ABSTRACT

Using a high resolution SQUID voltmeter, we have "easured the spectrum of low frequency voltage fluctuations across a thin-file Josephson tunnel function blased at a constant current I greater than the junction critical current I_c . We find that the frequency dependence of the voltage spectrum $V^2(f)$ may be accurately represented by the power law $V^2(f) \propto f^{-1}$ over the frequency range of our data: $10^{-2} < f < 10$ Hz. the dependence of the magnitude of the spectra at any single frequency upon the value of the bies current I and upon the sample temperature I supports our hypothesis that the observed voltage fluctuations arise iron a modulation of the junction critical current L by equilibrium, thermodynamic temperature fluctuations in the active function volume. We are able to interpret our reasurements in terms of the semi-empirical theory^I of Clarke and Voss for the low frequency fluctuarion spectrum of systems obeying a diffusion equation. This interpretation provides design criteria which any prove useful in reducing the level of longters drifts in systems employing Josephson runnel junctions.

1. EXPERIMENTAL TECHNIQUES

The Josephson junctions investigated in our exceriment are constructed by souther deposition of ob strips 2000A thick and 180 um wide followed by evaporation of Pb cross strips of similar dimensions. Prior to sputtering, the soda glass substrates are coated with 20 Å of Cr to insure mechanical adherence of the films. The junctions are shunted to a resistance of approximately 7 m by the evaporation of disc-shaped Cu underlays a few millimeters wide and 7000 A thick centered on the junction area. On some samples, the inductance of these shunts is reduced by the addition of a superconducting ground plane to insure that the I-V characteristic does not exhibit hysteresis. We estimate the hysteresis parameter $\beta_c = 2\pi I_c R^2 C/\phi_0$ to be approximately 0.2, where C is the junction capacitance, R the shunt resistance, and >, the flux quantum. We have also constructed samples whose shunts are excluded from the immediate junction region to preclude the possible formation of small SNS junctions at the points of mutual contact of the Pb, Nb, and Cu.² The formation of such junctions might be expected to alter the temperature dependence of the total junction critical current, because of the exponential dependence of 1_c upon T for SNS junctions.³ However, we have as yet no evidence for the occurrence of this effect in samples employing the full disc geometry. The sample junctions are counted in thermal contact with a Cu block suspended in a vacuum chamber. The thermal time constant of the block is chosen to be approximately 6 minutes in order to minimize the effects of temperature fluctuations of the He bath over the time scale of our measurements. All electrical connections to the junctions are made using 2 mil Nb leads spot welded to

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solder-coated brass tabs. Superconducting contact to the Nb strips cannot be achieved religibly by soldering and is accomplished by the use of eraporated Pb underlays.



Fig. 1. Experimental apparatum for the measurement of voltage fluctuations across a thin film Josephson function.

As shown in Fig. 1, an external current source provides the junction with a constant bias current I 2 Ic. The voltage V developed across the junction causes current to flow through standard resistor Re to a superconducting signal coil whose field is coupled to a de point-contact SQUID of toroidal geometry. In the feedback mode, the SQUID and its associated electronics act as a high gain (- 10^8), low noise dc amplifier whose output is directly proportional to V for frequencies below the 300 Hz response of the SQUID electronics. The advantages of this amplifier configuration in our experiment are twofold. First, the amlifier may easily be impedance matched to the mai resistances of our samples by a suitable choice of the standard resistor $H_{\rm S}$, typically 0.01 Å. This enables us to measure junction voltages .² as little as 10^{-13} V without amplifier noise limitation. Secondly, the input to the SQUID amplifier may be effectively do offset for the measurement of small fluctuations in junction voltages which themselves are so large as to exceed the dynamic range of the SQUID. Offset is achieved with no loss of amplifier stabilicy and with no deterioration of the do frequency response by opersting the SQUID with a large (but constant) number of flux quanta in the area enclosed by the point contacts.

11. RESULTS AND ANALYSIS

When the sample is biased with current $l \rightarrow l_c$, the voltage V across the junction exhibits scall fluctuations whose low frequency spectrm: is snalyzed by digitizing the elevenst Fourier transforms on a PDP-11 computer. Data points for the frequency spectrum V2(E) for a typical junction are displayed log-rithmically in Fig. 2 as a function of frequency forer the range 5 $\times 10^{-2}$ C < 10 Hz. For this junction, i = 3.0 kM and $L_c = 2.6$ mA st T = 1.5K. In Fig. 3, smooth line filts to our data for the voltage spectra of a second junction are bown for several values of the blas current I in the range I \approx L_c to $I = 2L_c$.

There are use important features displayed by the fluctuation spectra of Figs. 2 and 3. First, for all values of bias current I, the frequency dependence of the spectra is very nearly Γ^1 over a vide range of frequencies. The best straight like fits to our data for various sample junctions yield exponents in the range -0.9 to -1.15 for the frequency

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Fig. 2. Experimental measurements of the spectrum V²(f) of voltage fluctuations across a typical sample.



