

3.4.2 Equiaxed Grain Growth Region

Measurements of the fission gas concentrations within the equiaxed grain growth region have indicated that between 10 to 40% of the gas produced in this region is released. 9,22 Gas atoms and clusters of gas atoms within this region should be somewhat mobile because if the grain boundaries attain some degree of mobility as evidenced by grain growth there must be enough thermal energy present to allow some of the trapped fission gas to break away from the weaker trapping sites and find its way to an open pore.

3.4.3 Region of No Microstructural Change

Fission gas concentrations in the 1200 - 1400°C region indicate that less than 10% of the gas produced in this region is released. ^{9,22} The experiments performed by Lewis²² indicate that for tempertures below 1200°C, nearly 100% of the gas is retained. Several other investigators ^{8,25} have also concluded that the diffusion of fission gas below 1200°C is negligible. These conclusions are based on gas release data from fuel rods with centerline temperatures of less than 1200°C.

3.4.4 Description of Model

We have developed the following model for high temperature gas release:

$$F = AX_1 + BX_2 + CX_3$$

where

F = fraction of gas released

 X_1 = fractional amount of fission gas produced in the temperature region 1200 to 1400°C

 X_2 = fractional amount of fission gas produced in the temperature region 1400 to 1700°C (region of equiaxed grain growth)

 x_3 = fractional amount of fission gas produced in the temperature region 1700°C and above (region of columnar grain growth)

A = fraction of gas released from region X_1

B = fraction of gas released from region x_2

C = fraction of gas released from region X_{3}

The fractional amount of gas produced in each of these regions (X_1, X_2) and (X_3) is estimated by taking the ratio of the cross-sectional area between the temperatures that bound the region to the total cross-sectional area of the pellet. The effects of flux depression are also included. The cross-sectional areas of each temperature region are obtained from the radial

temperature profiles that have been determined from the temperature data (thermocouple or microstructural) associated with each data point, as explained in the section on Data Reduction.

3.5 CORRELATING THE MODEL TO THE DATA

Using a multiple linear regression code, we fit the model to the reduced data $(X_1, X_2 \text{ and } X_3)$ and obtained estimates of the coefficients A, B, and C associated with each temperature region. In the first attempt at a regression analysis, it was discovered that the X_1 and X_2 variables are linearly dependent on each other (i.e., $X_1 = GX_2$). Regressing X_1 against X_2 we find that G = 0.727. This dependency arises from the fact that if two temperature radii, such as the 1700°C and 1400°C boundaries used to obtain X_2 , are known within the radial cross-section of the fuel, then any other temperatures and their radii can be defined. A solution of the heat transfer equations will show that X_1 is linearly dependent on X_2 , but this is not covered here.

If data were available with centerline temperatures less than the upper boundary of X_2 (i.e.,<1700°C), then X_1 would be independent of X_2 since only one temperature boundary defines X_2 and thus the coefficients A and B could be determined through regression analysis. Because all of the selected data contain centerline temperatures greater than 1700°C, we cannot separate these two coefficients due to the dependency between X_1 and X_2 . Consequently, the regression analysis was performed with the terms X_2 and X_3 to obtain the coefficients B' = 0.177 and C = 0.807 with a correlation coefficient of 0.980 and a residual standard deviation of 0.047 in fraction of gas released. The coefficient B' obtained in our regression analysis is a combination of the A and B coefficients of our model. Since X_1 can be related in terms of X_2 (over the range of our data) with the linear relationship X_1 = GX_2 (as discussed above), our model can be expressed in the following manner:

$$F = A (GX2) + BX2 + CX3$$

The coefficient B' obtained from our regression analysis can be expressed by

$$B' = AG + B$$

and since B' = 0.177 and G = 0.727 a value for either A or B can be chosen on the basis of previous experimental evidence to get the other coefficient. As discussed earlier, experiments^{9,10,22,26} have been conducted in which small cores of fuel were ultrasonically drilled at various distances from the centerline of the pellet to determine the concentration of retained fission gas across the pellet radius. These experiments indicate that less than 10% of the gas produced in the 1200 - 1400°C range (X_1) and 10 - 40% in the region of equiaxed grain growth (X_2) is released. To be consistent with this evidence, we have selected a 5% release for region X_1 which yields 14.1% for the equiaxed region (i.e., B = B' - A·G = 0.177 - 0.05 (0.727) = 0.141) to obtain our full model:

$$F = 0.050 X_1 + 0.141 X_2 + 0.807 X_3$$

Estimating the partitioning of the A and B coefficients in terms of B' does not compromise the accuracy of estimating gas release for fuel operating with centerline temperatures greater than 1700°C. Gas release for fuel with centerline temperatures between 1200°C and 1700°C is between 1% to 4%, as calculated from the high temperature model. An error in partitioning A and B can result in a maximum error of only 1% release for the above temperature range, even if there are gross errors in our partitioning of the A and B coefficients (as in the extreme case where A = 0.0 and B = 0.177). While the possible percentage error is great, it is doubtful that gas release measurements in these low release regions can be measured with greater accuracy. Also, in most fuel performance calculations it is not critical if the release rate is predicted to be 2% but is really only 1%; however, it does become critical if the release rates are predicted to be 30% but really are around 10%. Consequently, it is the higher gas release term (0.807 X_{2}) which is of greatest interest and has the largest influence on calculations for steady state operation. It should also be noted that the 80.7% release predicted in this analysis for the columnar grain growth region (X_3) agrees

quite well with the core drilling experiments which show that 70 - 95% of the gas in this region is released.

Predicted percent release as determined from the model is compared with the experimental data in Figure 1. If perfect agreement existed between the model and the data, all of the points would lie on the 45° sloped line which begins at the origin. The upper dashed line in this figure is the upper 95% confidence limit of our data which can be represented with the following relationship:

$$F = 0.050 X_1 + 0.141 X_2 + 0.807 X_3 + 1.68 (0.002112 + 0.0052 X_2^2 - 0.00269 X_2 X_3 + 0.00217 X_3^2$$

where F, X_1 , X_2 and X_3 are the same variables used in the best estimate model.

The statistical significance of this upper limit is that you can be 95% confident that future gas release data, which meet the criteria we have used in selecting data, will lie below this line.

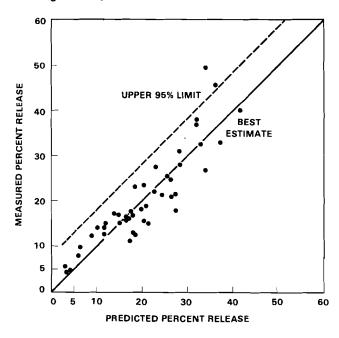


FIGURE 1. A Comparison of the High Temperature Release Model and the Data

As a check on the validity of our grain growth boundary temperatures, we compared the 41 data points based on grain boundaries to estimate fuel temperatures to the 4 data points that were obtained from thermocouple measurements. Good agreement between these two types of data is illustrated by placing a $l\sigma$ band around the data in Figure 1 and noting that three of the four thermocouple data lie within this band and the fourth within a $l.5\sigma$ band. This would indicate that our selection of grain growth temperatures is satisfactory.

A comparison of our model to models that have been proposed by other investigators^{1,5} is shown in Figures 2 and 3. Figure 2 shows the data and the relationship Hoffman and Coplin used in their volume-average temperature model. Also included is the proposed high temperature model expressed in terms of volume-average temperature, which was accomplished by selecting a typical commercial BWR fuel rod* and varying the power ratings while holding gap conductance constant at 1000 Btu/hr-ft 2 °F to insure the same fuel surface temperature as a function of power. The resulting temperature distributions were used to predict a value for gas release from our model and to calculate a volume-average fuel temperature to be used in plotting the curve for our high temperature model in Figure 2. This figure indicates that the scatter in the data used by Hoffman and Coplin is much larger than the scatter in the data used for the model developed here, as represented by the 95% confidence band. The 95% confidence band in Figure 2 bounds 95% of our data. This comparison provides additional support for the fact that the parameters we have controlled in the selection of the data do indeed lead to substantial amounts of variance between gas release data. The relationship developed here is also less conservative for volumeaverage fuel temperatures between 900 and 1525°C, which is the operating range of the peak power rods within most commercial LWR's. For example, at a volume-average temperature of 1200°C (fuel operating at ∿13 kw/ft) the Hoffman and Coplin model would predict a 24% increase while the best estimate model developed here would predict 13%.

^{*}Changing the fuel rod design will shift the curve represented by the model. In most cases the shift is small for a particular reactor type because fuel rod designs are usually similar.

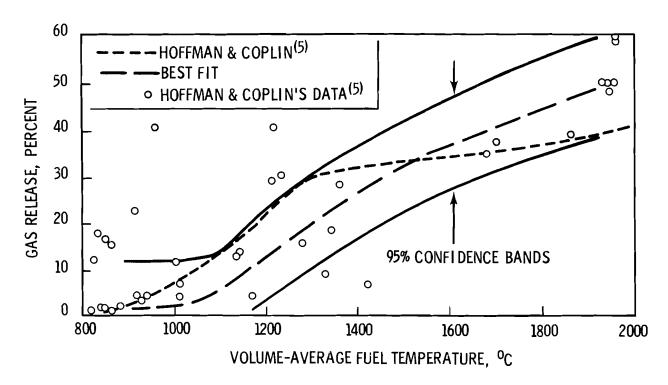


FIGURE 2. A Comparison of the High Temperature Release Model with Hoffman and Coplin's Volume-Average Temperature Model

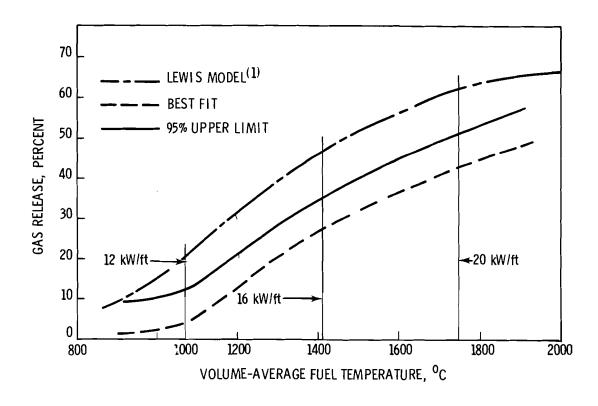


FIGURE 3. A Comparison of the High Temperature Release Model with Lewis' Model

Figure 3 shows a comparison of our model with the Lewis¹ model in terms of a volume-average temperature for a typical BWR fuel design. As seen here, the Lewis model is much more conservative than even the 95% upper limit of our relationship. This is not too surprising since Lewis intended the model to be conservative; however, it seems to be overly conservative in terms of the data and model reported here.

3.6 EFFECTS OF DENSITY AND BURNUP

There appears to be no general agreement on the effects of density and burnup on <u>high temperature</u> gas release for LWR $\rm UO_2$ fuel. The range of the data with respect to the parameters of theoretical density and burnup is 91.3% TD to 98.0% TD and 400 MWD/MTM to 18,300 MWD/MTM. To determine if either of these two parameters have an effect on the data, a linear term was added for each of these parameters to the temperature dependent model already derived, as shown below:

$$F = AX_1 + BX_2 + CX_3 + DP$$

and $F = AX_1 + BX_2 + CX_3 + KM$

where A, B, C, X_1 , X_2 and X_3 are the terms already described in the temperature dependent model and

D = coefficient describing the linear dependence between density and gas release

P = percent of theoretical density

K = coefficient describing the linear dependence between burnup and gas release

M = burnup

Fitting these two models against the data has shown that the linear coefficients for burnup and density, D and K, have a large amount of variance. Standard deviations associated with the linear coefficients, $\sigma_{\rm D}$ and $\sigma_{\rm K}$, are approximately equal to the coefficients themselves. Using a t test to determine the probability that

D = 0 and K = 0 (i.e.,
$$t = \frac{D}{\sigma_D} \simeq 1$$
 and $t = \frac{K}{\sigma_D} \simeq 1$)

shows that there is $\sim 50\%$ chance that D = 0 and K = 0 and thus indicates that neither burnup nor density has a significant influence on the data. If burnup or density effects were significant but nonlinear, the linear terms would still have been significant because they would have described some of the error structure in the data contributed by these two variables and resulted in lower values for σ_D and σ_K . As an additional check, the residual variance of each individual data point was plotted against both burnup and density and no structure was apparent within the data that might indicate a dependency on these two variables.

Although the data we have accumulated do not indicate any dependency between gas release and the two variables, burnup and density, this does not mean that such dependencies do not exist. There may be a small secondary effect within the range of our data; however, the error from other sources within the data obscures these effects. Also, it should be noted that the data covers the range of UO_2 densities 91.3 to 98.0% TD. Experimental evidence indicates that fuels with densities less than 90% TD release more gas than fuels with densities greater than 90% TD. In regard to a possible burnup dependency, it has been proposed by several investigators that the fission gas bubbles retained at the grain boundaries in fuel operating below 1700°C may become numerous enough to link up at high burnups and form a network by which gas can escape to an open pore and be released. Most of the data we collected from the literature have burnups between 4,000 MWD/MTM and 12,000 MWD/MTM, with a few data points going out to 18,000 MWD/MTM. We could not obtain data from well defined experiments on fuel designs typical of commercial thermal reactor fuel for burnups greater than 20,000 MWD/MTM. The need for such high burnup data is apparent since the high burnup rods in presently operating reactors may reach burnups of 40,000 - 50,000 MWD/MTM.

4.0 LOW TEMPERATURE GAS RELEASE MODEL

4.1 DEVELOPMENT OF THE MODEL

Low temperature gas release is dominated by a knock-out mechanism^{28,29} which is caused by a fission fragment passing through the fuel surface and ejecting a portion of the atoms near the surface. The material knocked out includes the matrix material and any trapped gas in that location. The amount of knock-out is a function of specimen surface area and irradiation dose.