Fig. 3. Voltage spectra for three values of junction bias current 1. Note that the fluctuations decrease with increasing 1.

dependence of the spectra. (We have been careful to ascertain that, at low frequencies, the clustuations associated with the detector, the standard registor, and the blas current supply are well below the level of functantems associated with the junction, typically by station of 10°. For frequencies greater than 10 Hz, the sectra begint to be deminated by the Johnson noise

produced in the standard tesistor R_3 .) Secondly, at any <u>single</u> frequency, the magnitude of the fluctuations decreases with increasing blas current L.

These observations are extremely important in delineating the mechanism by which large, low frequency fluctuations are produced in thin film Josephsor junc-tions. We propose that the f^{-1} frequency dependence of the spectra shown in Figs. 2 and 3 arises from thermodynamic cooperature fluctuations in the junction voluce, which modulate the junction critical current Ic through the derivative dI_/dI and hence modulate the voltage observed across the biased junction. This proposed mechanism is closely related to the fluctuation process responsible for "1/f" noise in the voltage spectrum of thin metal films biased at constant current. The experimental analysis presented in Ref. 1 provides strong evidence that, for thin film geometries, the spectrum of temperature fluctuations within the film obeys a 1/f power law over wide ranges of frequency. For metal films, these temperature fluctuations are coupled to the experimentally accessible variable (voltage) by a mechanism involving temperature modulation of the film registance through the derivative dR/dT. Hence $\delta V = I(dR/dT)\delta T$ and the fluctuation spectrum scales as I^2 . As in the case of thin metal films, the frequency dependence and the numerical magnitude of the power spectra of Josephson junctions provide strong evidence for the thermal origin of the fluctuations. However, for Josephson junctions, the analogous mechanism which couples thermal fluctuations to the expericentally observed junction voltages cannot be associated with thermal modulation of a resistive elecent, since the amplitudes of the spectra do not scale as 12 hut rather decrease with increasing I, as shown in Fig. 3. The observed dependence of $V^2(f)$ upon the bias current I instead supports the assertion that, for Josephson junctions, the primary coupling mechanism involves codulation of the critical current Ic(T), which in turn alters the junction voltage in accordance with the Stewart-HcCumber' relation

$$\left(\frac{\partial v}{\partial T_{c}}\right)^{2}_{1} = \frac{R^{2}}{\left(\frac{1}{T_{c}}\right)^{2} - 1}.$$
(1)

At high bits currents, the junction is note nearly an ideal resistive elecant whose value is increasingly insensitive to thermally induced fluctuations in I_c , thus accounting for the observed decrease in moise power with increasing I.

We may apply these qualitative observations to the theory of diffusive fluctuations developed by Clarke and Voss¹ to obtain the semi-empirical formula

$$v^{2}(f) = \left(\frac{\partial v}{\partial T_{c}}\right)^{2} \left(\frac{dL_{c}}{dT}\right)^{2} k_{B}T^{2}/C_{v}Gf$$
 (2)

as a prediction for the experimental voltage spectrum of thin film Josephson tunnel junctions. Here, 5 is a genmetric factor of roughly 3, and C., is the beat capacity of the active volume of the junction, which we take to be the junction area times the coherence length. Using our measured values of (dI_/dI), and computing $(3V/3l_c)_T$ from Eq. (1), we find that the predictions of Eq. (2) are in remarkably good agreement with the experimentally determined fluctuation spectra, as indicated by the dashed lines in Figs. 2 and 3. Both the frequency dependence of the spectra and the dependence upon bias current I are in quantitative accord with our theoretical expectations. The excellent egreement between theory and experiment regarding the magnitude of the fluctuations is especially saulefying, since normalization of the theoretical spectra relies on the fundamental thermodynamic relation $\langle \delta T^2 \rangle = k_B T^2/C_V$. Because of our imprecise knowledge of several of the parameters required to evaluate Eq. (2)(such as the effective junction volume), our theoretical estimates are probably no more accurate

tion an order of magnitude in $v^2(t)$, although the spectra on must of the samples we have studied differ from the predictions of Eq. (2) by less than a factor of 5. We note that, as $l \rightarrow l_c$, the increase in the valtage if luctuations is not as rapid as that suggested by the Stewart-Netweber estandard resistor $R_{\rm s}$ is only about a factor of two greater than the shuft resistance of the function. Hence, account must be taken of the current flow through the SQUID valtaceter, which adds a term (SRA) to the demonstrator of Eq. (1). In the extreme case, $R_{\rm s} < R_{\rm s}$ all the bias current in excess of $l_{\rm s}$ (lows through the SQUID signal coil and the observed fluctuation spectra become independent of I for $l \rightarrow l$.