The low temperature gas release model proposed by Bellamy and Rich was modified for this correlation. The Bellamy and Rich model was selected because it was the only one found in the literature that supplied and adequately described data applicable to LWR UO₂ fuel. The model expresses low temperature gas release in terms of the effective surface-to-volume ratio of the fuel, the fission rate, and the irradiation time in the following manner:

$$F = \frac{S}{V} \ell \left[\frac{3}{4} - \frac{3}{vft} \left\{ 1 - exp \left(-\frac{1}{4} vft \right) \right\} \right]$$
 (1)

where

F = fraction of gas release

S/V (%TD,BU)= effective surface-to-volume ratio of the fuel (a function of density and burnup), (cm^{-1})

 ℓ = recoil range of fission fragment (7 x 10⁻⁴ cm)

v = volume of fuel ejected from the fuel surface by "knock-out" (2 x 10^{-21} cm³)

f = fission rate, (fissions/cm³/sec)

t = irradiation time, (sec)

This relationship was derived by Bellamy and Rich from gas release data obtained from fuel rods over a wide range of burnups (7,000 - 43,000 MWD/MTM).

Fuel centerline temperatures were less than 1250°C for all the data, which is consistent with the high temperature model that assumes diffusional release is insignificant below 1200°C. Their data show a marked increase in gas release for burnups greater than 26,000 MWD/MTM. An experiment performed by Blieberg, et al., 30 with flat plate UO₂ fuel elements also indicated that low temperature gas release increases by a substantial amount at high burnups. The increase is believed to arise partly from the interconnection of grain boundary gas bubbles and partly from the fracture under thermal stress of grain boundaries weakened by gas bubbles which increases the effective surface area of the fuel. This behavior is substantiated by the appearance of fuel structures at high burnups which show extensive intergranular porosity and grain boundary cracking. A plot of the effective surface-to-volume ratios, as determined from the data and equation of Bellamy and Rich for low temperature gas release, is shown in Figure 4. The data in Figure 4 are from fuel with an as-manufactured

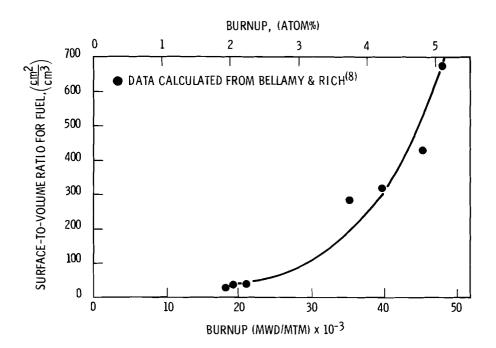


FIGURE 4. UO2 Surface-To-Volume Ratios as a Function of Burnup

density of 98% TD. The increase in $\frac{S}{V}$ fits an exponential function fairly well for burnups of 17,000 MWD/MTM and greater by the following relationship:

$$\frac{S}{V}$$
 (at burnup X) = $\frac{S}{V}$ (initial) 0.1938 exp (+.9391X) (2)

where

 $\frac{S}{V}$ (initial) = initial surface-to-volume ratio (a function of the fuel density)

X = burnup in atom percent

The functional relationship given in Figure 5 for the $\frac{S}{V}$ ratio in terms of the fuel as-manufactured theoretical density (i.e., $\frac{S}{V}$ [initial]) was taken from Lewis. By substituting the relationship for the surface-to-volume ratio as a function of burnup in Equation 2 into Equation 1, we can compare results from the low temperature release model with the data of Bellamy and Rich, as shown in Figure 6. The model predictions agree very well with this set of data. We have not attempted to correlate the low temperature release model to a large volume of data as was done with the high temperature release model because of the small effects of low temperature gas release on gap conductance calculations. This approach makes the accuracy of the model somewhat uncertain; however, in our opinion the model adequately describes low temperature gas release to within $\pm 1\%$ release.

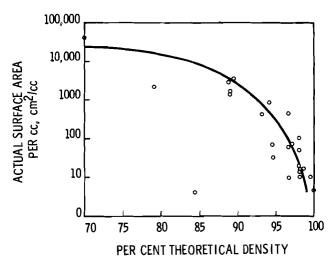
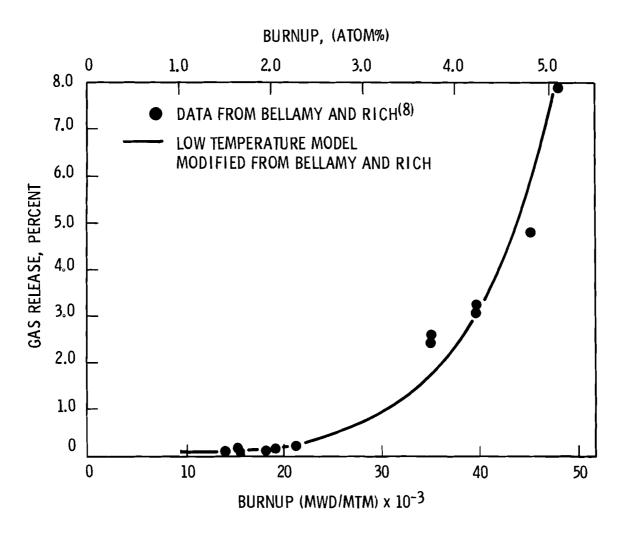


FIGURE 5. Measured Surface Area (BET) as a Function of Percent Theoretical Density for Sintered UO₂



 $\begin{tabular}{lll} \hline FIGURE~6. & A Comparison of the Low Temperature~Gas~Release\\ \hline Model~and~the~Data \\ \hline \end{tabular}$

5.0 LIMITATIONS OF THE GAS RELEASE MODELS

Neither model should be used beyond the range of data unless the extrapolated results can be checked against other sources of data. The models should not be used where a significant volume of the fuel is molten (>20%), because the molten fuel may release more than the maximum 80%. Although three data points used in the correlation have temperatures above the melting point of the fuel and they agree quite well with the model, these data points were from fuel rods with less than 20 volume-percent of the fuel molten. The high temperature model should also be restricted to the density and burnup range of our data, 91.3 - 98.0% TD and 400-18,300 MWD/MTM respectively. Although no density or burnup dependencies were found inside the range of our data there may be some strong dependencies outside this range, as was discussed in the section of Effects of Density and Burnup. The low temperature release model is limited to temperatures <1200°C and burnups <45,000 MWD/MTM and should be used in combination with the high temperature release.

Both models should belimited to steady state fuel operation until gas release data become available for significant power transients of a short time duration (e.g., accident transients). However, the models can be used for normal operating power changes, using the release algorithm developed by Notley⁸⁸ which is based on experimental evidence from Soulhier and Notley²⁴ providing the new power level maintains an equilibrium value for several hours.

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APPENDIX A

DESCRIPTION AND LISTING OF THE PROGRAM MAIN

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DESCRIPTION AND LISTING OF THE PROGRAM MAIN

The computer code MAIN was developed to compute radial temperature profiles across cylindrical fuel specimens given a location and a temperature within the fuel. The fuel was divided into 50 annular rings and the temperature difference across each increment was calculated assuming that the thermal conductivity and volumetric heat generation are constant within each ring.* The heat balance on an annular ring can be written as:

(heat in) + (heat generated) = (heat out)

or
$$q_{r_i} + 2\pi \dot{q} \int r dr = 2\pi r \frac{dt}{dr}$$

where q_{r_i} = heat entering annular ring at r_i per unit length (calculated from the total heat generation rate of the fuel, volume of fuel between center line and r_i , and the flux depression)

 r_i = inside radius of annular ring

q = heat generation for this particular annular ring
 (calculated from the total heat generation
 rate of the fuel, volume of annular ring, and the
 flux depression).

k = thermal conductivity of the fuel

r = any radial position within the ring

By integrating this expression with respect to temperature and radius the following equation is found.

^{*}This assumption is valid because the size of the rings are small enough that heat generation is relatively constant across them and because the ΔT across each ring is small and thus the variation of thermal conductivity is also small.

$$\int_{T_{i}}^{T_{0}} dT = \frac{1}{K} \left[\left(\frac{\dot{q}r_{i}^{2}}{2} - \frac{q_{r_{i}}}{2\pi} \right) \ln \frac{r_{0}}{r_{i}} - \frac{\dot{q}}{4} \left(r_{0}^{2} - r_{i}^{2} \right) \right]$$

Using this equation and knowing the temperature at a node in the fuel (r known, T known) the temperature at the nearest outer boundary of an annular ring (r 0, T 0) can be calculated as follows: an average temperature of the ring is assumed; an appropriate thermal conductivity value is assigned; temperature drop across the increment and, therefore, average temperature is calculated; and the calculated average temperature is compared to the assumed value. If the assumed and calculated values do not agree, a new value is assumed and the process is repeated. When agreement is reached to within 1° F the process proceeds to the next annular ring and continues in this manner until the outside surface of the fuel is reached and the temperature profile from r known and T known to the surface of the fuel is known. A similar method is then used to obtain the temperature profile from r known to the center line of the fuel.

The input data required to run the program is listed below:

Variable	Variable Name	Location	Comments
Linear Power (Kw/ft)	Р	Cols. 1-10	
Outer Pellet Radius (in.)	RFS	Cols. 11-20	
Inner Pellet Radius (in.)	RVIOD	Cols. 21-30	
Pellet Density	DEN	Cols. 31-40	Fractional density of the fuel pellet $\left(\frac{\% \text{ T.D.}}{100}\right)$
Enrichment	FR35	Cols. 41-50	Weight fraction of the U which is U-235

Temperature (°F)	TG	Cols. 51-60	Temperature within the fuel
No. of Data Points	FRACRG	Cols. 61-70	In terms of the fraction of pellet radius RTG RFS
Input for Flux Depression	NFLUX	Cols. 71-75	If this is left blank the code will calculate its own flux depression values.

The data listed above are contained on the first card in columns 1 thru 75. If flux depressions are to be input (recommended for enrichments \geq 4%) NFLUX additional cards are required with each card containing a diameter (inches) in columns 1-10 and the relative neutron flux at that diameter in columns 11-20. The cards must be arranged so that the diameters are either in ascending or descending order. As many cases can be input as desired with the flux depression cards (if desired) following each data card.

A listing of the code is given here along with a sample problem.

	PROGRAM MAIN	74/74	0PT=1	FTN 4.1+REL	06/20/74	17.45.03.
		DIMENSION RV (8,100),BB(8,100),Q(APE5=INPUT,TAPE6=OUTPUT) 50),R(60),TT(60),TS(60),DUM(60),D		2 3
	,	KUM(60),QIN(60		-D)+.5)))+((38.24/(402.4+T))+	MAIN Main	4 5
5	,		(T+273.) **3)))		MAIN	6
•		CONTINUE			MAIN	7
	-		RFS, RVOID, DEN, FR35	TG, FRACRG, NFLUX	MAIN	8
		IF(P.LE.D) GO	TO 999		MAIN	9
		PI=3.14159			MAIN	10
10		NF=11			MAIN	11
		FR38=(1-FR35)			MAIN	12
		OFS=2*RFS			MAIN	13
		DENSIT=10.97 IF (NFLJX) 90	DA 50		MAIN	14
15	94		,90,00 ENSIT,FR35,FR38,DFS	. DV1	MAIN Main	15 16
1)	70	GO TO 8B	E43114F K354F K3040F3	, KVI	MAIN	17
	60		RV(I, J), I=1, 2), J=1,	4FLUX)	MAIN	18
		NF=NFLUX			MAIN	19
	80	CONTINUE		•	MAIN	20
20	C	CALCULATE THE	VOLUME HEAT GENERA	TION IN FUEL	MAIN	21
		QTOT=P+3413.			MAIN	22
	_		*(RFS**2-RV0ID**2))		MAIN	23
	С		OF N NODES OF EQUA	. THICKNESS, RADII IN FEET	MAIN	24
25		N=50 AA1=N			MAIN	25
۷ ۶		OR=(RFS-RVOID	1 / 8 8 1 / 1 2		MAIN Main	25 27
		R0=RFS/12.	,, ,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,		MAIN	28
		33 100 I=1,N			MAIN	29
	C	R IS IN FEET			MAIN	30
3 O		R(I)=R0-DR*(I	-1)		MAIN	31
		RR=(2+2(I)-D	R) +12.		MAIN	32
		RATIO=TERP(RR	R,RV,2,NF)		MAIN	33
		ROR=R(I)-DR			MAIN	34
35	400		**2-RDR**2)*RATIO*Q	• 13	MAIN	35
3 2	C	CONTINUE	COUMINATION OF SPRO	R IN HEAT GENERATION	MAIN Main	36 37
	U	SUMQ=0.	CCONDENTION OF ERRO	TH HEAT GENERALION	MAIN	37 38
		33 110 I=1.N			MAIN	39
	1 10	SUMQ=SUYQ+Q(I)		MAIN	40
40		CORR=QTOT/SUM	Q		MAIN	41
		CORR1=CORR			MAIN	42
		33 120 I=1,N			MAIN	43
	1 20	Q(I)=CORR+Q(I			MAIN	44
45		QIN(1)=QTOT-Q DD 801 I=2.N	(1)		MAIN	45
49	8.04	JIN(I)=JIN(I-	11-0(1)		MAIN Main	46 47
	201	DO 130 I=1.N	1,-4(1)		MAIN	48
	130	R(I)=RFS/12	DR*(I-1)		MAIN	49
		RGRAIN=FRACEG	*RFS/12		MAIN	50
50		00 140 I=1.N			MAIN	51
			GRAIN) GO TO 150		MAIN	52
		CONTINUE			MAIN	53
	150	CONTINUE	TN-0/T))		MAIN	54
5 5		ROGZ=ABS (RGRA	1N-K(1)) 001) GD TO 155		MAIN Main	55 56
		RDG1=ABS(R(I-			MAIN	57
			DG2) 50 TO 160		MAIN	58