We have attempted to test the temperature dependence of the predictions of Eq. (2) for the voltage spectra by varying the remperature of the bath surrounding the vacuum can from 4.2K to 1.5K. Experimentally, we find that for most junctions the change in the magnitude of the noise spectra is not large, typically less than a factor of 5 over our expericentally accessible temperature range. This behavior may be understood from Eq. (2) by noting that, while the terms T2(dI,/dT)2 in the numerator decrease roughly two orders of magnitude from 4.2K to 2.0K, the specific heat C, in the denominator of Eq. (2) decreases over this temperature range by a factor of nearly 25, resulting in relatively little change in the noise power. At sufficiently low temperatures, the spectral power due to thermal modulation of the critical current should vanish as (dIc/dT)2/T. It would be important to investigate this temperature regime to ascertain the possible existence of other sources of low frequency noise not assoclated with thermal diffusion.

Although most of our sample junctions did not display marked variations in noise power as a function uf temperature, we did encounter one anomalous junction whose noise power varied by mearly three orders of markitude over a temperature range of 0.2%. This behavior was associated with, and could be explained by, the highly unusual temperature dependence of the critical current observed for this sample and shown in Fig. 4. The pronounced dip in the L₂ vs T characteristic, centered about 1.3%, was quitte reproducible and





persisted when the sample was recooled after being wared above T_c or to room tecperature. Although the origin of this behavior is far from certain, we comjecture that the abnoral temperature dependence of $T_c(T)$ for this sample can be interpreted in terms of the McMillan theory of the proxisity effect.⁶ During construction of the junction, the sputtering current was decreased slowly mear the end of the NM deposition. As a result, the last layers of NM were deposlied at a rate lower than that known to be required to produce Nb films which are superconducting above NK. Thus the junction formed was of the type Nb-N-Os-Pb. where N is a normal layer. HcMillian predicts that such a junction should in fact exhibit a minimum in the l_c wi T characteristic.

Regardless of the source of the annalous behavior, the regions for which (dL_dfT) = 0 were of considerable use in our study of the thermal origin of 1/1 maise in Josephson junctions. For this sample, we were able to alter the value of (dL_dfT) from essentially zero at the local maximum of the L_v ws T characteristic to a relatively large value (2.2 mA/K) on new steprest reduof the dip by changing the sepperature and 0.2%. Since this small temperature variation did not appreciably alter T² and C_y, we could directly observe the effact of the single term (dL_dfT) from essurements of fluctuation spectrum of the anounce junctions, the observed spectrum was indeed proportional to (dL_dfT)² and in fact decreased by times orders of magnifue to a



Fig. 5. Dependence of the fluctuation spectrum of the anomalous junction on the single parameter $(dl_c/dT)^2$.

level below our amplifier noise at the memperature for which L₂ vs T shifting a local maximum. Clearly, it would be of importance to further investigate the tenperature dependence of Eq. (2) by observing the fluctuations associated with other types of junctions, such as the SNS, for which the term (dL/dT) would dominate the temperature dependence of C₄.

Finally, we commant on two experimental complications associated with nearwarenets of low frequency fluctuations. In general, to obtain reliable spectra, it as 'mportant that (1) the experimental probe used to observe the fluctuations not unduly perturb the sysber under investigation, and (2) that the system itself be in thermal equilibrium with a reservoir whose temperature does not fluctuate appreciably over the time scale of experimental interest. Resarding rolint (1), we have observed that, for 1 \geq 10 th, the effects of thermal heating produce additional noise ad structure in the fluctuation spectra which cannot be desortbed by a simple power law dependence upon frequency. It is not clear whether this additional noise is associated with thermal fluctuations in a sample for from equilibrium, or whether the distortion of the spectrum arises from thermal feedback, which introduces local heating in proportion to local temperature fluctuations. Regarding (2), we have investigated the effects of sample contact with a thermal teservoir which is in greas non-equilibrium; for example, with a ie bath whose pressure is unregulated. For a wide waricty of such pen-poullibrium systems we find that the experimental vectra rise very repidly at ins frequencies, in approximate accordance with the power law . For irequencies shall compared to the reciprocal of the equilibration time of the sample and reservoir, we expect the voltage fluctuations across the junctions to airror the temperature fluctuations of the reservoir. For frequencies higher than the frequencies at which the reservoir fluctuates, the observed spectra are consistent with that expected from coullibrium remerature fluctuations within the junctions themselves.

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111. COSCLUSION

We have measured the low frequency voltage spectrum associated with the finite witage state of thin film, oxide tunnel junctions and have identified the primary source of these fluctuations as codulation of the junction critical current by thermodynamic temperature fluctuations in the junction volume. This interpretation is in good numerical accord with our experimental results and correctly predicts the dependence of the spectrum on both frequency and function bias curtent. Bur results have important implications for such devices as SQUID voltmeters and magnetometers, since a lower limit to the long-tern drift stability of systems employing Josephson junctions will be set by the behavfor of the low frequency fluctuations inherent in the junctions themselves. We feel it should be possible to formulate practical design criteris, such as a mini-nization of $T^{(d]_{2/C_{u}}}$ which could be used to achieve reduced levels of long-term drift in many systens relying on Josephson junctions to detect currents and magnetic fields.

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