	PROGRAM MAIN	74/74	0PT=1	FTN	4.1+REL	06/20/74	17.45.03.
	155	CONTINUE				MAIN	59
	•	RGRAIN=R(I)				MAIN	60
6 0		M=I				MAIN	61
		50 TO 170				MAIN	62
	1.60	RGRAIN=R(I-1	•			MAIN	63
	100	4=(I-1)				MAIN	64
	170	CONTINUE				MAIN	65
65	C		TURE CALCULATION	IS FROM A KNOWN TEMPE	RATURE	MAIN	65
	Č		R OF THE FUEL		,	MAIN	67
	v	30 249 I=M,N				MAIN	68
		27=R(I)				MAIN	69
		ROR=R(I)-DR				MAIN	70
70		IF (I.GT.M) (O TO 180			MAIN	71
		TAV=TG				MAIN	72
		TZ=TG				MAIN	73
		TT(M)=TG				MAIN	74
		GO TO 198				MAIN	75
75	1 80	TAV=TT(I)				MAIN	75
		TZ=TT(I)				MAIN	77
	190	CONTINUE				MAIN	78
		TAVC=(TAV-32.				MAIN	79
		TAVK=TAVC+27				MAIN	80
8 Q		3=57.8*TCOR(MAIN	81
			E-20) GO TO 200			MAIN	82
			(RZ++2-RUR++2)-0	IN(I)/Q(I))*ALOG(RZ/	KUKI	MAIN	83 84
	200	30 TO 210 Term=0.				MAIN Main	85
9 5			(I)/(2.*PI*3)*(.5	-TERMI		MAIN	86
85	210	TAV1=(TZ+TT()		- IERHI		MAIN	87
		TTAV=TAV				MAIN	88
		DIFF=ABS(TAV	-TAV1)			MAIN	89
		IF (DIF=-1.)				MAIN	90
90	220	TAV=TAV1	2.0,2.0,220			MAIN	91
•		IME=IME+1				MAIN	92
		IF (IME-10)	190,230,230			MAIN	93
	230	4RITE (5,602				MAIN	94
	240	IME=0	•			MAIN	95
95		IF (RGRAIN.G	.R(1)) GO TO 299	;		MAIN	95
		QT=QIN(4-1)				MAIN	97
		00 308 IK=2.	1			MAIN	98
		I=M-IK+2				MAIN	99
		RZ=R(I)				MAIN	100
100		RRR=(2.*R(I)	POR) *12			MAIN	101
		RDRO=R(I)+DR				MAIN	102
		RATIO=TERP(R		N. 0573		MAIN	103
	7.00	CONTINUE	*2-RDRD**2)*RATI	T-QF13		MAIN Main	104 105
405	C See	CORRECT FOR	ACC IM			MAIN	105
105	U	SUMQ=0.	400311			MAIN	107
		30 310 IK±2.	4			MAIN	108
		I=M-IK+2	•			MAIN	109
	310	SUMQ=SU1Q-Q(()			MAIN	110
110		D-TOTP = ARCC				MAIN	111
	C	BEGIN TEMPER	ATURE CALCULATION	NS FROM A KNOWN TEMPE	ERATURE	MAIN	112
	С	TO THE OUTS	IDE SURFACE OF TH	1E FUEL		MAIN	113
		JJ 320 IK=2,	1			MAIN	114
		I=M-IK+2				MAIN	115

	PROGRAM MAIN	74/74 0PT=1	FTN 4.1+REL	06/20/74	17.45.03.
115	320	Q(I)=CORR*Q(I)		MAIN	115
	,-,	00 290 IK=2.M		MAIN	117
		I=M+IK+2		MAIN	118
		RZ=R(I)		MAIN	119
		RDRO=R(I)+DR		MAIN	120
120		IF (I.LT.M) GO TO 250		MAIN	121
		TAV=TG		MAIN	122
		TZ=TG		MAIN	123
		GO TO 250		MAIN	124
	250	TAV=TT(I)		MAIN	125
125		TZ=TT(I)		MAIN	126
	260	TAVC=(TAV-32.)/1.8		MAIN	127
		TAVK=TAVC+273		MAIN	128
		C=57.8*TGOR(DEN,TAVC)		MAIN	129
		TERM= (RZ**2/(RZ**2-RDRO**2)-QIN(MAIN	130
130		TT(I-1)=TZ+Q(I)/(2.*PI*C)*(.5-TE	(H)	MAIN	131
		TAV1=(TZ+TT(I-1))/2		MAIN	132
		DIFF=ABS(TAV-TAV1) IF (DIFF-1) 290,290,270		MAIN Main	133 134
	270	TAV=TAV1			
135	270	IME=IME+1		MAIN Main	135 136
10)		IF(IME-10) 260,280,280		MAIN	137
	280	WRITE (6,602) TTAV, TAV1		MAIN	138
		IME=0		MAIN	139
	C	VOLUME AVERAGE THE TEMPERATURE		MAIN	148
140	-	CONTINUE		MAIN	141
		TSR(N+1)=RVOID		HAIN	142
		00 400 I=1.N		MAIN	143
		1=16		MAIN	144
	400	TSR(I) = RFS-((RFS-RVOID)/AA1*(BI-	1.01)	MAIN	145
145		VAFR=(TSR(1)*+2-TSR(2)*+2)*PI*((TT(1)+TT(2))=.5)	MAIN	146
		DO 410 I=2.N		MAIN	147
		VAFR=VAFR+(TSR(I)**2-TSR(I+1)**2	*PI*((TT(I)+TT(I+1))*0.5)	MAIN	148
	4 10	CONTINUE		MAIN	149
		VAVGT=VAFR/((RFS**2-RVOID**2)*PI		MAIN	150
150		VAVGTC=(VAVGT-32.)/1.8		MAIN	151
		00 420 I=1,N		MAIN	152
		8B(1,I)=TT(I)		MAIN	153
	4.20	BB(2,I)=TSF(I) CONTINUE		MAIN Main	154 155
155	420	VJLIN=(RFS**2-RV0ID**2)*PI		MAIN	156
277		R1200=TERP(2192BB.2.N)		MAIN	157
		R1400=TERP(2552BB.2.N)		MAIN	158
		21700=TERP (3092.,BB.2,N)		MAIN	159
		V1200=(R1200+*2-R1400+*2)*PI/VOL	[N	MAIN	160
150		V1700=(21700**2-RV0ID**2)*PI/VOL	[N	MAIN	161
		V1400=(R1400*#2-R1700*#2)*PI/VOL	EN	MAIN	1 62
		RR=2*R1200		MAIN	163
		RAT12=TERP(RRR, RV, 2, NF)		MAIN	164
		RAT12=RAT12*CORR1		MAIN	165
155		RRR=2*R1400		MAIN	166
		RAT14=TERP(RRR,RV,2,NF)		HAIN	167
		RAT14=RAT14+CORR1		MAIN	168
		RRR=2*R1700 RAT17=TERP(RRR.RV.2.NF)		MAIN Main	169 170
170		RAT17=TERFTRRRFRVF2FNFF		MAIN	171
		RRR=0.0		MAIN	172
				···-	- · -

	PROGRAM	MA IN	74/74	0 P T = 1	FTN 4.1+REL [6/20/74	17.45.03.
			RATO=TERP(RRR	,RV,2,NF)		MAIN	173
			RATO=RATO+COR	R1		MAIN	174
			VC012=V1200*(RAT12+RAT14)/2		MAIN	1 75
175			V2014=V1400*(RAT14+RAT17)/2		MAIN	176
				RAT17+RAT0)/2		MAIN	177
				5+4CD14+0.79889*VCD	17	MAIN	178
			TFS=TT(L)			MAIN	179
			TCL=TT(51)			MAIN	189
180			DO 500 I=1,N			MAIN	181
			TS(I)=R(I)*12			MAIN	182
			(I) TT)=(I) MUC			MAIN	183
		5.00	DOUM(I)=(TS(I	1+2.541		MAIN	184
405		560	CONTINUE			MAIN	185
185			WRITE(6,700)	P.RFS.RVOID.DEN.FR3	E TO EDACOO	MAIN Main	186
			ARITE(6,705)	P + K + 2 + K 4 O 1 11 + U E N + F K 2	5,10,FRMURU	MAIN	187 188
			4RITE(6.606)			MAIN	189
				(RV(1,J),RV(2,J),J=	(- NE)	MAIN	198
190			WRITE(6,710)	(11,5),11(2,5),5-	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	MAIN	191
1,0				VAVGT.VAVGTC.VC012.	V CD1 & - VCD1 7	MAIN	192
				(TS(I).TT(I).DOUM(I		MAIN	193
			GD TO 1		,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	HAIN	194
		999	STOP			MAIN	195
195			FORMAT (2F10.	Q)		MAIN	196
		601	FORMAT (7F10.0	,15)		MAIN	197
		602	FORMAT (1HB, "N	O CONVERGENCE TEMP	=",F7.2," CALCULATED TEMP.",F7.2	MAIN	198
)	(,/)			MAIN	199
			FORMAT (1HO.			MAIN	200
200		1	K24X,"RADIUS",	10x, TEMPERATURE",1	5x,"RADIUS",12x,"TEMPERATURE",/,24	MAIN	201
					CM)",15X,"(DEG C)",//,(24X,F6.4,9)		202
				.4,13X,F10.2,))		MAIN	203
			FORMAT (/,			MAIN	204
			(40x, "HEAT RAT		",4x,F6.2,2x,"KH/FT",/	MAIN	205
205			K49X,"FUEL RAD		7,4x,F8.5,2x, "INCHES",/	MAIN	206
			K40 X, "CENTER V		",4X,F8.5,2X,"INCHES",/	MAIN	207
			K40X, "FUEL DEN		",4X,F8.5,2X,/	MAIN	208
			K40X, "WEIGHT F		",4X,F8.5,2X,/	MAIN Main	209
210				GRAIN GROWTH TEMP. OF RADIUS FOR CGG		MAIN	210 211
210				"DIAMETER (IN)",12X		MAIN	211
			FORMAT (43X.FE		, FLOX RATIO ,//	MAIN	213
					AL INPUT DATA *******,)	MAIN	214
					LCULATED FLUX DEPRESSIONS ******)	MAIN	215
215					VALUES *******,/,)	MAIN	216
					UEL TEMPERATURE".2X.F8.2.2X."DEG.F		217
			X (".F8.2.1X."		· · · · · · · · ·	MAIN	218
					THE 1200-1400 DEG. C TEMPERATURE	MAIN	219
		1	KREGION", 2X,F8	.6,/,		MAIN	220
220		:	X24X,"FRACTION	OF GAS PRODUCED IN	THE 1400-1700 DEG. C TEMPERATURE	MAIN	221
			KREGION™,2X,F8		•	MAIN	222
					THE 1700-*** DEG. C TEMPERATURE	MAIN	223
		:	KREGION",2X,F8	.6,//,)		MAIN	224
			END			MAIN	225

	FUNCTION TERP	74/74	0 P T = 1	FTN	4.1+REL	06/20/74	17.45.11.
		FUNCTION TERP	(TT,TABLE,L,N)			TERP	2
	C	L = THE INDEX	TO THE TABLE			TERP	3
		DIMENSION TAB	LE(8,100)			TERP	4
		I=1				TERP	5
5		IF (TABLE (I,1)	.GT.TABLE(I,N)) G	O TO 110		TERP	6
		IF (TT.LE.TA	BLE(1,1)) GO TO 1	04		TERP	7
		IF (TT.GE.TA	BLE(I,N)) 50 TO 1	ũ6		TERP	8
		D3 100 J=1,N				TERP	9
		IF (TT-TABLE)	1,J)) 101,102,100			TERP	10
10	100	CONTINUE				TERP	11
	164	TERP = TABLE	L,1)			TERP	12
		RETURN				TERP	13
	106	TERP = TABLE (L,N)			TERP	14
		RETURN				TERP	15
15	102	TERP = TABLE(L, J)			TERP	16
		RETURN				TERP	17
	161	TERP=TABLE(L,	J-1)+(TABLE(L,J)-	TABLE(L,J-1))*(TT-T	ABLE(I, J-1))/	TERP	18
		X(TABLE(I,J)-T	ABLE(I,J-1))			TERP	19
		RETURN				TERP	20
20	110	IF (TT.GE.TABL	E(I,1)) GO TO 104			TERP	21
			E(I,N)) GO TO 106			TERP	22
		00 120 J=1,N				TERP	23
		IF (TT-TABLE(1	,J)) 120,102,101			TERP	24
	120	CONTINUE				TERP	25
25		END				TERP	26

รบลลงบ	TINE DEFRES	74/74	0 > T=1	FTN 4	4.1+REL	06/20/74	17.45.14.
	Sauz	OUTINE D	EPRES (DENSIT,FR1	.D.FR1.DFS.RV)		DEPRES	2
		NSION PV	-			DEPRES	3
	DATA	SIGA5.S	IGA8.SIGAO.SIGT5.	SIGT8.SIGTO/5782.33	.0.,586.5,10.8	DEPRES	4
	X4.2/	,-				DEPRES	4 5
5			R10*.00225927			DEPRES	6
	EN8=	DENSIT *F	R1*.00223079			DEPRES	7
	ENO=	(ENS+EN8	1*2.			DEPRES	8
	SGA=	(ENS +SIG	A5+EN8*SIGA8+ENO	SIGAO)		DEPRES	9
	SST=	(EN5 + SIG	T5+EN8*SIGT8+ENO*	SIGTO)		DEPRES	10
10	CAPS	Q= 3. *S GA	*SGT/(18*SGA/S	GT)		DEPRES	11
	CAPP	A=SQRT (C	APSQ)			DEPRES	12
	RV (1	.11=0.				OEPRES	13
	RV (2	(,1)=1.				DEPRES	14
	00 1	. T= 2, 11				DEPRES	15
15	10 RV (1	.I)=RV(1	,I-1)+DFS/10.			DEPRES	16
)) 2	0 I=2.11				DEPRES	17
	र≠RV	(1.I) *2.	54/4.*CAPPA			OEPRES	18
	20 RV (2	-I)=1.+R	**2.+R**4./4.+R**	6./36.+R**8./576.		DEPRES	19
	RETU	RN				DEPRES	20
20	END					DEPRES	21

												<u></u>	<u></u>	<u></u>
					المسمير	09 65 85	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	2222	FICKET 673 673 673 673 673	4 4 4 4 4 0 15 15 15 15 15 15 15 15 15 15 15 15 15 1	999999	11111	50 50 50 50	3 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5
				.310	. 269 1	5 2 2 2 2 3	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	11.1111111	3 3333333	44444444444 66 51 51 51 51 51 51 51 51 51 51 51 51 51	999999 999	1111111111	8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8	9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9
				3092.	3092.	80 20 20 20 20	30000000 Sessionera 1111111	111,111111	333 3333	4444444444 888888888888888888888888888	9999999999		23 89 89 89 89 89 89 89 89 89 89 89 89 89	
				. 045	. 024	35 38 39 40	.80000000 4433333333333333333333333333333	1111111111111	3333333	444 ⁷ 44444 ++++++++++++++++++++++++++++++++	999999999	1111111111	83 83 85 85 85 85 85 85 85 85 85 85 85 85 85	6 6 6 6 5 5 6 6
				. 979	786	र स्टाया स्टाया स्टाया	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	7	, 3 3 3 3 3 3 3 3 3	444444 3440000 55555	999999999	1111,1111	8 8 8 8 8 8 8 8 8 8	9 2 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9
2793 2004	2			0.0	0.0	2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	1000°0°0°0°0°0°0°0°0°0°0°0°0°0°0°0°0°0°	11111111111111111	33,3333333	4444444444 naaannaasan 5555555555	9999999999	11111111111111	80 80 83 83 80 80 80	න සි න සි න සි න ස න ස න ස න ස න ස න ස න ස න ස න ස න ස
62 1.	1.00	1,0442	1.0163	. 32126	.3189	<u> </u>		7	, 33333333	4 4 4 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	99999999999	1 1	80 80 80 80 80 81 81 81 81	න ස න ස න ස
	321	.241	0.0	17.10	17.80	10 6 2 2 9 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	1111111111111111111111111	3333333,3333333,3333333	444444444 6) 11 12 13 13 15 15 5 5 5 5 5 5 5 5	99999999999999999	1111111111111111111111111111111	88 88 88 88 88 88	68 25 68 25 68 25 68 25 68 25
	•					3 4 2 -	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	1111	3 3 3 3 3	5 5 5 5 5	99999	11111	ಟ ಹ ಹ ಹ	6 65 65 65 65

FIGURE A-1. Data Input for Sample Problem

Output From Sample Problem

***** INITIAL INPUT DATA *****

HEAT RATING	17.80 K	W/FT
FUEL RADIJS	.3819G	INCHES
CENTER VOID RADIUS	0.00000	INCHES
FUEL DENSITY	.95700	
WEIGHT FRACTION U235	.02400	
COLUMAR GRAIN GROWTH TEMP.	3092.	DEG F
FRACTION OF RADIUS FOR CGG	.26900	

**** INPUT OR CALCULATED FLUX DEPRESSIONS ****

DIAMETER (IN)	FLUX RATIO
0.0000	1.0000
.0764	1.0838
.1528	1.0152
.2291	1.0343
.3055	1.0613
.3819	1.0966
• 4583	1.1406
.5347	1.1937
.6110	1,2566
.6874	1.3300
.7638	1.4147

***** CALCULATED VALUES ******

AVERAGE VOLUMETRIC FUEL TEMPERATURE 1895.97 DEG.F (1035.54 DEG.C)
FRACTION OF GAS PRODUCED IN THE 1230-1400 DEG. C TEMPERATURE REGION .114368
FRACTION OF GAS PRODUCED IN THE 1400-1700 DEG. C TEMPERATURE REGION .156872
FRACTION OF GAS PRODUCED IN THE 1700-**** DEG. C TEMPERATURE REGION .056997

RADIUS	TEMPERATURE	RADIUS	TEMPERATURE
(INCHES)	(DEG F)	(CM)	(DEG C)
.3819	740.28	.9700	393.49
.3743	809.56	• 95 0 6	431.98
.3666	880.11	•9312	471.17
.359 0	951.82	.9118	511.01
.3513	1024.59	.8924	551.44
.3437	1098.29	.8730	592.38
.3361	1172.79	. 85 36	633.77
.3284	1247.96	.8342	675.53
.3208	1323.65	.8148	717.58
.3132	1399.72	. 79 54	759.84
3155	1476.00	• 77 60	802.22
.2979	1552.35	• 75 66	844.64
. 2902	1528.61	.7372	887.00
.2826	1704.59	.7178	929,22
.2750	1780.15	.6984	971.19
.2673	1855.11	.6790	1012.84
.2597	1929.30	• 65 96	1054.06
.2521	2002.58	.6482	1094.77
.2444	2074.78	.6208	1134.88
.2368	2145.75	•6014	1174.30
.2291	2215.34	•5820	1212.97

.2215	2283.42	•5626	1250.79
.2139	2349.86	• 54 32	1287.70
.2062	2414.54	• 52 38	1323.63
-1986	2477.35	• 50 44	1358.53
.1910	2538.19	• 48 50	1392.33
.1833	2596.98	• 46 56	1424.99
•1757	2653.63	. 44 62	1456.46
.1580	2708.08	• 42 68	1486.71
.1504	2760.27	. 48 74	1515.70
.1528	2810.14	. 3880	1543.41
.1451	2857.67	. 3686	1569.82
.1375	2902.81	• 34 92	1594.89
.1298	2945.53	. 32 98	1618.63
.1222	2985.83	• 31 04	1641.01
.1146	3023.67	• 2910	1662.04
1069	3059.07	. 2716	1681.70
.1993	3092.00	. 25 22	1700.00
.0917	3122.47	.2328	1716.93
.0340	3150.47	. 21 34	1732.48
.0764	3176.01	•1940	1746.67
.1587	3199.10	• 17 46	1759.50
.0611	3219.74	• 15 52	1770.97
.0535	3237.93	.1358	1781.07
.0458	3253.67	•1164	1789.82
.0382	3266.99	.0970	1797.22
.0306	3277.87	.0776	1803.26
.0229	3286.34	.0582	1807.97
.0153	3292.38	.0388	1811.32
.0076	3296.00	.0194	1813.33

***** INITIAL INPUT DATA *****

HEAT RATING	17.10 KH/FT
FUEL RADIJS	.32126 INCHES
CENTER VOID RADIUS	0.00000 INCHES
FUEL DENSITY	•97900
WEIGHT FRACTION U235	• 04500
COLUMAR GRAIN GROWTH TEMP.	3092. OEG F
FRACTION OF RADIUS FOR CGG	• 31000

**** INPUT OR CALCULATED FLUX DEPRESSIONS ****

DIAMETER (IN)	FLUX RATIO
0.0000	1.0000
.1600	1.0163
.2410	1.0442
• 3 21 0	1.0834
.4020	1.1356
.4820	1.2004
.562C	1.2793
.6425	1.3740

***** CALCULATED VALUES *****

AVERAGE VOLUMETRIC FUEL TEMPERATURE 2007.26 DEG.F (1097.37 DEG.C) FRACTION OF GAS PRODUCED IN THE 1200-1400 DEG. C TEMPERATURE REGION .123347 FRACTION OF GAS PRODUCED IN THE 1400-1700 DEG. C TEMPERATURE REGION .06969 FRACTION OF GAS PRODUCED IN THE 1700-**** DEG. C TEMPERATURE REGION .077292

RADIUS	TEMPERATURE	RADIUS	TEMPERATURE
(INCHES)	(DEG F)	(CH)	(DEG C)
• 3213	872.43	·8160	466.90
.3148	942.48	• 79 97	505.82
.3384	1013.59	. 78 34	545.33
.3020	1085.65	•7670	585.36
•2956	1158.53	.7507	625.85
.2391	1232.12	•7344	666.74
.2827	1306.29	.7181	707.94
•2763	1380.91	.7018	749.39
•2599	1455.82	. 68 54	791.01
.2634	1530.89	•6691	832.72
·2570	1605.96	• 65 28	874.42
•2506	1580.89	• 63 65	916.05
.2442	1755.51	•6202	957.50
.2377	1829.67	•6038	998.71
.2313	1903.23	•5875	1039.57
•2249	1976.02	• 57 12	1080.01
.2185	2047.90	• 55 4 9	1119.94
.2120	2118.71	.5386	1159.28
-2056	2188.33	• 52 22	1197.96
•1992	2256.61	•50 59	1235.90
.1928	2323.44	• 48 96	1273.02
.1863	2388.69	• 47 33	1309.27
.1799	2452.25	• 45 70	1344.58
.1735	2514.82	. 4406	1378.90

•1671	2573.92	• 42 43	1412.18
.1606	2631.86	•40 80	1444.36
•1542	2687.77	•3917	1475.43
.1478	2741.58	• 37 54	1505.32
•1414	2793.26	• 3590	1534.83
.1349	2842.74	. 3427	1561.52
.1285	2889.99	• 32 64	1587.77
•1221	2934.98	•3101	1612.77
•1157	2977.69	• 2938	1636.50
.1192	3018.11	•2774	1658.95
.1028	3056.22	• 26 11	1680.12
• 3964	3092.00	• 24 48	1760.00
.0900	3125.46	• 22 85	1718.59
.0835	3156.60	• 21 22	1735.89
.0771	3185.42	•1958	1751.90
.0707	3211.92	•17 95	1766.62
.0543	3236.10	•1632	1780.06
.0578	3257.97	•1469	1792.20
.0514	3277 • 52	.1306	1803.06
.0450	3294.75	• 11 42	1812.64
.0386	3309.67	.0979	1820.93
.0321	3322.28	.0816	1827.93
.0257	3332.59	•0653	1833.66
.0193	3340.60	.0490	1838.11
.0129	3346.32	.0326	1841.29
.0064	3349.75	.0163	1843.19
•			

APPENDIX B

Reduced Fuel Temperatures

TABLE B-1. Reduced Fuel Temperature

REFERENCE	SPECIMEN NUMBER	HEAT RATING (kw/ft)	SURFACE TEMPERATURE	CENTERLINE TEMPERATURE (°C)	GAS RELEASE (PERCENT)
CYRANO EXP.	CYRANO-11 CYRANO	13.9 11.5	752/758 819/843	1990/2069* 1890/1969*	15.0 13.0
HPR-129	116-5 117-1	22.8 21.0	360/341 530/512	2070/2374* 2060/2329*	27.5 25.4
BELGONUCLEATRE AND CEA	EPL-4 EPL-5 EPL-6 EPL-9 EPL-10 EPL-12	12.3 13.5 15.1 14.9 14.9 13.3	617/ - + 513/ - + 670/688+ 600/618 600/656 691/674	1743/ - + 1693/ - + 2133/2160 + 2000/2030 2000/2089 1971/1945	9.9 4.4 21.3 23.2 18.3 17.8
AECL-2662	LFL LFF LFB LFS LFW LFT LFX LFM LFH LFD	18.0 17.8 17.3 24.5 25.0 24.1 24.9 22.7 22.1	351/ - 473/ - 540/551 450/509 343/403 490/500 453/467 357/431 495/502 546/606	1678/ - 1974/ - 2108/2128 2500/2596 2343/2459 2679/2694 2614/2638 2156/2305 2434/2447 2586/2673	5.7 17.3 23.4 37.9 24.8 49.6 36.8 15.5 31.1 45.8
AECL-2230 (TEST X-501)	CBN CBO CB CBR CBT CBV CBY CBX	17. 1 17. 3 16. 8 17. 4 16. 6 17. 5 16. 55 17. 1	443/467 435/490 432/483 459/534 446/545 425/515 471/565 471/579	1797/1843 1802/1843 1762/1862 1880/2019 1795/1981 1854/2027 1871/2043 1923/2117	12.3 14.9 14.1 15.7 15.3 16.5 16.8 18.8
AECL-1676 (TEST X-211)	DFE DFH DFD DFB DFA	35.8 29.5 29.05 24.0 17.7	- /399 - /385 - /476 - /458 391/ -	- /3248 - /2799 - /2903 - /2469 1734/ -	40.1 32.6 33.0 17.9 4.95
CEA-R-3358	4110-AE1 -AE2 -BE1 -BE2 4112-AE1 -AE2 -BE1 -BE2 4113-AE1 -AE2 -BE1 -BE2	18. 1 17. 6 15. 1 17. 8 19. 5 17. 7 15. 4 16. 6 17. 1 15. 6 16. 0 15. 9	612/ - 570/ - 548/ - 485/ - 440/399 504/462 425/ - 498/427 731/725 756/701 532/544 718/670	2296/ - 2175/ - 1876/ - 2047/ - 2167/2085 2097/2019 1699/ - 1971/1832 2419/2426 2278/2199 1942/1988 2239/2169	21.6 22.1 13.9 15.9 12.6 11.2 7.9 12.6 26.7 28.0 17.0 21.0

^{*} TEMPERATURE MEASUREMENT BY A THERMOCOUPLE AT FUEL CENTERLINE / CORRECTED CENTERLINE TEMPERATURES FOR THAT PORTION OF THE FUEL WITHOUT AN ANNULAR HOLE AND THERMOCOUPLE

NOTE: SEE TABLE 1 IN REPORT FOR MORE INFORMATION

[†] TEMPERATURE DETERMINED FROM EQUIAXED BOUNDARY/TEMPERATURE DETERMINED FROM COLUMNAR BOUNDARY

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